

STACKS AND QUEUES

Data Structures and Algorithms
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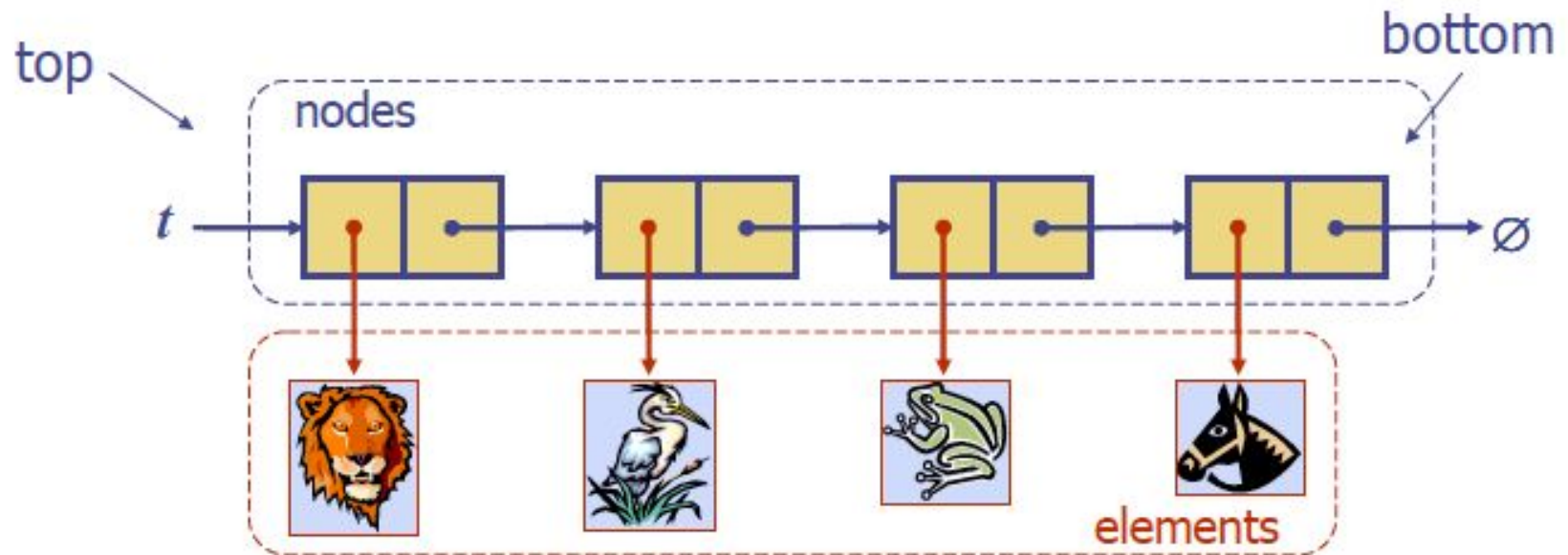
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Stack

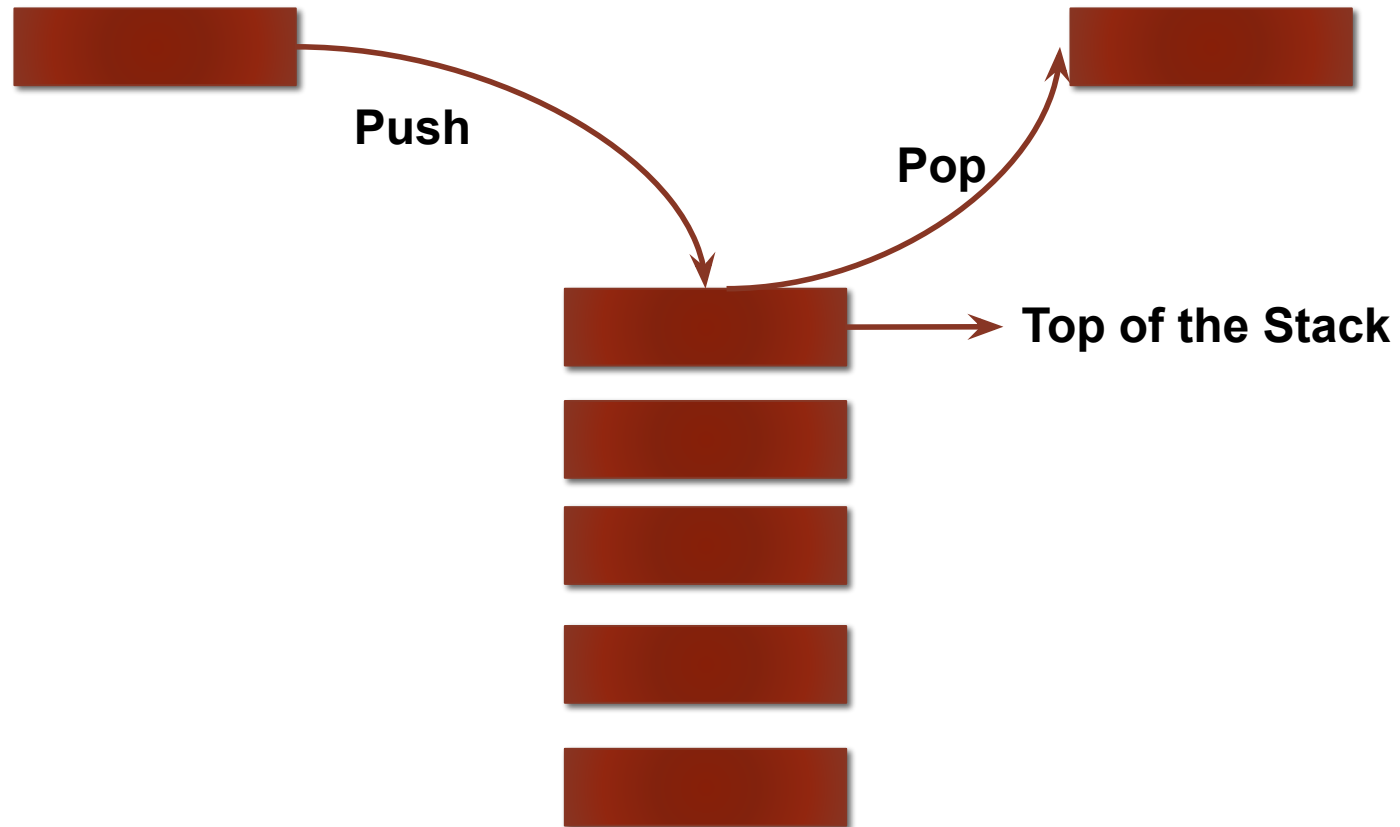
- Stack is a data structure that allows access to items in a last in first out (**LIFO**) style
- Main Stack operation:
 - **push(object)**: insert an element to the stack
 - **pop()**: return the last inserted element and remove it
- Auxiliary stack operations:
 - **top() / peek()**: return the element on top of the stack (last inserted element)
 - **size()**: return the number of elements stored
 - **isEmpty()**: return a boolean value indicating elements are store or not in the stack



Stack Implementation Using Linked List



Stack (Cont.)



Stack Example

Operation	output	stack
• push(8)	-	(8)
• push(3)	-	(3, 8)
• pop()	3	(8)
• push(2)	-	(2, 8)
• push(5)	-	(5, 2, 8)
• top()	5	(5, 2, 8)
• pop()	5	(2, 8)
• pop()	2	(8)
• pop()	8	()
• pop()	"error"	()
• push(9)	-	(9)
• push(1)	-	(1, 9)

Python list can be used as stack!

```
stack = []

# append() function to push
# element in the stack
stack.append('a')
stack.append('b')
stack.append('c')

print('Initial stack')
print(stack)

# pop() function to pop
# element from stack in
# LIFO order
print('\nElements popped from stack:')
print(stack.pop())
print(stack.pop())
print(stack.pop())

print('\nStack after elements are popped:')
print(stack)
```

Python list can be used as stack!

```
stack = []
```

```
# append() function to push
```

```
# element in the stack
```

```
stack.append('a')
```

```
stack.append('b')
```

```
stack.append('c')
```

```
print('Initial stack')
```

```
print(stack)
```

```
# pop() function to pop
```

```
# element from stack in
```

```
# LIFO order
```

```
print('\nElements popped from stack:')
```

```
print(stack.pop())
```

```
print(stack.pop())
```

```
print(stack.pop())
```

```
print('\nStack after elements are popped:')
```

```
print(stack)
```

Python needs to reallocate memory to grow the underlying list for accepting new items, these operations are slower and can become **$O(n)$**

Stack Implementation Using Linked List

Consider the following classes and implement the functions:

```
class Node:  
    def __init__(self, data):  
        self.data = data  
        self.next = None
```

```
class StackLinkedList:  
    def __init__(self):  
        self.top = None  
  
    def is_empty(self):  
  
    def push(self, data):  
  
    def pop(self):  
  
    def peek(self):
```

```
stack = StackLinkedList()  
stack.push(1)  
stack.push(2)  
stack.push(3)  
  
print("Top of the stack:", stack.peek())  
print("Popped item:", stack.pop())  
print("Top of the stack after pop:", stack.peek())
```


Stack Implementation Using Linked List

Consider the following classes and implement the functions:

```
class Node:
    def __init__(self, data):
        self.data = data
        self.next = None
```

```
class StackLinkedList:
    def __init__(self):
        self.top = None
```

```
    def is_empty(self):
```

```
    def push(self, data):
```

```
    def pop(self):
```

```
    def peek(self):
```

```
    def is_empty(self):
        return self.top is None

    def push(self, data):
        new_node = Node(data)
        new_node.next = self.top
        self.top = new_node

    def pop(self):
        if self.is_empty():
            return "Stack Underflow"
        data = self.top.data
        self.top = self.top.next
        return data

    def peek(self):
        if self.is_empty():
            return "Stack is empty"
        return self.top.data
```

Stack Implementation Using Linked List

Consider the following classes and implement the functions:

```
class Node:  
    def __init__(self, data):  
        self.data = data  
        self.next = None
```

```
class StackLinkedList:  
    def __init__(self):  
        self.top = None
```

```
    def is_empty(self):
```

```
    def push(self, data):
```

```
    def pop(self):
```

```
    def peek(self):
```

Write a function which returns the size of the stack?

Applications of Stack

- Reversing data
- Detecting unmatched parentheses
- Page-visited history in a Web browser
- Undo sequence in a text editor
- Implementing recursion

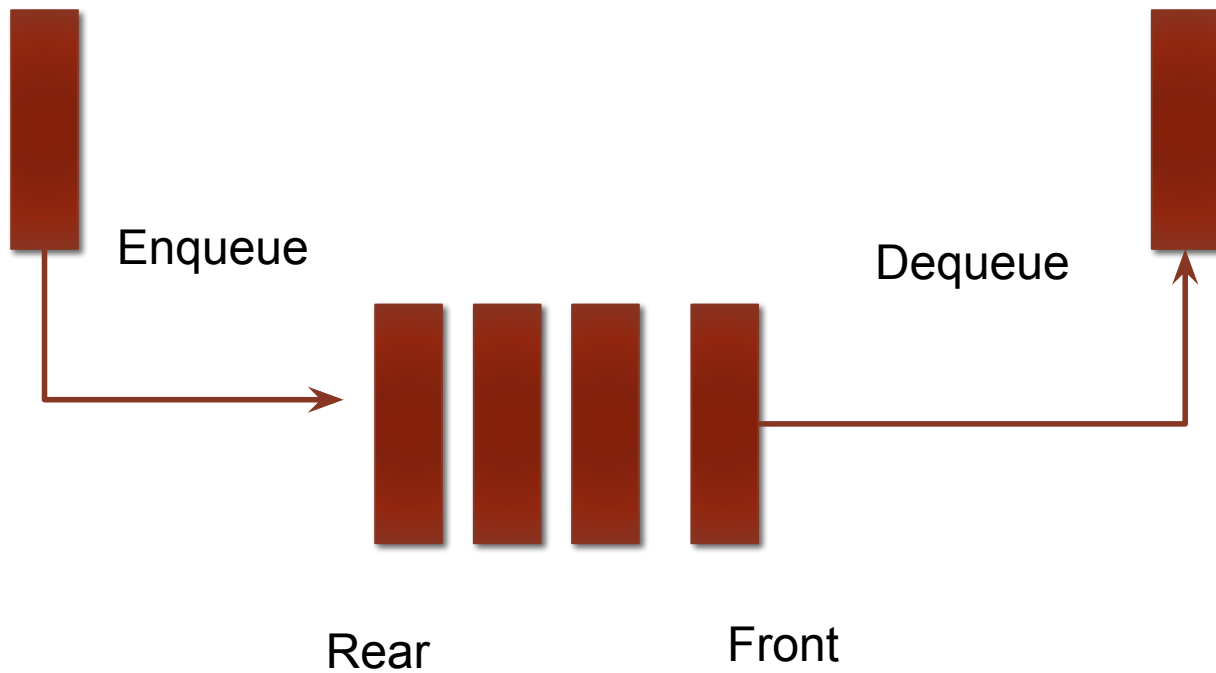
Many other you may need to explore!

Queue

- Queue is a data structure that allows access to items in a first in, first out style (FIFO)
- Main Operations:
 - **enqueue (item)**: add to the queue
 - **dequeue ()**: remove the *oldest* item in the queue
- Auxiliary Operations:
 - **front()**: returns the element at the front without removing it
 - **size()**: returns the number of elements stored
 - **isEmpty()**: returns a Boolean value indicating whether no elements are stored



Queue (Cont.)



Queue Example

Operation	output	queue
• enqueue(5)	-	(5)
• enqueue(3)	-	(5, 3)
• dequeue()	5	(3)
• enqueue(7)	-	(3, 7)
• dequeue()	3	(7)
• front()	7	(7)
• dequeue()	7	()
• dequeue()	"error"	()
• isEmpty()	true	()
• enqueue(9)	-	(9)
• size()	1	(9)

Application of Queue

- Waiting lists e.g., customer checkout on a point of sale counter
- Access to shared resources e.g., printer

- Queue in Python can be implemented using **deque** class from the collections module.
- **Deque** is preferred over list in the cases where we need quicker **append** and **pop** operations, as deque provides an **O(1)** time complexity for **append** and **pop** operations as compared to **list which provides O(n)** time complexity, whenever resizing is done!
- Instead of enqueue and deque, append() and popleft() functions are used.

```
from collections import deque
q = deque()
q.append('a')
q.append('b')
q.append('c')
print("Initial queue")
print(q)
print("\nElements dequeued from the queue")
print(q.popleft())
print(q.popleft())
print(q.popleft())

print("\nQueue after removing elements")
print(q)
```


Queue using Linked List

```
class QueueNode:
    def __init__(self, data):
        self.data = data
        self.next = None

class QueueLinkedList:
    def __init__(self):
        self.front = None
        self.rear = None

    def is_empty(self):
        return self.front is None

    def enqueue(self, data):
        new_node = QueueNode(data)
        if self.is_empty():
            self.front = new_node
            self.rear = new_node
        else:
            self.rear.next = new_node
            self.rear = new_node
```

```
    def dequeue(self):
        if self.is_empty():
            return "Queue Underflow"
        data = self.front.data
        self.front = self.front.next
        if self.front is None:
            self.rear = None
        return data
```

```
    def peek(self):
        if self.is_empty():
            return "Queue is empty"
        return self.front.data
```

Example usage:

```
queue = QueueLinkedList()
queue.enqueue(1)
queue.enqueue(2)
queue.enqueue(3)
```

```
print("Front of the queue:", queue.peek())
```

```
print("Dequeued item:", queue.dequeue())
```

Palindromes

Palindromes are words which can be read same from forward and reverse. Few examples are:

- Radar
- Mom
- Dad
- Stats
- Madam
- Wassamassaw

How we may use Stack and Queue to determine a given word is palindrome?

Some Problems Solve Easily Using Stack/Queue

- Reverse a String: Reverse a given string.
- Valid Parentheses: Determine if a given string of parentheses is valid.
- Implementing Cache: Implement a cache with a fixed size using a queue.