



AuE 8200: Machine Perception and Intelligence

Lecture: Signal, spectrum, and vehicle sensors

Instructor: Bing Li, Ph.D.
bli4@clemson.edu

Assistant Professor
Department of Automotive Engineering
Clemson University International Center for
Automotive Research (CU-ICAR)



Outline

- Introduction
- Signal and Sensor Perception
- 1D Signal and A/D
- 1D Signal Time-domain Analysis
- 1D Signal Frequency Analysis
- 1D Signal Noise Analysis
- 1D Signal Processing and Filter Design
- Electromagnetic Spectrum
- Vehicle Sensors (Perception)



1D Signal: Wave

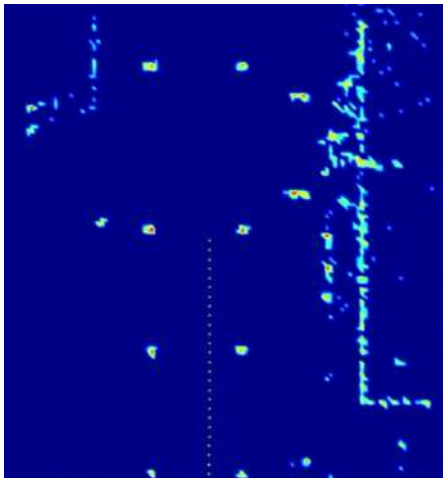
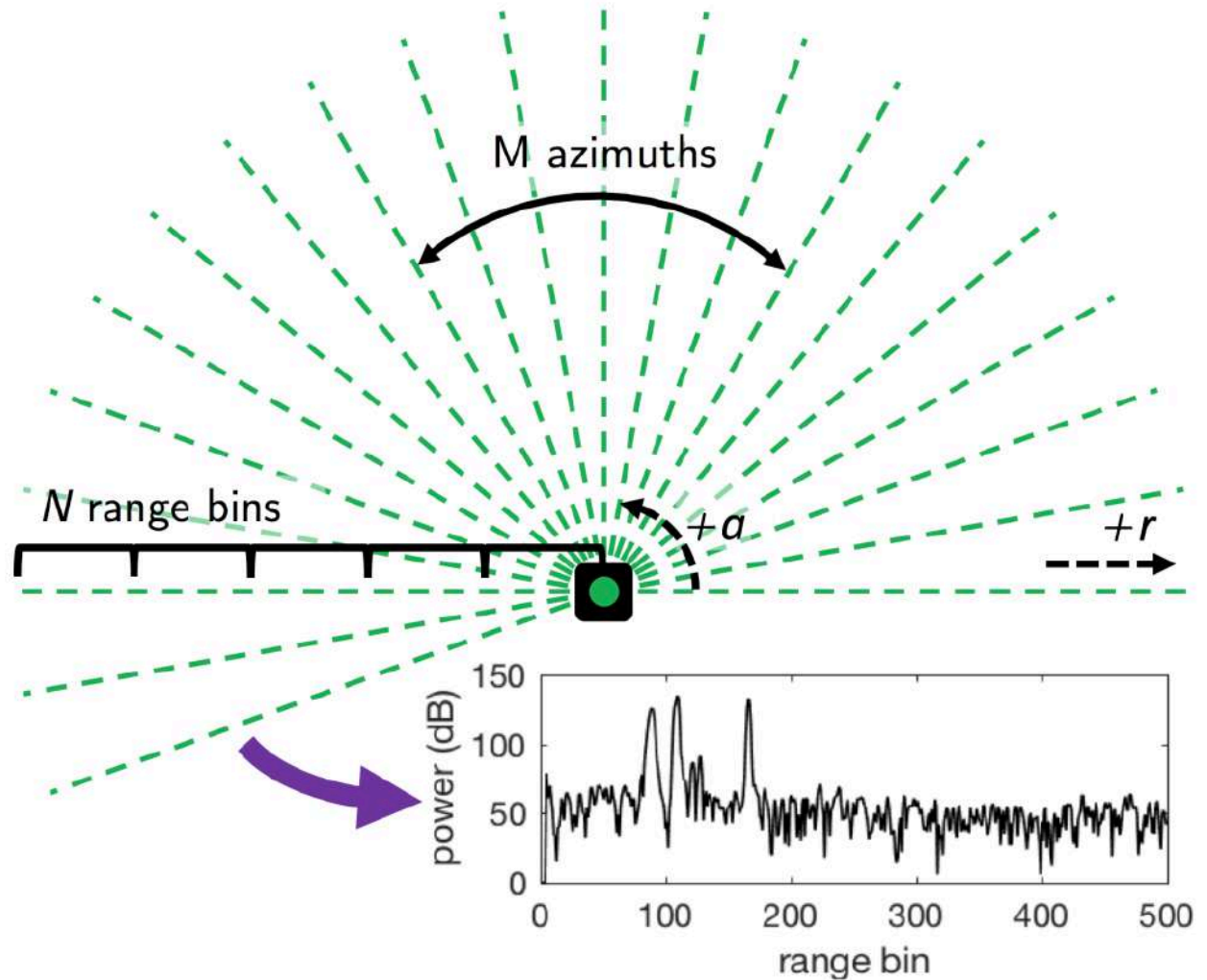
Time domain

Frequency domain

Noise filter

Patterns

...





2D Signal: Image

Time domain

Frequency domain

Noise filter

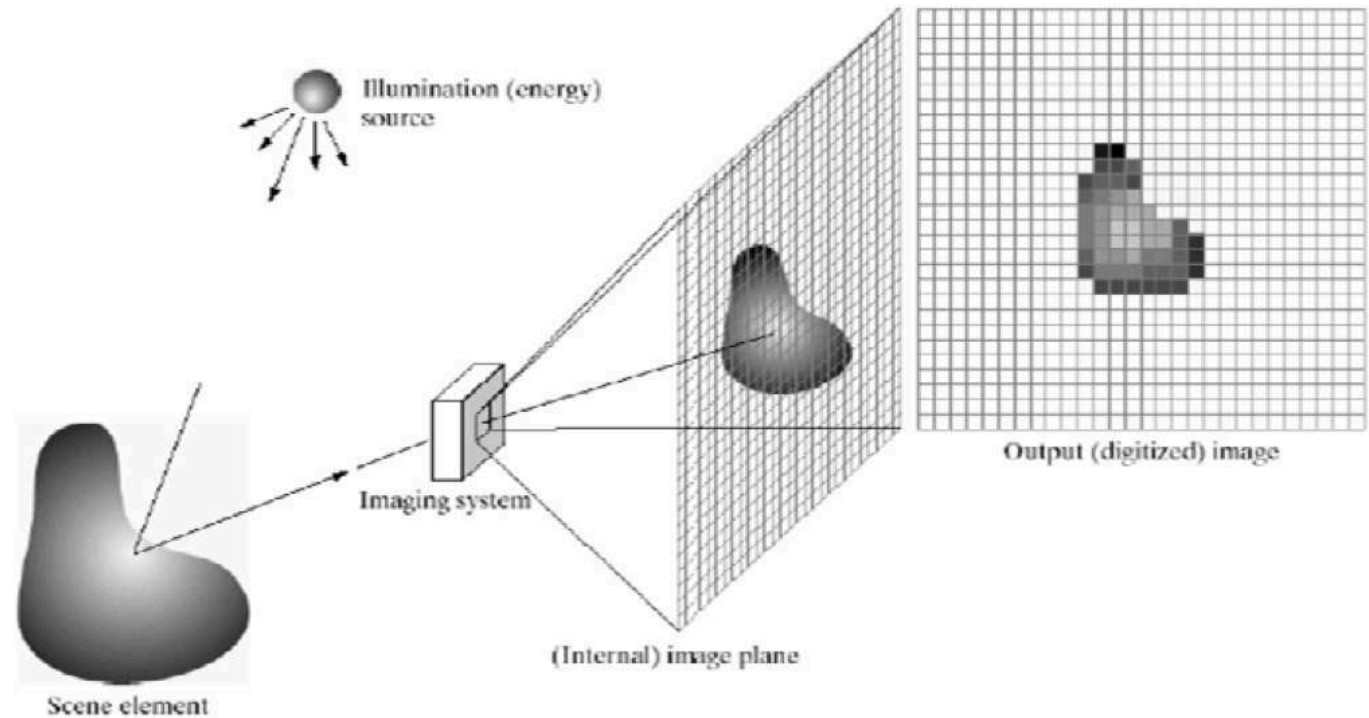
Multi-view

Features

Patterns

Understanding

...





3D Signal: Point Cloud

Time domain

Frequency domain

Noise filter

Geometry analysis, mapping

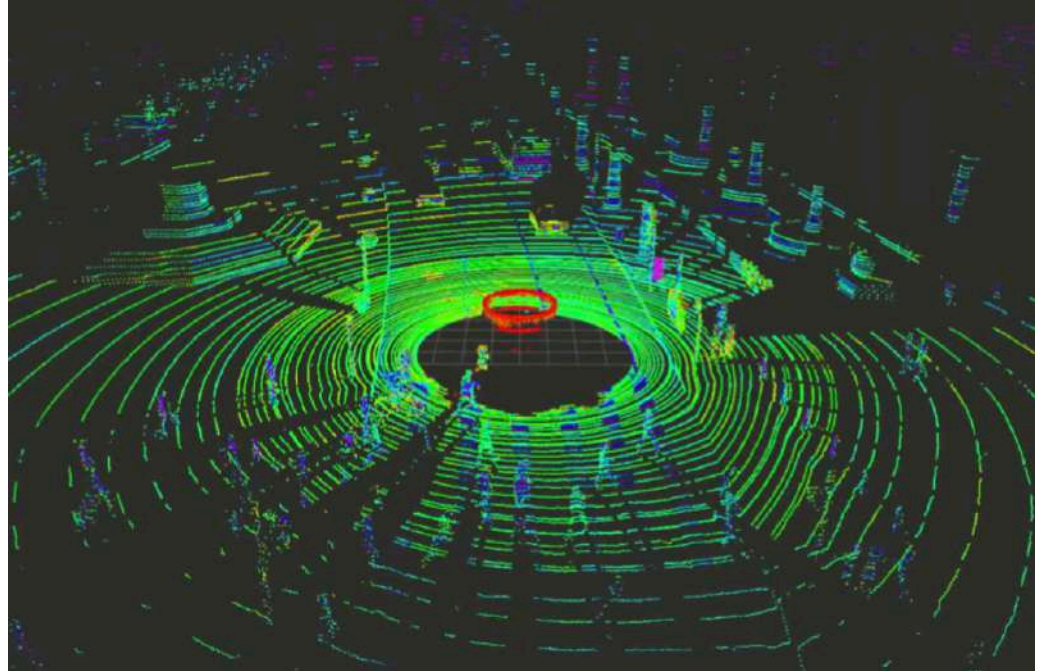
Features

Patterns

Understanding

...

Fuse with 2D vision



Signal and Sensor Data Analysis

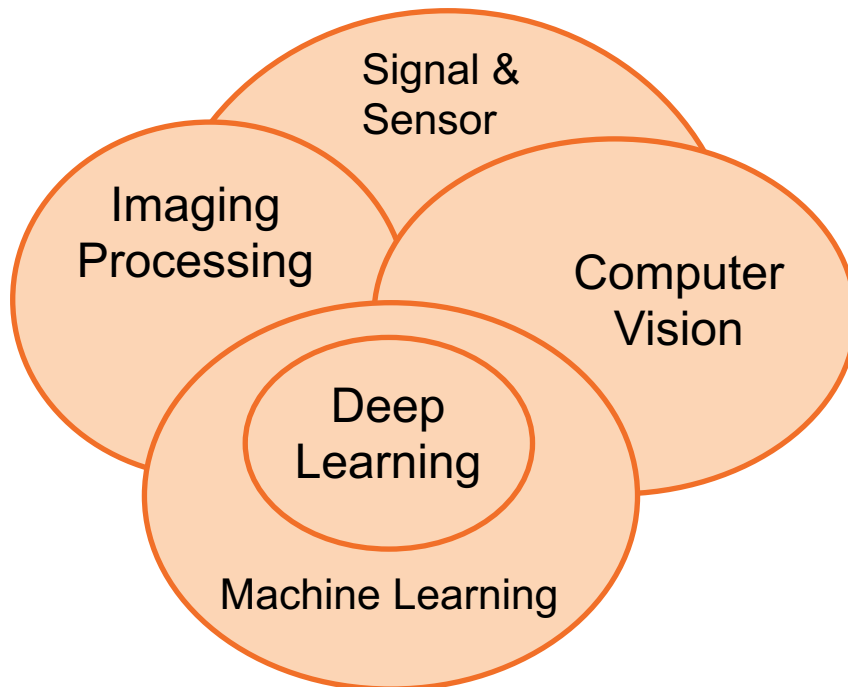
• Applications

Vehicle perception

ADAS (Advanced driver-assistance systems)

Autonomy

• Areas



Space

- Space photograph enhancement
- Data compression
- Intelligent sensory analysis by remote space probes

Medical

- Diagnostic imaging (CT, MRI, ultrasound, and others)
- Electrocardiogram analysis
- Medical image storage/retrieval

Commercial

- Image and sound compression for multimedia presentation
- Movie special effects
- Video conference calling

Telephone

- Voice and data compression
- Echo reduction
- Signal multiplexing
- Filtering

Military

- Radar
- Sonar
- Ordnance guidance
- Secure communication

Industrial

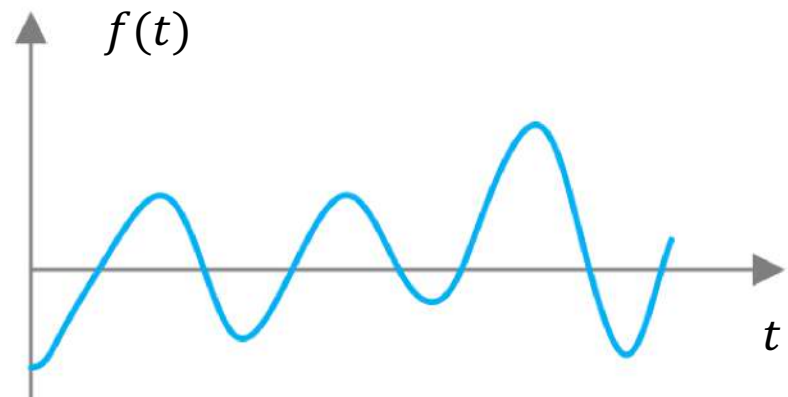
- Oil and mineral prospecting
- Process monitoring & control
- Nondestructive testing
- CAD and design tools

Scientific

- Earthquake recording & analysis
- Data acquisition
- Spectral analysis
- Simulation and modeling

Signal and Sensor Perception

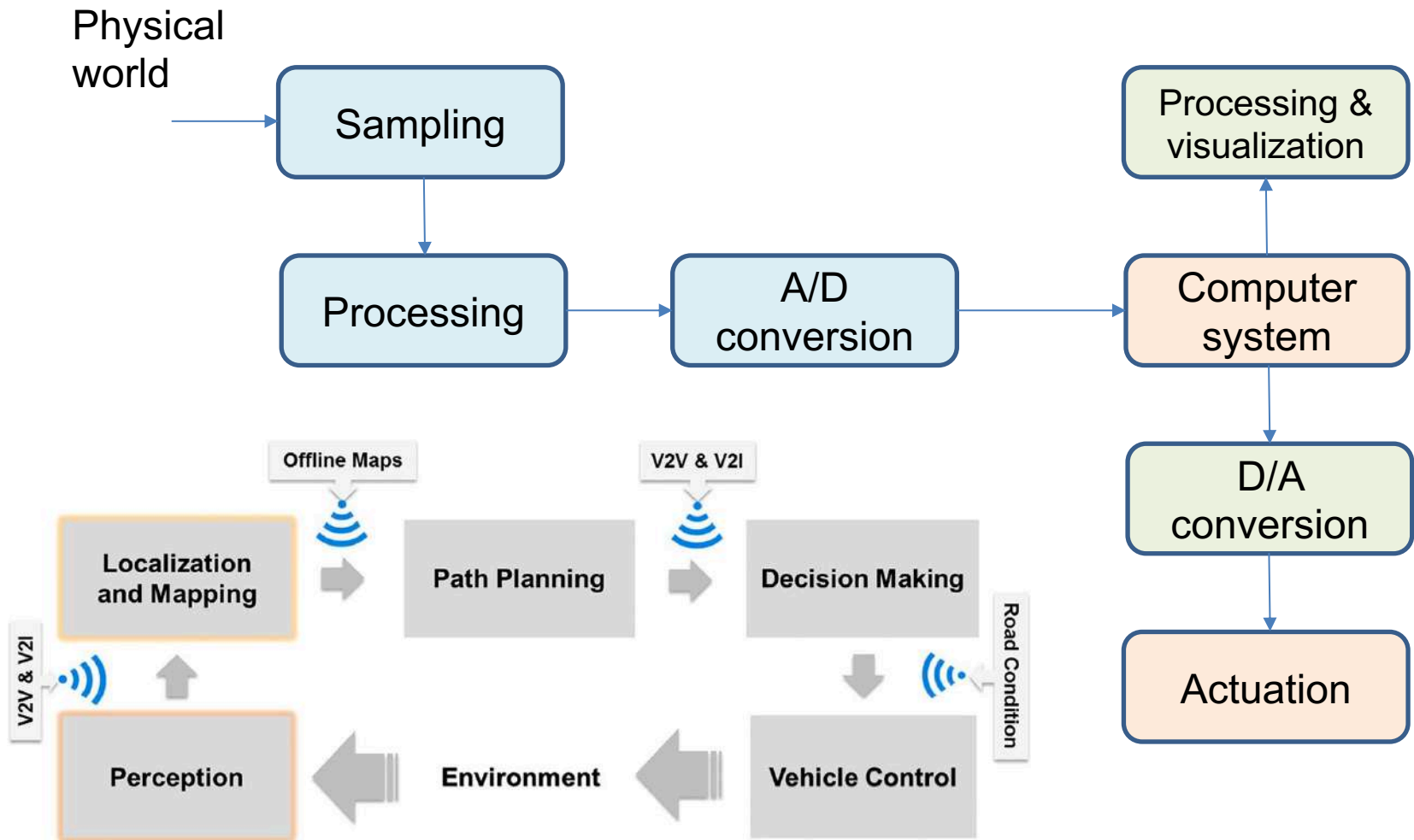
- Perception for physical quantities
Transduction principle - conversion of energy from one form to another
- Proprioception:
Position, speed, acceleration, torque, battery level ...
- Exteroceptive:
Scene, geometry, object, ...
- Analog signal
Continuity in
 - Time domain
 - Amplitude





Signal and Sensor Perception

- Sensor perception → vehicle actuator control

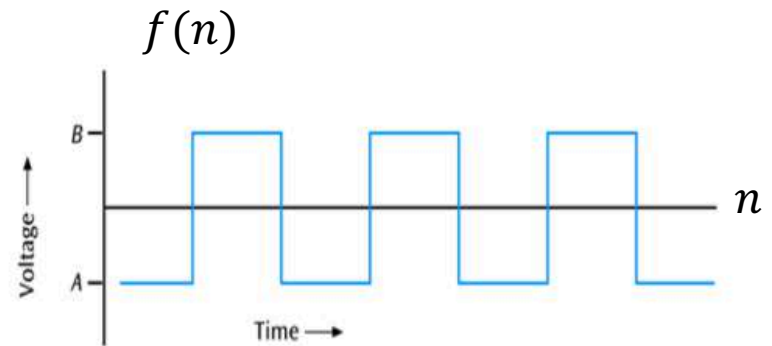
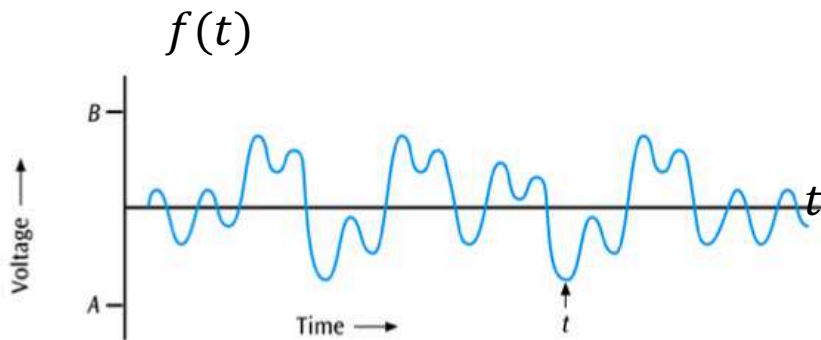




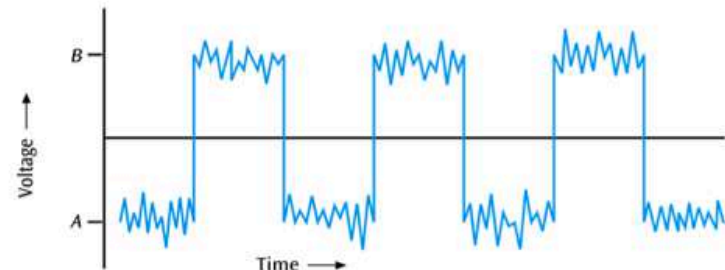
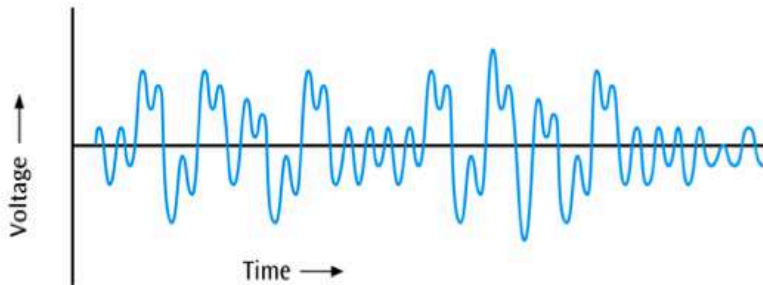
Signal and Sensor Perception

- Analog signal VS. Digital signal

A/D (Analog-to-Digital)



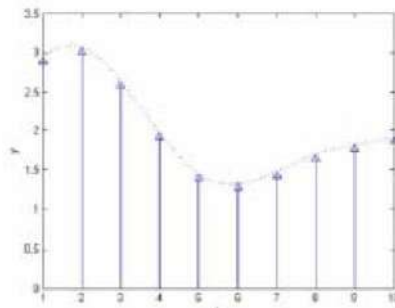
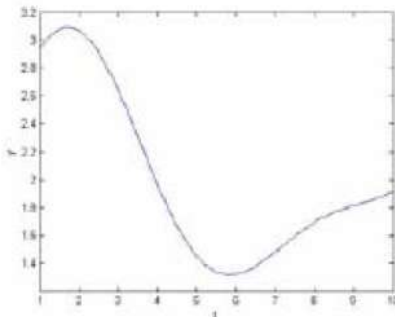
Affected by noise or EMI (Electromagnetic interference)



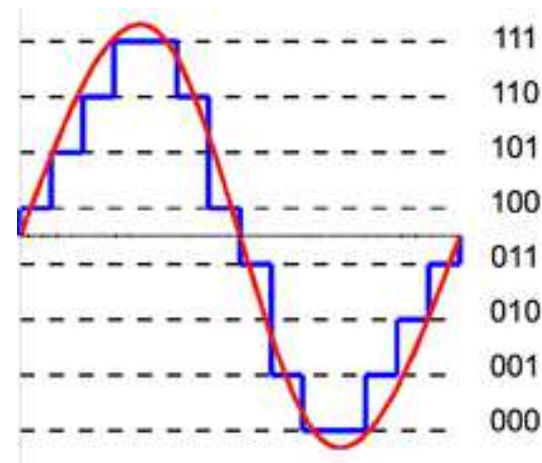


Signal A/D (Analog-to-Digital)

- Sampling
 - From continuous signal to discrete signal
- PCM (Pulse Code Modulation)
 - Sampling \rightarrow Quantization \rightarrow Encoding



Uniform quantization

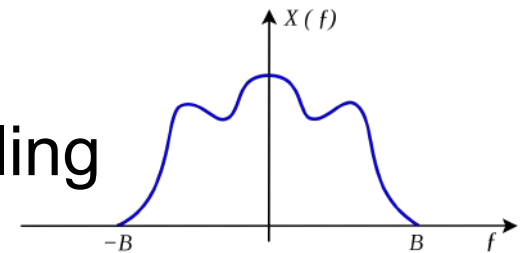


Binary encoding



Signal A/D (Analog-to-Digital)

- Sampling
- Nyquist–Shannon sampling theorem (Harry Nyquist and Claude Shannon)
- Sufficient no-loss condition for sampling
 - Nyquist sampling rate: $2B$
- Usage example:
 - The frequency of human voice is mostly less than 5kHz, ...
- Signal analysis
 - Time domain analysis
 - Frequency domain analysis
 - Time-Frequency domain analysis





Time Domain Analysis

- The expectation (μ_x) of a signal (or called mean)

$$\mu_x = E[x(t)] = \frac{1}{T} \lim \int_0^T x(t) dt$$

- Mean square (A_{RMS}^2) and root mean square (RMS) (A_{RMS}) of a signal

$$A_{RMS}^2 = E[x^2(t)] = \frac{1}{T} \lim \int_0^T x^2(t) dt$$

- Variance (σ^2) and standard deviation (σ) of a signal

$$\sigma^2 = E[(x(t) - \mu_x)^2] = \frac{1}{T} \lim \int_0^T (x(t) - \mu_x)^2 dt$$



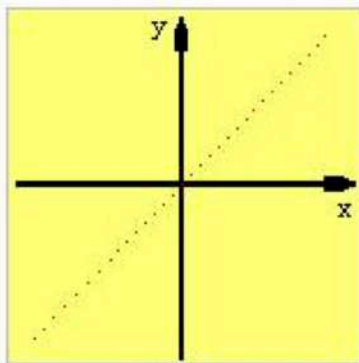
Time Domain Analysis

- Covariance

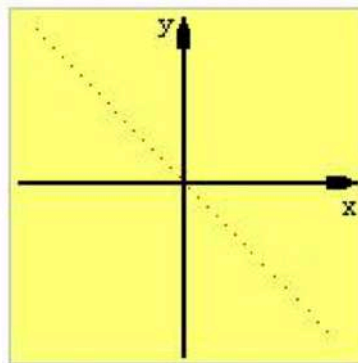
$$\text{cov}(x, y) (= E[(x(t) - \mu_x)(y(t) - \mu_y)])$$

- Statistical correlation

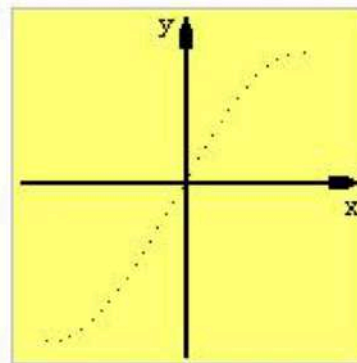
$$\rho_{xy} = \frac{\text{cov}(x, y)}{\sigma_x \sigma_y} = \frac{E[(x(i) - \mu_x)(y(i) - \mu_y)]}{\sqrt{E[(x(i) - \mu_x)^2]E[(y(i) - \mu_y)^2]}}$$



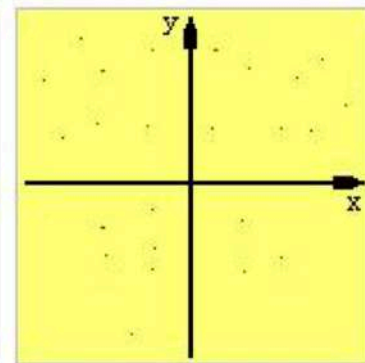
$$\rho_{xy} = 1$$



$$\rho_{xy} = -1$$



$$0 \leq \rho_{xy} \leq 1$$



$$\rho_{xy} = 0$$

Relationship?

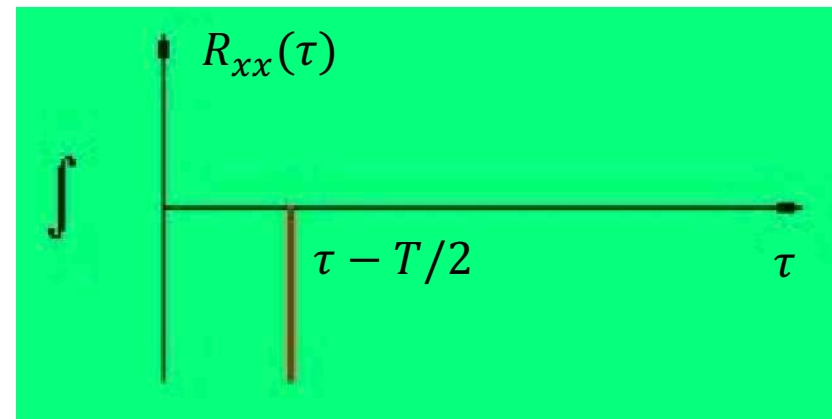
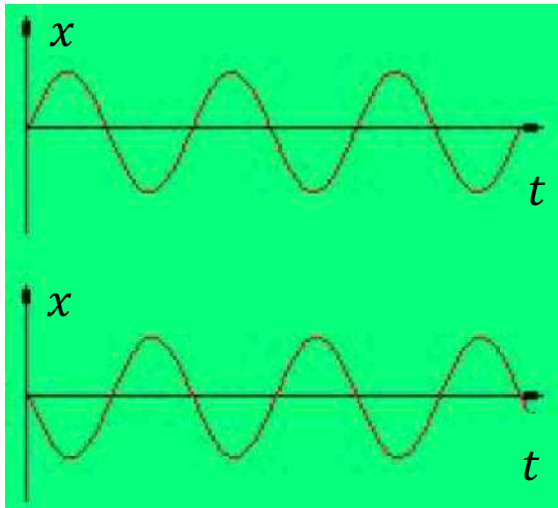


Time Domain Analysis

- Correlation function for continuous signals

$$R_{xy}(\tau) = \lim_{T \rightarrow \infty} \int_{-T/2}^T x(t)y(t - \tau)$$

- Auto-correlation function $R_{xx}(\tau)$



Similarity between two signals, or one signal with time shift

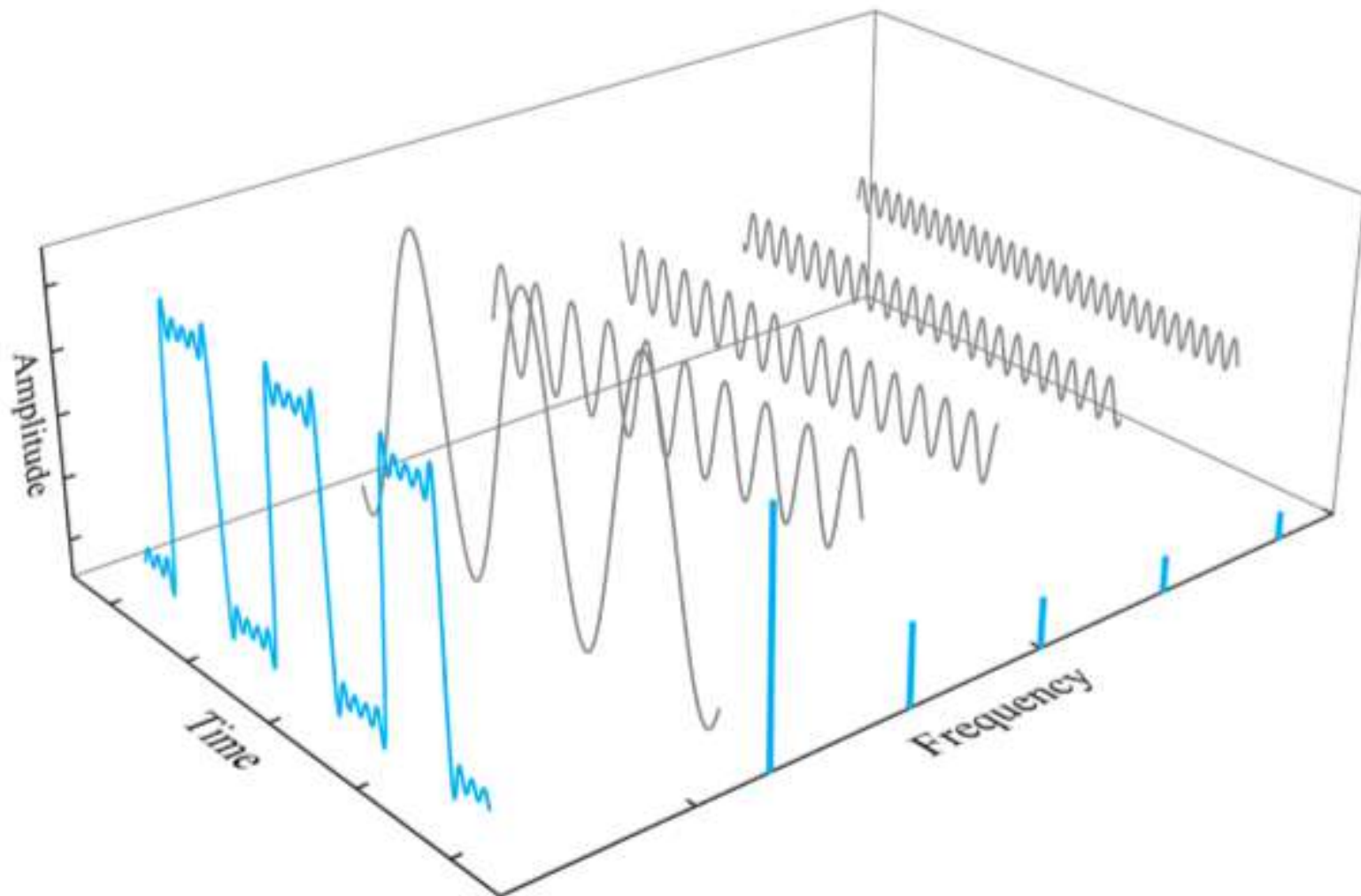


Time Domain Analysis

- Time-domain operations for digital signals
 - Amplitude modifications $y[k] = a \sum x_m[k] + b$
 - Time modifications $y[k] = x[k - m]$
 - Down-sampling $y[k] = x[\lambda k]$
 - Up-sampling or interpolation
 - Cross-correlation (\otimes): $y[k] = \sum_{n=-\infty}^{\infty} x_1[n]x_2[n - k]$
 - Auto-correlation $y[k] = \sum_{n=-\infty}^{\infty} x[n]x[n - k]$
 - Convolution ($*$): $y[k] = \sum_{n=-\infty}^{\infty} x_1[n]x_2[k - n]$



Signal Frequency Analysis





Signal Frequency Analysis

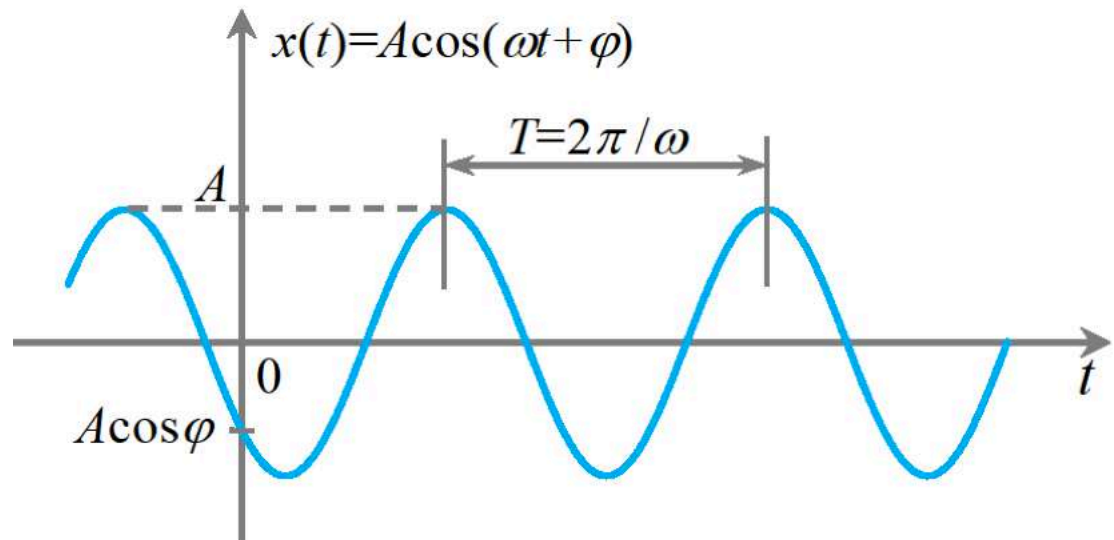
- Frequency domain
- A typical signal: *sin* wave

$$x(t) = A \cos(\omega t + \varphi)$$

Amplitude: A

Frequency: $f = \omega / 2\pi$

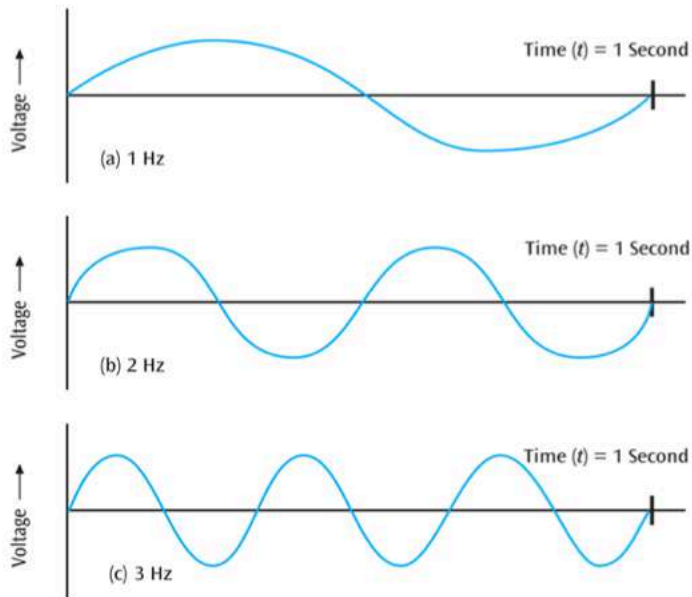
Phase: φ





Signal Frequency Analysis

- Frequency of a signal



Constant-amplitude signal?



Step signal?





Signal Frequency Analysis

- Fourier transform and inverse transform
(under Dirichlet condition of convergence)

$$X(\omega) = \int_{-\infty}^{\infty} x(t) e^{-j\omega t} dt$$
$$x(t) = \int_{-\infty}^{\infty} X(\omega) e^{j\omega t} d\omega$$

- Fourier series expansion
DFT (Discrete-time Fourier Transform)

$$x(t) = \sum_{k=-\infty}^{\infty} A_k \cos(k\omega_0 t + \varphi_k), \omega_0 = 2\pi/T$$

Decomposes periodic complex signal to a (possibly infinite) set of simple sine waves;

Applicable for aperiodic signal, considering $T \rightarrow \infty$



Signal Frequency Analysis

- Given Euler's formula

$$e^{j\theta} = \cos(\theta) + j\sin(\theta), \theta = \omega t, \cos(\omega t) = \frac{e^{j\omega t} + e^{-j\omega t}}{2}$$

$$\text{Then: } A\cos(\omega t + \varphi) = \frac{A}{2} e^{j(\omega t + \varphi)} + \frac{A}{2} e^{-j(\omega t + \varphi)}$$

- Exponential form of Fourier series

$$x(t) = \sum_{k=-\infty}^{\infty} X_k e^{jk\omega_0 t}$$

where X_k are complex numbers:

$$X_k = \frac{1}{T} \int_0^T x(t) e^{-jk\omega_0 t} dt$$

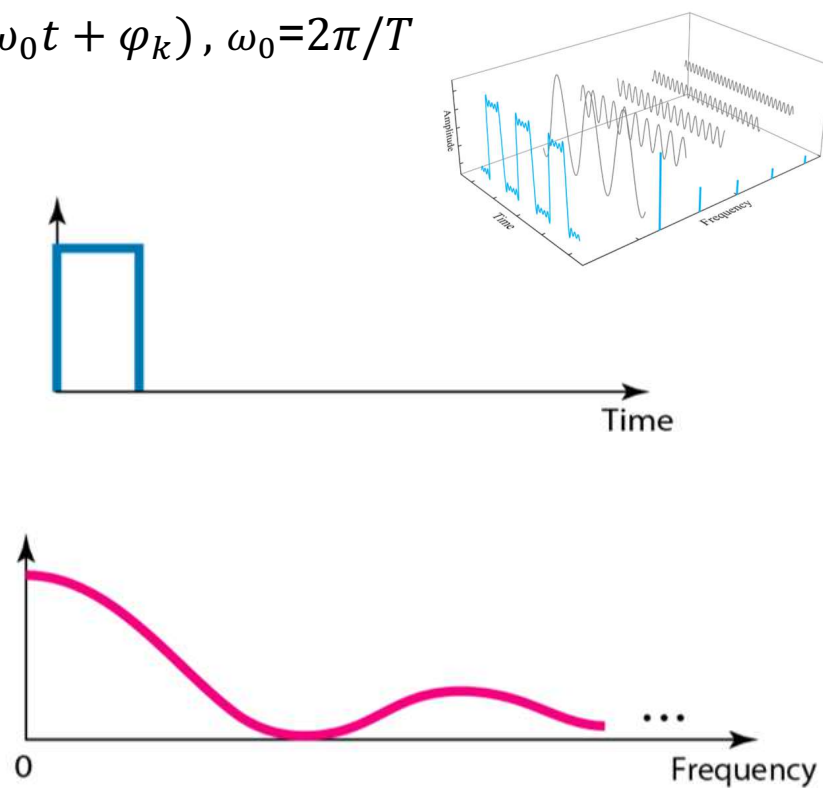
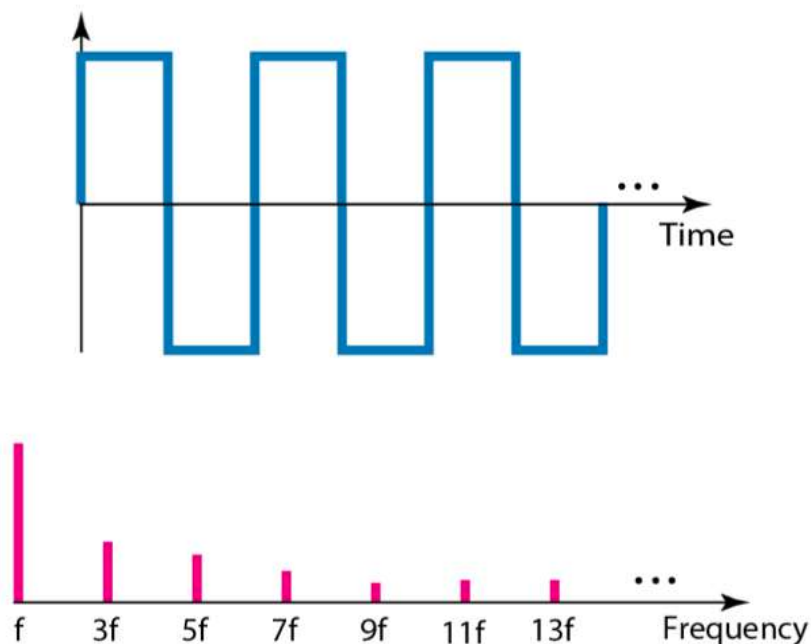
- For each frequency components:

Frequencies $k\omega_0$; Amplitude $|X_k|$; Phase $\arctan \frac{\text{Im}(X_k)}{\text{Re}(X_k)}$, atan2

Signal Frequency Analysis

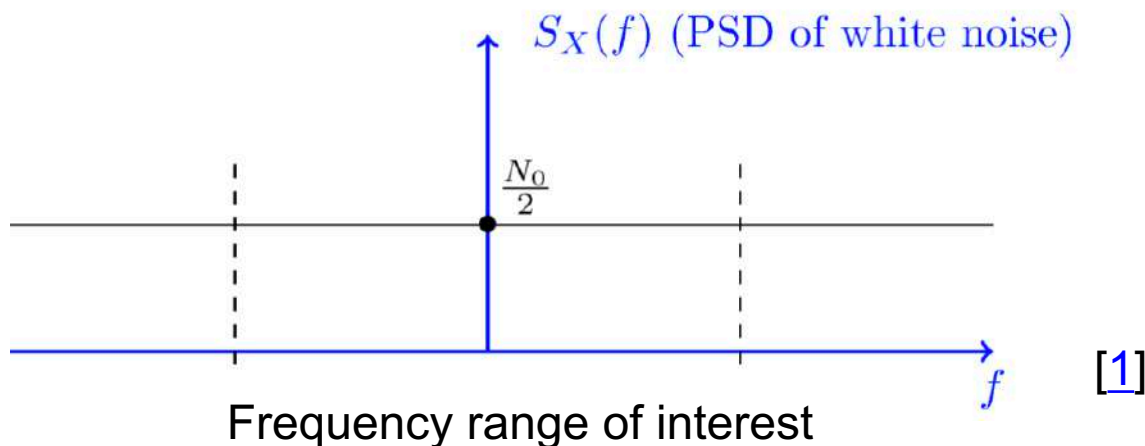
- DFT difference for periodic and aperiodic signal in Trigonometric series

$$x(t) = A_0 + \sum_{k=-\infty}^{\infty} A_k \cos(k\omega_0 t + \varphi_k), \quad \omega_0 = 2\pi/T$$



Signal Noise

- Fourier transformation: F
 - Time, Frequency
- Power Spectral
 - $F(y[k])$, where Auto-correlation $y[k] = \sum_{n=-\infty}^{\infty} x[n]x[n-k]$
 - Power Spectral Density (PSD): $|X(f)|^2$, X is the F of $x(k)$
- White noise
 - refers to "uniform power across the frequency".





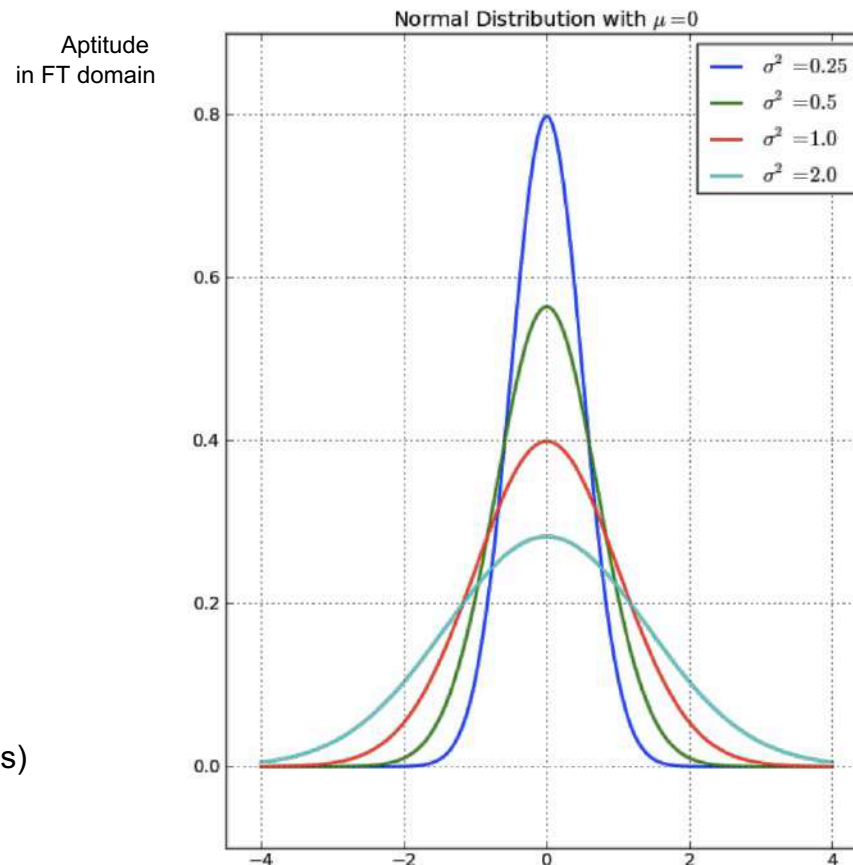
Signal Noise

- Gaussian noise
refers to "normal distribution in the frequency domain"

A Gaussian random variable W with
mean μ and
variance σ^2 has a PDF described by

$$f_W(w) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(w-\mu)^2}{2\sigma^2}}$$

- White Gaussian noise
(random sampling from Gaussian process)
 - Good approximation of many real-world situations;
 - Mathematically tractable models [\[2\]](#);



Signal Noise

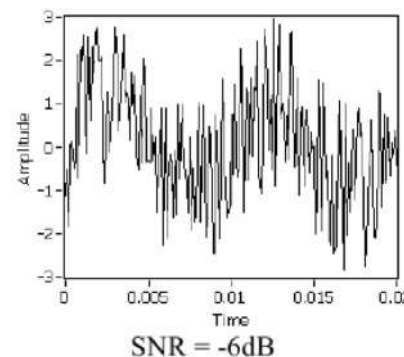
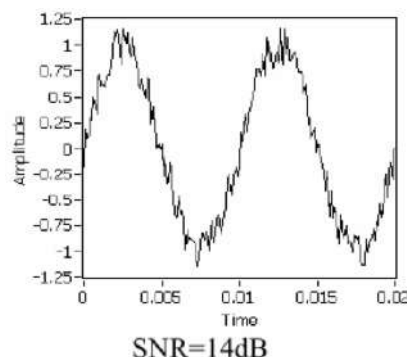
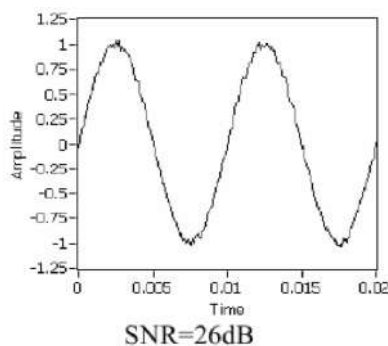
- Signal-to-noise ratio (**SNR**)

$$SNR = \frac{P_{signal}}{P_{noise}} = \left(\frac{A_{RMS,s}}{A_{RMS,n}} \right)^2$$

- Logarithmic decibel (dB) scale

$$P_{dB} = 10 \log_{10} P$$

$$SNR_{dB} = 10 \log_{10} \frac{P_{signal}}{P_{noise}} = 20 \log_{10} \frac{A_{RMS,s}}{A_{RMS,n}}$$



Signal Noise

- Naturally, sensor data is noisy.

- Hardware filters
- Algorithm filters



- Noise

- A general term for all unwanted (probably immeasurable) modifications during signal capturing to processing process.
- Wrong measurement doesn't belong to noise.

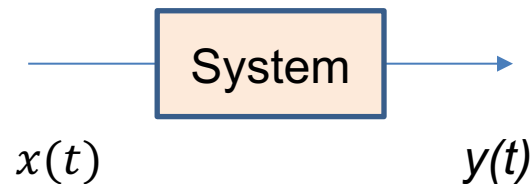
- Noise types

- Additive noise (White noise, Gaussian noise, Cauchy noise ...)
- Multiplicative noise (multiplies or modulates the intended signal)
- Quantization error (due to conversion from continuous to discrete values)
- Phase noise (random time shifts in a signal)
- et al.



Digital Signal Processing Systems

- From signal to systems



examples

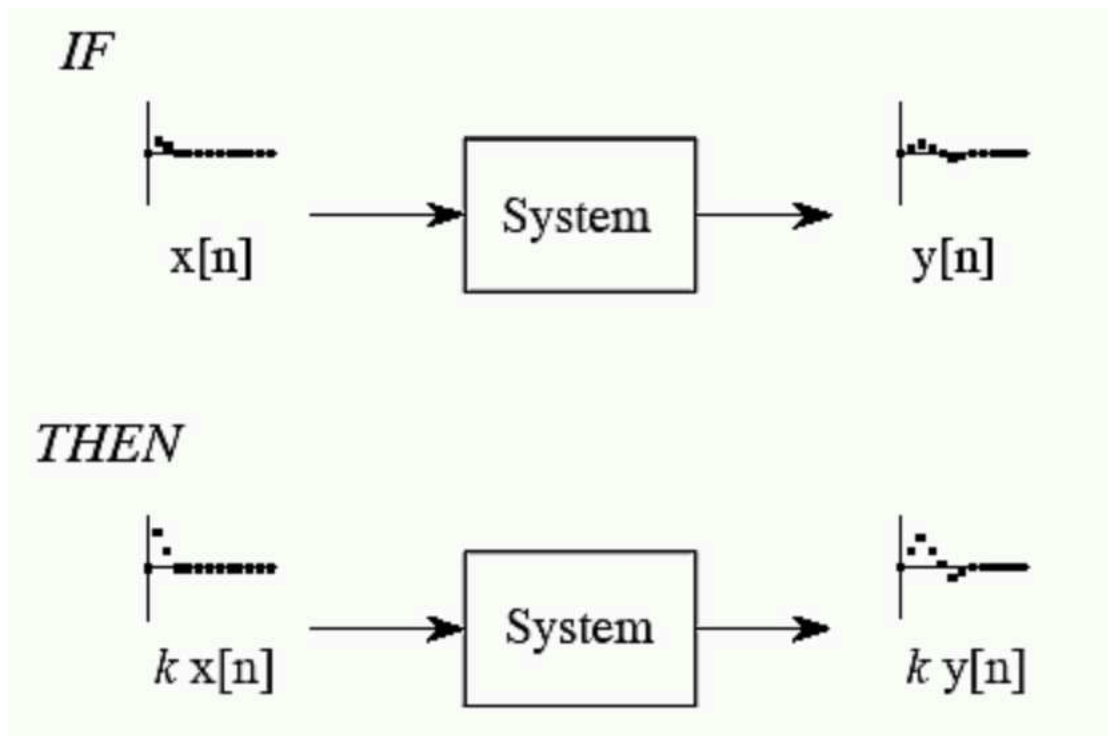
$x(t) \rightarrow \boxed{\int} \rightarrow y(t)$	$y(t)$	$\int_0^t x(\tau) d\tau$
$x(t) \rightarrow \boxed{A} \rightarrow y(t)$	$y(t)$	$Ax(t)$
$x(t) \rightarrow \boxed{\otimes} \rightarrow y(t)$	$y(t)$	$x_1(t)x_2(t)$
$x(t) \rightarrow \boxed{\oplus} \rightarrow y(t)$	$y(t)$	$x_1(t) + x_2(t)$

- Linear VS. Non-linear systems
- Characteristics of linear system
 - Homogeneity
 - Additivity
- Linear Time-invariant (LTI):
 $y(t)$ for $x(t) \rightarrow y(t - T)$ for $x(t - T)$



Digital Signal Processing Systems

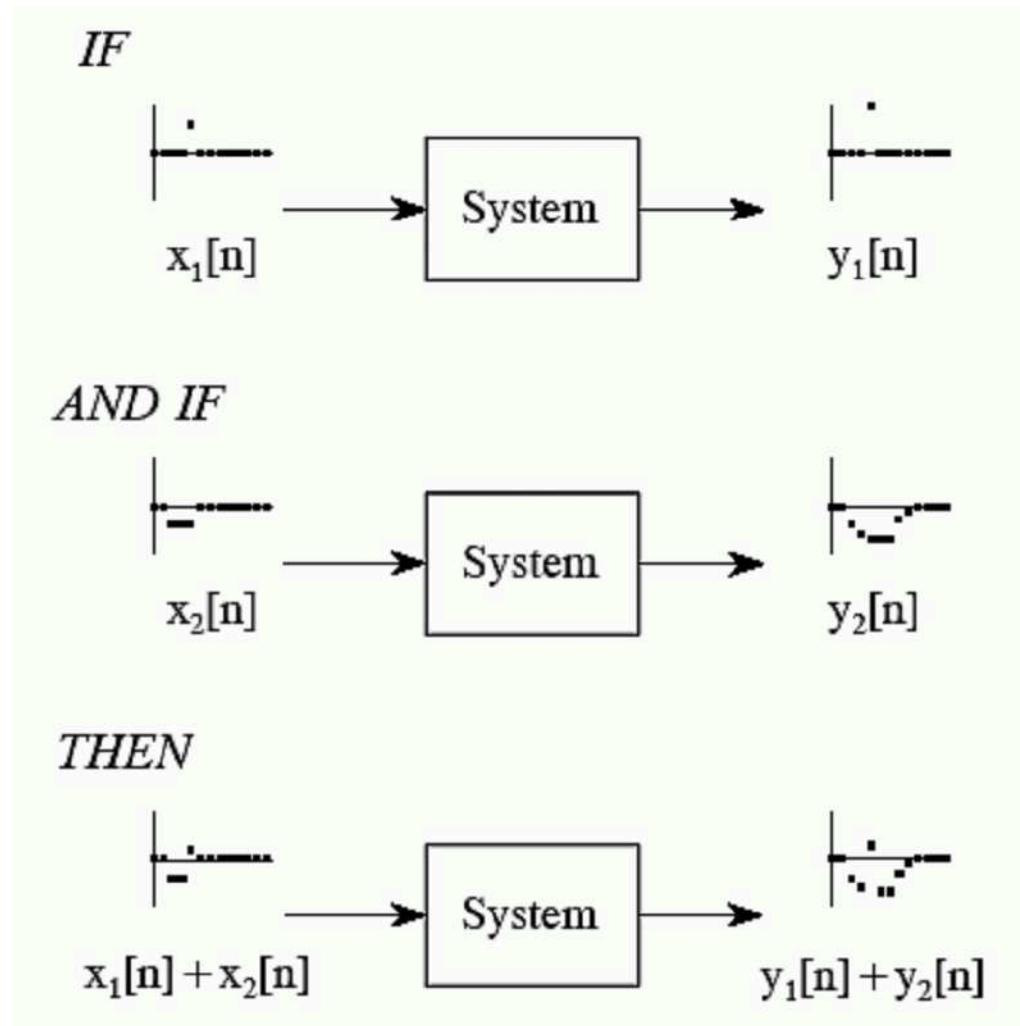
- Homogeneity of linear systems





Digital Signal Processing Systems

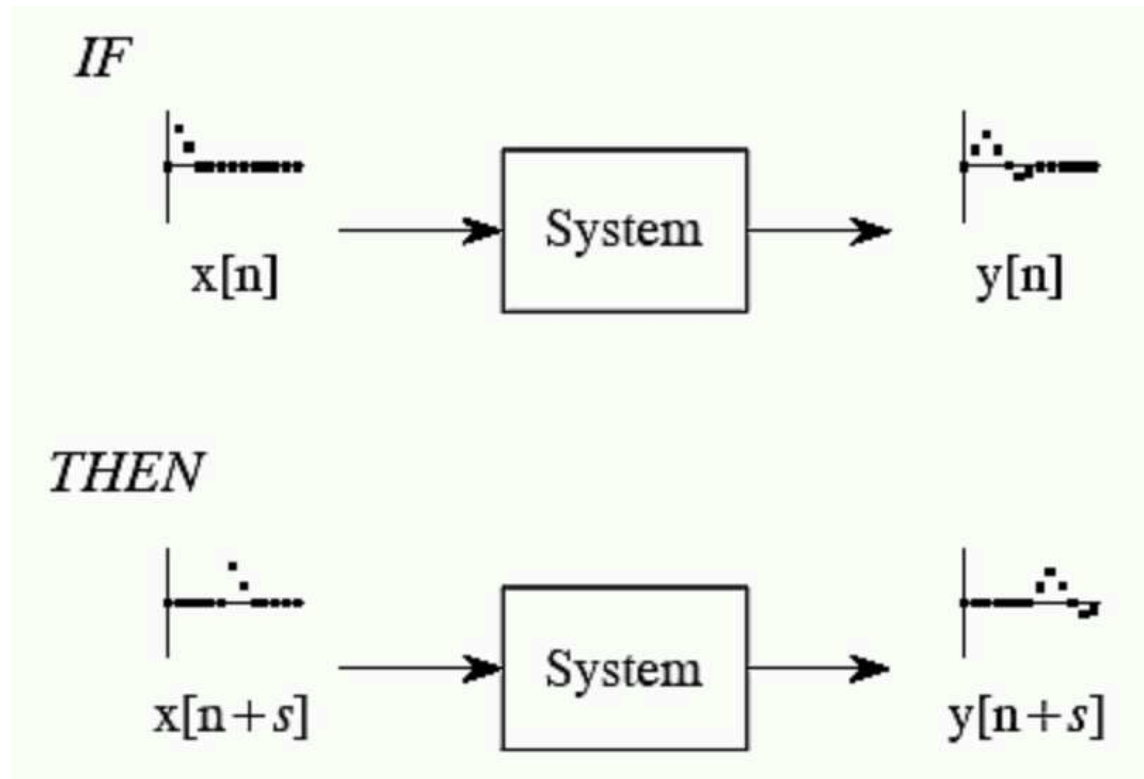
- Additivity of linear systems





Digital Signal Processing Systems

- Time-invariant systems



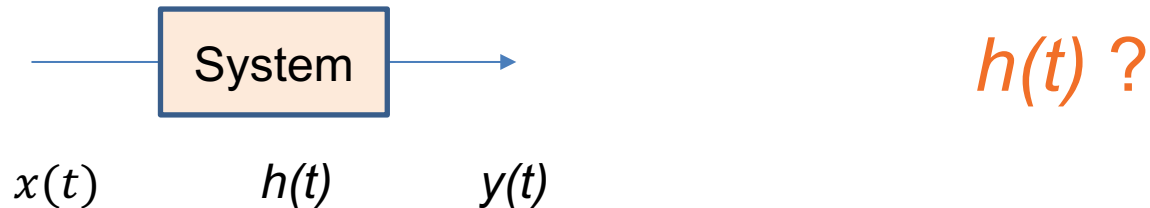
Important !

The characteristics of the system do not change with time.



Digital Signal Processing Systems

- System analysis

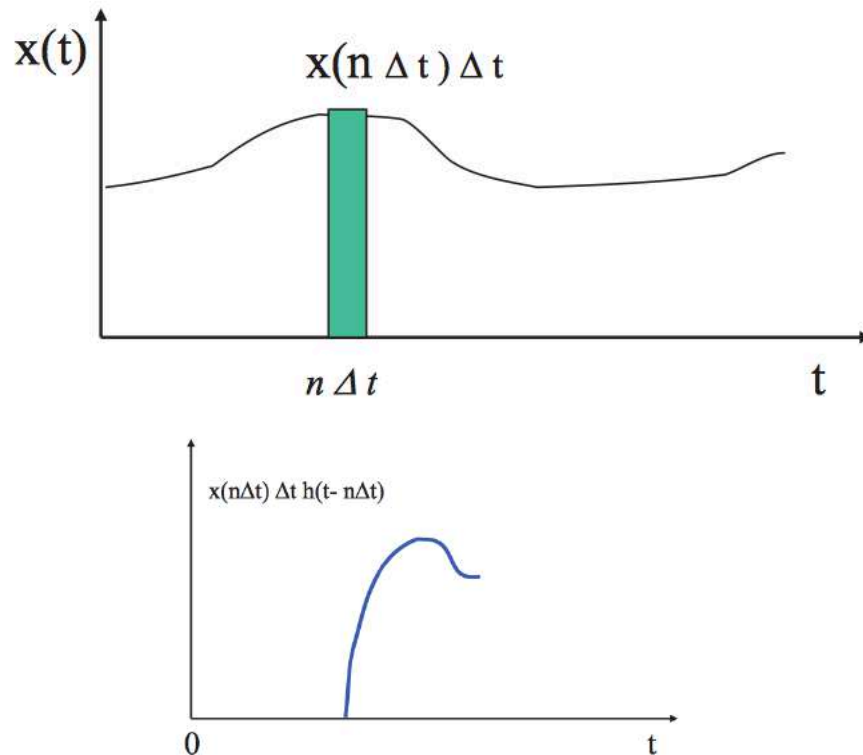


- How to mathematically describe a system?
- How to design such a system?



Digital Signal Processing Systems

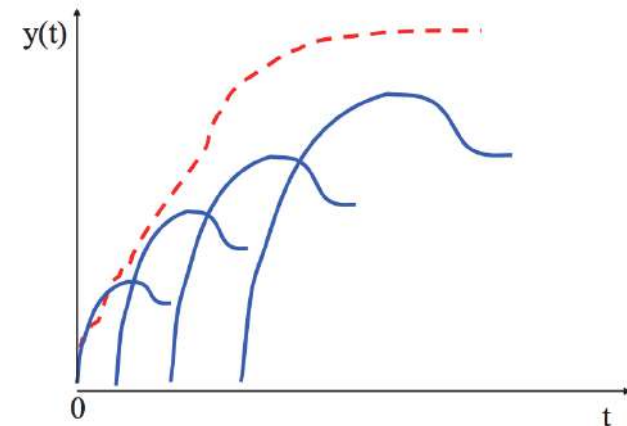
- System response



Response:

$$x(n\Delta t)\Delta t h(t - n\Delta t)$$

$$y(t) = \sum_{n=0}^{\infty} x(n\Delta t)\Delta t h(t - n\Delta t)$$



Signal convolution:

$$\begin{aligned} y(t) &= x(t) * h(t) \\ &= \int_{-\infty}^{\infty} x(\tau)h(t - \tau)d\tau \end{aligned}$$

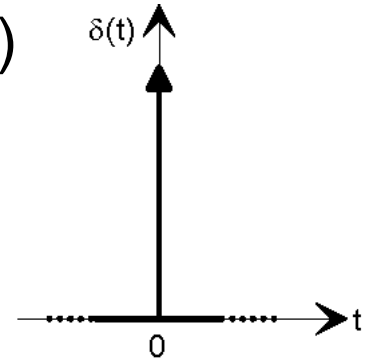


Digital Signal Processing Systems

- (Unit) Delta function (impulse signal, Paul Dirac)

$$\delta(t - \tau_0) = 0, x \neq 0$$

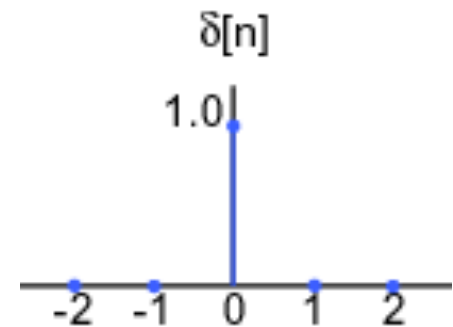
$$\lim_{\varepsilon \rightarrow 0} \int_{\tau_0 - \varepsilon}^{\tau_0 + \varepsilon} \delta(t - \tau_0) dt = 1$$



- Characteristic

$$x(\tau_0) = \int_{-\infty}^{\infty} x(t) \delta(t - \tau_0) dt$$

$$x[n] = \sum_{k=-\infty}^{\infty} x[k] \delta(n - k)$$



- $h(t)$ is defined as impulse response, which is the system response when input signal is $\delta(t)$



Digital Signal Processing Systems

- We have seen signal can be characterized by frequency content (pros?)
- LTI system analysis
 - Time-domain impulse response $h(t)$
 - Frequency response --- $H(\omega)$?
- For system analysis, introduce dampening factor, and Laplace transform and z transform:

$$L(\omega) = \int_{-\infty}^{\infty} x(t)e^{-(\sigma+j\omega)t}dt \rightarrow L(s) = \int_{-\infty}^{\infty} x(t)e^{-st}dt, \text{ where } s = \sigma + j\omega$$

For discrete signal: $X(z) = \sum_{-\infty}^{\infty} x[n]z^{-n}$,
 where $z = e^{sT} = r e^{j\omega}$

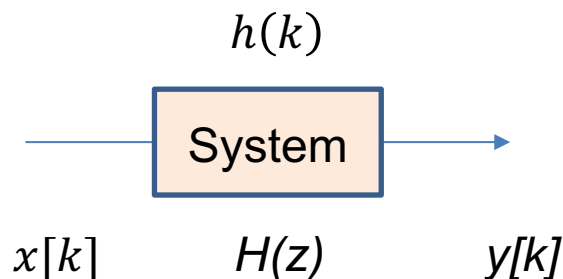
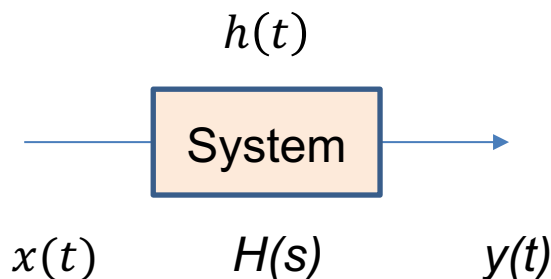
Digital Signal Processing Systems

- All three transforms convert time-domain convolutions to polynomial equations

$$y(t) = x(t) * h(t) = \int_{-\infty}^{\infty} x(\tau)h(t - \tau)d\tau$$

$$Y(\omega) = H(\omega)X(\omega), Y(s) = H(s)X(s), Y(z) = H(z)X(z)$$

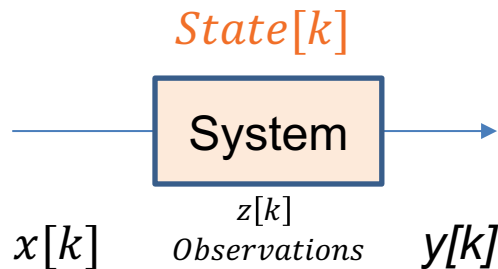
- Why Laplace transform and z transform?
 - Complex frequency-domain for Stability and Causality analysis





Digital Filter Design

- State-space filter



Using dynamic model

e.g.: Kalman filter

$$\bar{\mu}_t = A_t \mu_{t-1} + B_t u_t$$

$$\bar{\Sigma}_t = A_t \Sigma_{t-1} A_t^T + R_t$$

$$K_t = \bar{\Sigma}_t C_t^T (C_t \bar{\Sigma}_t C_t^T + Q_t)^{-1}$$

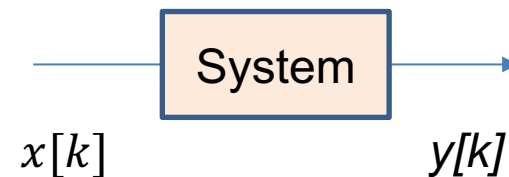
$$\mu_t = \bar{\mu}_t + K_t (z_t - C_t \bar{\mu}_t)$$

$$\Sigma_t = (I - K_t C_t) \bar{\Sigma}_t$$

- Conventional digital filters

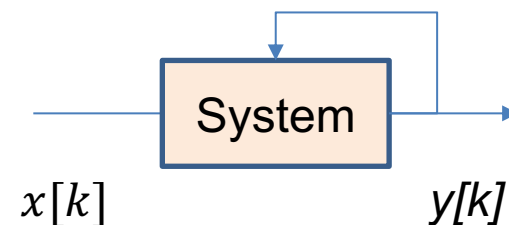
Finite Impulse Response (FIR) filters:

$$y[k] = \sum_{n=0}^N b_n x[k - n]$$



Infinite Impulse Response (IIR) filters:

$$y[k] = \sum_{n=0}^N b_n x[k - n] + \sum_{m=0}^M a_m y[k - m]$$





Digital Filter Design

- FIR Filters

- Pros:

- Inherently stable
 - Linear phase characteristics

- Cons:

- Need lots of memory and math terms required

- IIR Filters

- Pros:

- Very efficient in term of resources

- Cons:

- Inherently less stable

Design approaches:

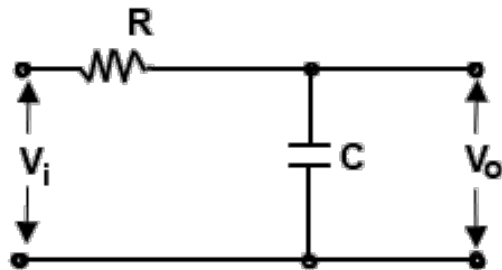
Frequency sampling design
Fourier transform design

Bilinear transformation
Pole zero placement

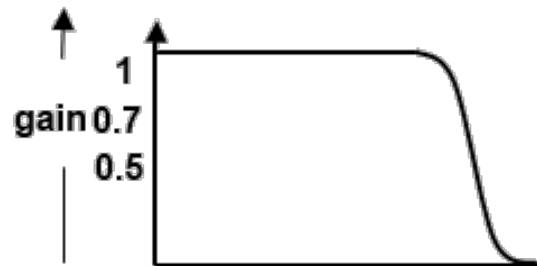


Digital Filter Design

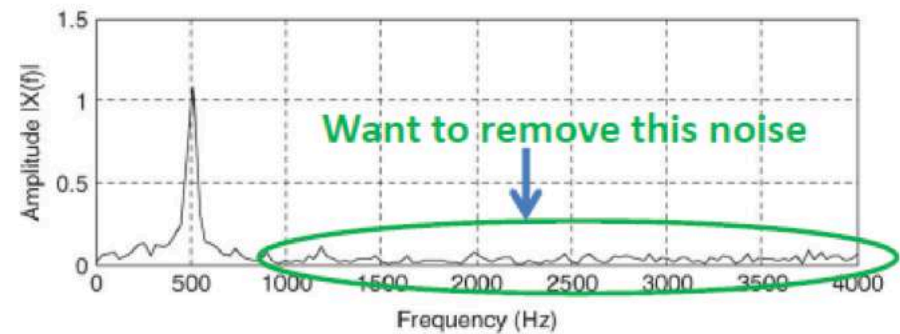
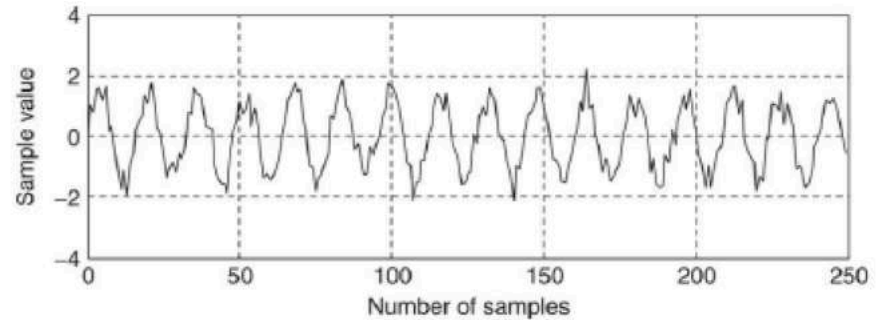
- Example: low pass filter design



(a) RC low Pass Filter Circuit



(b) Frequency Response Curve





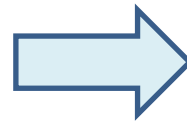
Digital Filter Design

- 1st example: A simple average digital filter:

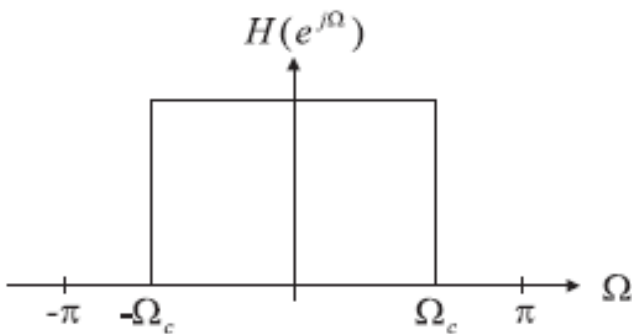
$$y[k] = \frac{1}{4} (x[k] + 2x[k-1] + x[k-2])$$

- 2nd example: (ideal) FIR low pass filter (LPF) design [[1](#)]

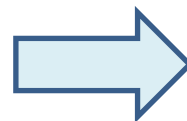
$$y[k] = \sum_{n=0}^N b_n x[k-n]$$



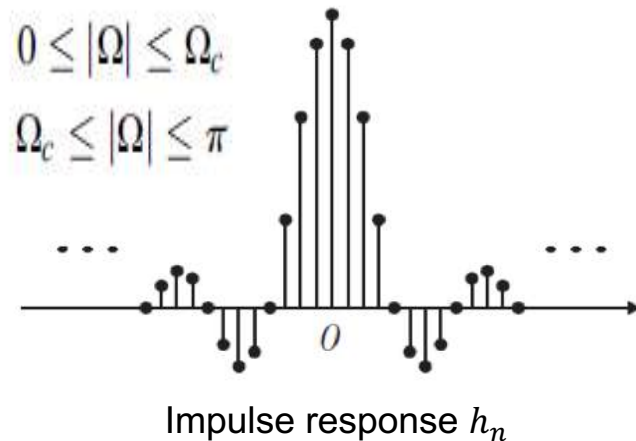
b_n : filter coefficients
(aka: kernel)



$$H(e^{j\Omega}) = \begin{cases} 1, & 0 \leq |\Omega| \leq \Omega_c \\ 0, & \Omega_c \leq |\Omega| \leq \pi \end{cases}$$



Inverse FFT

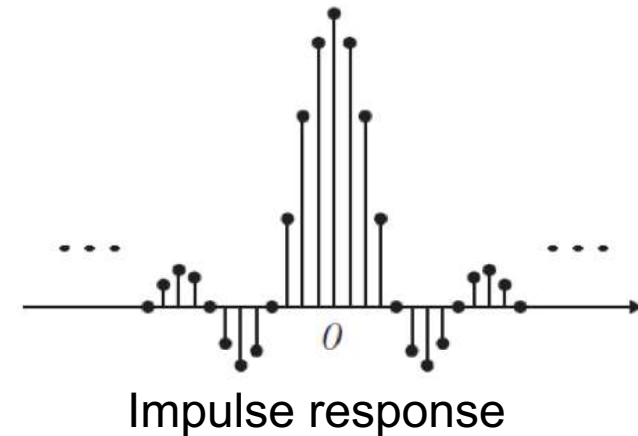




Digital Filter Design

- (ideal) FIR low pass filter design [1]

- $h_n \rightarrow z$ transformation $H(z)$



$$H(z) = h(M)z^M + \cdots + h(1)z^1 + h(0) + h(1)z^{-1} + \cdots + h(M)z^{-M}$$

Symmetric

Two blue arrows point from the word "Symmetric" to the terms $h(M)z^M$ and $h(M)z^{-M}$ in the equation above, highlighting the coefficient symmetry.

By After truncating $2M+1$ major components using the coefficient symmetry, where h_n is just a shift of b_n for causal design.



Digital Filter Design

Filter	Type	Ideal Impulse Response $h(n)$ (noncausal FIR coefficients)
Lowpass:		$h(n) = \begin{cases} \frac{\Omega_c}{\pi} & \text{for } n = 0 \\ \frac{\sin(\Omega_c n)}{n\pi} & \text{for } n \neq 0 \end{cases} \quad -M \leq n \leq M$
Highpass:		$h(n) = \begin{cases} \frac{\pi - \Omega_c}{\pi} & \text{for } n = 0 \\ -\frac{\sin(\Omega_c n)}{n\pi} & \text{for } n \neq 0 \end{cases} \quad -M \leq n \leq M$
Bandpass:		$h(n) = \begin{cases} \frac{\Omega_H - \Omega_L}{\pi} & \text{for } n = 0 \\ \frac{\sin(\Omega_H n)}{n\pi} - \frac{\sin(\Omega_L n)}{n\pi} & \text{for } n \neq 0 \end{cases} \quad -M \leq n \leq M$
Bandstop:		$h(n) = \begin{cases} \frac{\pi - \Omega_H + \Omega_L}{\pi} & \text{for } n = 0 \\ -\frac{\sin(\Omega_H n)}{n\pi} + \frac{\sin(\Omega_L n)}{n\pi} & \text{for } n \neq 0 \end{cases} \quad -M \leq n \leq M$



Digital Filter Design

- (ideal) FIR low pass filter design [1]
- **Example:** Design a 3-tap FIR LPF with cut-off frequency of 800 Hz and a sampling rate of 8,000 Hz using the Fourier transform method.

Normalized cut-off frequency →

$$\Omega_c = 2\pi f_c T_s = 2\pi \times 800 / 8,000 = 0.2\pi \text{ radians}$$

3-tap filter → $2M + 1 = 3$ → $M = 1$

→ $h(n)$ for n from $-M$ to M → $n = -1, 0, 1,$



Digital Filter Design

- (ideal) FIR low pass filter design [1]

filter coefficients $\Rightarrow h(0) = \frac{\Omega_c}{\pi}$ for $n = 0$
From previous slide table

and
$$h(n) = \frac{\sin(\Omega_c n)}{n\pi} = \frac{\sin(0.2\pi n)}{n\pi} \quad \text{for } n \neq 0$$

compute coefficients $\Rightarrow h(0) = \frac{0.2\pi}{\pi} = 0.2$

and
$$h(1) = \frac{\sin[0.2\pi \times 1]}{1 \times \pi} = 0.1871$$

Using symmetry $\Rightarrow h(-1) = h(1) = 0.1871$



Digital Filter Design

- (ideal) FIR low pass filter design [1]

Delaying $h(n)$ by
 $M = 1$ sample

$$\Rightarrow b_n = h(n - M)$$

for $n = 0, 1, \dots, 2M$.

$$\Rightarrow \begin{cases} b_0 = h(0 - 1) = h(-1) = 0.1871 \\ b_1 = h(1 - 1) = h(0) = 0.2 \\ b_2 = h(2 - 1) = h(1) = 0.1871 \end{cases}$$

FIR low pass filter: transfer function

$$H(z) = 0.1871 + 0.2z^{-1} + 0.1871z^{-2} \Rightarrow \frac{Y(z)}{X(z)} = H(z) = 0.1871 + 0.2z^{-1} + 0.1871z^{-2}$$

$$\Rightarrow Y(z) = 0.1871X(z) + 0.2z^{-1}X(z) + 0.1871z^{-2}X(z)$$

Digital Filter Design

- (ideal) FIR low pass filter design [1]
- Further discussion
 - Undesirable Gibbs oscillations
 - Solution: window functions

1. Rectangular window:

$$w_{\text{rec}}(n) = 1, -M \leq n \leq M$$

2. Triangular (Bartlett) window:

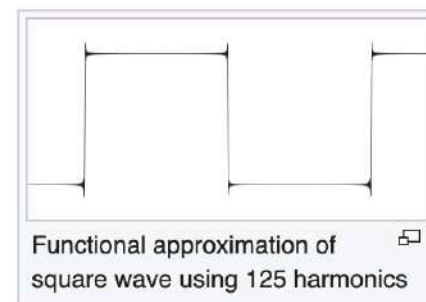
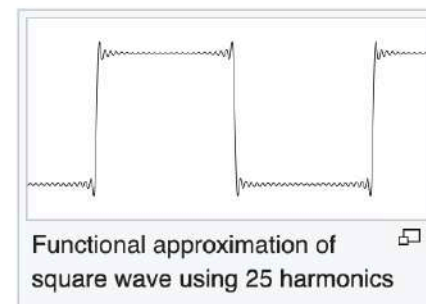
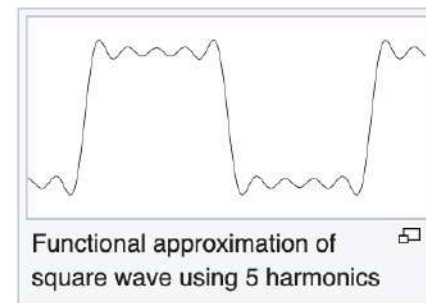
$$w_{\text{tri}}(n) = 1 - \frac{|n|}{M}, -M \leq n \leq M$$

3. Hanning window:

$$w_{\text{han}}(n) = 0.5 + 0.5 \cos\left(\frac{n\pi}{M}\right), -M \leq n \leq M$$

Applying the window sequence $w(n)$ to the filter coefficients

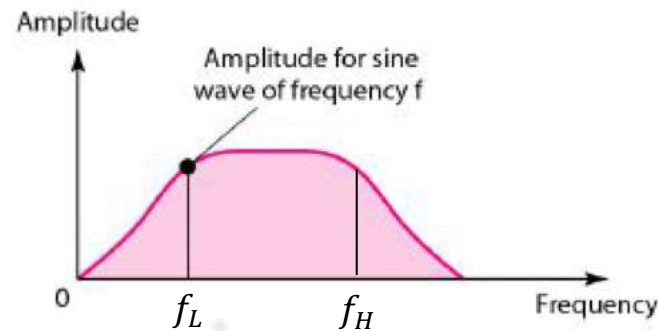
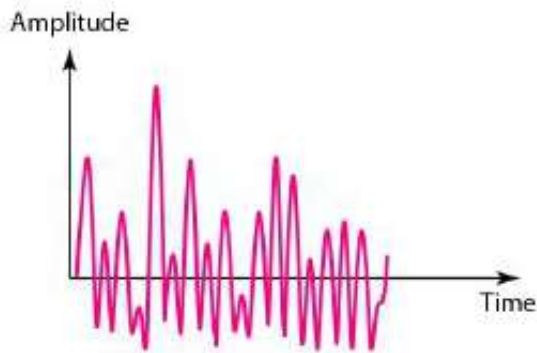
$$h_w(n) = h(n) \cdot w(n)$$





Spectrum in Frequency Domain

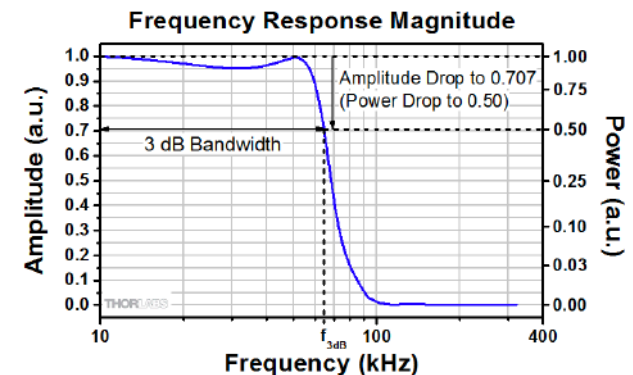
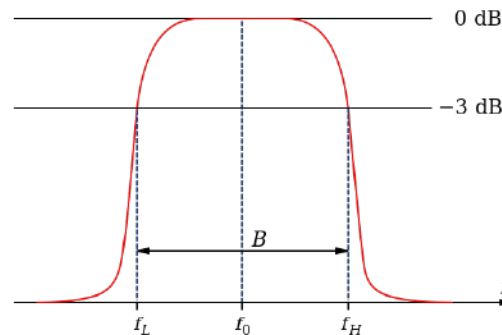
- Frequency spectrum to bandwidth



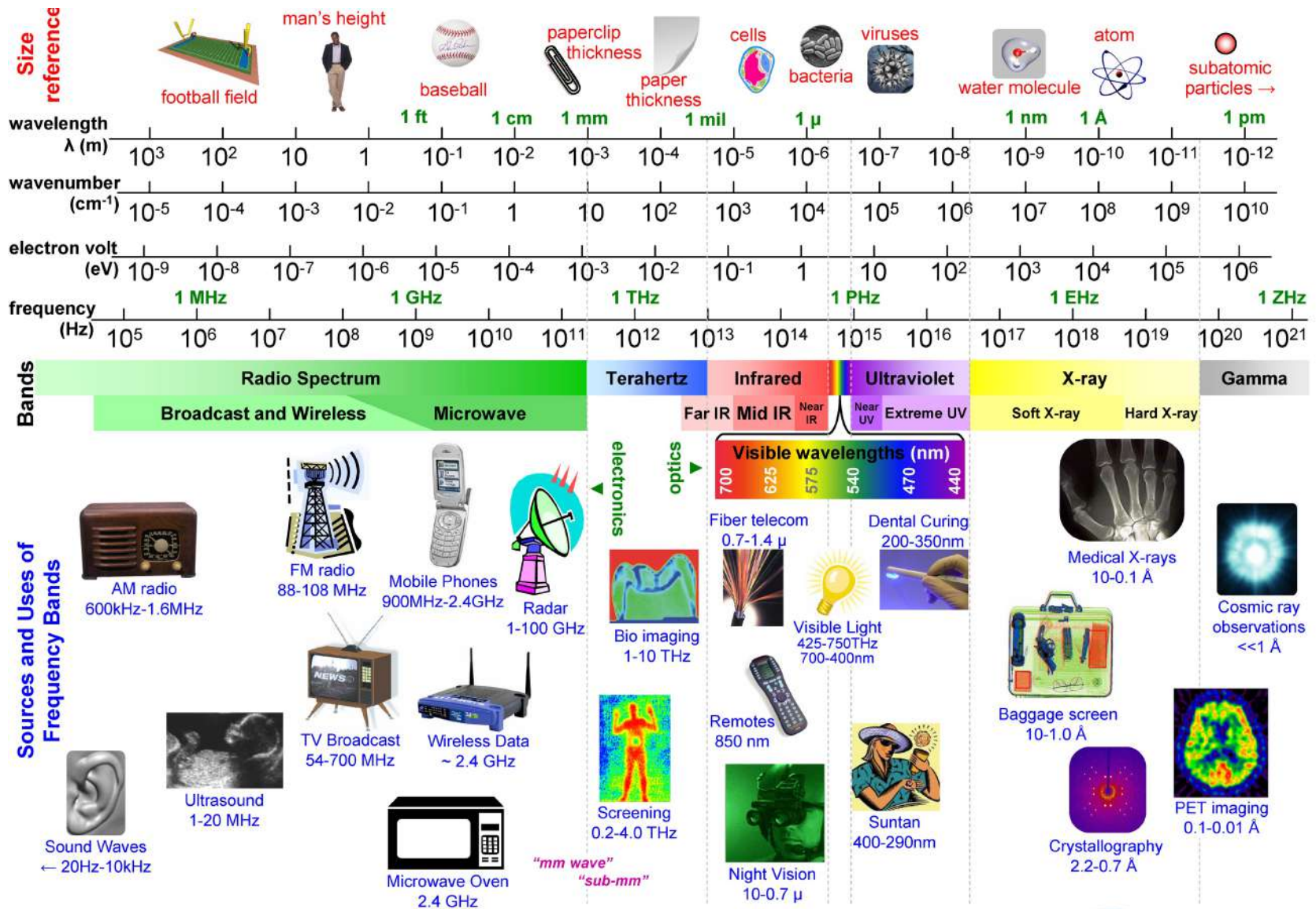
Bandwidth

Effective bandwidth

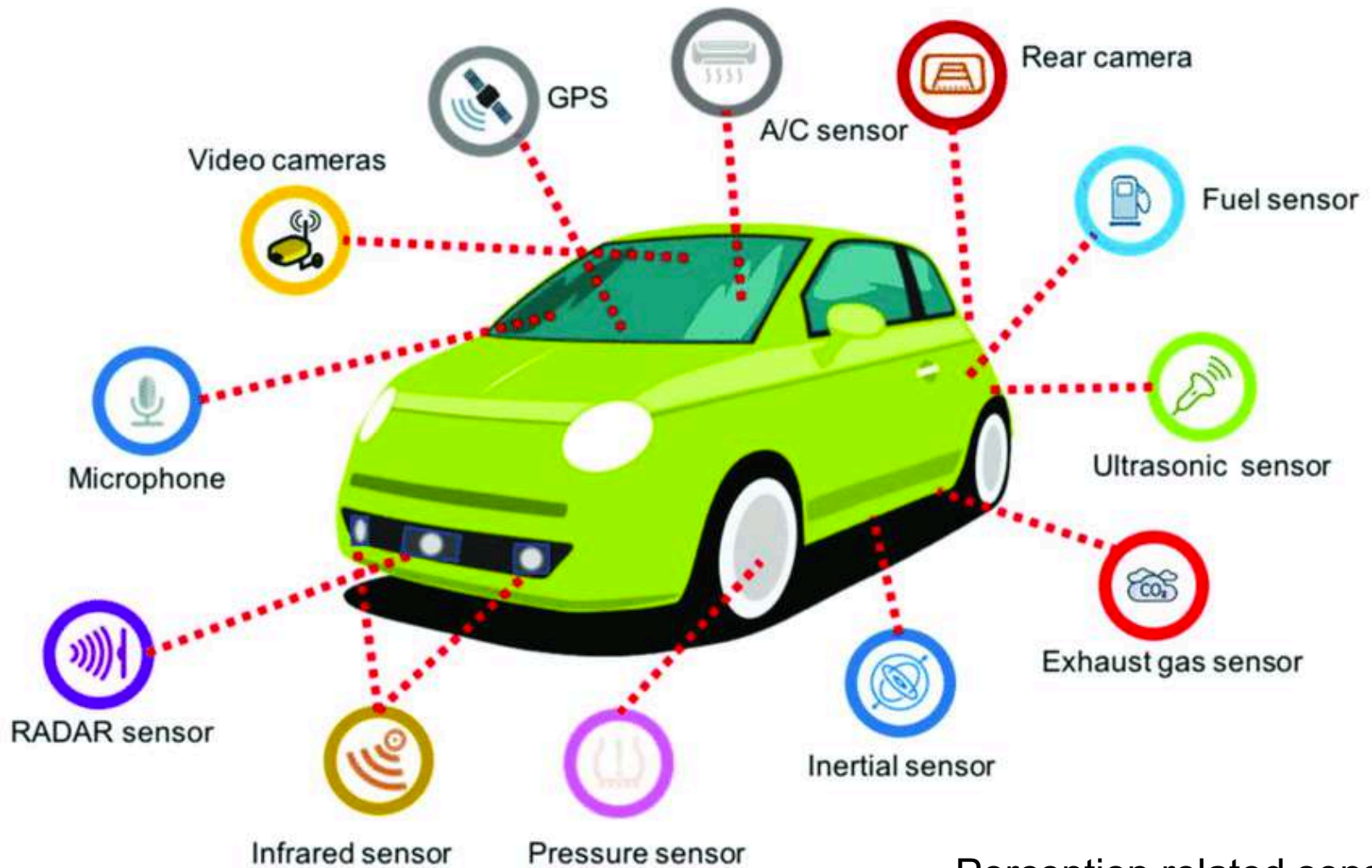
$$dB = 10 \log_{10} \frac{P_{f_L \sim H}}{P_S}$$



Electromagnetic Spectrum



Vehicle Sensors

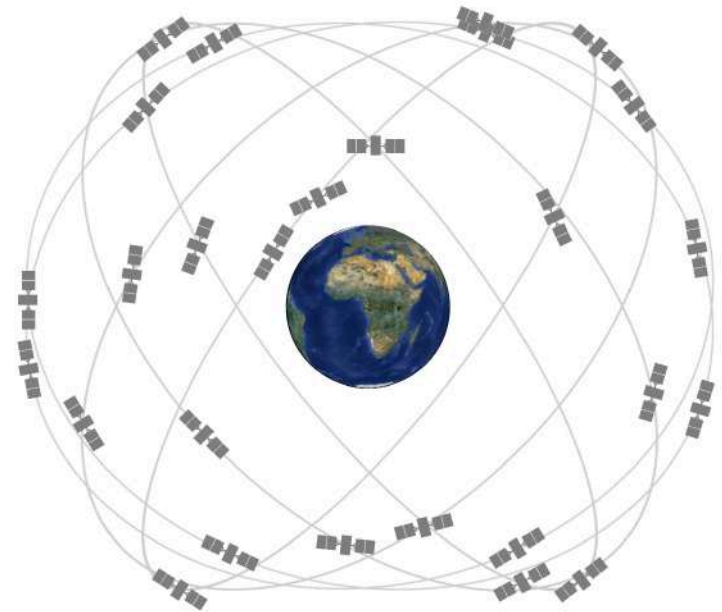


Perception related sensors



Vehicle Sensors

- GPS (Global Positioning System)
- A constellation of 24 satellites (+several spares)
- Broadcast time; identity; orbital parameters (latitude, longitude, altitude);
- Carriers - there are two carrier radio waves:
 - L1, with frequency 1575.42 MHz
 - L2, with frequency 1227.6 MHz



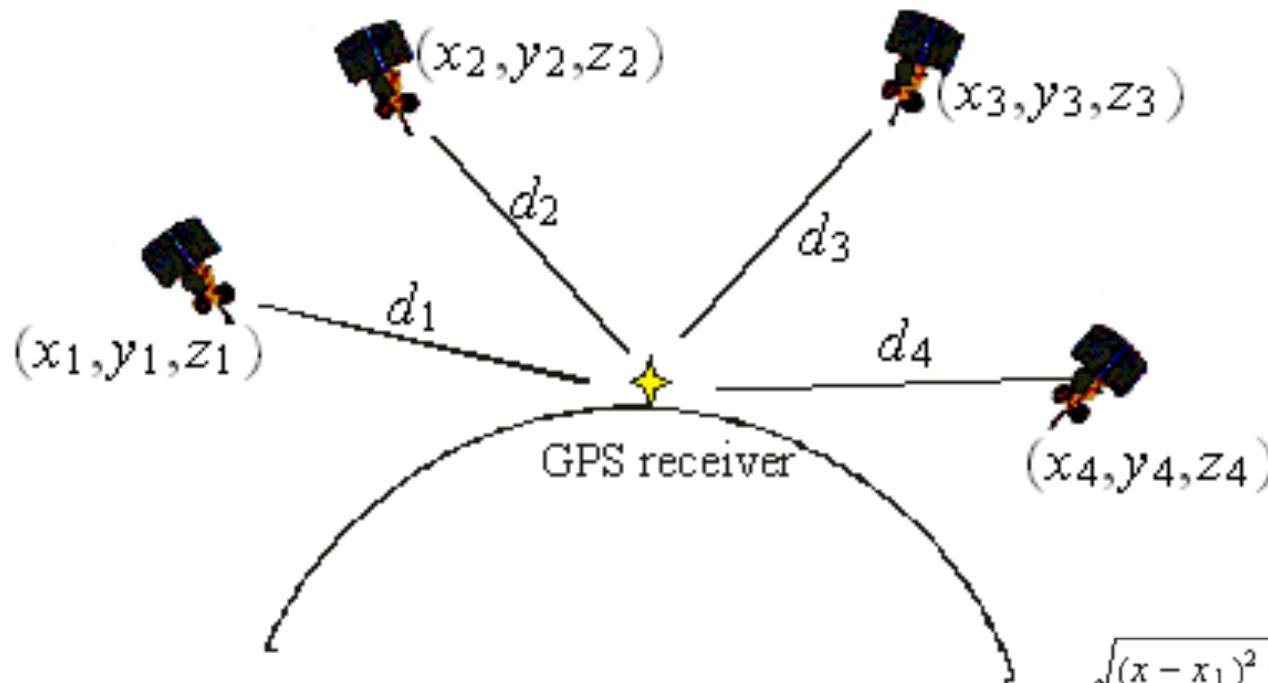
Space Segment

<https://www.gps.gov>



Vehicle Sensors

- GPS (Global Positioning System)



Triangulation

$$\sqrt{(x - x_1)^2 + (y - y_1)^2 + (z - z_1)^2} + ct_B = d_1$$

$$\sqrt{(x - x_2)^2 + (y - y_2)^2 + (z - z_2)^2} + ct_B = d_2$$

$$\sqrt{(x - x_3)^2 + (y - y_3)^2 + (z - z_3)^2} + ct_B = d_3$$

$$\sqrt{(x - x_4)^2 + (y - y_4)^2 + (z - z_4)^2} + ct_B = d_4$$

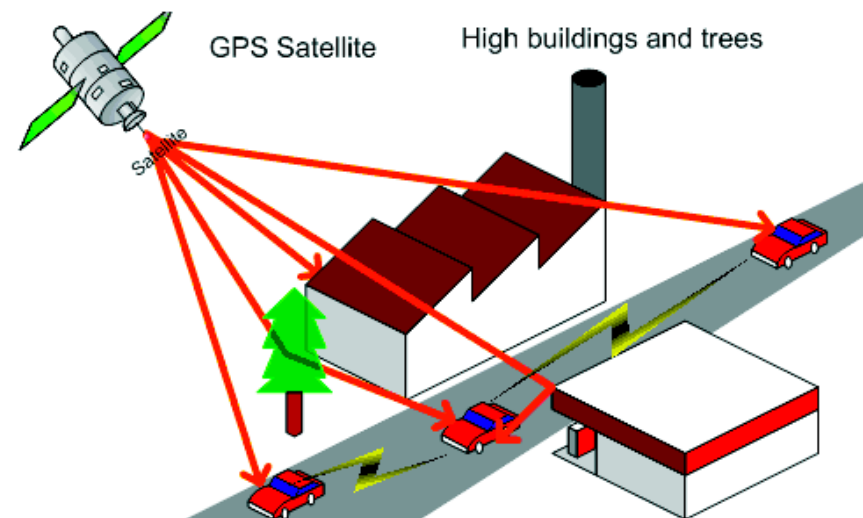


Vehicle Sensors

- GPS (Global Positioning System)
- Spherical coordinates
 - latitude
 - longitude
 - altitude (above sea level)
- PPS - Precise Positioning Service
 - uses multiple signals
 - for military use only
- DGPS - Differential GPS
 - 2 receivers
 - 1 known fixed position

Expected errors:

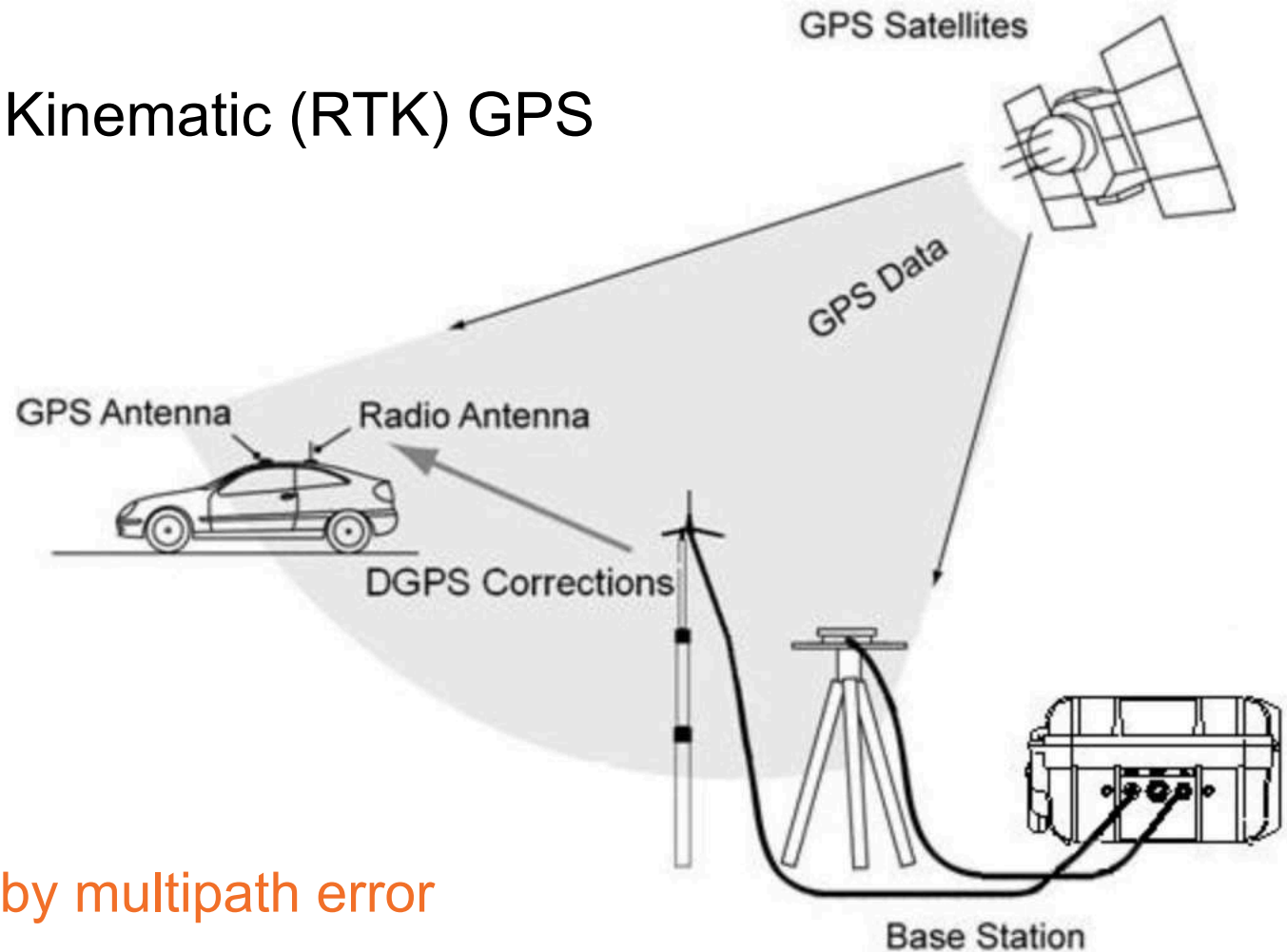
ionospheric range error
tropospheric range error
satellite clock range error
receiver clock range error
multipath error
noise





Vehicle Sensors

- GPS (Global Positioning System)
- Real-Time Kinematic (RTK) GPS



Still degraded by multipath error



Vehicle Sensors

- **GNSS** global geo-spatial positioning system
 - Global Navigation Satellite System (GNSS) with global coverage.
- GNSS systems:
 - GPS, GLONASS, Galileo, Beidou and other regional systems.
- **GNSS+INS fusion**
 - Example: NovAtel SPAN-CPT GNSS-INS

SPAN[®] SPAN-CPT[™]



SINGLE ENCLOSURE GNSS+INS
RECEIVER DELIVERS 3D POSITION,
VELOCITY AND ATTITUDE





Vehicle Sensors

- GNSS+INS
- NovAtel
SPAN-CPT

SPAN SYSTEM PERFORMANCE¹

Horizontal Position Accuracy (RMS)

Single point L1/L2 1.2 m

NovAtel CORRECT™

» SBAS² 60 cm

» DGPS 40 cm

» PPP³ 4 cm

» RTK 1 cm + 1 ppm

Data Rate

GPS measurement 20 Hz

GPS position 20 Hz

IMU measurement 100 Hz

INS solution Up to 100 Hz

Time Accuracy⁴ 20 ns RMS

Max Velocity⁵ 515 m/s

IMU PERFORMANCE⁶

Gyroscope Performance

Gyro technology FOG

Output range $\pm 375^\circ/\text{s}$

Bias $20^\circ/\text{hr}$

Bias stability $\pm 1^\circ/\text{hr}$

Scale factor 1500 ppm

Angular random walk
 $0.0667^\circ/\sqrt{\text{hr}}$ (max)

Accelerometer Performance

Range $\pm 10\text{ g}$

Bias 50 mg

Bias stability $\pm 0.75\text{ mg}$

Scale factor 4000 ppm

PHYSICAL AND ELECTRICAL

Dimensions

152 x 168 x 89 mm

Weight

2.28 kg

Power

Power consumption 16 W max

Input voltage +9 to +18 VDC

Antenna Port Power Output

Output voltage +5 VDC

Maximum current 100 mA

Connectors

Power and I/O

MIL-DTL-38999 Series 3

Antenna Input TNC Female

COMMUNICATION PORTS

RS-232 UART COM 2

USB Device 1

CAN 1

Event Input Trigger 1

Configurable PPS 1

ENVIRONMENTAL

Temperature

Operating -40°C to $+65^\circ\text{C}$

Storage -50°C to $+80^\circ\text{C}$

Humidity 95% non-condensing

Waterproof

MIL-STD-810F, 506.4,
Procedure I

INCLUDED ACCESSORIES

- Combined I/O and power cable

OPTIONAL ACCESSORIES

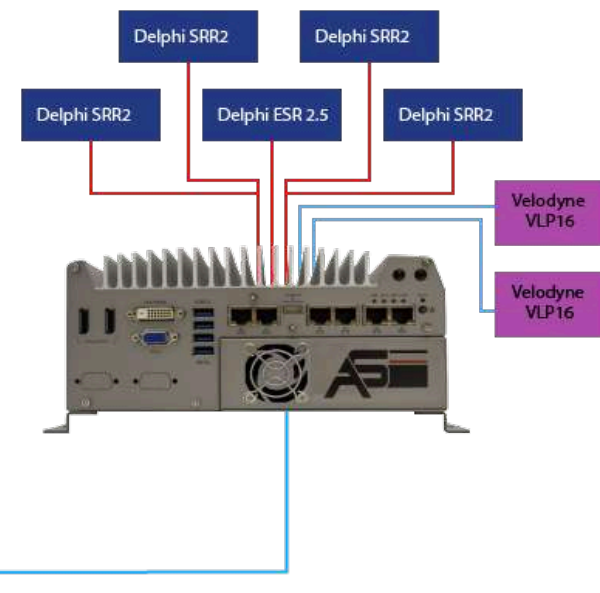
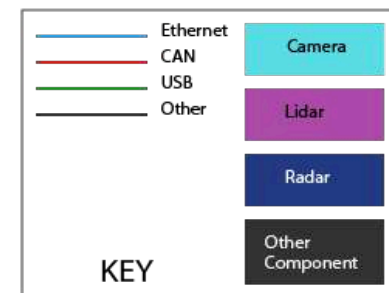
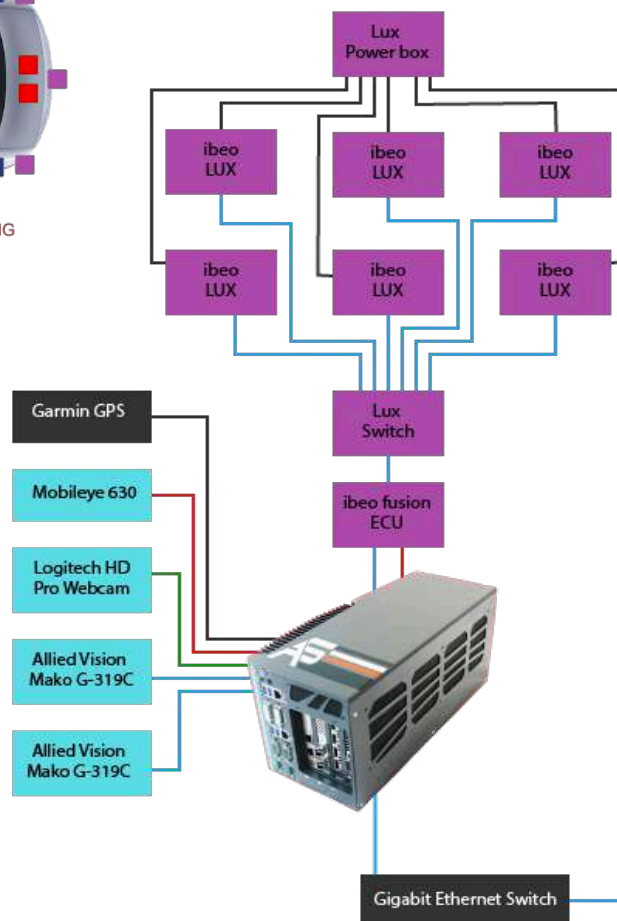
- GPS-700 series antennas (dual-frequency required)
- ANT series antennas (dual-frequency required)
- RF cables—5, 10 and 30 m lengths
- Inertial Explorer post-processing software

Optional Dual Antenna⁷

Baseline	Accuracy
0.5 m	0.4°
1.0 m	0.2°
2.0 m	0.1°

Vehicle Sensors

• Perception kit configuration example



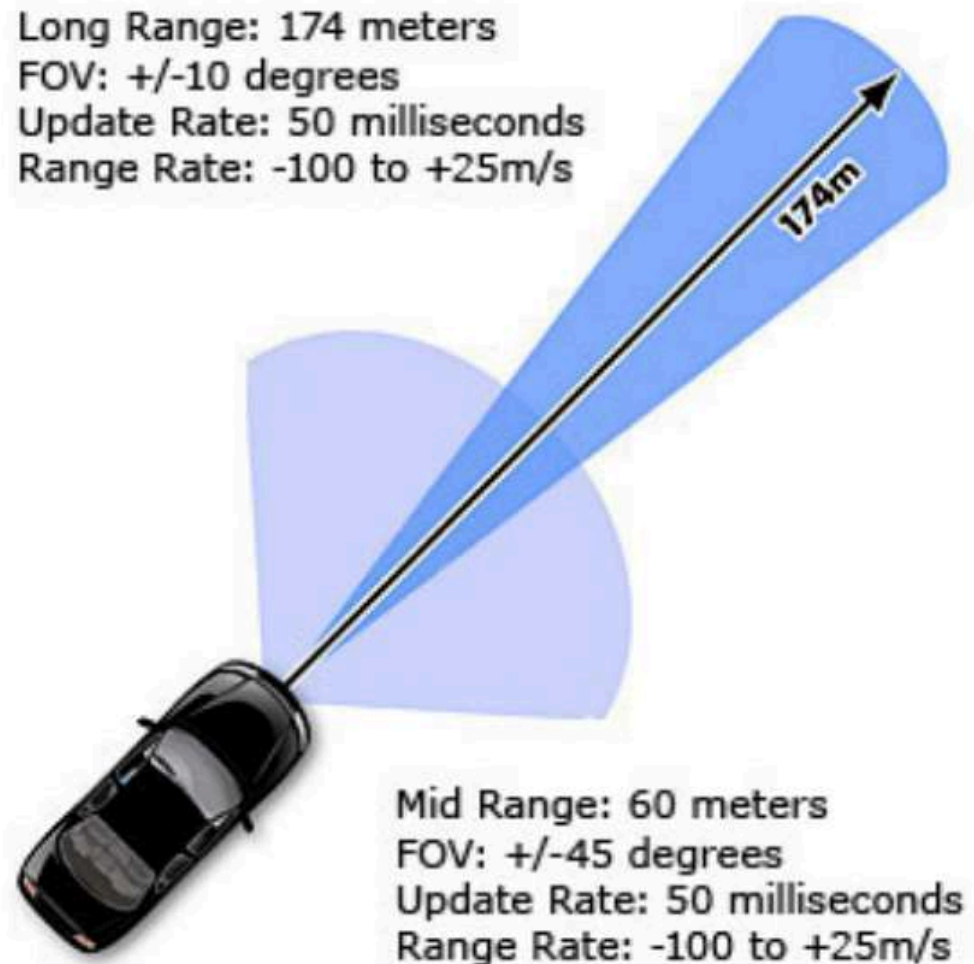


Vehicle Sensors

- Delphi ESR 2.5 Radar

- DEL-ESR-2.5
-24VDC+

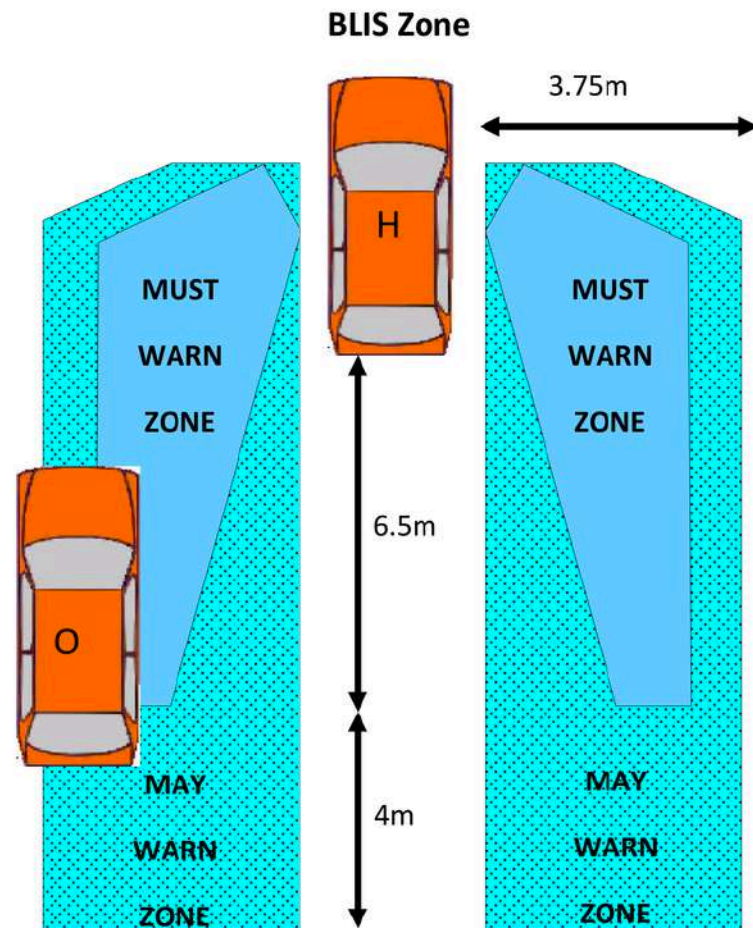
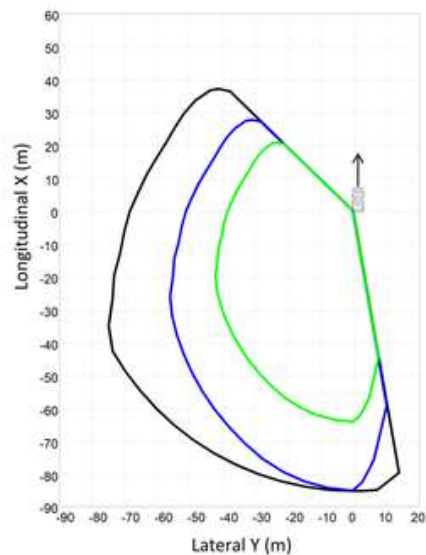
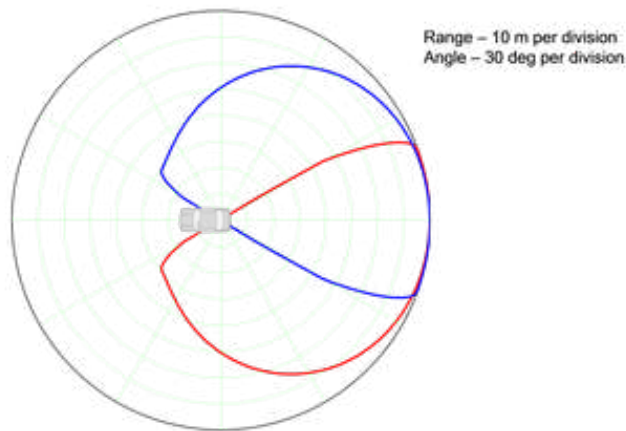
- Delphi's multimode
Electronically
Scanning
RADAR (ESR)





Vehicle Sensors

- Delphi SRR2 Rear & Side Radar



Vehicle Sensors

- ibeo "IBE-1000003-LUX+" LiDAR
- Range up to 200m/650ft
- Object tracking (up to 65 objects)







LASER / OPTICAL	ibeo LUX 4L	ibeo LUX 8L	ibeo LUX HD
Laser class:	Class 1		
Wave length:	905 nm		
Technology:	Time of flight, Output of distance and echo pulse width		
Range:	50 m / 164 ft @ 10% remission	50 m / 164 ft @ 10% remission	30 m / 98 ft @ 10% remission
Horizontal field of view:	110° (50° to -60°)		
Vertical field of view:	3.2°	6.4°	3.2°
Multi-layer:	4 parallel scanning layers	8 layers (2 pairs of 4 layers)	4 parallel scanning layers
Multi echo:	Up to 3 distance measurements per shot (allow measurements through atmospheric clutter like rain and dust)		
Data update rate:	25.0 Hz		

Vehicle Sensors

- Mobileye "MBL-630-CAM-KIT+"
 - EyeQ2® Image Processing SOC
 - EyeWatch® display
 - 2 seconds ahead warning:
 - Forward Collision
 - Pedestrian & Cyclist Collision

Item	Description	Value
Signals Cables	Car inputs	BAT+, GND, Ignition, High Beam, CAN-Bus (High/Low)
Voltages	Input	12 - 36VDC
	Current Load (full operation)	12v > 360mA, 24v > 180mA**
	Stand-by Current Load (Ignition off)	12v > 10µA, 24v > 10µA
	Power consumption	Nominal 5.2W



-  Forward Collision Warning
-  Pedestrian and Cyclist Collision Warnings
-  Lane Departure Warning
-  Headway Monitoring and Warning
-  Intelligent High-Beam Control *
-  Speed Limit Indication



Vehicle Sensors

- Allied Vision "AVT-MAKO-G-319C+" Camera

- Mono and Color modes

- Global Shutter

V.S. rolling shutter?

- Auto exposure

- Gamma correction

Interface	IEEE 802.3 1000BASE-T, IEEE 802.3af (PoE)
Resolution	2064 (H) × 1544 (V)
Sensor	Sony IMX265
Sensor type	CMOS
Sensor Size	Type 1/1.8
Cell size	3.45 μm x 3.45 μm
Lens mount	C-Mount
Frame rate	37.5 fps
ADC	12 Bit
Image buffer (RAM)	64

Vehicle Sensors - Perception

- Velodyne "VEL-VLP-16+" LiDAR

- 16 Channels
- Measurement Range: 100 m
- Range Accuracy: Up to ± 3 cm (Typical) 1
- Field of View (Vertical): $+15.0^\circ$ to -15.0° (30°)
- Angular Resolution (Vertical): 2.0°
- Field-of-View (Horizontal): 360°
- Angular Resolution (Horizontal/Azimuth): $0.1^\circ - 0.4^\circ$
- Rotation Rate: 5 Hz – 20 Hz

- 3D LiDAR Data Points Generated:
 - - Single Return Mode: $\sim 300,000$ points per second
 - - Dual Return Mode: $\sim 600,000$ points per second





Summary

- Signal
- Noise
- Time-domain Analysis
- Frequency-domain Analysis
- Signal processing filter design
- Electromagnetic spectrum
- Vehicle sensors (perception)

END, Thank you!



Reference

- Smith, Steven W. "The scientist and engineer's guide to digital signal processing." (1997): 35.
- Digital Signal Processing and Analysis, Lecture Notes, The University of Michigan, Jeffrey A. Fessler.
- Introduction to Electronics, Signals, and Measurement, Lecture Notes, Massachusetts Institute of Technology, Manos Chaniotakis and David Cory.



Appendix Related Resource

- [The Scientist and Engineer's Guide to DSP](#)
- [Vehicle Environment Sensing \(Perception\)](#)
- [Signals & Systems Series](#) (Video)
- [Fourier Transform - A visual introduction](#) (Video)
- [Signal Processing and Machine Learning Techniques for Sensor Data Analytics in Matlab](#) (Video)
- [Signal Processing - create A Digital Filter in Python](#) (Video)
- [Automotive Sensors](#) (Video)