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# **AuE 8200: Machine Perception and Intelligence**

## **Lecture: Automotive radar principles and analysis**

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# Outline

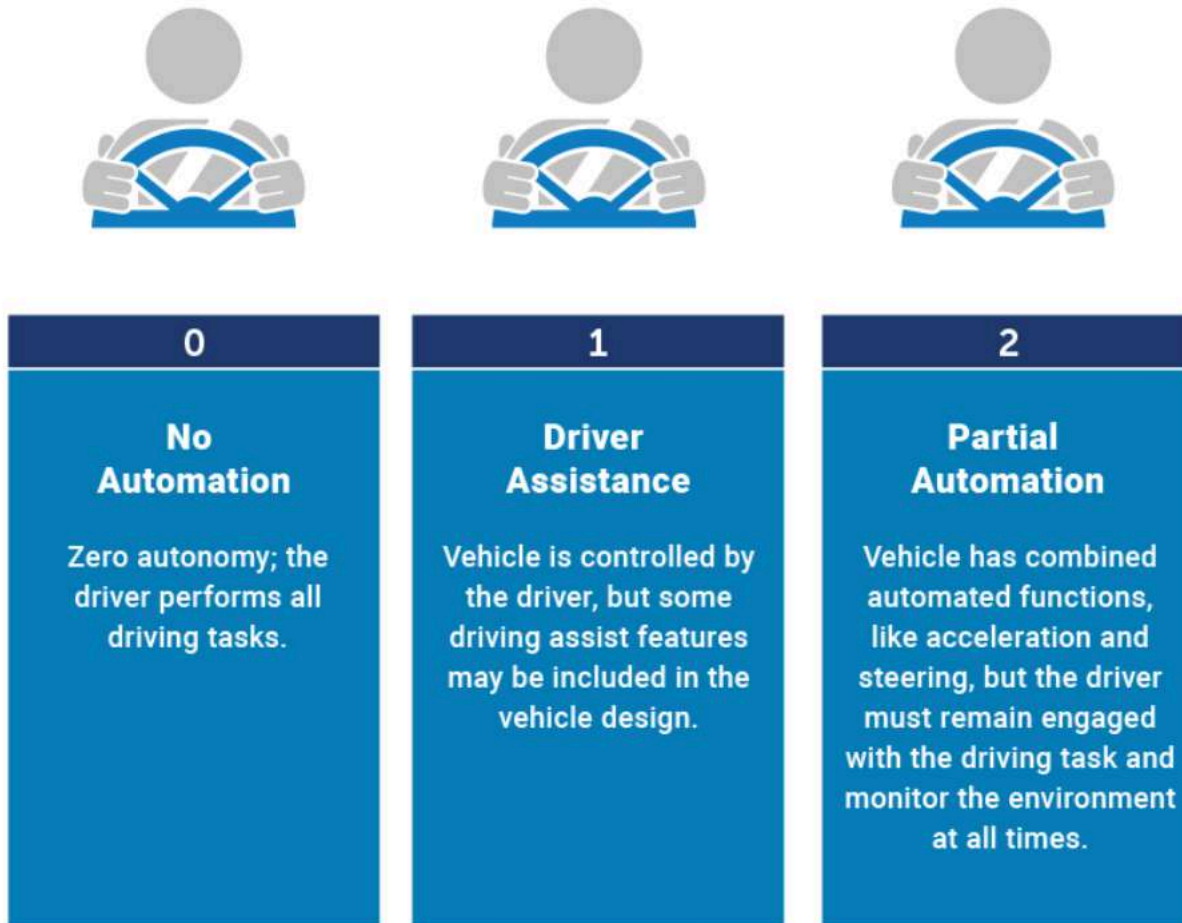
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- Automotive Radar Motivation
- Automotive Radar History
- Automotive Radar Basics
  - Ranges
  - Frequency Bands
- Automotive Radar Principle
  - Pulsed Radar
  - FMCW Radar
  - DOA
- Automotive Radar Object Detection
  - Object Clustering
  - Object Classification
  - Object Tracking



# Automotive Radar Motivation

Society of Automotive Engineers (SAE) automation levels



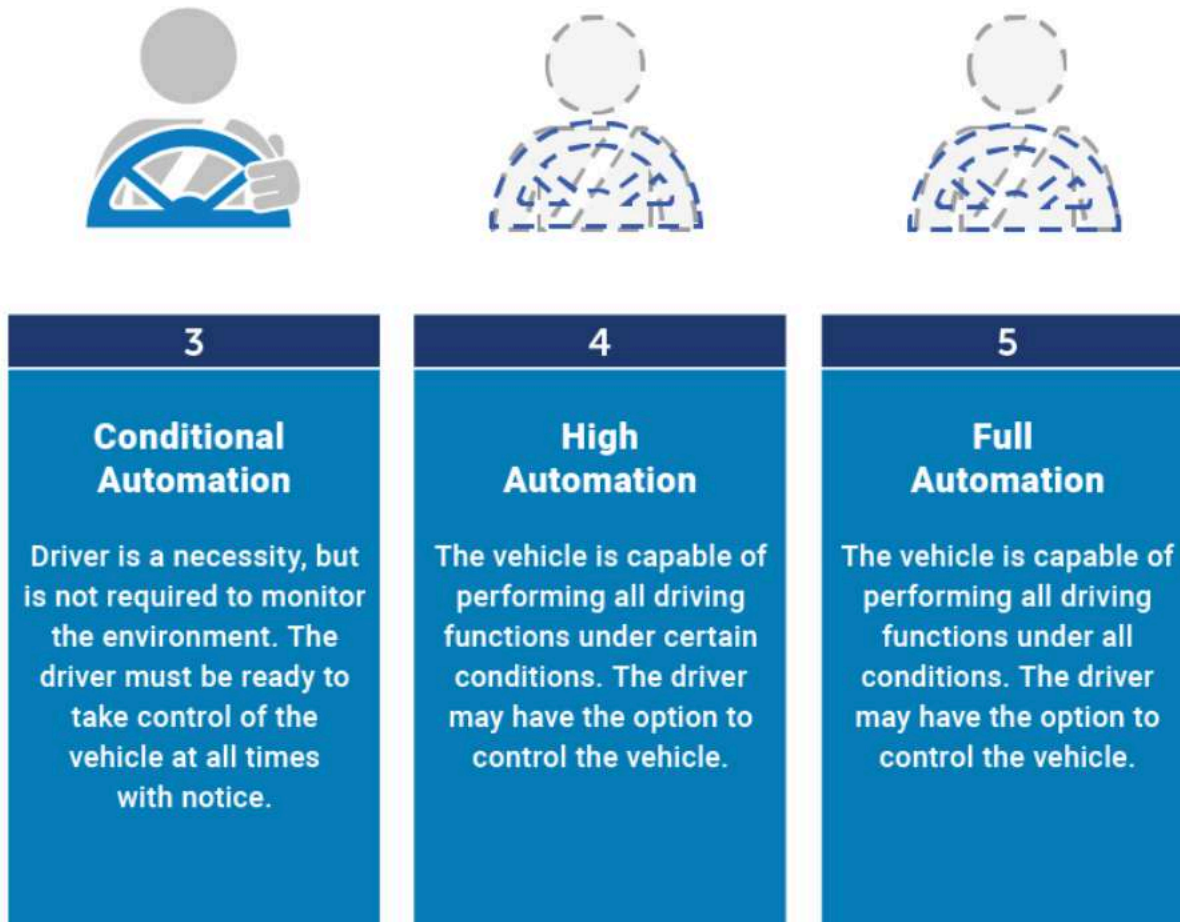
[NHTSA](https://www.nhtsa.gov/roadway/autonomous-vehicles)

Advanced driver assistance system (ADAS)



# Automotive Radar Motivation

Society of Automotive Engineers (SAE) automation levels



[NHTSA](https://www.nhtsa.gov/automated-driving)

Automated driving system (ADS)

# Automotive Radar Motivation

Consumer Electronics Show (CES) 2019

**CES 2019: NVIDIA launches Level 2+ automated driving solution**



# Automotive Radar Motivation

More  
features

## Blind Spot Detection (BSD)

Majorly based on RADAR sensors. However it can be built on LiDAR, Camera and Ultrasonic sensor

## Forward / Rear Collision Warning System (FCW & RCW)

Majorly based on RADAR and LiDAR sensors

## Intelligent Parking Assistance (IPA)

It is based on Camera and Ultrasonic sensor sensors

## Cross Traffic Alert (CTA)

Normally based on RADAR sensors. However it can be build on LiDAR and Camera sensors

## Lane Change Assist (LCA)

It is build on Camera and LiDAR sensors

## ADAS FEATURES IN AUTOMOBILE INDUSTRY

## Autonomous Emergency Braking (AEB)

Majorly based on RADAR and LiDAR sensors

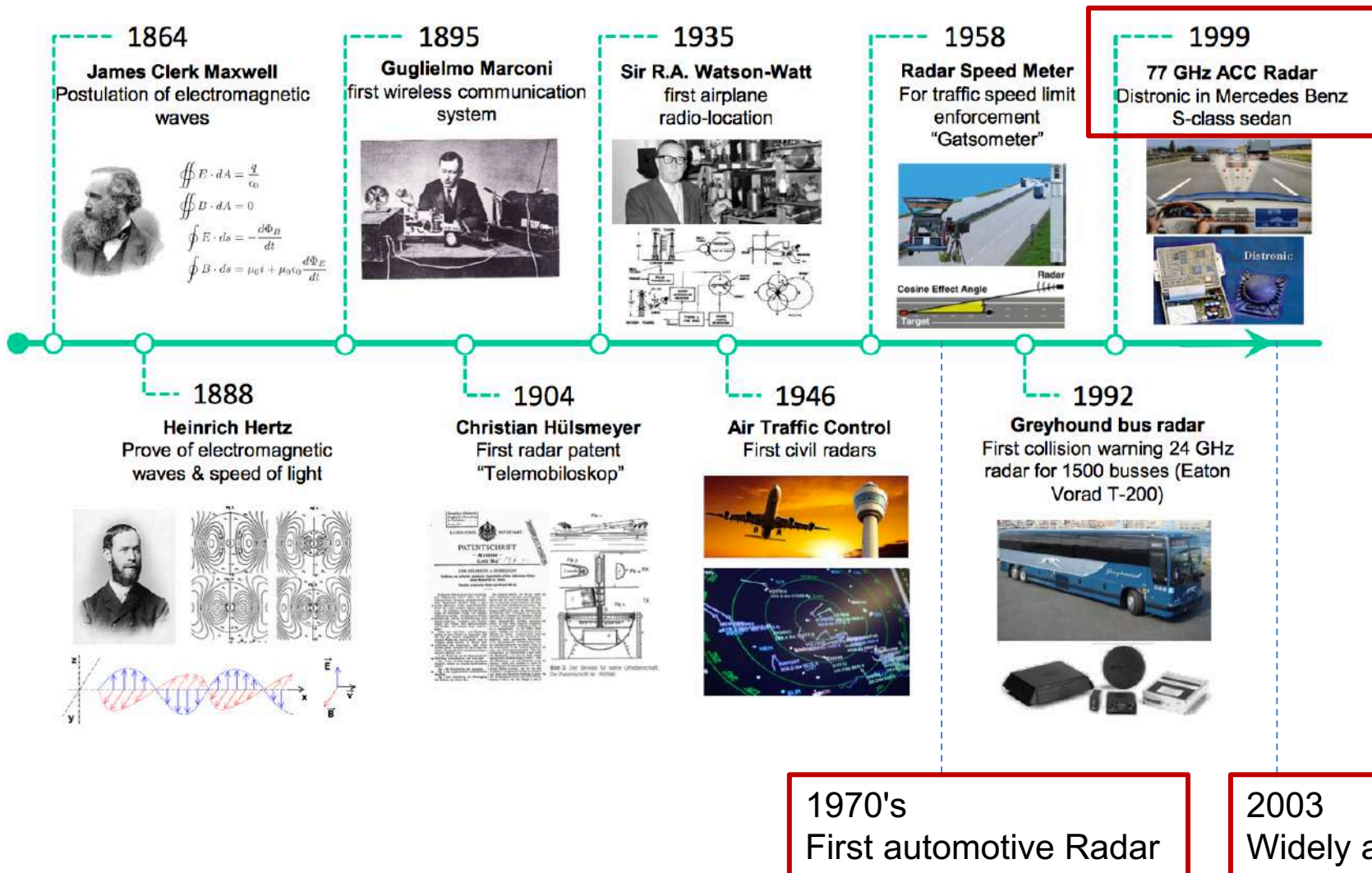
## Adaptive Cruise Control (ACC)

Majorly based on RADAR and LiDAR sensors



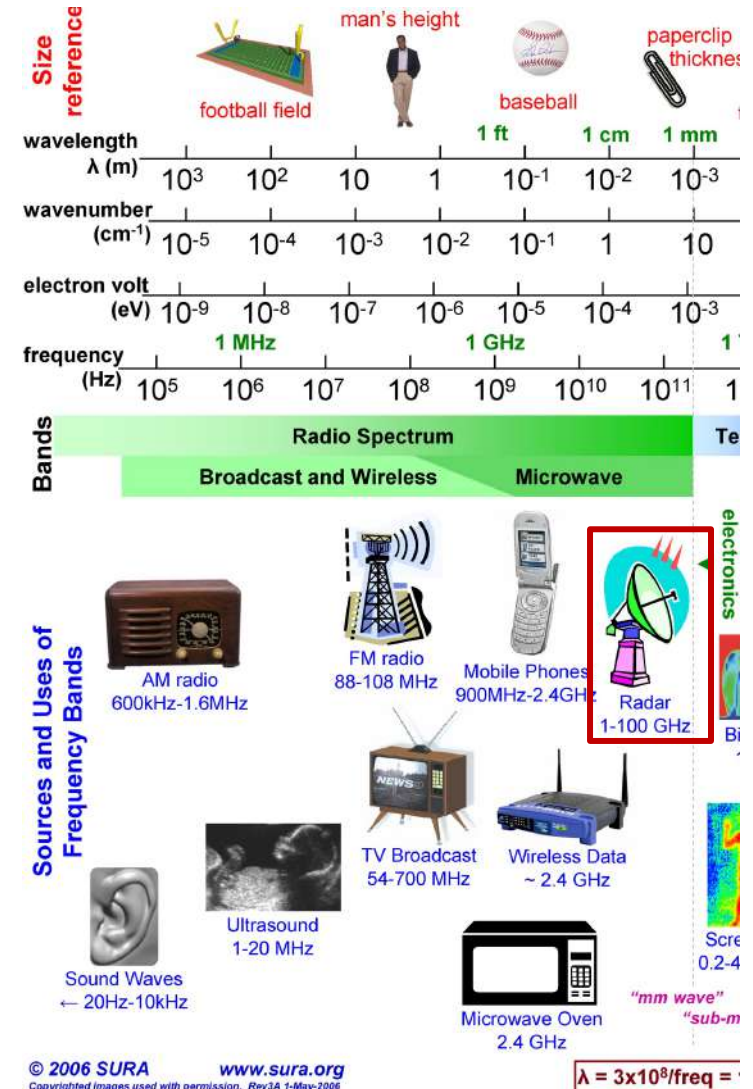


# Automotive Radar History



# Automotive Radar Basics

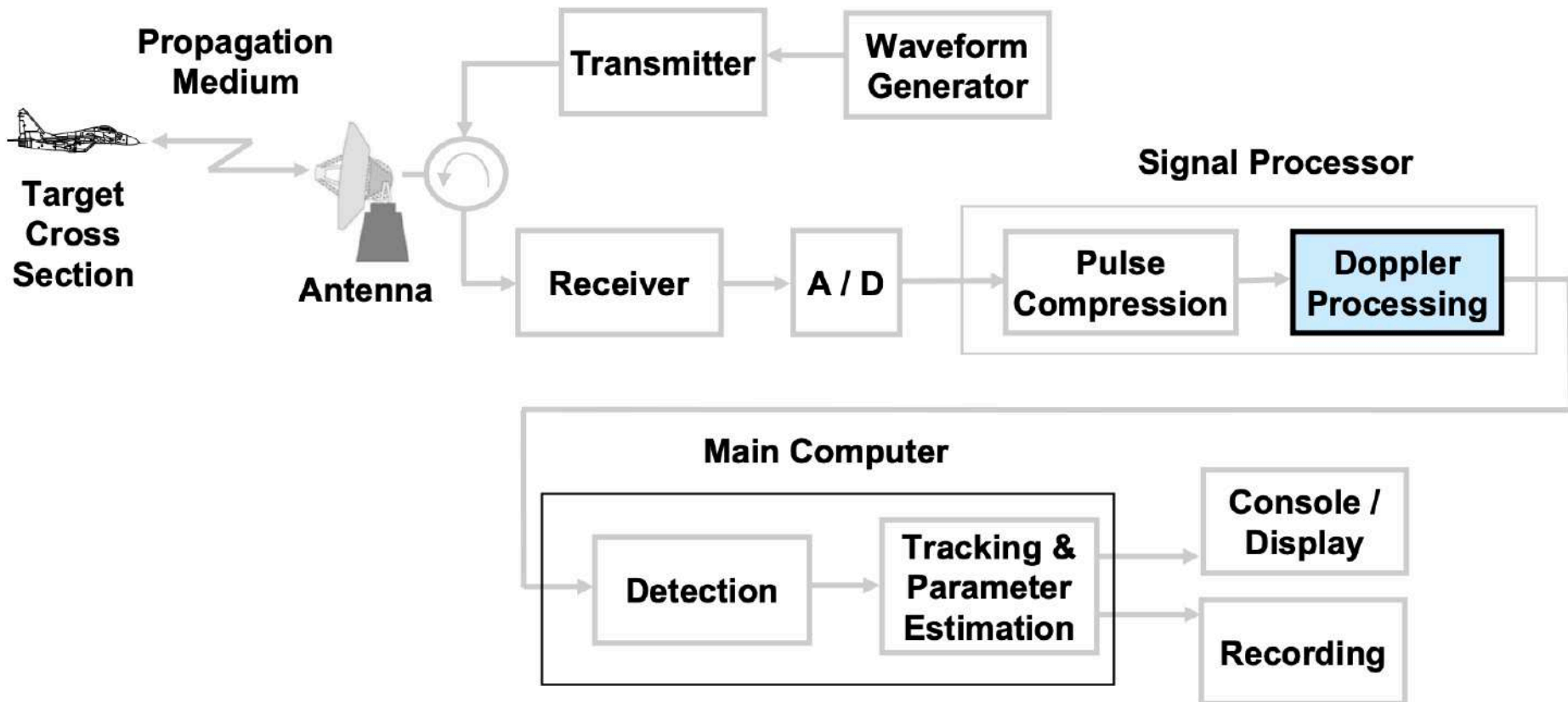
- Radar (RAdio Detection And Ranging)
  - Relative position
  - Relative speed
  - Relative azimuth angle
- Electromagnetic wave
  - Radio wave
  - Signal echo
- Advantages over optical sensors
  - Robustness in harsh weather conditions (darkness/brightness, fog, rain, temperature, et al)
  - Long, middle and short ranges
  - High accuracy







# Automotive Radar Basics



# Automotive Radar Basics - Ranges

## Long Range

Adaptive Cruise Control

**ACC: 150 to 200m**

**FOV: +/-8°**

## Short/Medium Range

Blind Spot Detection

**BSD: 10m**

Lane Change Assist

**LCA: 70m**

Cross Traffic Alert

**CTA: 30m**

Forward Collision Warning

**FCW: 70m**

Forward Collision Mitigation

**FCM: 70m**

Rear Collision Warning

**RCW: 70m**

Stop & Go

**S&G: 70m**

**FOV: +/-75°**

**FOV: +/-65°**



Field of View (FOV)

# Automotive Radar Frequency Bands

24GHz NB	24GHz UWB	26GHz UWB	77GHz	79GHz UWB
Worldwide	US/Canada  Japan  EU until 2013/ will be extended to 2022 but with reduced bandwidth	US/Canada  Japan	"Worldwide"	Singapore   EU
different bandwidth EU: 200MHz (75cm) [450MHz] (33cm) US: 200MHz (75cm) JP: 200MHz (75cm)	US: 7GHz (2.2cm)  JP+EU: 5GHz (3cm)	US: 1 GHz (15cm)  JP: July 2010 5 GHz (3cm)	1 GHz (15cm) JP: 500MHz (30cm)	4 GHz (4cm)
20dBm	-41dBm	-41dBm	23.5dBm	-9dBm

24/26 GHz → 76-81 GHz

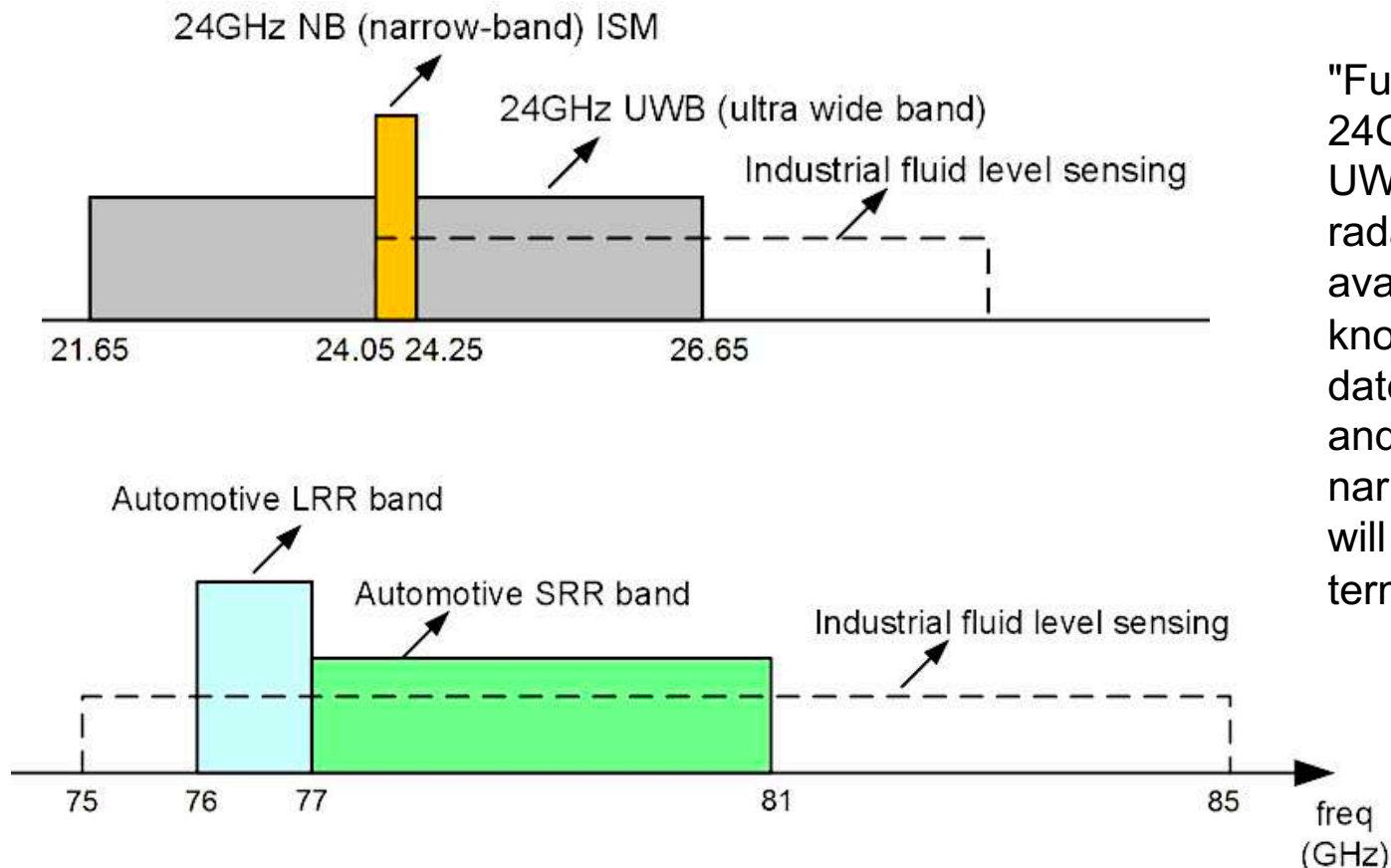
K Band (24 GHz)    E Band (77 GHz)

regulations



# Automotive Radar Frequency Bands

## Moving from 24GHz to 77GHz radar



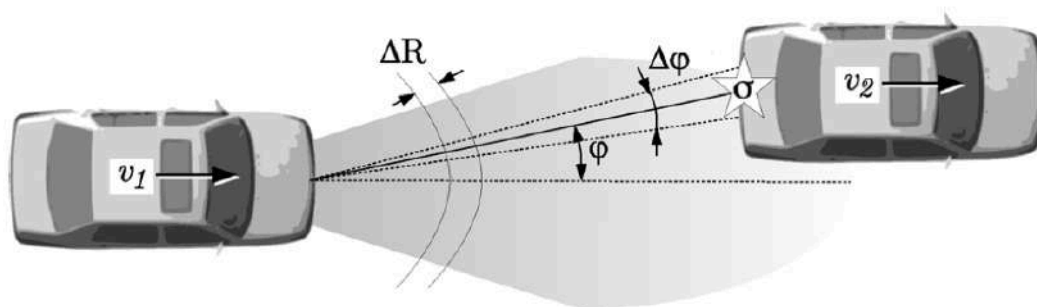
"Future use of the 24GHz wideband and UWB band vehicular radars will not be available after 2021, known as the "sunset date," both in Europe and the U.S.; only the narrowband ISM band will be available long term." [1]

Range resolution, Velocity resolution and Smaller components

# Automotive Radar Frequency Bands

Type		LRR	MRR	SRR
Maximum power (EIRP)	transmit	55 dBm	-9 dBm/MHz	-9 dBm/MHz
Frequency band		76-77 GHz	77-81 GHz	77-81 GHz
Bandwidth		600 MHz	600 MHz	4 GHz
Distance range				
$R_{\min} \dots R_{\max}$		10-250 m	1-100 m	0.15-30 m
Distance resolution $\Delta R$		0.5 m	0.5 m	0.1 m
Distance accuracy $\delta R$		0.1 m	0.1 m	0.02 m
Velocity resolution $\Delta v$		0.6 m/s	0.6 m/s	0.6 m/s
Velocity accuracy $\delta v$		0.1 m/s	0.1 m/s	0.1 m/s
Angular accuracy $\delta \varphi$		0.1°	0.5°	1°
3 dB beamwidth in azimuth $\pm \varphi_{\max}$		$\pm 15^\circ$	$\pm 40^\circ$	$\pm 80^\circ$
3 dB beamwidth in elevation $\pm \vartheta_{\max}$		$\pm 5^\circ$	$\pm 5^\circ$	$\pm 10^\circ$
Dimensions		74x77x58 mm	50x50x50 mm	50x50x20 mm

\* SRR:  
24 GHz is still being  
used in SRR.



[1]



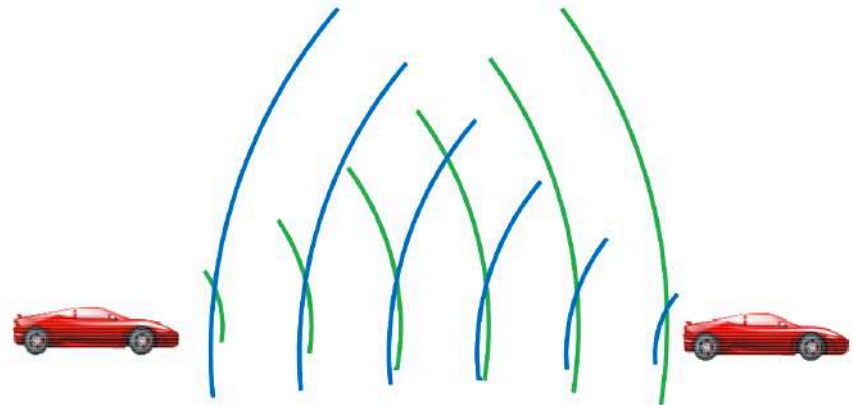


# Automotive Radar Principle

- Radar signal and echo

$$R = \frac{c\tau}{2}$$

- $R$ : relative distance
- $c$ : EM wave travel speed as a constant
- $\tau$ : time of flight (ToF)



- Radar P, R models

$$P_r = \frac{P_t G^2 \lambda^2 \sigma}{(4\pi)^3 R^4 L} \quad \rightarrow \quad R = \sqrt[4]{\frac{P_t G^2 \lambda^2 \sigma}{(4\pi)^3 L P_r}}$$

$$R \leftrightarrow \lambda$$

$$R \leftrightarrow \sigma$$

$P_t$ : Transmit signal power

$G$ : Antenna gain ( $A_o/A_i$ )

$\lambda$ : Radar wavelength

$\sigma$ : Radar cross section (RCS)

$R$ : relative distance

$L$ : Other losses (propagation,)

# Automotive Radar Principle

- Automotive radar measures what?
- Distance
- Speed



Race cars approach and then recede from us, what's the sound difference?



# Automotive Radar Principle

- Radar echo back time

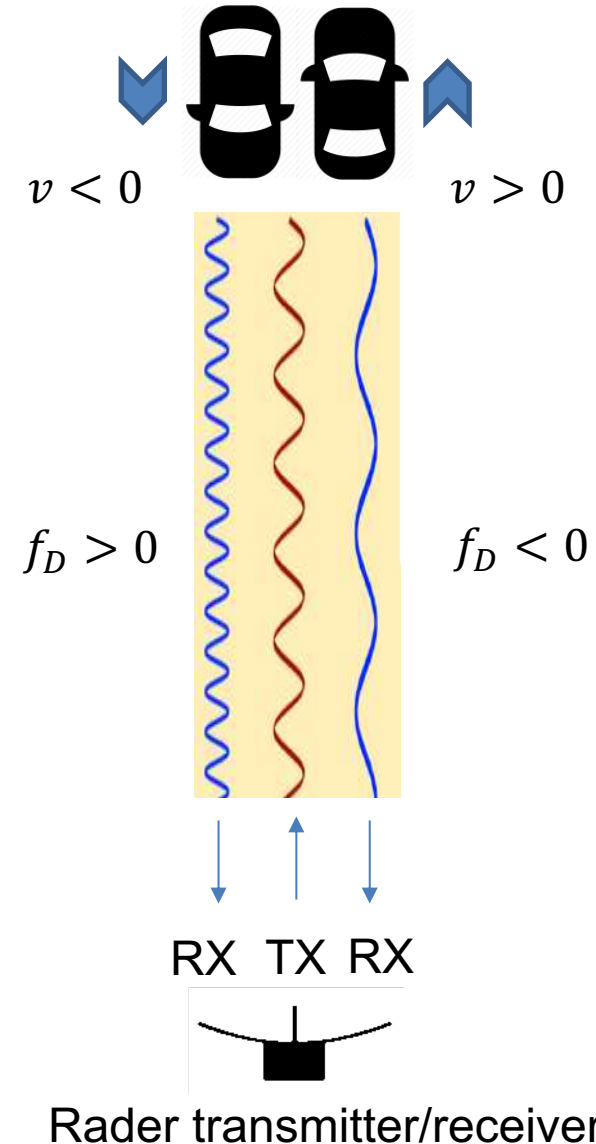
$$\tau = \frac{R}{c} \quad \tau_{echo} = \frac{(R+v\Delta t)}{c}$$

- The difference causes a frequency change  $f_D$  :

$$f_D \sim v, \lambda_c ?$$

$\lambda_c$  is the wavelength of carrier

Doppler effect





# Automotive Radar Principle

- Doppler shift effect:

Transmitted signal:  $\cos(2\pi f_c t)$

Received signal:  $\cos(2\pi f_c (t + \frac{2R}{c}))$

Range change w.r.t velocity in one cycle:  $R = R_o + v_o t$

Substituting:

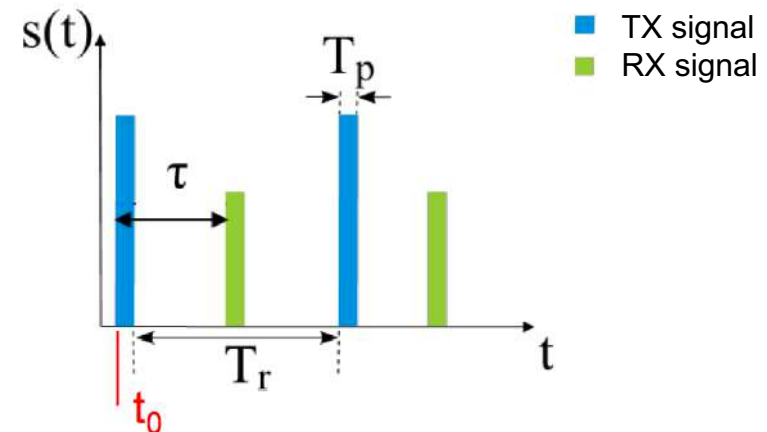
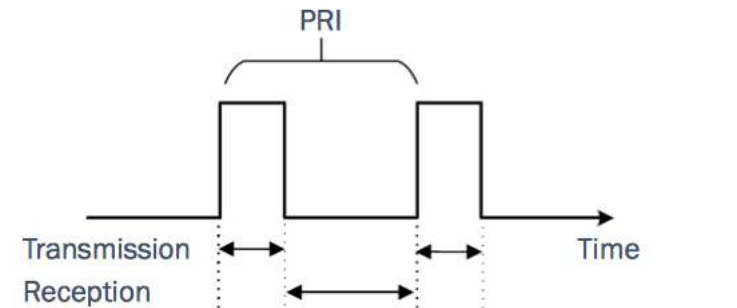
$$\begin{aligned} \cos\left(2\pi f_c \left(t + \frac{2(R_o + v_o t)}{c}\right)\right) &= \\ \cos\left(2\pi \left(f_c + \underbrace{f_c \frac{2v_o}{c}}_{-f_D}\right)t + \frac{2\pi f_c R_o}{c}\right) &= \\ f_D = -f_c \frac{2v_o}{c} = -\frac{2v_o}{\lambda_c} & \end{aligned}$$

# Automotive Radar - Pulse Radar

- Pulse radar
  - $T_r$  Pulse Repetition Interval (PRI)
  - Pulse Repetition Frequency (PRF)  
 $PRF = 1 / PRI$
  - One antenna for both transmission and reception
- Range measurement  $R = \frac{c\tau}{2}$
- Maximum unambiguous range  

$$R_{max} = \frac{c}{2} T_r = \frac{c}{2 PRF}$$
- Range ambiguity resolution  

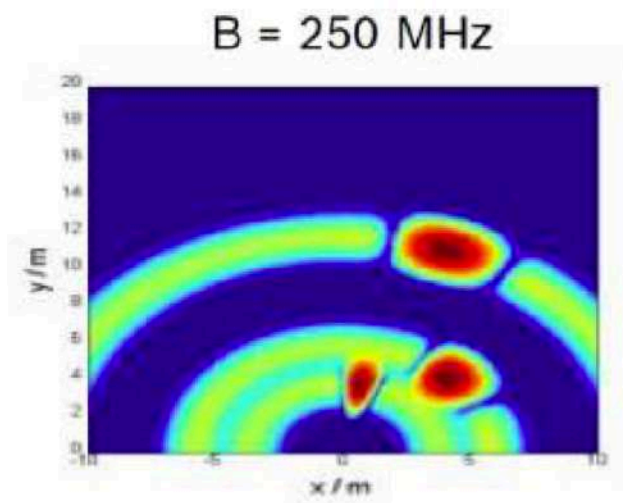
$$\Delta R = \frac{cT_p}{2} \approx \frac{c}{2B}, \text{ where } B \text{ is the Bandwidth}$$



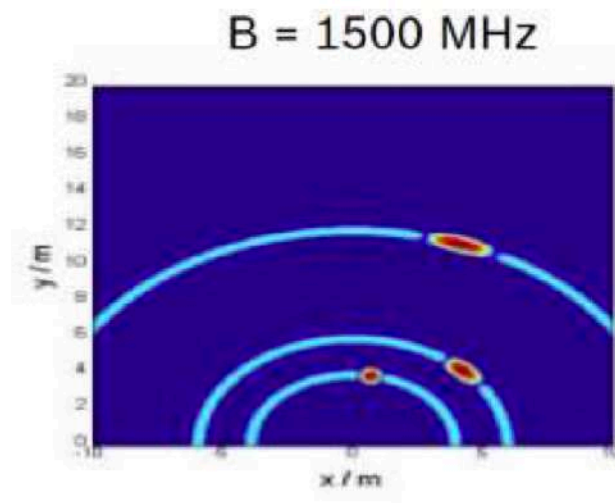


# Automotive Radar - Pulse Radar

- Target separation capability



Long range radar bandwidth

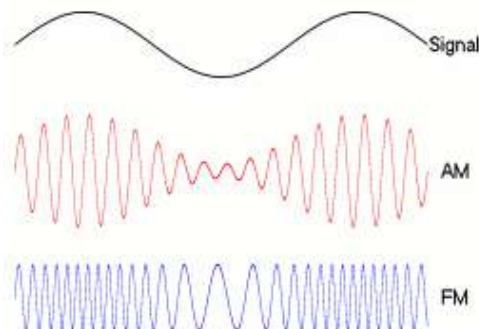
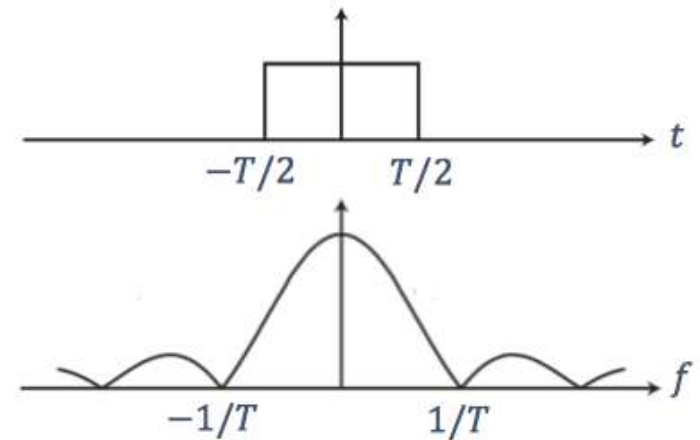


High-range resolution radar bandwidth



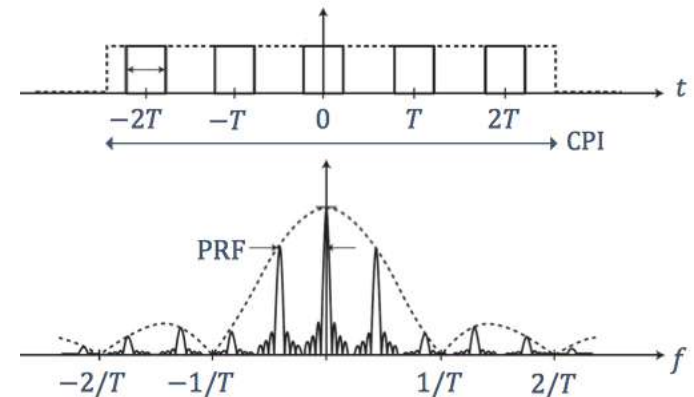
# Automotive Radar - Pulse Radar

- How to measure velocity?
- Spectrum of pulsed radar signal
  - Fourier transform (FT)
- Coherent pulse interval (CPI)
  - Phase  $\rightarrow$  Frequency modulation
  - What is Frequency modulation?



Amplitude  
modulation

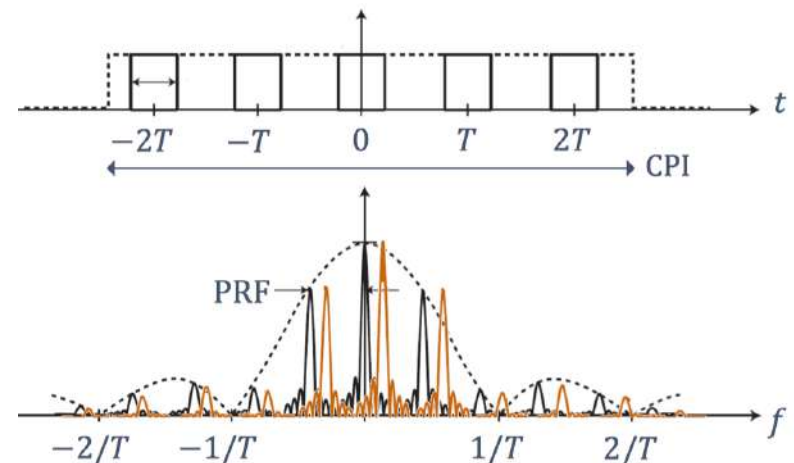
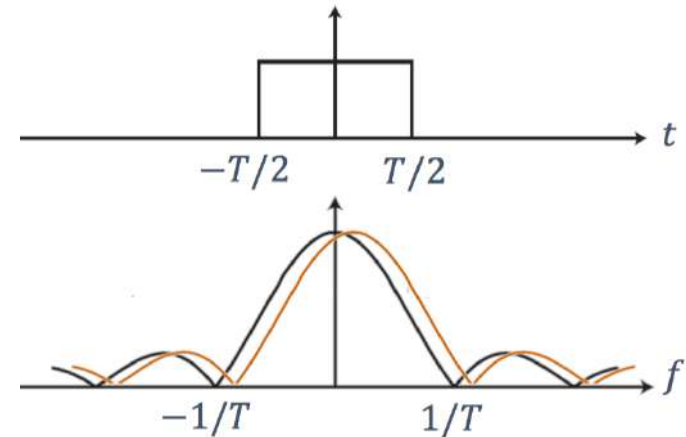
Frequency  
Modulation





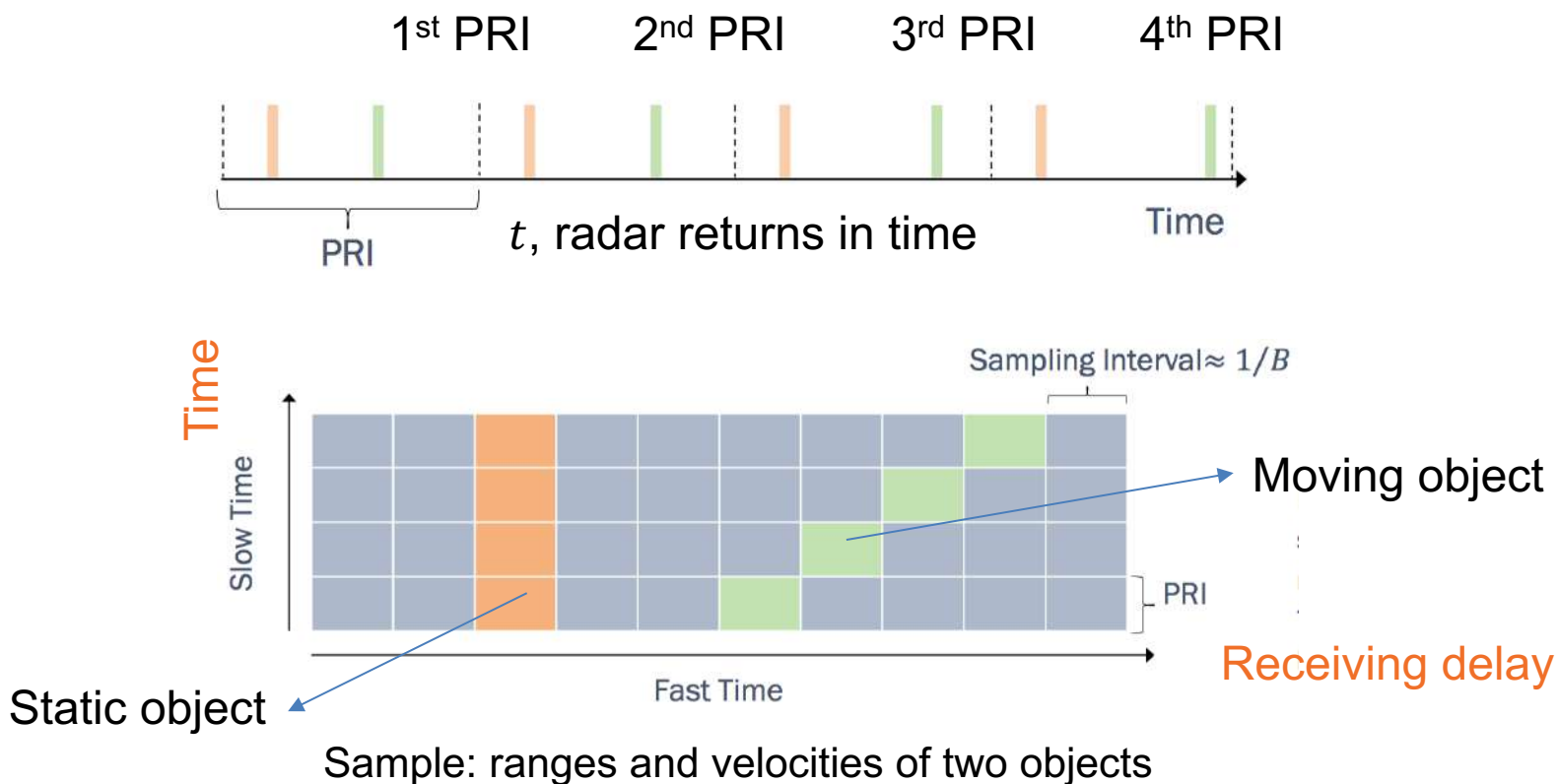
# Automotive Radar - Pulse Radar

- Spectrum of coherent pulsed signals
- Reflection signal:
  - An object is detected
- Velocity estimation
  - Doppler shift



# Automotive Radar - Pulse Radar

- Coherent pulsed signal **data matrix**
  - Fast Time: the different time slots composing a PRI, sampling rate dependent;
  - Slow Time: the time axis of PRI;

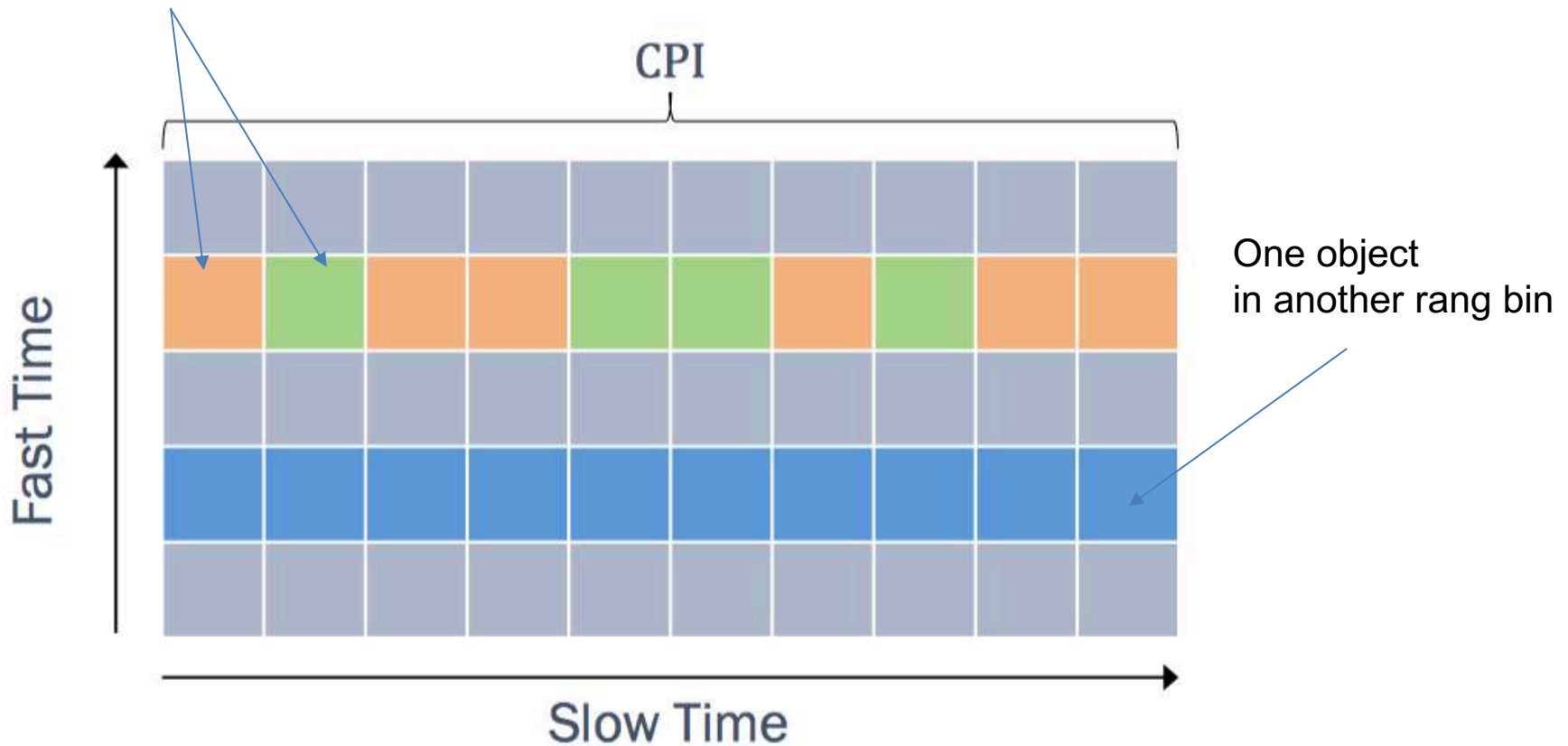




# Automotive Radar - Pulse Radar

- Coherent pulsed signal **data matrix**

Two objects are in the same rang bin, but different velocity



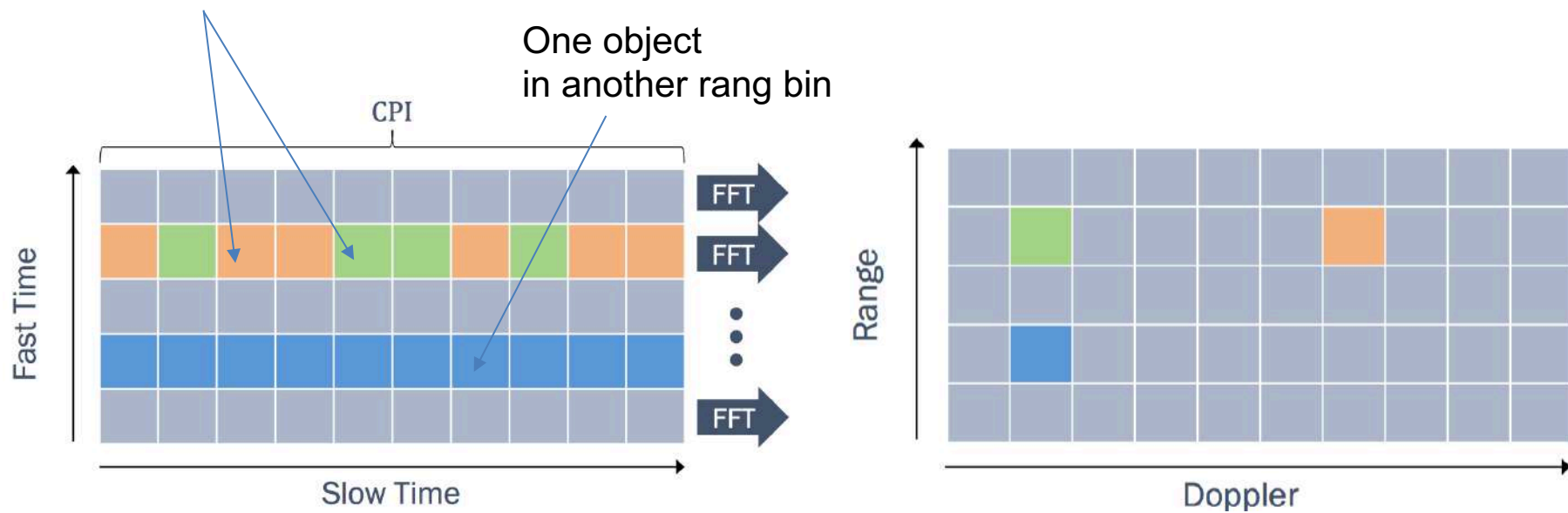
Sample: ranges and velocities when there are three objects



# Automotive Radar - Pulse Radar

- Coherent and Doppler processing
  - Different returns show differently in the Doppler domain.
  - By applying Fourier Transform, range-Doppler map transfer Fast time -> Range and Slow time -> Doppler

Two objects are in the same rang bin, but different velocity



Sample of three objects

Range-Doppler Maps



# Automotive Radar - Pulse Radar

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- Pulse radar characteristics
  - Low cost circuitry
  - Higher power consumption
  - High accuracy for the detection
  - Environment distortions
- Applications
  - Short range radar, et al
- Pulse Radar
  - (1) Pulse Doppler Radar
    - High pulse repetition frequency (PRF)
    - No Doppler ambiguities
    - Numerous range ambiguities
  - (2) Moving Target Indicator Radar
    - Low pulse repetition frequency
    - No range ambiguities
    - Doppler ambiguities



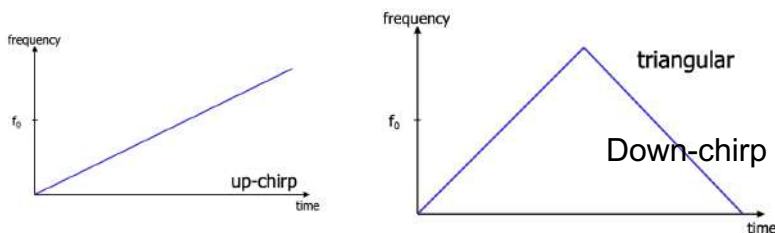
# Automotive Radar - FMCW Radar

- Continuous wave (CW) radar
  - Constantly transmit and receive

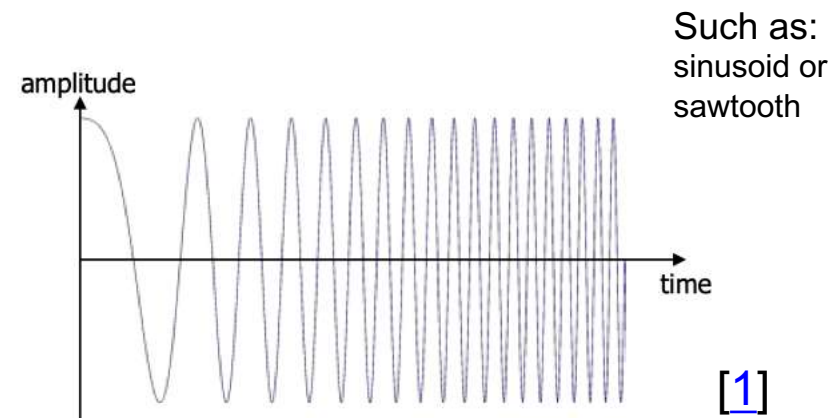


- Frequency Modulated Continuous Wave (**FMCW**)

## Frequency modulation



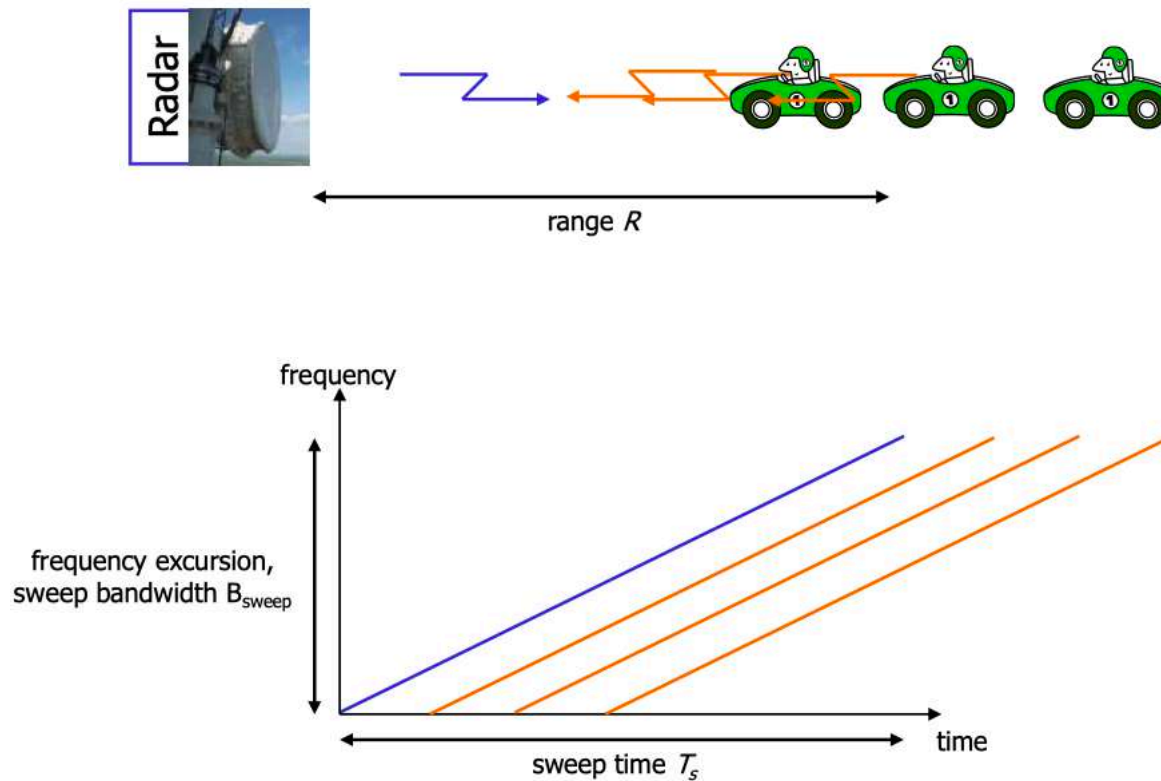
## continuous-wave



We concentrate on: linear FMCW Radar

# Automotive Radar - FMCW Radar

- FMCW – single target





# Automotive Radar - FMCW Radar

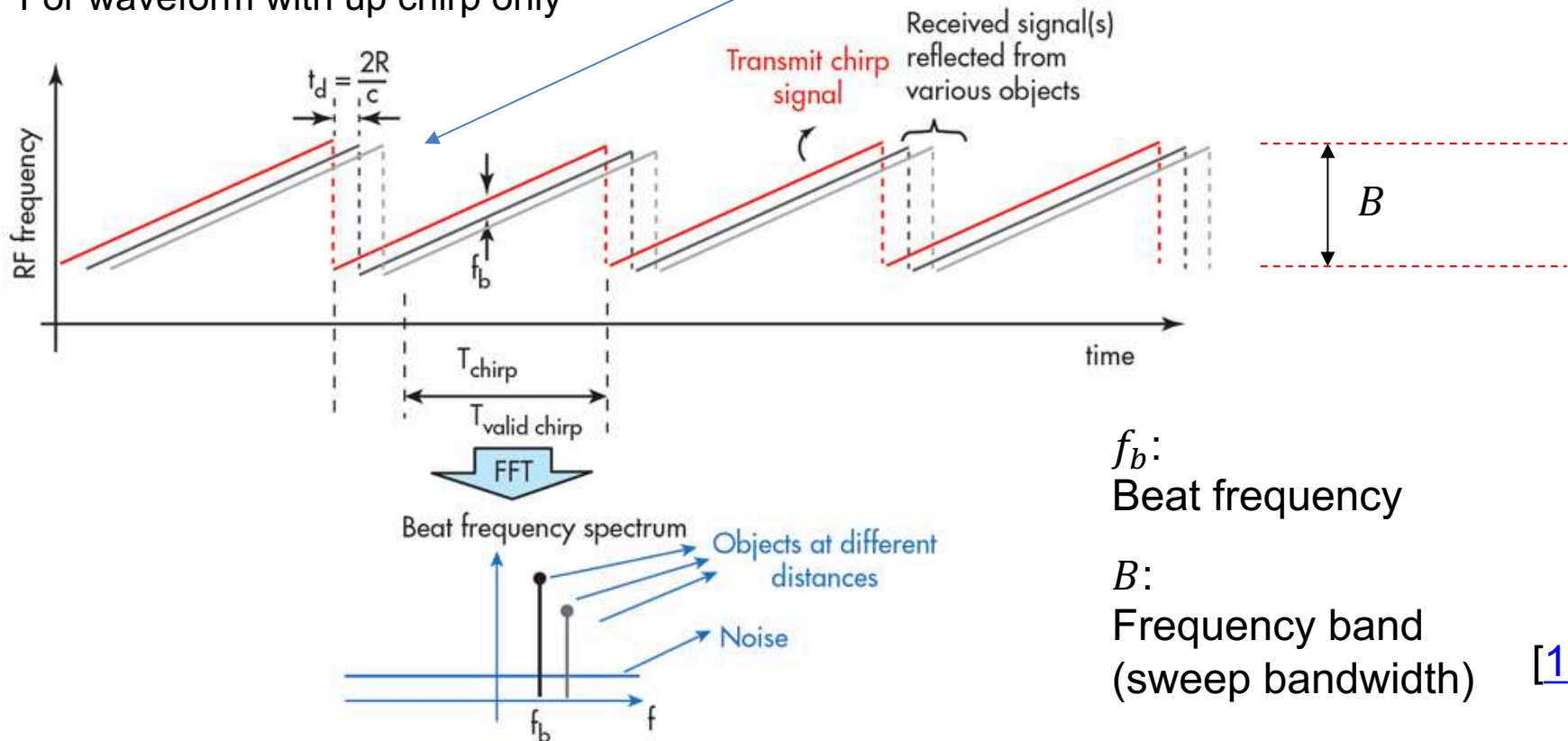
- For waveform with up chirp only - Range

$$R = \frac{ct_d}{2} \rightarrow t_d = \frac{2R}{c}$$

Based on triangle similarity:

$$\frac{t_d}{f_b} = \frac{T}{B} \rightarrow R = f_b \frac{cT}{2B}$$

For waveform with up chirp only

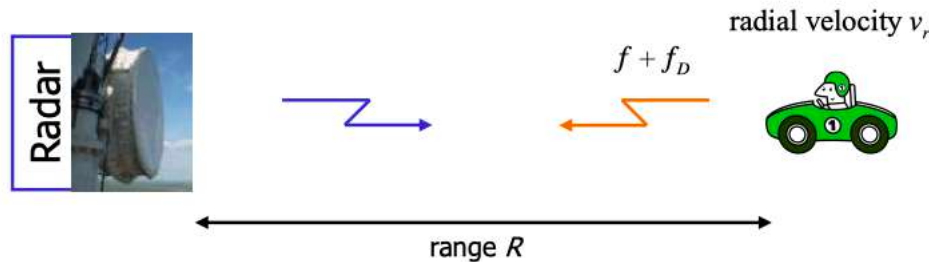






# Automotive Radar - FMCW Radar

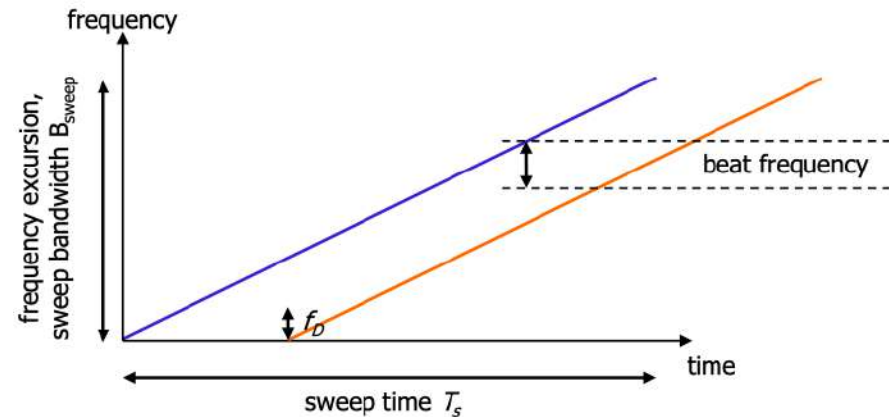
- For waveform with up chirp only - Speed



Re-visit

$$\begin{aligned} \cos\left(2\pi f_c \left(t + \frac{2(R_0 + v_0 t)}{c}\right)\right) &= \\ \cos\left(2\pi \left(f_c + f_c \frac{2v_0}{c}\right)t + \frac{2\pi f_c R_0}{c}\right) &= \\ \underbrace{-f_D}_{-f_D} \quad f_D = -f_c \frac{2v_0}{c} = -\frac{2v_0}{\lambda_c} \end{aligned}$$

- A moving target induces a Doppler frequency shift with the radar wavelength  $\lambda$   
$$f_d = \frac{2V}{\lambda_c}$$



The beat frequency is not only related to the range of the target, but also to its relative radial velocity with respect to the radar.

Both are mixed, how to resolve it?



# Automotive Radar - FMCW Radar

- For waveform with both up and down chirps

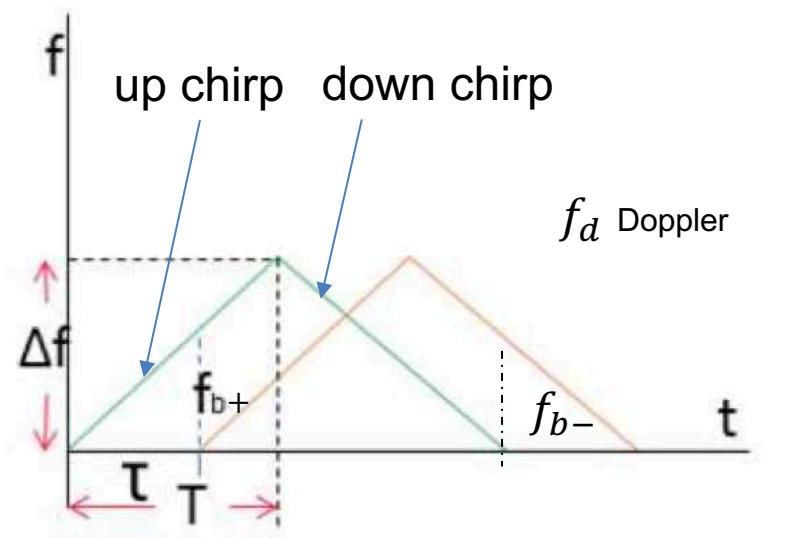
$$f_b = \frac{2BR}{cT} \quad f_d = \frac{2V}{\lambda_c}$$

Upsweep Beat Frequency

$$f_{b+} = f_b - f_d$$

Downsweep Beat Frequency

$$f_{b-} = f_b + f_d$$



Advantage of both up and down chirps?

- Less bandwidth for same transmitted power

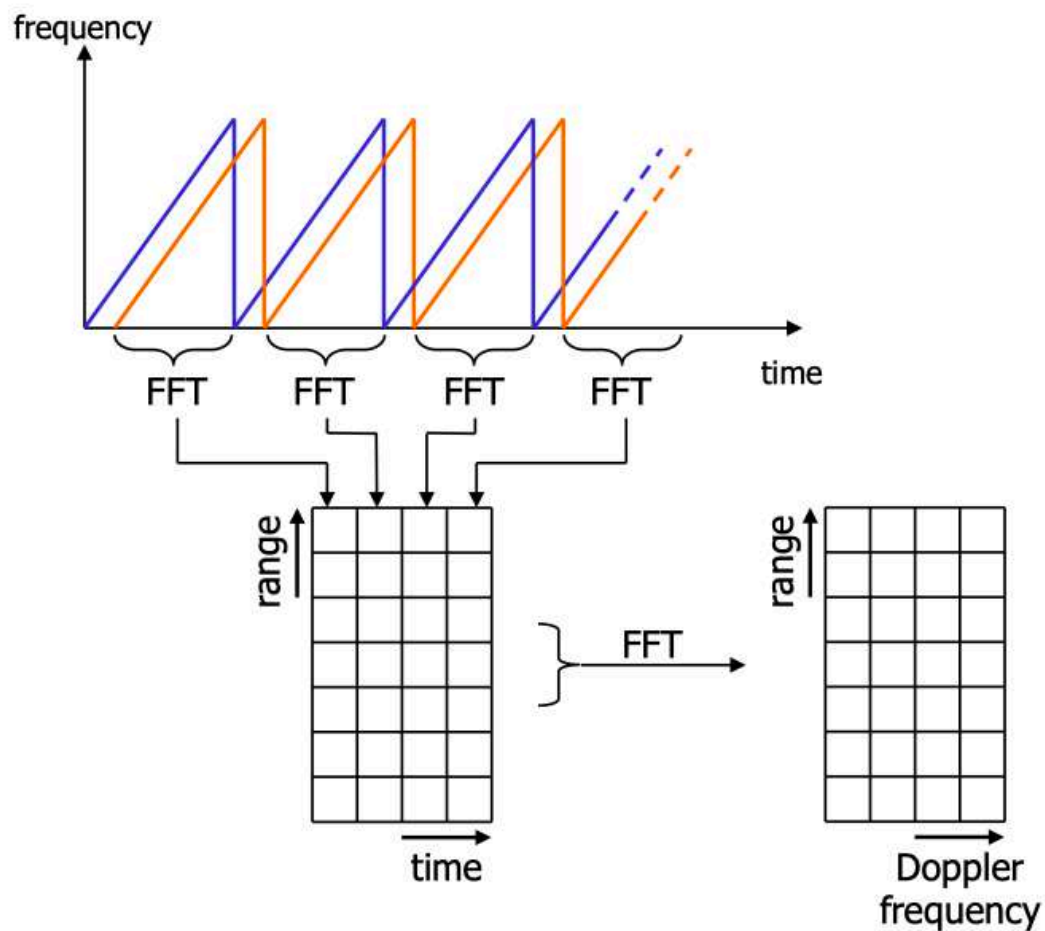
$$P = \frac{1}{\pi} \int_{B_{low}}^{B_{high}} F(\omega) d\omega$$

Range  $R = \frac{cT}{4B} f_{b+} + f_{b-}$

Speed  $V = \frac{\lambda}{4} f_{b+} - f_{b-}$

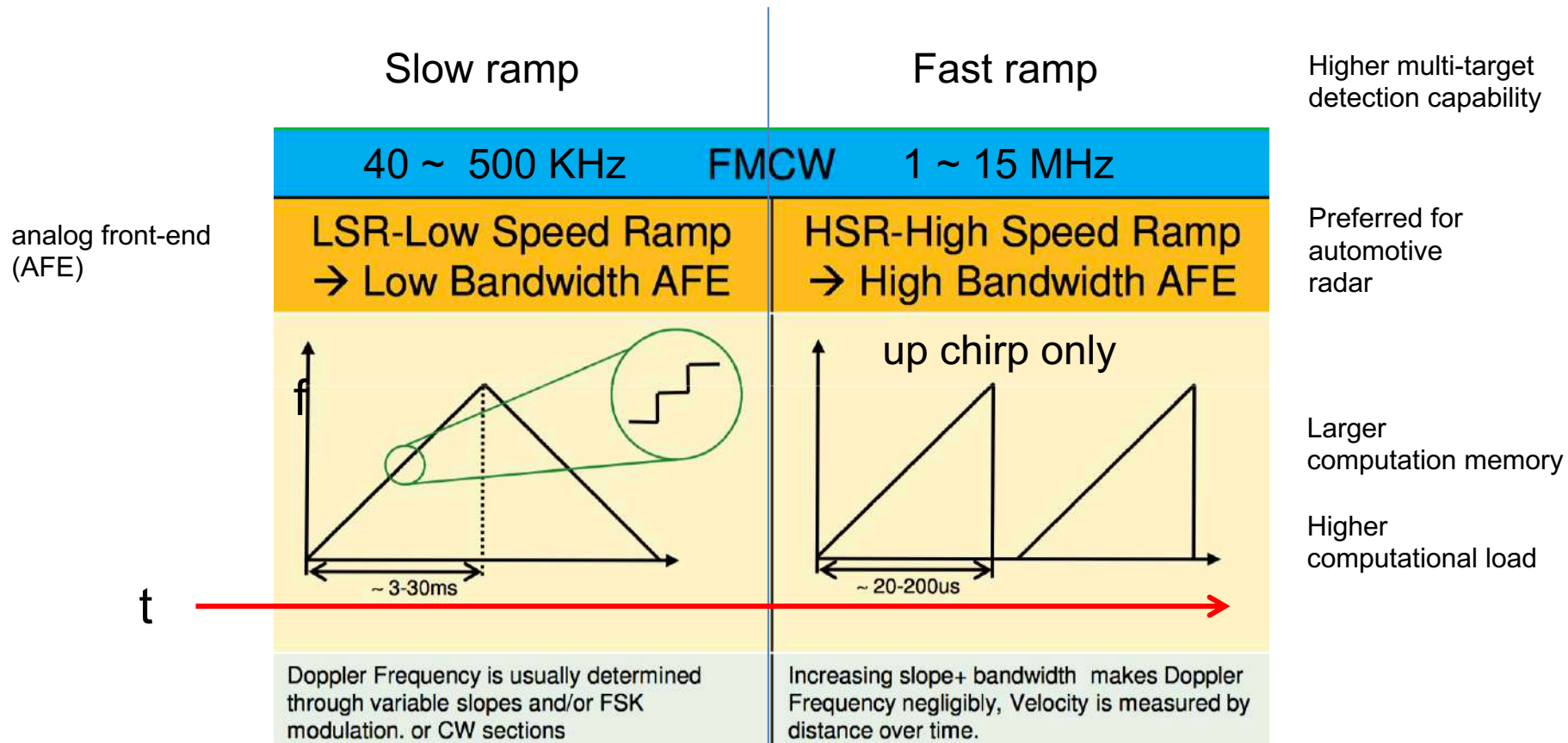
# Automotive Radar - FMCW Radar

- FMCW Radar signal processing



# Automotive Radar - FMCW Radar

- Two categories of FMCW radar modulated frequency [1]



Two types for Fast ramp waveforms:

- Up or down chirp only
- Both up and down chirps

# Automotive Radar - FMCW Radar

- FMCW radar characteristics
  - Higher cost circuitry
  - Lower power consumption
  - Lower accuracy for the detection
  - Simultaneous range and radial velocity
- Applications:
  - Long range radar, et al

Table: Comparison of UWB and FMCW Radar.  
(Bold text represents the superior system in each category)

Category	UWB ( <i>Pulsed radar</i> )	FMCW (tested at 5.8 GHz)
Precision indoor	1.3 cm to 2.8 cm	<b>1.1 cm to 2.3 cm</b>
→ relative	< <b>0.4 %</b>	< 0.8 %
Precision outdoor	1.4 cm to 2.2 cm	<b>1.2 cm to 2.2 cm</b>
→ relative	< 0.6 %	< <b>0.4 %</b>
Accuracy indoor	<b>always &lt;2 % or 25 cm</b>	generally <3 % or 25 cm
Accuracy outdoor	generally <1 % or 20 cm	<b>generally &lt;1 % or 10 cm</b>
Maximum range	32 m at high data rate	<b>At least 70 m</b>
→ theoretical	240 m with 10 % packet loss	<b>245 m</b>
Update rate	<b>Around 400 Hz</b>	Around 4 Hz
Track moving targets	<b>Very good</b>	Glitches, low update rate
Spectral efficiency	$1.36 \cdot 10^{-2} \text{ bit/s/Hz}$	no data transfer
Bandwidth	500 MHz	<b>100 MHz/150 MHz</b> at 2.4 GHz/5.8 GHz
Output power	-12 dBm	18 dBm
Transceiver power	520 mW peak	≈ 900 mW
Processing power	≈ 8 mW	≈ 700 mW
Computational effort	<b>Very low</b> (timestamp subtraction)	High (very large FFTs)

# Automotive Radar - FMCW Radar

- FMCW radar V.S. Pulse Doppler radar

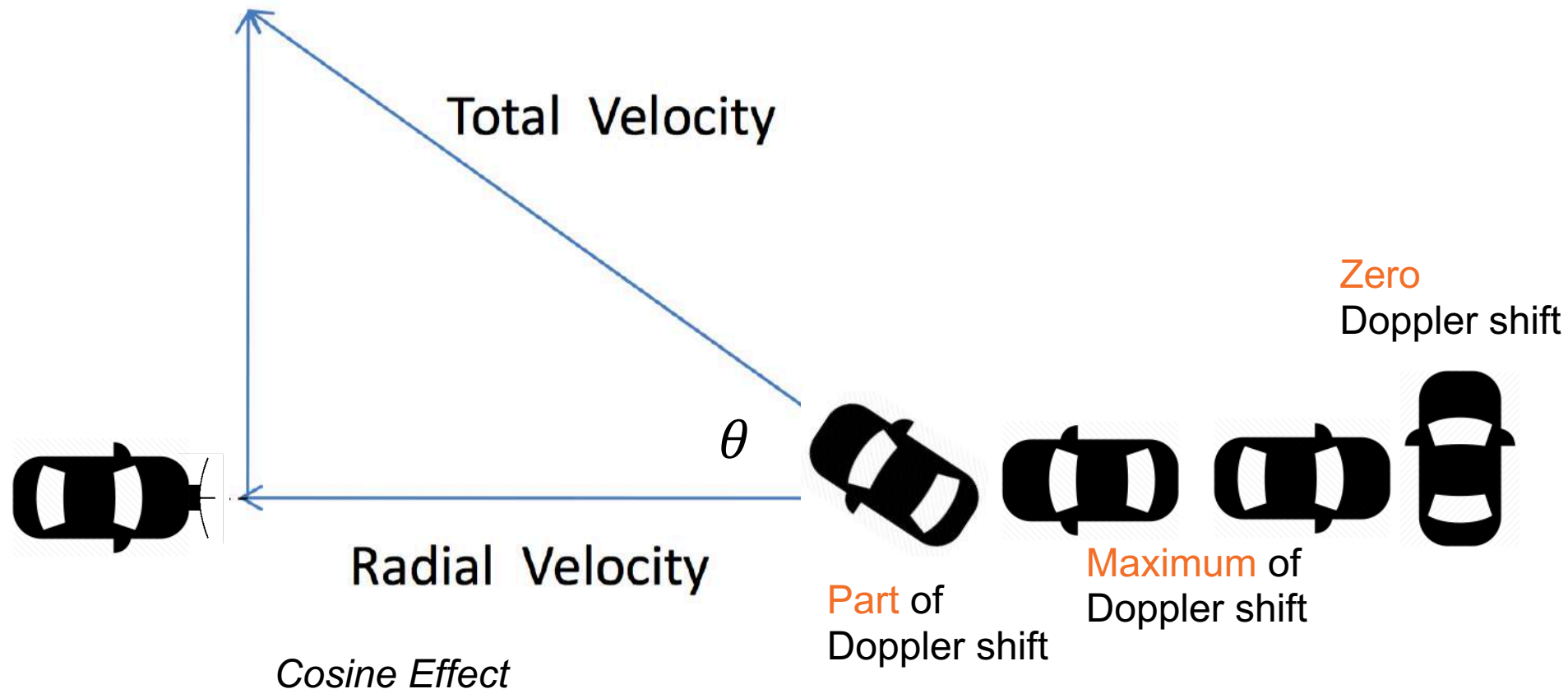
Architecture	FMCW	Pulse Doppler
Principle of operation	Imaging	Doppler
Transmission	Continuous, low power	Pulse, high power
Cause of detection	change in return look to look	Phase shift caused by motion
Resolution	High, approx 800,000 cells	Low, approx 100,000 cells
Zones of low Probability of Detection (PD)	No	Yes
Target radial motion threshold	zero	Approx 2.5 mph
Sensitivity to wind blown false alarms	Almost zero	High
Detection sensitive to direction of travel	No	Highly
Detect zero speed target	Yes	No





# Automotive Radar DOA

- Direction of Arrival (DOA)
- Motivation (Relative) horizontal angle  $\theta$





# Automotive Radar DOA

## Application for ACC

### Azimuth estimation



LRR typically  $\pm 5\sim 10^\circ$  in 250 m

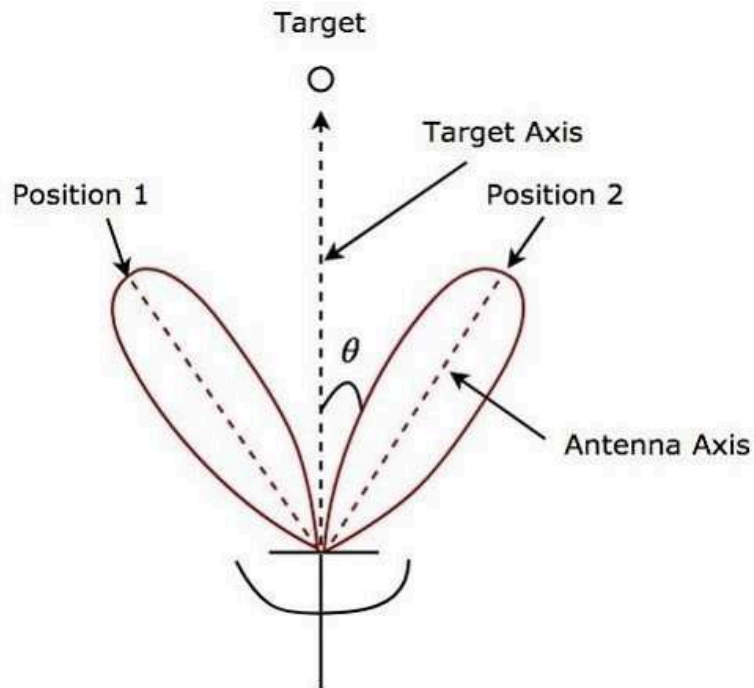
MRR typically  $\pm 45^\circ$  in 60 m

## Adaptive cruise control

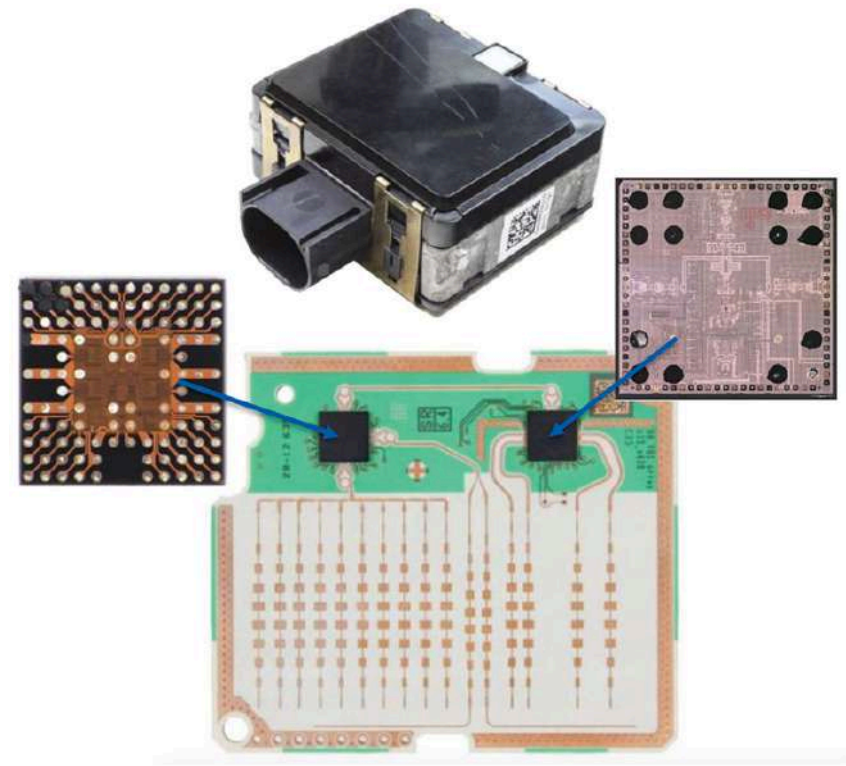


## Automotive Radar DOA

- Digital beamforming with antenna-array
- Multiple radar beams



Sequential lobing



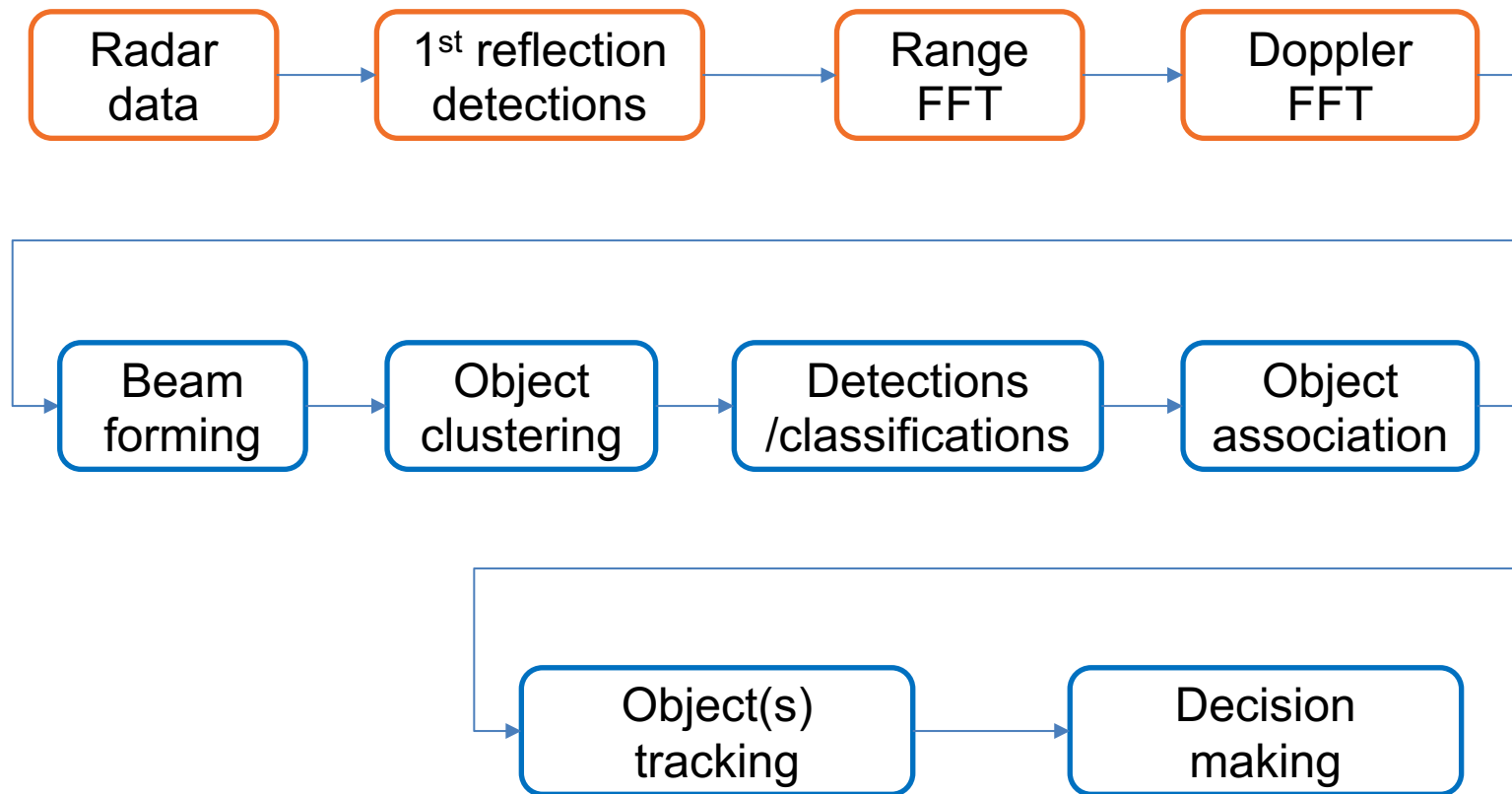
Bosch MRR sensor

Main antenna:  $\pm 10^\circ$  in 60 m  
Elevation antenna:  $\pm 25^\circ$  in 36 m



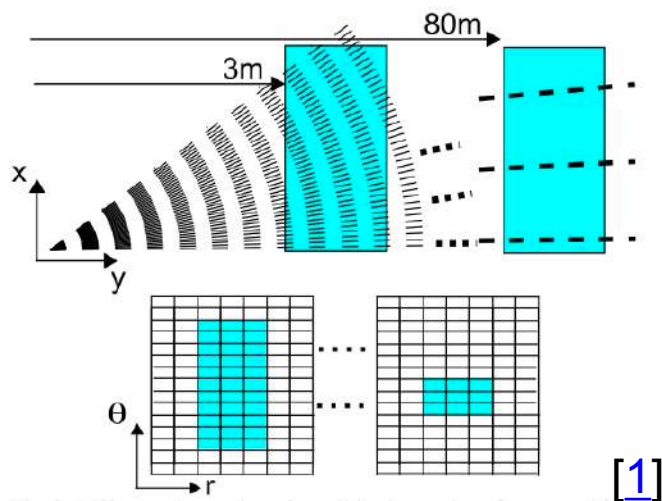
# Automotive Radar Object Detection

- Object detection and tracking procedure



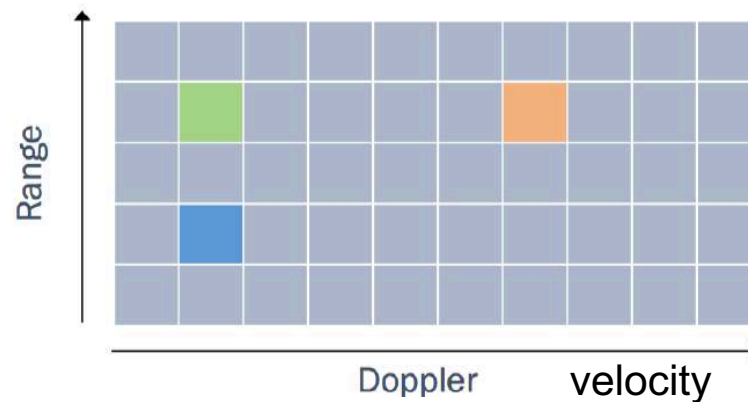
FFT (Fast Fourier Transform)

# Automotive Radar Object Clustering

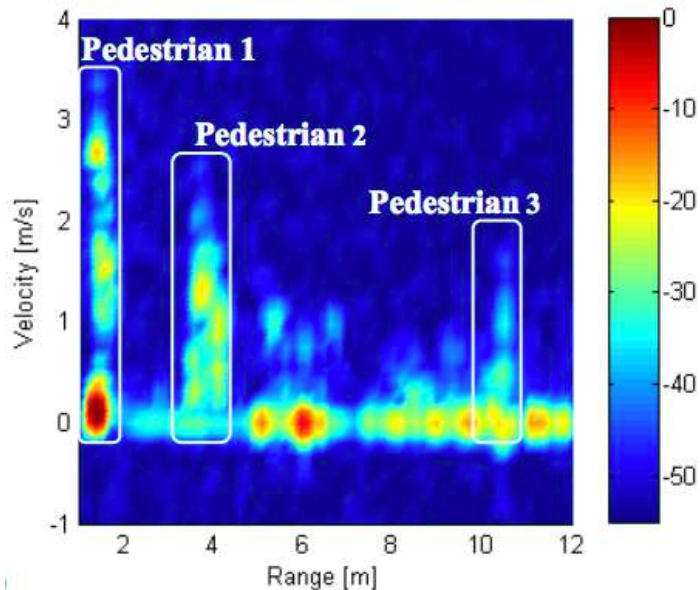


[1]

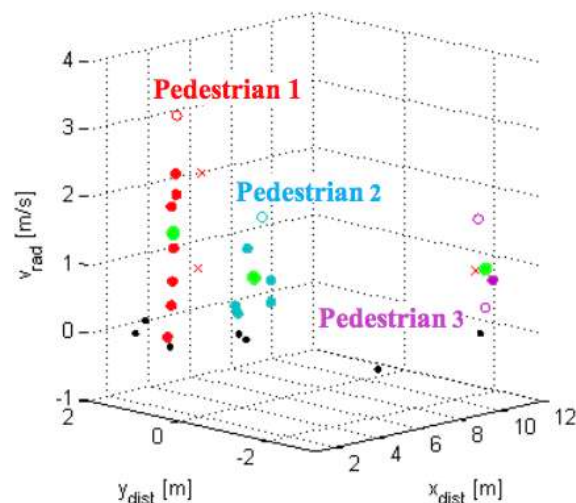
Ranges and velocities of three objects:



Detection data:



Based on Constant false alarm rate (CFAR) techniques:



[2]



# Automotive Radar Object Clustering

- DBSCAN approach (parameter-based)
  - Density-Based Spatial Clustering of Applications with Noise (DBSCAN)

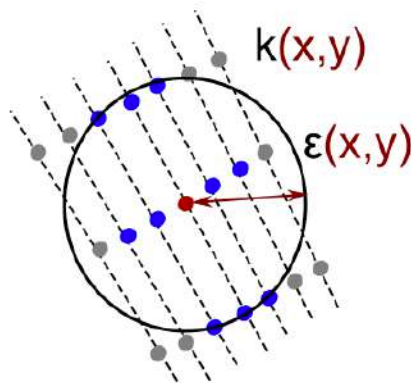
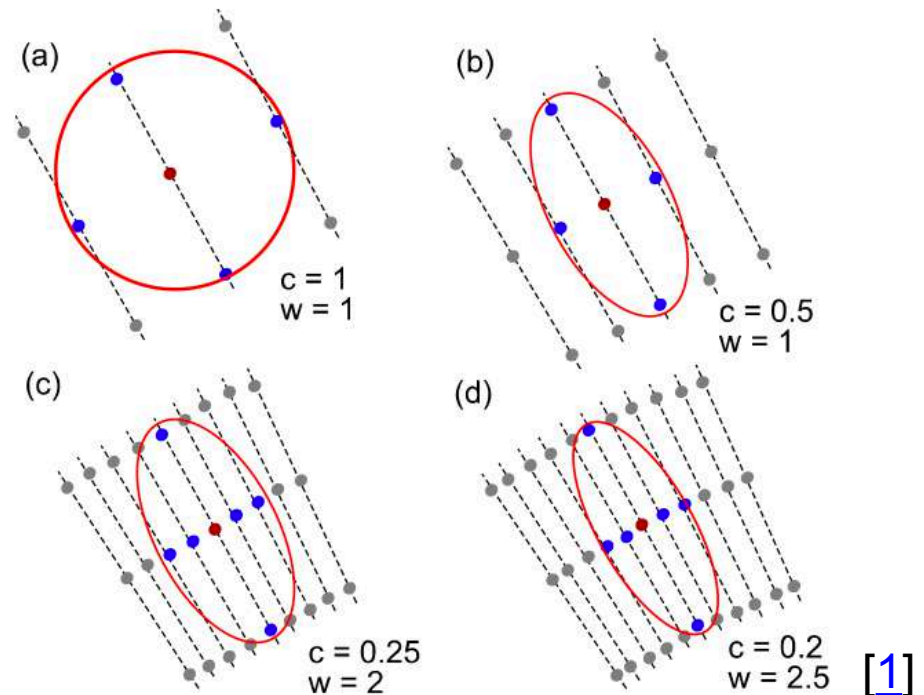
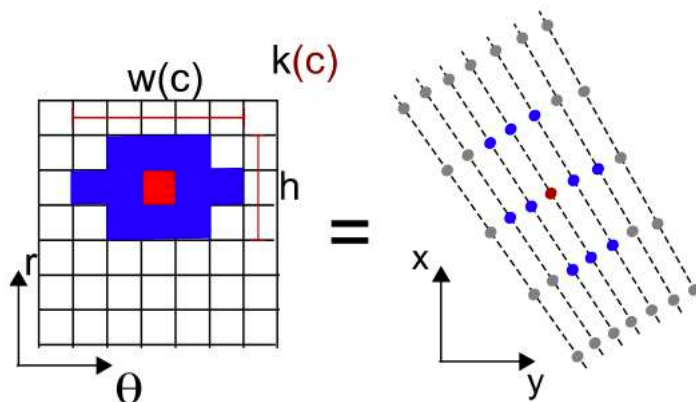


Fig. 4: Calculation of the density criterion using DBSCAN with an adaptive search radius  $\epsilon$  and adaptive threshold  $k$  in Cartesian coordinates

$$w_{i,j}(c) = \frac{g}{f \cdot c_{i,j}}$$

$$c_{i,j} = \frac{r_{i,j}}{2\Delta r} (\sin(\theta_{i,j+1} - \theta_{i,j}) + \sin(\theta_{i,j} - \theta_{i,j-1}))$$

with:  $i,j$  index of grid in  $r/\theta$  - direction  
 $r_{i,j}$  radial distance  
 $\Delta r$  radial resolution (constant)  
 $\theta_{i,j}$  azimuth angle





# Automotive Radar Object Clustering

- DBSCAN result
- Segmentation

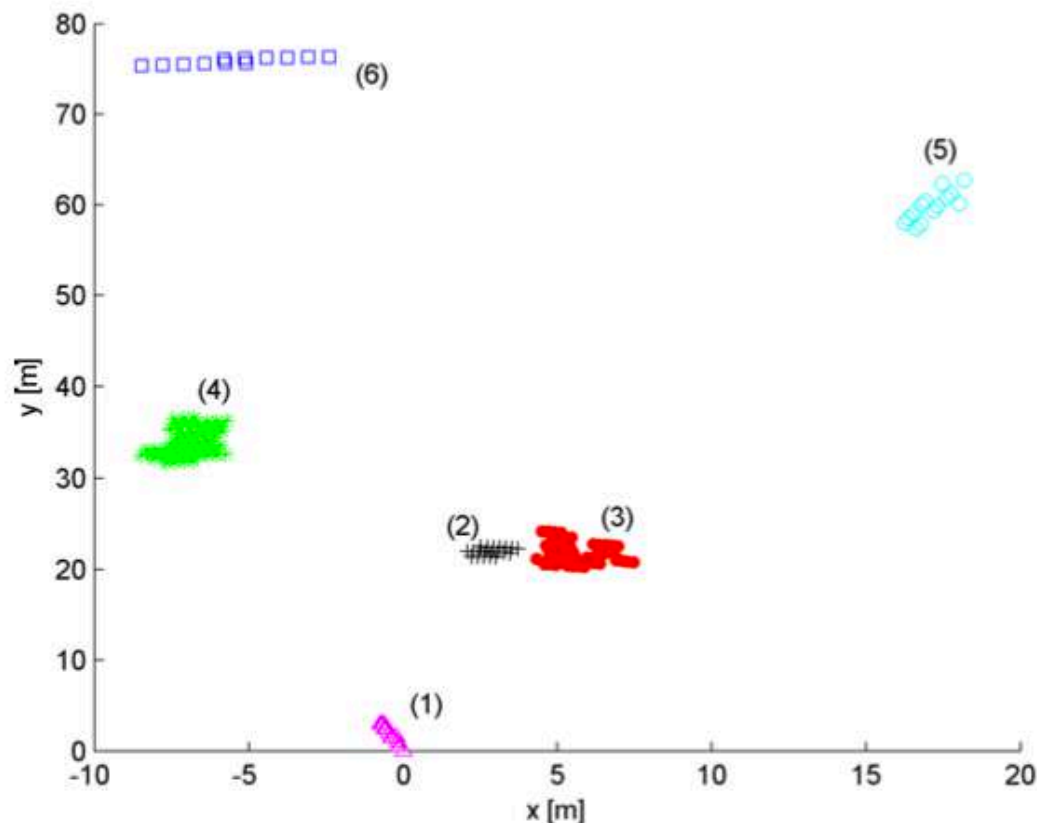
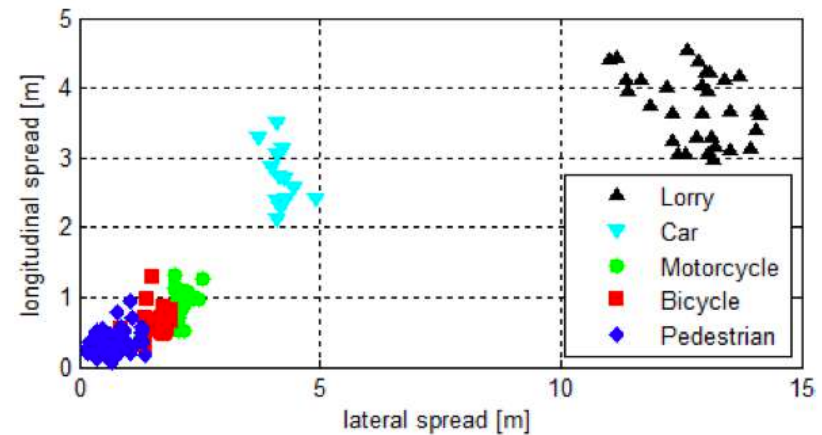
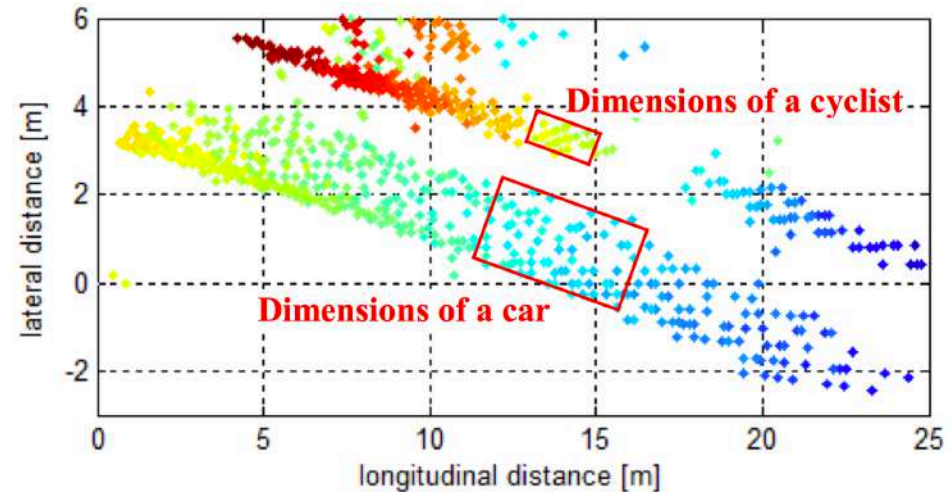
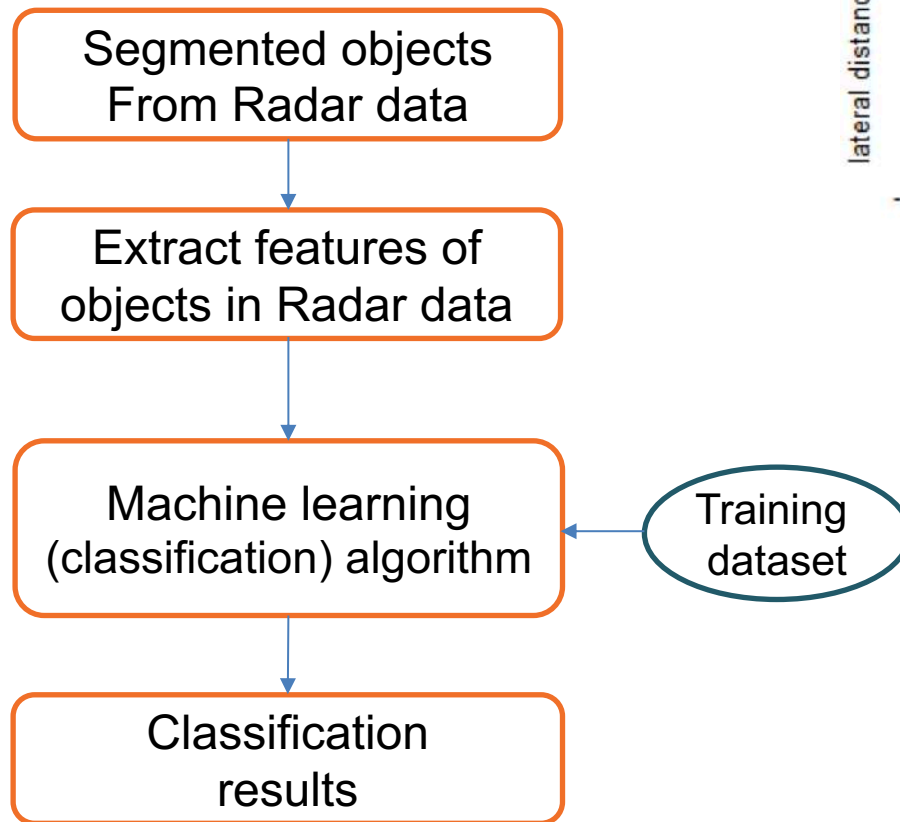


Fig. 9: Clustering results for grid-based DBSCAN ( $f = 2$ ) showing outliers (pink triangle) and 5 clusters (red, green, black, blue, cyan) for clutter (1), a pedestrian (2) next to a car (3), two other vehicles (4-5) and a barrier (6)

# Automotive Radar Object Classification

- Classification approach



Features: Distance spread, Dimension, Velocity  
 $\sigma$ : Radar cross section (RCS) ...



# Automotive Radar Object Tracking

- Tracking based on motion model

$$\mu_t = [x, y, v_x, v_y, \dots]^T$$

- For linear model trajectory
  - zero acceleration model

$$\mu_t = \begin{bmatrix} 1 & 0 & \Delta t & 0 \\ 0 & 1 & 0 & \Delta t \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \mu_{t-1}$$

- For non-linear model trajectory
  - Linearization

$$H_t = \frac{\partial h(\bar{\mu}_t)}{\partial x_t} \quad G_t = \frac{\partial g(u_t, \mu_{t-1})}{\partial x_{t-1}}$$

Kalman filter:

$$\bar{\mu}_t = A_t \mu_{t-1} + B_t u_t$$

$$\bar{\Sigma}_t = A_t \Sigma_{t-1} A_t^T + R_t$$

$$K_t = \bar{\Sigma}_t C_t^T (C_t \bar{\Sigma}_t C_t^T + Q_t)^{-1}$$

$$\mu_t = \bar{\mu}_t + K_t (z_t - C_t \bar{\mu}_t)$$

$$\Sigma_t = (I - K_t C_t) \bar{\Sigma}_t$$

Extended Kalman filter:

$$\bar{\mu}_t = g(u_t, \mu_{t-1})$$

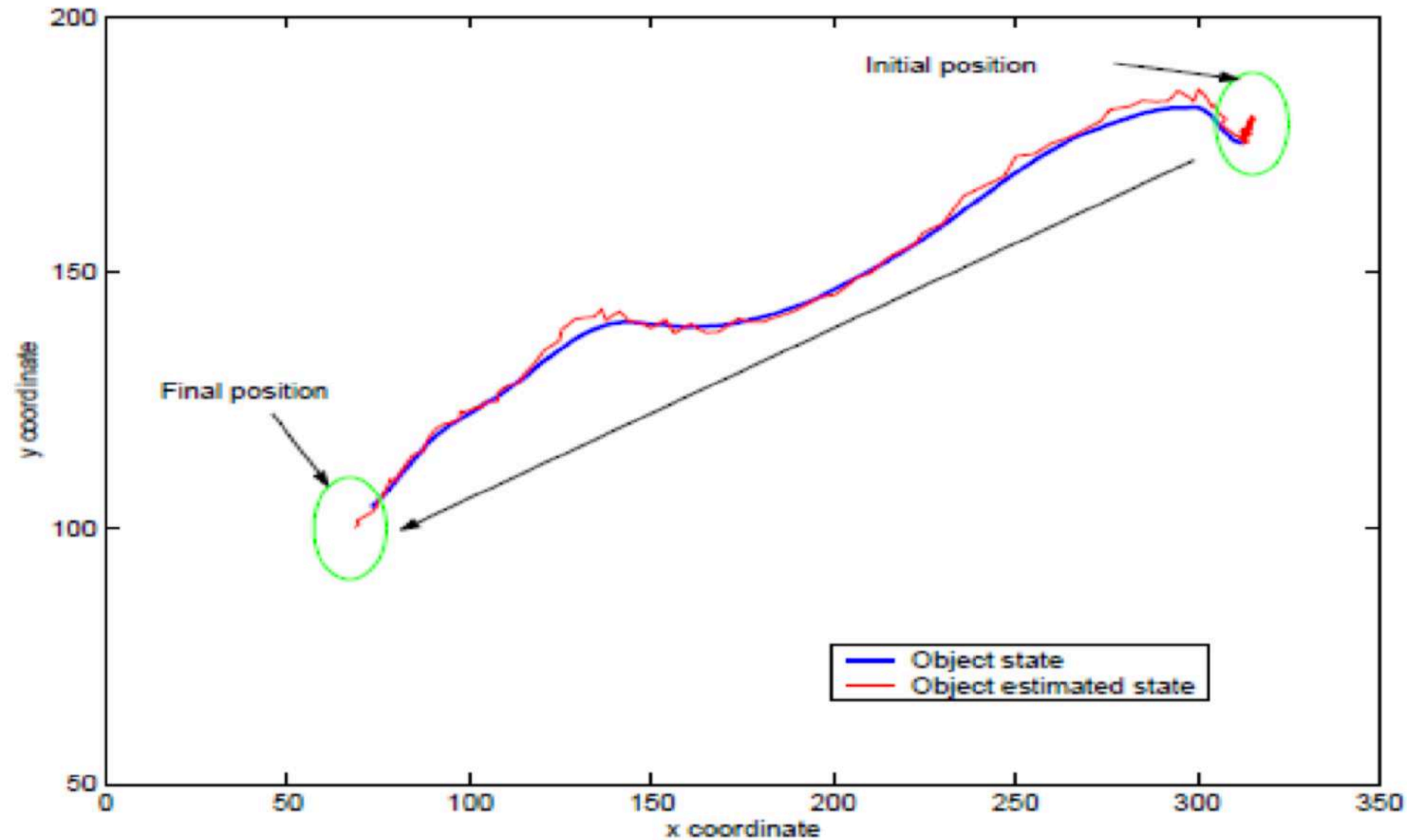
$$\bar{\Sigma}_t = G_t \Sigma_{t-1} G_t^T + R_t$$

$$K_t = \bar{\Sigma}_t H_t^T (H_t \bar{\Sigma}_t H_t^T + Q_t)^{-1}$$

$$\mu_t = \bar{\mu}_t + K_t (z_t - h(\bar{\mu}_t))$$

$$\Sigma_t = (I - K_t H_t) \bar{\Sigma}_t$$

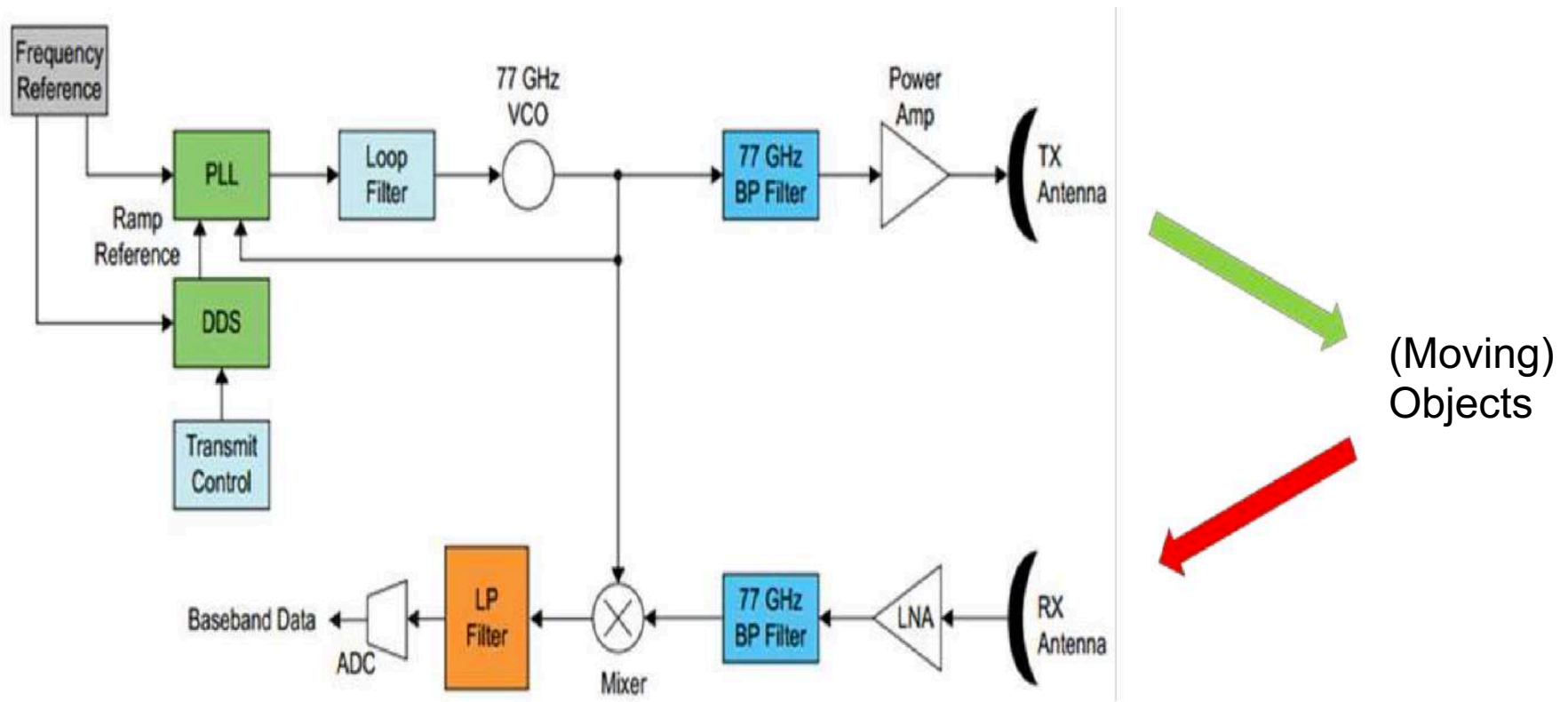
# Automotive Radar Object Tracking





# Automotive Radar Systems

- 77 GHz Automotive Radar system example



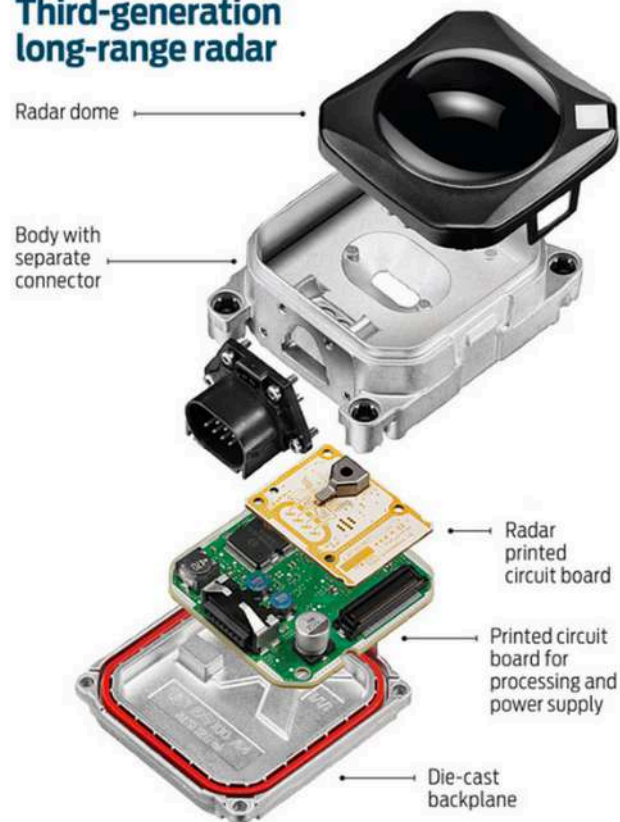
# Automotive Radar Systems

**EVOLUTION OF A RADAR** Bosch's latest long-range system greatly simplifies the radar's printed circuit board. Instead of a handful of gallium arsenide chips to generate, amplify, and detect the 77-gigahertz micro-waves, the system uses just one or two (as shown) of Infineon's silicon germanium chips.

## Second-generation long-range radar



## Third-generation long-range radar



Bosch based on SiGe Infineon Chipset

FCMW modulation

LRR 7dBm Pout,  
4 channels (2 TX/RX)

Two PCB boards

On-board Integrated antennas

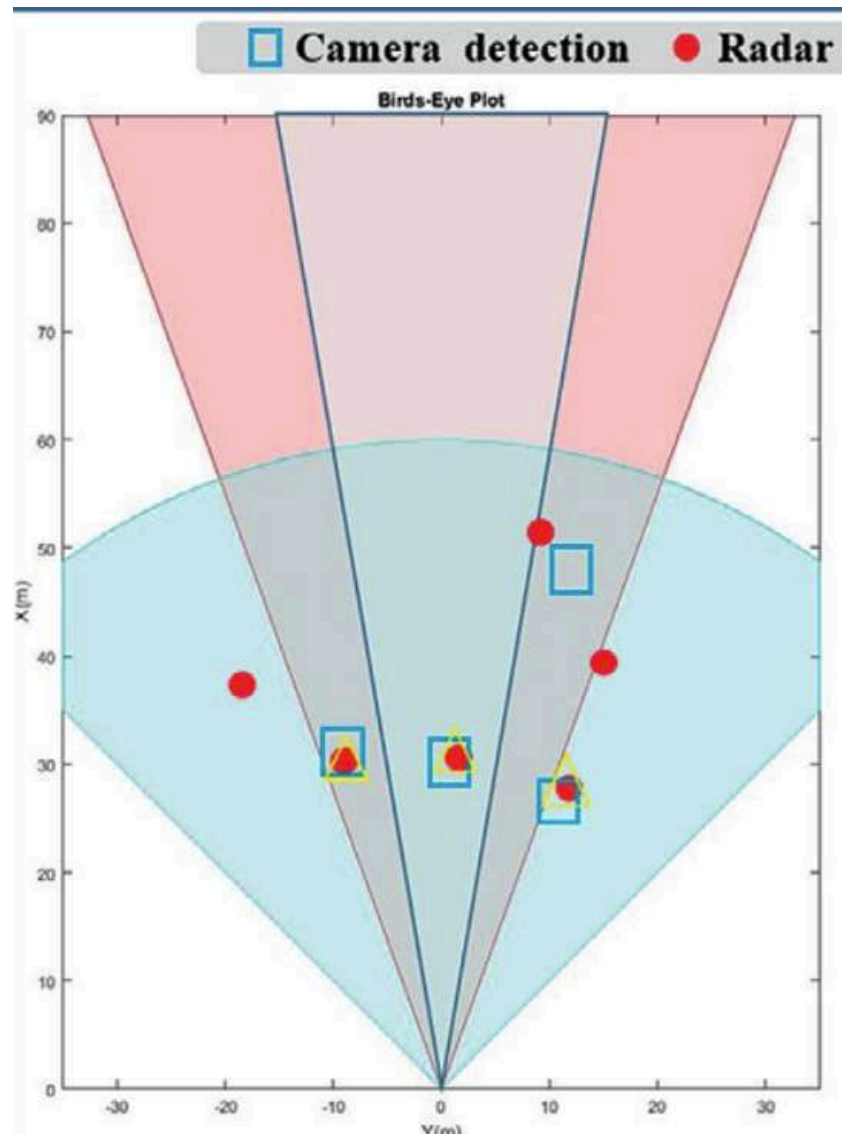
7.4 x 7 x 5.8 cm

Bosch radar generations  
(Source: Bosch)



# Automotive Radar Systems

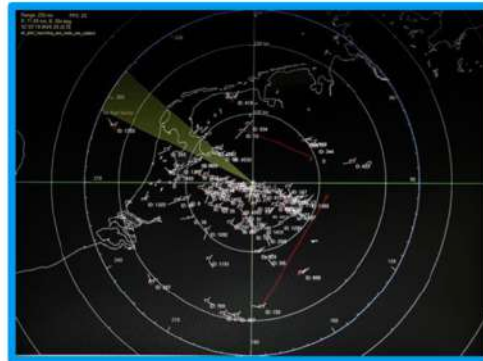
- Radar-camera fusion



# Radar: Other Application Examples

## Automotive localization and mapping

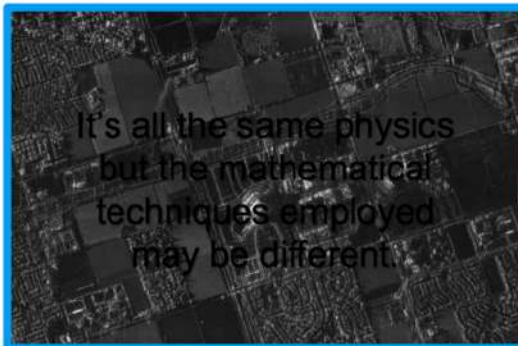
### Military



### Weather



### Imaging



### Speed enforcement





# Summary Highlights

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- Automotive radar
  - SRR/MRR/LRR
  - Range, relative velocity
  - Bandwidth
  - Pulsed VS. FMCW
  - Doppler shift
  - Antenna-array and radar beams
  - Object detection and tracking

END, Thank you



# Reference

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- Maria S. Greco. "Automotive Radar.", IEEE Radar Conference 2012.
- Hasch, Jürgen, Eray Topak, Raik Schnabel, Thomas Zwick, Robert Weigel, and Christian Waldschmidt. "Millimeter-wave technology for automotive radar sensors in the 77 GHz frequency band." IEEE Transactions on Microwave Theory and Techniques 60, no. 3 (2012): 845-860.
- Greg Kregoski. "FMCW Radar in Automotive Applications.", ROHDE & SCHWARZ
- Prasad Malai. "Automotive Radar System.",
- Larry Hawkins, et al. "Radar Defense VS. Automotive.", Analog Devices.
- Brian Su. "Automotive Radar Signal Generation, Analysis And Test Challenges", Keysight Technologies.
- Helena Perslow, and Jeremy Carlson. "ADAS – Current & Future Perspectives". IHS Automotive 2015.



# Appendix Related Resource

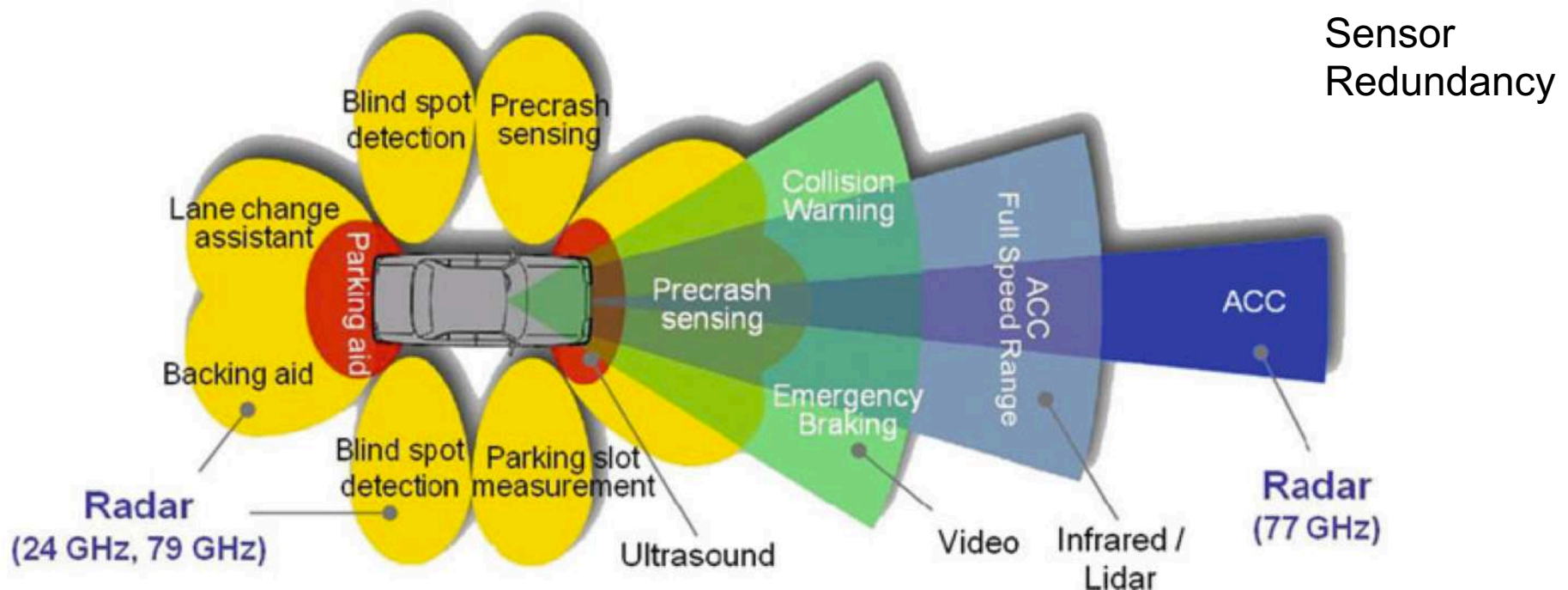
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- [Why are automotive radar systems moving from 24GHz to 77GHz?](#)
- Automotive Dataset: [nuScenes](#) (Data and Python Code), which includes Automotive Radar data
- [Distance Sensors - RADAR](#), Clemson CVEL
- [Automotive Radar Signals: Analysis and Limitations](#) (Video)
- [Radar System Modeling and Simulation for Automotive Advanced Driver Assistance Systems](#) (Video)



# Appendix

- Advanced Driver-Assistance Systems (ADAS)
- Society of Automotive Engineers (SAE): autonomous vehicle levels 0 ~ 5
  - Level 3: Environment detection
- **Level 2+** Automated Driving System on CES 2019





# Appendix

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## Consumer Electronics Show (CES) 2019 --- Level 2+

- Self-driving autopilot capabilities:
  - highway merge
  - lane change
  - lane splits
  - personal mapping
- Inside the vehicle:
  - driver monitoring
  - AI co-pilot capabilities
  - advanced in-cabin visualization