

Given the following equation:

$$z = \frac{\sin(x^2 + 3y^2)}{0.1 + r^2} + (x^2 + 5y^2) * \frac{e^{1-r^2}}{2}, r = \sqrt{x^2 + y^2} \quad (1)$$

The following three algorithms were used to optimize and find the maximum of the function. Hill climbing from position $x = 0.0$ and $y = 0.0$. Then hill climbing with random restarts between -10 and 10 for about 20 times. The third test is simulated annealing with the probability function of $e^{\frac{\text{new-current}}{\text{temperature}}}$

The results of each set:

Name	Highest Point	Time
Hill Climbing	3.7262941710588473	0.008549928665161133
Hill Climb with Restart	0.5166799641198613	1.2141141891479492
Simulated Annealing	3.72795512062296	0.062128305435180664

The Hill Climbing without random restarts is just a lucky example as 0,0 has a good path straight to one of the highest points. Hill climbing with random restarts sometimes gets lucky and follows the path straight up the wall or get stuck in a valley. Simulated Annealing more often than not will get the highest but takes slightly longer than the first test. Given the random restarts not always getting the highest and taking more time (a more accurate representation of the algorithm) it can be assumed that it will more often than not produce results that are not favorable. Whereas simulated annealing gives the highest within a short amount of time. So in a simple conclusion the simulated annealing algorithm is the best. Below you can see the example graphs in 3D space of the paths taken by each algorithm. Running the python code will result in an interactive version of the graph.



