



$$\left. \begin{matrix} \hat{n}_s \\ \hat{\omega} \\ \hat{n}_z \\ \hat{n}_x \end{matrix} \right\} \text{define initially}$$

$$n_z = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}, n_x = \begin{bmatrix} \cos \theta \\ \sin \theta \\ 0 \end{bmatrix} \quad \theta: \text{arbitrary}$$

$$\hat{e}_z = \frac{\tilde{\omega}}{\|\tilde{\omega}\|}$$

$$\hat{n}_z = \begin{bmatrix} \|\hat{n}_z - (\hat{n}_z \cdot \hat{e}_z) \hat{e}_z\| \cos(\omega t) \\ \|\hat{n}_z - (\hat{n}_z \cdot \hat{e}_z) \hat{e}_z\| \sin(\omega t) \\ (\hat{n}_z \cdot \hat{e}_z) \end{bmatrix}$$

$$\hat{n}_x = \begin{bmatrix} \|\hat{n}_x - (\hat{n}_x \cdot \hat{e}_z) \hat{e}_z\| \cos(\omega t + \phi_0) \\ \|\hat{n}_x - (\hat{n}_x \cdot \hat{e}_z) \hat{e}_z\| \sin(\omega t + \phi_0) \\ (\hat{n}_x \cdot \hat{e}_z) \end{bmatrix} \Rightarrow \text{to calculate } \phi_0$$

$$\phi_0 = \arctan \left(\frac{n_{xI}}{\|\hat{n}_x - (\hat{n}_x \cdot \hat{e}_z) \hat{e}_z\|}, \frac{n_{xI}}{\|\hat{n}_x - (\hat{n}_x \cdot \hat{e}_z) \hat{e}_z\|} \right)$$

$$\hat{n}_x = \begin{bmatrix} n_{xI} \\ n_{xJ} \\ n_{xK} \end{bmatrix}$$

$$\hat{n}_y = \hat{n}_z \times \hat{n}_x$$

\Downarrow

$$\left. \begin{matrix} -\hat{n}_s \\ -\hat{n}_y \\ -\hat{n}_z \end{matrix} \right\} \begin{matrix} \hat{n}_x(t) \\ \hat{n}_y(t) \\ \hat{n}_z(t) \end{matrix} \rightarrow \begin{matrix} \varphi_x = \hat{n}_s \cdot \hat{n}_x \\ \varphi_y = \hat{n}_s \cdot \hat{n}_y \\ \varphi_z = \hat{n}_s \cdot \hat{n}_z \\ \varphi_{-y} = -\hat{n}_s \cdot \hat{n}_y \\ \varphi_{-y} = -\hat{n}_y \cdot \hat{n}_s \\ \varphi_{-z} = -\hat{n}_z \cdot \hat{n}_s \end{matrix}$$