

Write a program to generate Yokoi connected number:



Original



Binary 128



Downsampling



Yokoi

(a) Binary 128

```
def getBinaryImage(originalImage, threshold):  
    """  
    :type originalImage: Image (from PIL)  
    :type threshold: int  
    :return type: Image (from PIL)  
    """  
  
    from PIL import Image  
    # New image with the same size and 'binary' format.  
    binaryImage = Image.new('1', originalImage.size)  
    # Scan each column in original image.  
    for c in range(originalImage.size[0]):  
        # Scan each row in original image.  
        for r in range(originalImage.size[1]):  
            # Get pixel value in original image at (c, r).  
            originalPixel = originalImage.getpixel((c, r))  
            if (originalPixel >= threshold):  
                # Put pixel value '1' to binary image.  
                binaryImage.putpixel((c, r), 1)  
            else:  
                # Put pixel value '0' to binary image.  
                binaryImage.putpixel((c, r), 0)  
    # Return binary image.  
    return binaryImage
```

```
if __name__ == '__main__':  
    from PIL import Image  
    import numpy as np  
  
    # Load image from file.  
    originalImage = Image.open('lena.bmp')  
    # Get binary image.  
    binaryImage = getBinaryImage(originalImage, 128)  
    # Save binary image to file.  
    binaryImage.save('binary.bmp')
```

(b) Downsampling (128x128 divided by 8x8)

```
def downsampling(originalImage, sampleFactor):
    """
    :type originalImage: Image (from PIL)
    :type sampleFactor: int
    :return type: Image (from PIL)
    """
    from PIL import Image
    # Calculate the width and height of downsampling image.
    downsamplingWidth = int(originalImage.size[0] / sampleFactor)
    downsamplingHeight = int(originalImage.size[1] / sampleFactor)
    # New image with the downsampling size and 'binary' format.
    downsamplingImage = Image.new('1', (downsamplingWidth, downsamplingHeight))
    # Scan each column in downsampling image.
    for c in range(downsamplingImage.size[0]):
        # Scan each row in downsampling image.
        for r in range(downsamplingImage.size[1]):
            # Get pixel value in original image at (c * sampleFactor, r * sampleFactor).
            originalPixel = originalImage.getpixel((c * sampleFactor, r * sampleFactor))
            # Put pixel to downsampling image.
            downsamplingImage.putpixel((c, r), originalPixel)
    # Return downsampling image.
    return downsamplingImage
```

```
if __name__ == '__main__':
    from PIL import Image
    import numpy as np

    # Load image from file.
    originalImage = Image.open('lena.bmp')
    # Get binary image.
    binaryImage = getBinaryImage(originalImage, 128)
    # Save binary image fo file.
    binaryImage.save('binary.bmp')

    # Get downsampling image.
    downsamplingImage = downsampling(binaryImage, 8)
    # Save downsampling image fo file.
    downsamplingImage.save('downsampling.bmp')
```

(c) Yokoi

a. 4 connected neighborhood detection

```

def getNeighborhoodPixels(originalImage, position):
    """
    :type originalImage: Image (from PIL)
    :type position: tuple
    :return type: numpy array
    """
    # Allocate memory space of neighborhoodPixels.
    neighborhoodPixels = np.zeros(9)
    # Get x and y of position.
    x, y = position
    # Scan dx from -1 to 1.
    for dx in range(3):
        # Scan dy from -1 to 1.
        for dy in range(3):
            # Calculate destination x, y position.
            destX = x + (dx - 1)
            destY = y + (dy - 1)
            # Avoid out of image range.
            if ((0 <= destX < originalImage.size[0]) and \
                (0 <= destY < originalImage.size[1])):
                # Get neighborhood pixel values.
                neighborhoodPixels[3 * dy + dx] = originalImage.getpixel((destX, destY))
            # It is out of image range.
            else:
                # Padding zeros when it is out of image range.
                neighborhoodPixels[3 * dy + dx] = 0
    # Original order: [[x0, x1, x2], [x3, x4, x5], [x6, x7, x8]]
    # Sort pixels in [[x7, x2, x6], [x3, x0, x1], [x8, x4, x5]] order.
    neighborhoodPixels = [
        neighborhoodPixels[4], neighborhoodPixels[5], neighborhoodPixels[1],
        neighborhoodPixels[3], neighborhoodPixels[7], neighborhoodPixels[8],
        neighborhoodPixels[2], neighborhoodPixels[0], neighborhoodPixels[6]]
    # Return Neighborhood Pixels.
    return neighborhoodPixels

```

b. Detect the edge and counting in Yokoi

```

def hFunctionYokoi(b, c, d, e):
    """
    :type b: int
    :type c: int
    :type d: int
    :type e: int
    :return type: str
    """
    if ((b == c) and (b != d or b != e)):
        return 'q'
    if ((b == c) and (b == d and b == e)):
        return 'r'
    if (b != c):
        return 's'

def fFunctionYokoi(a1, a2, a3, a4):
    """
    :type a1: str
    :type a2: str
    :type a3: str
    :type a4: str
    :return type: str
    """
    # a1 == a2 == a3 == a4 == r
    if ([a1, a2, a3, a4].count('r') == 4):
        # Return label 5 (interior).
        return 5
    else:
        # Return count of 'q'.
        # 0: Isolated, 1: Edge, 2: Connecting, 3: Branching, 4: Crossing.
        return [a1, a2, a3, a4].count('q')

```

c. Mapping Yokoi number to image

```
def YokoiConnectivityNumber(originalImage):
    """
    :type originalImage: Image (from PIL)
    :return type: numpy array
    """
    # Allocate memory space of Yokoi Connectivity Number.
    YokoiConnectivityNumber = np.full(downsamplingImage.size, ' ')

    # Scan each column in original image.
    for c in range(originalImage.size[0]):
        # Scan each row in original image.
        for r in range(originalImage.size[1]):
            # This point is object.
            if (originalImage.getpixel((c, r)) != 0):
                # Get neighborhood pixel values.
                neighborhoodPixels = getNeighborhoodPixels(originalImage, (c, r))
                YokoiConnectivityNumber[c, r] = fFunctionYokoi(
                    hFunctionYokoi(neighborhoodPixels[0], neighborhoodPixels[1], neighborhoodPixels[6],
                                   neighborhoodPixels[0], neighborhoodPixels[2], neighborhoodPixels[7],
                                   neighborhoodPixels[0], neighborhoodPixels[3], neighborhoodPixels[8],
                                   neighborhoodPixels[0], neighborhoodPixels[4], neighborhoodPixels[5],
                                   neighborhoodPixels[0], neighborhoodPixels[5], neighborhoodPixels[8],
                                   neighborhoodPixels[6], neighborhoodPixels[7], neighborhoodPixels[8]),
                    neighborhoodPixels[0], neighborhoodPixels[1], neighborhoodPixels[2], neighborhoodPixels[3],
                    neighborhoodPixels[4], neighborhoodPixels[5], neighborhoodPixels[6], neighborhoodPixels[7],
                    neighborhoodPixels[8])
            # This point is background.
            else:
                YokoiConnectivityNumber[c, r] = ' '

    # Return Yokoi Connectivity Number.
    return YokoiConnectivityNumber
```

```
if __name__ == '__main__':
    from PIL import Image
    import numpy as np

    # Load image from file.
    originalImage = Image.open('lena.bmp')
    # Get binary image.
    binaryImage = getBinaryImage(originalImage, 128)
    # Save binary image to file.
    binaryImage.save('binary.bmp')

    # Get downsampling image.
    downsamplingImage = downsampling(binaryImage, 8)
    # Save downsampling image to file.
    downsamplingImage.save('downsampling.bmp')

    # Get Yokoi Connectivity Number.
    YokoiConnectivityNumber = YokoiConnectivityNumber(downsamplingImage)
    # Save Yokoi Connectivity Number to file.
    np.savetxt('YokoiConnectivityNumber.txt',
               YokoiConnectivityNumber.T,
               delimiter=' ', fmt='%s')
```