MPS[1] Protocol – BAN logic

Sign Up Real Protocol

M_1: A → S: $K_a, E_{k_s}(A, N_a)$

M_2: S → A: $E_{k_a}(A, N_a, N_s)||E_{k_s^-}(S(E_{k_a}(A, N_a, N_s)))$

M_3: A → S: $E_{k_s}(A, N_s, g_a, p_a)||E_{k_a^-}(S(E_{k_a}(A, N_s, g_a, p_a)))$

M_4: S → A: $E_{k_a}(A, N_s, g_a, p_a)||E_{k_s^-}(S(E_{k_a}(A, N_s, g_a, p_a)))$

Sign Up Idealized Protocol

M_1: A → S: $\{A, N_a\}_{k_s}$

M_2: S → A: $\{A, N_a, \#(N_a), N_s\}_{k_a}||\{S(\{A, N_a, \#(N_a), N_s\}_{k_a})\}_{k_s^-}$

M_3: A → S: $\{A, N_s, \#(N_s), g_a, p_a\}_{k_s}||\{S(\{A, N_s, \#(N_s), g_a, p_a\}_{k_s})\}_{k_a^-}$

M_4: S → A: $\{A, N_s, \#(N_s), g_a, p_a\}_{k_a}||\{S(\{A, N_s, \#(N_s), g_a, p_a\}_{k_a})\}_{k_s^-}$

Sign Up Protocol Analysis

Objectives

$S \models (g_a, p_a)$ # Diffie Hellman Parameters

$A \models S \models (g_a, p_a)$ # DH Parameters confirmation

Assumptions

$A \models \xrightarrow{k_s} S$ # Hardcoded Server's Public Key

$S \models \xrightarrow{k_a} A$ # Alice's Public Key sent in plaintext in the first message

$S \models A \Rightarrow g_a, p_a$

After M_1:

$S \lhd \{A, N_a\}_{k_s}$

After M_2:

$$\frac{A \models \xrightarrow{k_s} S \ , \ A \lhd \{A, N_a, \#(N_a), N_s\}_{k_s^-}}{A \models S \mid\sim (A, N_a, \#(N_a), N_s)}$$

[1] Magherini – Pochiero – Sieni (MPS)

$$\frac{A \models S \mid\sim (A, N_a,\ \#(N_a), N_s),\ A \models \#(N_a)}{A \models S \models (A, N_a,\ \#(N_a), N_s)}$$

After M_3:

$$\frac{S \overset{k_a}{\models\!\rightarrow} A,\ S \lhd \{A, N_s, \#(N_s), g_a, p_a\}_{k_a^-}}{S \models A \mid\sim (A, N_s, \#(N_s), g_a, p_a)}$$

$$\frac{S \models A \mid\sim (A, N_s, \#(N_s), g_a, p_a),\ S \models \#(N_s)}{S \models A \models g_a, p_a}$$

$$\frac{S \models A \Rightarrow g_a, p_a, S \models A \models (A, N_s, \#(N_s), g_a, p_a)}{S \models (g_a, p_a)}$$

After M_4:

$$\frac{A \overset{k_s}{\models\!\rightarrow} S,\ A \lhd \{A, N_s,\ \#(N_s), g_a, p_a\}_{k_s^-}}{A \models S \mid\sim (A, N_s,\ \#(N_s), g_a, p_a)}$$

$$\frac{A \models S \mid\sim (A, N_s,\ \#(N_s), g_a, p_a),\ A \models \#(N_s)}{A \models S \models g_a, p_a}$$

Authentication Real Protocol

M_1: A → S: $E_{k_s}(A, N_a) \,||\, E_{k_a^-}(S(E_{k_s}(A, N_a)))$

M_2: S → A: $E_{k_a}(A, N_a, N_s, K_{as}) \,||\, E_{k_s^-}(S(E_{k_a}(A, N_a, N_s, K_{as})))$

M_3: A → S: $E_{k_{as}}(A, N_s)$

Authentication Idealized Protocol

M_1: A → S: $\{A, N_a\}_{k_s} \,||\, \{S(\{A, N_a\}_{k_s})\}_{k_a^-}$

M_2: S → A: $\{A, N_a, \#(N_a), N_s,\ (A \overset{k_{as}}{\leftrightarrow} S)\}_{k_a} \,||\, \{S(\{A, N_a, \#(N_a), N_s,\ (A \overset{k_{as}}{\leftrightarrow} S)\}_{k_a})\}_{k_s^-}$

M_3: A → S: $\{A,\ N_s, \#(N_s),\ (A \overset{k_{as}}{\leftrightarrow} S)\}_{k_{as}}$

Authentication Analysis

Objectives

$A \models \#(N_s)$, $S \models A \models \#(N_s)$ # Session ID

$A \models A \overset{k_{as}}{\leftrightarrow} S$ $A \models \#(A \overset{k_{as}}{\leftrightarrow} S)$ # Session Key

$S \models A \models A \overset{k_{as}}{\leftrightarrow} S$ # Session Key confirmation

Assumptions

$S \models A \overset{k_{as}}{\leftrightarrow} S$ # Session Key

$A \models \overset{k_s}{\rightarrow} S$ # Hardcoded Server's Public Key

$S \models \overset{k_a}{\rightarrow} A$ # Alice's Public Key

$A \models S \Rightarrow N_s$ # Nonce Authority

$A \models S \Rightarrow A \overset{k_{as}}{\leftrightarrow} S$ # Session Key Authority

After M_1:

$$\frac{S \models \overset{k_a}{\rightarrow} A, \ S \lhd \{A, N_a\}_{k_a^-}}{S \models A \mid\sim (A, N_a)}$$

After M_2:

$$\frac{A \models \overset{k_s}{\rightarrow} S \ , \ A \lhd \left\{A, N_a, \#(N_a), N_s, \ (A \overset{k_{as}}{\leftrightarrow} S)\right\}_{k_s^-}}{A \models S \mid\sim (A, N_a, \#(N_a), N_s, \ (A \overset{k_{as}}{\leftrightarrow} S))}$$

$$\frac{A \models S \mid\sim \left(A, N_a, \#(N_a), N_s, \ (A \overset{k_{as}}{\leftrightarrow} S)\right), \ A \models \#(N_a)}{A \models S \models \left(A, N_a, \#(N_a), N_s, \ (A \overset{k_{as}}{\leftrightarrow} S)\right)}$$

$$\frac{A \models S \models N_s \, , \ A \models S \Rightarrow N_s}{A \models N_s}$$

$$\frac{A \models S \models (A \overset{k_{as}}{\leftrightarrow} S), \ A \models S \Rightarrow (A \overset{k_{as}}{\leftrightarrow} S)}{A \models (A \overset{k_{as}}{\leftrightarrow} S)}$$

$$\frac{A \models N_s, \ A \models \#(N_a)}{A \models \#(N_s)}$$

$$\frac{A \models A \overset{k_{as}}{\leftrightarrow} S, \ A \models \#(A \overset{k_{as}}{\leftrightarrow} S)}{A \models \#(A \overset{k_{as}}{\leftrightarrow} S)}$$

After M_3:

$$\frac{S \models A \overset{k_{as}}{\leftrightarrow} S \ , \ S \lhd \left\{A, \ N_s, \#(N_s), \ (A \overset{k_{as}}{\leftrightarrow} S)\right\}_{k_{as}}}{S \models A \mid\sim (A, \ N_s, \#(N_s), \ (A \overset{k_{as}}{\leftrightarrow} S))}$$

$$\frac{S \models A \mid\sim (A,\ N_s, \#(N_s),\ (A \overset{k_{as}}{\leftrightarrow} S)),\ S \models \#(N_s)}{S \models A \models \#(N_s)}$$

$$\frac{S \models A \mid\sim (A,\ N_s, \#(N_s),\ (A \overset{k_{as}}{\leftrightarrow} S)),\ S \models \#(N_s)}{S \models A \models A \overset{k_{as}}{\leftrightarrow} S}$$

Online Key Exchange Real Protocol

M_1: A → S: $E_{k_{as}}(A, B, N_{sa})$

M_2: S → A: $E_{k_{as}}\left(A, B, N_{sa}, g_b, p_{b,} k_{b,} E_{k_{bs}}(k_a, N_{sb}, N_{sa})\right)$

M_3: A → B: $E_{k_b}\left(A, B, Y_A, E_{k_{bs}}(k_a, N_{sb}, N_{sa})\right) || E_{k_{\bar{a}}}(S(E_{k_b}\left(A, B, Y_{A,} E_{k_{bs}}(k_a, N_{sb})\right)))$

M_4: B → A: $E_{k_a}\left(A, B, Y_B, N_{sa}, E_{k_{ab}}(N_b)\right) || E_{k_{\bar{b}}}(S(E_{k_a}\left(A, B, Y_B, E_{k_{ab}}(N_b)\right)))$

M_5: A → B: $E_{k_{ab}}(N_b)$

M_x: A → B: $E_{k_{ab}}(data,\ SeqNum)$

Online Key Exchange Idealized Protocol

M_1: A → S: $\{A, B, N_{sa}\}_{k_{as}}$

M_2: S → A: $\left\{A, B, N_{sa}, g_b, p_{b,} \overset{k_b}{\rightarrow} B, \left\{\overset{k_a}{\rightarrow} A, N_{sb}, N_{sa}\right\}_{k_{bs}}, \#(N_{sa})\right\}_{k_{as}}$

M_3: A → B: $\left\{A, B, Y_A, \left\{\overset{k_a}{\rightarrow} A, N_{sb}, N_{sa}\right\}_{k_{bs}}, \#(N_{sb})\right\}_{k_b} || \left\{S(\left\{A, B, Y_A, \left\{\overset{k_a}{\rightarrow} A, N_{sb}\right\}_{k_{bs}}, \#(\overset{k_a}{\rightarrow} A)\right\}_{k_b})\right\}_{k_{\bar{a}}}$

M_4: B → A: $\left\{A, B, Y_b, N_{sa}, \{N_b\}_{k_{ab}}\right\}_{k_a} || \left\{S(\left\{A, B, Y_b, \{N_b\}_{k_{ab}}\right\}_{k_a})\right\}_{k_{\bar{b}}}$

M_5: A → B: $\{N_b\}_{k_{ab}}$

Online Key Exchange Analysis

Objectives

$A \models A \overset{k_{ab}}{\leftrightarrow} B$,	$B \models A \overset{k_{ab}}{\leftrightarrow} B$	# Key Authentication
$A \models B \models A \overset{k_{ab}}{\leftrightarrow} B$,	$B \models A \models A \overset{k_{ab}}{\leftrightarrow} B$	# Key Confirmation

Assumptions

$A \models A \overset{k_{as}}{\leftrightarrow} S\,, \quad S \models A \overset{k_{as}}{\leftrightarrow} S$ # A-S Session keys (authentication protocol)

$B \models B \overset{k_{bs}}{\leftrightarrow} S\,, \quad S \models B \overset{k_{bs}}{\leftrightarrow} S$ # B-S Session keys (authentication protocol)

$S \models \#(N_{sa}), \quad A \models \#(N_{sa}), B \models \#(N_{sb})$ # Freshness session ids (authentication protocol)

$S \models (g_b, p_b)$ # Diffie Hellman's parameters

$A \models B \Rightarrow Y_B\,, \quad B \models A \Rightarrow Y_A$ # Authority on Y parameters

After M_1:

$$\frac{S \models A \overset{k_{as}}{\leftrightarrow} S\,, \quad S \lhd \{A, B, N_{sa}\}_{k_{as}}}{S \models A \mid\sim (A, B, N_{sa})}$$

$$\frac{S \models A \mid\sim (A, B, N_{sa}), \quad S \models \#(N_{sa})}{S \models A \models (A, B, N_{sa})}$$

After M_2:

$$\frac{A \models A \overset{k_{as}}{\leftrightarrow} S\,, \quad A \lhd \left\{A, B, N_{sa}, g_b, p_{b,} \overset{k_b}{\rightarrow} B, \left\{\overset{k_a}{\rightarrow} A, N_{sb}, N_{sa}\right\}_{k_{bs}}, \#(N_{sa})\right\}_{k_{as}}}{A \models S \mid\sim (A, B, N_{sa}, g_b, p_{b,} \overset{k_b}{\rightarrow} B, \left\{\overset{k_a}{\rightarrow} A, N_{sb}, N_{sa}\right\}_{k_{bs}}, \#(N_{sa}))}$$

$$\frac{A \models S \mid\sim (X), \quad A \models \#(N_{sa})}{A \models S \models (X)}$$

$$\frac{A \models S \models \overset{k_b}{\rightarrow} B\,, \quad A \text{ trusts } S \text{ on } k_b}{A \models \overset{k_b}{\rightarrow} B}$$

$$\frac{A \models S \models (g_b, p_b)\,, \quad A \text{ trusts } S \text{ on } (g_b, p_b)}{A \models (g_b, p_b)}$$

After M_3:

$$\frac{B \models B \overset{k_{bs}}{\leftrightarrow} S\,, \quad B \lhd \left\{\overset{k_a}{\rightarrow} A, N_{sb}, N_{sa}\right\}_{k_{bs}}}{B \models S \mid\sim \left(\overset{k_a}{\rightarrow} A, N_{sb}, N_{sa}\right)}$$

$$\frac{B \models S \mid\sim \left(\overset{k_a}{\rightarrow} A\right), \quad B \models \#(N_{sb})}{B \models S \models \left(\overset{k_a}{\rightarrow} A\right)}$$

$$\frac{B \models S \models \overset{k_a}{\rightarrow} A\,,\ B\ trusts\ S\ on\ k_a}{B \models \overset{k_a}{\rightarrow} A}$$

$$\frac{B \models \overset{k_a}{\rightarrow} A\ ,\ B \lhd \left\{A, B,\ Y_A, \left\{\overset{k_a}{\rightarrow} A, N_{sb}, N_{sa}\right\}_{k_{bs}}, \#(N_{sb})\right\}_{k_a^-}}{B \models A \mid\sim (A, B,\ Y_A, \left\{\overset{k_a}{\rightarrow} A, N_{sb}, N_{sa}\right\}_{k_{bs}}, \#(N_{sb}))}$$

$$\frac{B \models A \mid\sim (A, B,\ Y_A, \left\{\overset{k_a}{\rightarrow} A, N_{sb}, N_{sa}\right\}_{k_{bs}}, \#(N_{sb})),\ B \models \#(N_{sb})}{B \models A \models (A, B,\ Y_A, \left\{\overset{k_a}{\rightarrow} A, N_{sb}, N_{sa}\right\}_{k_{bs}}, \#(N_{sb}))}$$

$$\frac{B \models A \models Y_A,\ B \models A \Rightarrow Y_A}{B \models Y_A}$$

$$\frac{B \models Y_A,\ B \Rightarrow Y_B}{B \models A \overset{k_{ab}}{\leftrightarrow} B}$$

After M_4:

$$\frac{A \models \overset{k_b}{\rightarrow} B\ ,\ A \lhd \left\{A, B, Y_b, N_{sa}, \{N_b\}_{k_{ab}}\right\}_{k_b^-}}{A \models B \mid\sim (A, B, Y_b, N_{sa}, \{N_b\}_{k_{ab}})}$$

$$\frac{A \models B \mid\sim \left(A, B, Y_b, N_{sa}, \{N_b\}_{k_{ab}}\right),\ A \models \#(N_{sa})}{A \models B \models \left(A, B, Y_b, N_{sa}, \{N_b\}_{k_{ab}}\right)}$$

$$\frac{A \models B \models Y_B,\ A \models B \Rightarrow Y_B}{A \models Y_B}$$

$$\frac{A \models Y_B,\ A \Rightarrow Y_A}{A \models A \overset{k_{ab}}{\leftrightarrow} B}$$

$$\frac{A \models A \overset{k_{ab}}{\leftrightarrow} B,\ A \lhd \{N_b\}_{k_{ab}}}{A \models B \mid\sim (N_b)}$$

$$\frac{A \models B \mid\sim (N_b),\ A \models \#(N_{sa})}{A \models B \models A \overset{k_{ab}}{\leftrightarrow} B}$$

After M_5:

$$\frac{B \models A \overset{k_{ab}}{\leftrightarrow} B,\ B \lhd \{N_b\}_{k_{ab}}}{B \models A \mid\sim (N_b)}$$

$$\frac{B \models A \mid\sim (N_b),\ B \models \#(N_b)}{B \models A \models A \overset{k_{ab}}{\leftrightarrow} B}$$

Offline Communication Real Protocol

M_1: A → S: $E_{k_{as}}(A, B, N_{sa})$

M_2: S → A: $E_{k_{as}}(A, B, N_{sa}, k_b)$

M_x: A → S: $E_{k_b}\left(data, SeqNum,\ E_{k_a^-}(S(data, SeqNum))\right)||E_{k_a^-}(S(data, SeqNum,\ E_{k_a^-}(S(data, SeqNum))))$

Offline Communication Idealized Protocol

M_1: A → S: $\{A, B, N_{sa}\}_{k_{as}}$

M_2: S → A: $\left\{A, B, N_{sa}, \overset{k_b}{\rightarrow} B, \#(N_{sa})\right\}_{k_{as}}$

Offline Communication Analysis

Objective

$A \models \overset{k_b}{\rightarrow} B$ # Bob's Public Key

Assumptions

$A \models A \overset{k_{as}}{\leftrightarrow} S$, $S \models A \overset{k_{as}}{\leftrightarrow} S$ # Session key (authentication protocol)

$S \models \#(N_{sa})$, $A \models \#(N_{sa})$ # Freshness session ids (authentication protocol)

After M_1:

$$\frac{S \models A \overset{k_{as}}{\leftrightarrow} S,\ S \lhd \{A, B, N_{sa}\}_{k_{as}}}{S \models A\ |\sim (A, B, N_{sa})}$$

$$\frac{S \models A\ |\sim (A, B, N_{sa}),\ S \models \#(N_{sa})}{S \models A \models (A, B, N_{sa})}$$

After M_2:

$$\frac{A \models A \overset{k_{as}}{\leftrightarrow} S,\ A \lhd \left\{A, B,\ N_{sa}, \overset{k_b}{\rightarrow} B, \#(N_{sa})\right\}_{k_{as}}}{A \models S\ |\sim (A, B, N_{sa}, \overset{k_b}{\rightarrow} B, \#(N_{sa}))}$$

$$\frac{A \models S\ |\sim (X),\ A \models \#(N_{sa})}{A \models S \models (X)}$$

$$\frac{A \models S \models \overset{k_b}{\rightarrow} B\ ,\ \ A\ trusts\ S\ on\ k_b}{A \models \overset{k_b}{\rightarrow} B}$$