## Task 2: Ensemble Classifiers

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## 1 Introduction

### 1.1 Objectives

Our main objective with this work is that of building and fitting ensemble-based tree models that, based on a dataset of cancer patients, predicts recurrence (reappearance of the disease) of cancer from putative recurrence biomarkers. To do so, we build, tune and compare (using python) three different types of models - Random Forests, Gradient Boosting and XGBoost, and then evaluate their performance on our dataset.

#### 1.2 Materials and methods

#### 1.2.1 Datasets and packages

The main python libraries used across the code are: - numpy: fundamental package for scientific computing in Python. - pandas: for a more powerful handling of datasets. - pyplot: we will use this submodule from matplotlib to do most of the plots. - sklearn: open source tool built on top of NumPy, and matplotlib. Along with its submodules, it will be the package used to carry out the coding related to the learning procedures. The submodules imported include tools to tune the models (such as GridSearchCV) or to build specific models (e.g. GradientBoostingClassifier)

Apart from the libraries pre-imported in the following cell, we import other sklearn submodules when needed and the libraries: itertools (for readable and fast iteration) and xgboost (to build the model of the same name).

The datasets used are found in the cancerDat.csv and cancerInfo.csv, and include of cancer patients with the presence of 102 different peptides in the patients' organisms, which have been found to be related to recurrence. These are broken down and studied in the following section.

#### 1.2.2 Procedure

The procedure followed involves four main steps.

Firstly, we clean up the data to ensure it is ready to be used to build the model. This step involves the handling of missing data, renaming the variables and encoding them correctly. To that effect we perform a simple exploratory data analysis.

Secondly, we randomly partition our data into train and test splits using functions from the scikit-learn library. The split will be of size 2/3 for training and 1/3 for testing.

Thirdly, we will build the models, a Random Forest Classifier, a Gradient Boosted decision tree and XGBoost, on the training data (with the imported libraries) and tune their hyperparameters via a grid search.

Lastly, we will analyse the strength of our models by looking at their predicted performance using the test set and evaluate their strengths and weaknesses.

This study has been developed first answering the Questions posed in the assignment one by one and then developing a cohesive report exposing and analysing the results in depth. We have chosen Python to develop the program out of personal preference, but the R programming language is also a viable option.

## 2 Exploratory Data Analysis

We visualize the structure of the data after importing the csv format files. We can see how the data is composed of a table of 129 patients with 102 variables, 101 of which are peptide biomarkers and the other one is the response variable on the recurrence.

The other table corresponds to the same patients but with a single, extra variable site, which is of factor type, that may be related to the kind of recurrence, but the authors are not experts in the domain of clinical oncology. As such, it was decided to omit the treatment of this variable to focus solely on the statistical analysis of the raw recurrence.

```
[6]: print(df1.shape) print(df2.shape)
```

```
(129, 102)
(129, 1)
```

By a coarse inspection of the datafile, we can immediately see that the data ingestion pipeline will require some work, given the combination of the response and patient index into the same variable.

First, we define a single response variable according to whether the cancer sees a recurrence or not. This is originally coded into the key (index) of the patient, so a separate binary vector is created to encode this response, where 0 denotes non-recurrence and 1 denotes recurrence, stored as a Pandas series y = labels\_1.

```
[10]: y = pd.Series(y)
```

The next step in the exploration phase is checking for missing values and calculating some descriptive statistics of the data. With the Pandas library one can easily locate the missing values; in fact there is a substantial amount of missing values (5151) in the dataset, so in order to avoid discarding such a large amount of information, we resort to imputing the linear interpolation of the missing entries, as calculated by Pandas' interpolate method. This artificially increases the amount of information that we work with, but we claim that for the final results this is preferable to eliminating the entire rows and rendering our dataset significantly smaller. The following outputs show the amount of missing values and how they are removed by linear interpolation.

```
[20]: for col in df1:
    df1[col] = pd.to_numeric(df1[col], errors='coerce')
    df1.dtypes;
```

```
[21]: print(df1.isnull().values.any())
    print(sum(df1.isnull()))
    df1 = df1.interpolate(method ='linear', limit_direction ='forward')
    print(df1.isnull().values.any())
```

True 5151 False

Now that we have handled the missing values, we can go ahead and perform some more sophisticated exploration techniques. We provide a small snapshot (the first 9 variables) of the descriptive statistics of the dataset, but note that due to its large size, it is only possible to show a handful of the biomarker variables.

```
[9]: df1.describe()
```

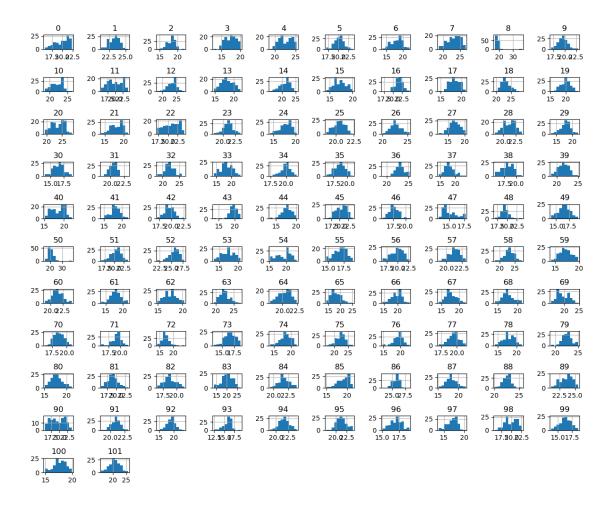
```
[9]:
                    0
                                  1
                                               2
                                                            3
                                                                         4
                                                                                       5
             129.000000
                          129.000000
                                       129.000000
                                                    129.000000
                                                                  129.000000
                                                                               129.000000
     count
                           23.286214
              19.930039
                                        18.226328
                                                      17.331228
                                                                   22.591467
                                                                                20.193446
     mean
     std
               1.646143
                            0.784218
                                         1.126192
                                                       1.477403
                                                                    1.562914
                                                                                 1.185180
              15.836862
                           21.313713
                                        14.401524
                                                      12.976690
                                                                   18.807566
                                                                                16.963778
     min
```

25% 50% 75% max	18.547029 20.341514 21.362745 22.315946	22.755110 23.374865 23.793517 25.387870	17.440432 18.349787 18.968572 21.837865	16.166380 17.373647 18.501081 19.994349	21.321595 22.461809 23.992847 25.306821	19.397560 20.264099 20.961033 23.671558
	6	7	8	9		
count	129.000000	129.000000	129.000000	129.000000		
mean	18.133973	23.193300	18.687522	19.516615		
std	1.751196	1.860021	1.744740	1.068425		
min	13.770822	18.824646	16.818849	16.952402		
25%	17.001766	22.036426	18.109188	18.830477		
50%	18.421874	23.469361	18.548956	19.546749		
75%	19.426085	24.633681	18.967436	20.108405		
max	21.934433	26.596796	36.306672	22.920624		

[8 rows x 102 columns]

In the following compound graph, the distribution of each of the 101 biomarkers is shown in histogram form. In this way, one can observe at a birdseye view the distribution of the different peptide markers.

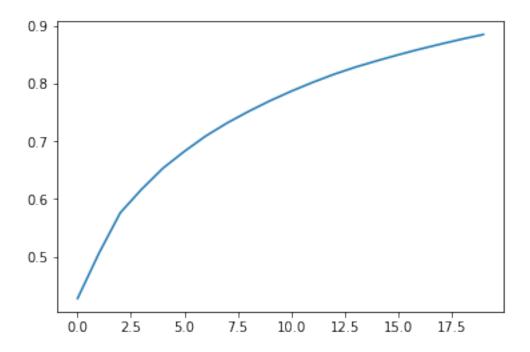
From the histograms, one can observe some erratic distributions for some of the covariates, where they do not seem to fit very well with the statement of the law of large numbers. By this we mean that the shapes of the distributions do not fit our expectations of normal distributions. Specifically, as an example, the covariates indexed in positions 15, 54 or 78 have some interesting shapes as they show multimodal distributions and signs of heavy tails.



We continue the analysis with a Principal Component Analysis (PCA), which lets us identify the directions of largest variation in the data. The data is of high dimension, given that we have 101 explanatory variables, so using a dimensionality reduction technique allows us to potentially examine a how the datapoints could fit into a lower dimensional subspace. We conclude that the amount of variance accumulated by the first twenty principal components amounts to almost 90%. This justifies our final choice of having the classifiers only include ten peptides as features to train on.

```
[11]: plt.plot(list(itertools.accumulate(pca.explained_variance_ratio_)))
```

[11]: [<matplotlib.lines.Line2D at 0x779719e76560>]



## 3 Train-Test Split

We separate the data into two sets: the training set, containing two thirds of the data, and the test set, containing the rest. We will use these sets to fit different models in the next section. We also set a numpy seed to allow for the reproducibility of the results. The exact size of the train-test split is provided for completeness.

```
[26]: np.random.seed(1234)

[32]: print(X_train.shape, X_test.shape, y_train.shape, y_test.shape)

(86, 102) (43, 102) (86,) (43,)
```

# 4 Model building and fitting

The following models are fitted: a Random Forest Classifier and two Boosting Classifiers (Gradient boosting and XGBoost).

### 4.1 Random Forest Classifier

A random forest classifier is built using the scikit-learn library, with the same seed as the one used in the train-test split and limiting the number of total features to 10. The hyperparameters are explored and tuned using a grid search procedure, which is automated thanks to internal methods also from the scikit-learn library.

A simple implementation of the grid search procedure with a *PMSE* given by cross validation is achieved by calling the **GridSearchCV** function, shown in the following cell.

```
[33]: grid_rf = GridSearchCV(rf, parameters)
grid_rf.fit(X_train, y_train)
```

The following table shows the results of the grid search procedure, where the hyperparameters of the best model after validation are shown to be 7 total features and 10 weak estimators. Note that the performance is quite unimpressive, barely improving on the null model.

```
[34]:
         param_max_features param_n_estimators
                                                   mean_test_score
                                                                      std_test_score
      36
                                                           0.594118
                                                                            0.118234
      55
                           10
                                               30
                                                           0.582353
                                                                            0.079792
      48
                            9
                                               10
                                                           0.572549
                                                                            0.142693
      1
                            1
                                               30
                                                           0.569935
                                                                            0.044213
```

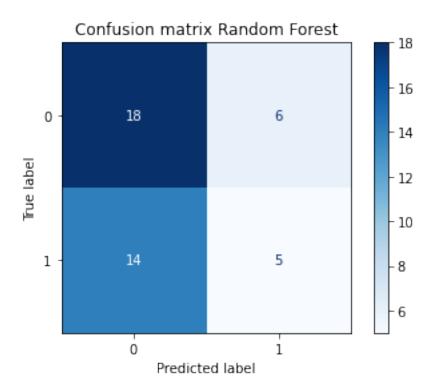
Best Parameters: {'max\_features': 7, 'n\_estimators': 10}

[35]: RandomForestClassifier(max\_features=7, n\_estimators=10, random\_state=1234)

The accuracy and performance of the Random Forest on the test set is shown below, with a confusion matrix to showcase its quantitiy of type I and type II errors.

```
[19]: y_pred = best_rf.predict(X_test)
accuracy_score(y_pred, y_test)
```

[19]: 0.5348837209302325



Finally, the most relevant variables in the prediction, as defined by a weighted average of how many times they appear in a node of the random forest are given by the following table.

	Feature	Importance
51	51	0.057151
11	11	0.043937
25	25	0.032852
96	96	0.030232
78	78	0.029687
76	76	0.028671
5	5	0.027653
34	34	0.026475
12	12	0.026456
62	62	0.024448

### 4.2 Gradient Boosting

Using stumps as classification trees for the response variable, we now build a gradient boosting model on the stumps as weak learners to then compute the misclassification rates of both the learning set and the test set, across 2,000 iterations. As was done with the random forest in the previous subsection, the hyperparameters of the model are tuned with a grid search.

```
[36]: from sklearn.ensemble import GradientBoostingClassifier
gb = GradientBoostingClassifier(n_estimators=2000, random_state=1234)
parameters = {'max_depth' : (1,4,8,16)}
```

```
[37]: grid_gb = GridSearchCV(gb, parameters)
grid_gb.fit(X_train, y_train)
```

[37]: GridSearchCV(estimator=GradientBoostingClassifier(n\_estimators=2000, random\_state=1234),

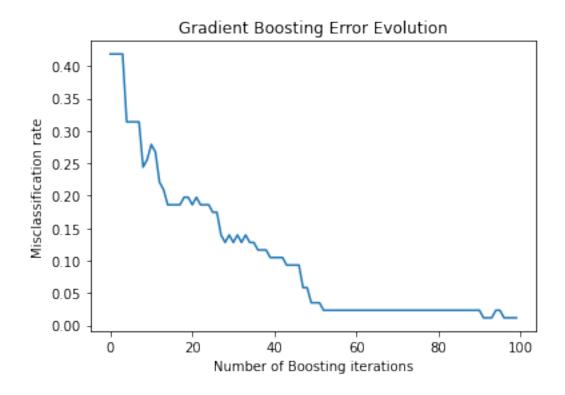
param\_grid={'max\_depth': (1, 4, 8, 16)})

[24]:	param_max_depth	mean_test_score	std_test_score
0	1	0.524183	0.069834
2	8	0.454248	0.103714
3	16	0.454248	0.103714
1	4	0.442484	0.090319

The results of comparing the validation-set misclassification rates attained by different ensemble classifiers based on trees with varying maximum depth is shown in the previous table, where we find the stumps as being the best performing validation-set learners. We may observe already hints of the strong overfitting tendencies of this type of model, given their poor out-of-sample performance. In fact, we may track the training error across iterations, and as shown in the following plot *Gradient Boosting Error Evolution*, the training error decreases to almost perfection, while the validation set error remains close to the null model, which is a clear sign of overfitting.

Best Parameters: {'max\_depth': 1}

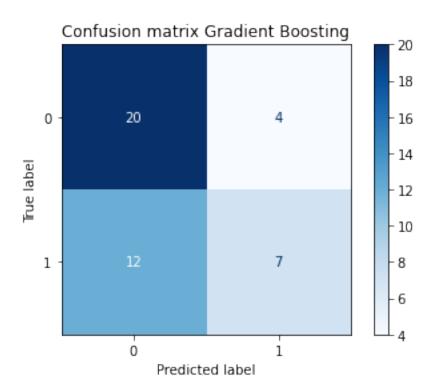
[25]: Text(0.5, 1.0, 'Gradient Boosting Error Evolution')



The test-set accuracy and performance of the Gradient Boosting is as follows, with its corresponding confusion matrix in the figure below.

```
[34]: y_pred = best_gb.predict(X_test)
accuracy_score(y_pred, y_test)
```

#### [34]: 0.627906976744186



### 4.3 XGBoost

To conclude, we introduce another boosting flavour and analyse its performance. It is well-known that the XGBoost attains state of the art performance in a wide variety of learning tasks, although as most models of its kind, it also shows a tendency to overfit the training data. As in the previous two cases, the model's hyperparameters, which are the maximum depth of the decision trees and the learning rate, are explored in a grid search.

```
[42]: grid_xgb = GridSearchCV(xgb, parameters)
grid_xgb.fit(X_train, y_train)
```

The best performing out-of-sample models are shown in the following table, where the best four all have the same error rate (the one corresponding to the null model) and a learning rate of 0. This is because the model strongly overfits the data, which is a consequence of the extremely noisy dataset. In fact, due to the powerful fitting capabilities of XGBoost, it strongly favours fitting the large noise in the dataset instead of sticking to the weak signal present. Some recent analysis on this behaviour and why zero training error is sometimes (but not in this case) a good sign can be found in Bartlett et al. (2020) and Hastie et al. (2020)

```
[46]:
        param_learning_rate param_max_depth mean_test_score
                                                                   std_test_score
      0
                            0
                                              1
                                                         0.581699
                                                                          0.013072
      1
                            0
                                              4
                                                         0.581699
                                                                          0.013072
      2
                            0
                                              8
                                                         0.581699
                                                                          0.013072
      3
                            0
                                             16
                                                         0.581699
                                                                          0.013072
                            2
      4
                                              1
                                                         0.511765
                                                                          0.125613
```

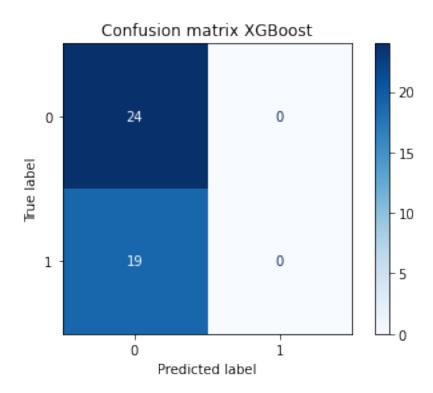
Best Parameters: {'learning\_rate': 0, 'max\_depth': 1}

```
[47]: XGBClassifier(base_score=None, booster=None, callbacks=None, colsample_bylevel=None, colsample_bynode=None, colsample_bytree=None, device=None, early_stopping_rounds=None, enable_categorical=False, eval_metric=None, feature_types=None, gamma=None, grow_policy=None, importance_type=None, interaction_constraints=None, learning_rate=0, max_bin=None, max_cat_threshold=None, max_cat_to_onehot=None, max_delta_step=None, max_depth=1, max_leaves=None, min_child_weight=None, missing=nan, monotone_constraints=None, multi_strategy=None, n_estimators=None, n_jobs=None, num_parallel_tree=None, random_state=1234, ...)
```

The reason for the inclusion of the previous chunk of text is that we intend to show that the chosen model by the grid search is indeed the null model. The accuracy and performance on the test set of XGBoost is as follows, with its corresponding confusion matrix in the figure below, which again shows how the final preferred model is just the null model that always predicts the most common class.

```
[48]: y_pred = best_xgb.predict(X_test)
accuracy_score(y_pred, y_test)
```

[48]: 0.5581395348837209



We can see how the gradient boosting always predicts the most common class, and so has a large amount of misclassification errors, and in particular Type II errors.

# 5 Predictor comparison and Conclusions

The test set accuracies of the three proposed models are the following:

Accuracy of RF: 0.5348837209302325 Accuracy of GB: 0.627906976744186 Accuracy of XGB: 0.5581395348837209

F1-loss of XGB: 0.0

We can see that, in general, they're not very high. This can be due to the large number of NaNs in the data used and them being fitted by interpolation, which may have dampened the signal present in the data. However, a similar analysis removing the data altogether (not present in the final report) showed no improvement. As such, we may conclude that the issue is the large amount of noise in the data where our models are all very good at fitting the training data and therefore extremely vulnerable at overfitting it.

In terms of relative performance, the Gradient Boosting method obtained the best test-set performance, in fact it is considerably better than the other two methods which are essentially the null model (XGBoost), and a noisy version of it (Random Forest). For this reason, the classifier we

would choose would be Gradient Boosting.

Using Gradient Boosting, the best performing model, the ten most relevant recurrence biomarkers are the following peptides:

	Feature	Importance
51	51	0.123774
11	11	0.112551
65	65	0.089577
60	60	0.067424
38	38	0.067323
70	70	0.067106
76	76	0.058383
19	19	0.048530
75	75	0.036543
67	67	0.032089

### 6 Discussion

Since there is a considerable amount of missing values in the dataset, we resorted to imputing the linear interpolation of the missing entries. This allowed us to work with more information, but it can be argued that some quality was lost (as we saw in the accuracies). More advanced techniques to deal with the missing values for this dataset could be considered, however, the authors claim that an ideal study of this field should be done with a more complete dataset, of with more field knowledge about the biomarkers themselves.

Due to the large amount of noise in the dataset, as seen in the histogram distribution of the pepties in section 2, and the large overfitting tendencies of all three models, other approaches which are more robust to noisy datasets should be considered. For instance, regularisation techniques could help in avoiding strong overfitting and the use of **LightGBM** as a more robust ensemble method could be tried out in future studies.

All in all, the best performing model was found to be better than the null model, which is a positive result, despite the fact that its overall performance was far from impressive.

### 7 References

- Bartlett, P. L. Long, P. M. Lugosi, G. Tsigler, A. (2020) Benign Overfitting in Linear Regression. ArXiv.
- Hastie, T. Montanari, A. Rosset, S. Tibshirani, R. J. (2020) Surprises in high-dimensional Ridgeless Least Squares Interpolation. ArXiv.

## 8 Appendix

All the code may be found in this appendix to be reproducible

```
[49]: import numpy as np
      import pandas as pd
      import matplotlib.pyplot as plt
      import sklearn
      from sklearn.metrics import accuracy_score, zero_one_loss, f1_score
      from sklearn.metrics import confusion_matrix, classification_report,_
      →ConfusionMatrixDisplay
      from sklearn.model_selection import GridSearchCV
[19]: # cancerDat.csv
      df1 = pd.read_csv("cancerDat.csv", sep = ";", decimal = ",")
      df1 = df1.T
      df1 = df1.drop('Unnamed: 0', axis=0)
      # cancerInfo.csv
      df2 = pd.read_csv("cancerInfo.csv", sep = ";")
      df2 = df2.drop(['Unnamed: 0', 'Group'], axis = 1)
      df2.index = df2.iloc[:,0]
      df2 = df2.drop(['sampleNames'], axis = 1)
 [7]: print(df1.shape)
      print(df2.shape)
      display(df1.head())
      display(df2.head())
     (129, 102)
     (129, 1)
                                                      3
                     0
                                1
                                                                 4
                                                                            5
     NO.REC_1 21.923472 24.442617 19.050562 18.482667
                                                           24.086793
                                                                       20.32946
     NO.REC_2 21.020165 23.649841 18.402413 19.088996
                                                           24.710323
                                                                      21.495392
     NO.REC_3 19.585788 23.736128 18.191527
                                                 16.33124
                                                           21.917326
                                                                      20.284533
     NO.REC_4 19.061767 23.374865
                                     17.692775
                                                 15.36272
                                                           21.484924
                                                                      18.379603
     NO.REC_5 18.547029 23.039588 19.066973 15.835721 21.339587
                                                                      19.550809
                                7
                                                      9
                     6
                                           8
                                                                      92
     NO.REC_1 19.304363 24.270429
                                     18.878984
                                               18.752264
                                                           . . .
                                                                19.439382
     NO.REC_2 19.454826 25.807051 19.091796
                                                                20.631064
                                               19.213397
                                                           . . .
     NO.REC_3 16.853825 22.661125 18.215654 20.821777
                                                           . . .
                                                                19.123832
     NO.REC_4 16.513507 21.401436
                                      18.38696 19.847221
                                                           . . .
                                                                17.958307
     NO.REC_5 16.831653 21.776832
                                      17.85408 20.368534
                                                           . . .
                                                                18.212854
                     93
                                94
                                           95
                                                      96
                                                                 97
                                                                            98
                                                                      20.912124
     NO.REC_1 16.142102 22.858297
                                     22.262118
                                                18.079186
                                                           17.151515
     NO.REC_2
                                     22.031468 17.101384 18.315637
                     NaN
                          22.028998
                                                                      21.512601
```

```
NO.REC_3 16.171227 23.143305 22.334392 17.159968 16.859732 19.076147
     NO.REC_4
                     NaN 19.183961 17.851328 16.564709 15.161135 18.190653
     NO.REC_5
                     NaN 22.228449
                                     21.385404 17.072001 15.071656 18.896095
                     99
                                100
                                           101
     NO.REC_1 17.298159 19.097263
                                      21.21211
     NO.REC_2 17.100711 18.875548 23.980238
     NO.REC_3 15.417028 16.340283 19.810886
     NO.REC_4 15.269443 15.411408 18.351433
     NO.REC_5 15.147357
                                NaN
                                      20.28779
     [5 rows x 102 columns]
                 sites
     sampleNames
     NO.REC_1
                     Α
     NO.REC_2
                     В
                     С
     NO.REC_3
                     С
     NO.REC 4
     NO.REC_5
                     С
 [8]: indices1 = np.array(df1.index).astype(str)
      index_array1 = np.zeros(len(indices1))
      labels_1 = np.where(np.char.startswith(indices1, 'NO.REC_'), 0, np.where(np.char.
      →startswith(indices1, 'REC_'), 1, index_array1))
      indices2 = np.array(df2.index).astype(str)
      index_array2 = np.zeros(len(indices2))
      labels_2 = np.where(np.char.startswith(indices2, 'NO.REC_'), 0, np.where(np.char.
      →startswith(indices2, 'REC_'), 1, index_array2))
      print("Labels are equal: " + str(np.array_equal(labels_1, labels_2))) # That is_
      →we can define a single response variable y for the two files
      v = labels_1
     Labels are equal: True
[11]: y = pd.Series(y)
      display(y)
     0
            0.0
     1
            0.0
     2
            0.0
     3
            0.0
     4
            0.0
           . . .
     124
            1.0
     125
            1.0
     126
            1.0
```

```
127
            1.0
     128
            1.0
     Length: 129, dtype: float64
[20]: for col in df1:
          df1[col] = pd.to_numeric(df1[col], errors='coerce')
      df1.dtypes;
[]: print(df1.isnull().values.any())
      print(sum(df1.isnull()))
      df1 = df1.interpolate(method ='linear', limit_direction ='forward')
      print(df1.isnull().values.any())
[]: print(df2.isnull().values.any()) # False -> No nulls
[]: df1.describe()
[]: df1.hist(figsize=(12,10))
      plt.tight_layout()
      plt.show()
[]: from sklearn.decomposition import PCA
      import itertools
      pca = PCA(n_components=20)
      pca.fit_transform(df1)
      #print(pca.explained_variance_ratio_)
      #print(list(itertools.accumulate(pca.explained_variance_ratio_)))
      plt.plot(list(itertools.accumulate(pca.explained_variance_ratio_)))
[]: from sklearn.model_selection import train_test_split
      np.random.seed(1234)
[]: from sklearn.ensemble import RandomForestClassifier
      rf = RandomForestClassifier(random_state = 1234)
      parameters = {'n_estimators' : range(10,130,20),
                    'max_features' : (1,2,3,4,5,6,7,8,9,10)
                   }
 []: grid_rf = GridSearchCV(rf, parameters)
      grid_rf.fit(X_train, y_train)
 []: rf_results = pd.DataFrame(grid_rf.cv_results_)
      rf_results.filter(regex = '(param.*|mean_t|std_t)') \
          .drop(columns = 'params') \
          .sort_values('mean_test_score', ascending = False) \
          .head(4)
```

```
[]: best_params = grid_rf.best_params_
     print("Best Parameters:", best_params)
     best_rf = RandomForestClassifier(**best_params, random_state=1234)
     best_rf.fit(X_train, y_train)
[]: y_pred = best_rf.predict(X_test)
     accuracy_score(y_pred, y_test)
[]: confusion_mtx = confusion_matrix(y_test, y_pred)
     disp = ConfusionMatrixDisplay(confusion_matrix= confusion_mtx, display_labels=__
     →None)
     disp.plot(cmap= plt.cm.Blues)
     plt.title("Confusion matrix Random Forest")
     plt.show()
[]: feature_importances = best_rf.feature_importances_
     importance_df = pd.DataFrame({'Feature' : X_train.columns, 'Importance' : ___
      →feature_importances})
     print(importance_df.sort_values(by=['Importance'], ascending=False).head(10))
[]: from sklearn.ensemble import GradientBoostingClassifier
     gb = GradientBoostingClassifier(n_estimators=2000, random_state=1234)
     parameters = {'max_depth' : (1,4,8,16)}
[]: grid_gb = GridSearchCV(gb, parameters)
     grid_gb.fit(X_train, y_train)
[]: gb_results = pd.DataFrame(grid_gb.cv_results_)
     gb_results.filter(regex = '(param.*|mean_t|std_t)') \
         .drop(columns = 'params') \
         .sort_values('mean_test_score', ascending = False) \
         .head(4)
[]: y_pred = best_gb.predict(X_test)
     accuracy_score(y_pred, y_test)
[]: best_params = grid_gb.best_params_
     print("Best Parameters:", best_params)
     train_errors = []
     best_gb = GradientBoostingClassifier(**best_params, random_state=1234)
     best_gb.fit(X_train, y_train)
     for i, y_pred_train in enumerate(best_gb.staged_predict(X_train)):
         train_errors.append(zero_one_loss(y_train, y_pred_train))
     plt.plot(np.arange(0,100), train_errors)
```

```
plt.xlabel('Number of Boosting iterations')
     plt.ylabel('Misclassification rate')
     plt.title('Gradient Boosting Error Evolution')
[ ]: y_pred = best_gb.predict(X_test)
     accuracy_score(y_pred, y_test)
[]: confusion_mtx = confusion_matrix(y_test, y_pred)
     disp = ConfusionMatrixDisplay(confusion_matrix= confusion_mtx, display_labels=___
      →None)
     disp.plot(cmap= plt.cm.Blues)
     plt.title("Confusion matrix Gradient Boosting")
     plt.show()
[]: import xgboost
     xgb = xgboost.XGBClassifier(n_estimators=2000, random_state=1234)
     parameters = {'max_depth' : (1,4,8,16),
                  'learning_rate' : [0,2]
[]: grid_xgb = GridSearchCV(xgb, parameters)
     grid_xgb.fit(X_train, y_train)
[]: xgb_results = pd.DataFrame(grid_xgb.cv_results_)
     xgb_results.filter(regex = '(param.*|mean_t|std_t)') \
         .drop(columns = 'params') \
         .sort_values('mean_test_score', ascending = False) \
         head (5)
[ ]: best_params = grid_xgb.best_params_
     print("Best Parameters:", best_params)
     best_xgb = xgboost.XGBClassifier(**best_params, random_state=1234)
     best_xgb.fit(X_train, y_train)
[]: y_pred = best_xgb.predict(X_test)
     accuracy_score(y_pred, y_test)
[]: confusion_mtx = confusion_matrix(y_test, y_pred)
     disp = ConfusionMatrixDisplay(confusion_matrix= confusion_mtx, display_labels=__
     →None)
     disp.plot(cmap= plt.cm.Blues)
     plt.title("Confusion matrix XGBoost")
     plt.show()
[]: print("Accuracy of RF:", accuracy_score(best_rf.predict(X_test), y_test))
     print("Accuracy of GB:", accuracy_score(best_gb.predict(X_test), y_test))
```