

feature-extraction-selection-pca

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0.1 Principal Component Analysis (PCA) –

0.1.1 Read Curse of Dimensionality

0.1.2 PCA ?

PCA (Principal Component Analysis) , -

0.1.3 Step 1: Standardization

:

$$Z = \frac{X - \mu}{\sigma}$$

- X : (: $n \times p$)
- μ :
- σ :

Sample	X	X
1	2	3
2	4	1
3	6	5

: :

$$\mu_{X_1} = 4, \quad \mu_{X_2} = 3$$

:

$$Z = \begin{bmatrix} \frac{2-4}{\sigma_{X_1}} & \frac{3-3}{\sigma_{X_2}} \\ \frac{4-4}{\sigma_{X_1}} & \frac{1-3}{\sigma_{X_2}} \\ \frac{6-4}{\sigma_{X_1}} & \frac{5-3}{\sigma_{X_2}} \end{bmatrix}$$

0.1.4 Step 2:

:

$$\Sigma = \frac{1}{n} Z^T Z$$

- Σ : (: $p \times p$)

:

$$\Sigma = \begin{bmatrix} \text{Var}(Z_1) & \text{Cov}(Z_1, Z_2) \\ \text{Cov}(Z_2, Z_1) & \text{Var}(Z_2) \end{bmatrix}$$

0.1.5 Step 3:

:

$$\Sigma \mathbf{v} = \lambda \mathbf{v}$$

- λ : Eigenvalue
- \mathbf{v} : Eigenvector

:

1. Characteristic Equation:

$$\det(\Sigma - \lambda I) = 0$$

2. $(\Sigma - \lambda I)\mathbf{v} = 0$ \mathbf{v}

:

$$\Sigma = \begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix} \Rightarrow \lambda = 1, 3$$

Eigenvectors:

- $\lambda = 3$: $\begin{bmatrix} 1 \\ 1 \end{bmatrix}$
 - $\lambda = 1$: $\begin{bmatrix} -1 \\ 1 \end{bmatrix}$
-

0.1.6 Step 4: Principal Components

:

$$\text{Cumulative Variance} = \frac{\sum_{i=1}^k \lambda_i}{\sum_{i=1}^p \lambda_i}$$

:

$$\lambda_1 = 3, \lambda_2 = 1 \Rightarrow \text{Total Variance} = 4 \Rightarrow PC1 = 75\%, \quad PC1 + PC2 = 100\%$$

0.1.7 Step 5:

:

$$Y = ZW_k$$

- W_k : k
- Y :

:

$$Y = Z \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

0.2 Python Code: PCA

```
import numpy as np
from sklearn.decomposition import PCA
from sklearn.preprocessing import StandardScaler

# Step 1: Raw Data
X = np.array([[2, 3], [4, 1], [6, 5]])

# Step 2: Standardization
scaler = StandardScaler()
Z = scaler.fit_transform(X)

# Step 3: PCA
pca = PCA(n_components=1)
X_pca = pca.fit_transform(Z)

# Output
print("          :\n", X_pca)
print("          :", pca.explained_variance_ratio_)

:

:
[[-1.414]
 [ 0.    ]
 [ 1.414]]

: [0.75]
```

0.3 Practical Application: PCA ?

0.4

Q: PCA ? A: ,

Q: PCA - ? A: Kernel PCA

Q: PC ? A: , 85-95% ;

0.4.1

PCA

- PCA !

##More on My Hand Note: ML-5 and ML-6

```
[ ]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import plotly.express as ex
```

```
[ ]: df=pd.read_csv('/content/Titanic-Dataset.csv')
df.head(3)
```

```
[ ]: PassengerId  Survived  Pclass  \
0               1         0       3
1               2         1       1
2               3         1       3
```

```
                                Name    Sex  Age  SibSp  \
0                Braund, Mr. Owen Harris  male  22.0     1
1  Cumings, Mrs. John Bradley (Florence Briggs Th... female  38.0     1
2                Heikkinen, Miss. Laina  female  26.0     0
```

```
    Parch    Ticket   Fare Cabin Embarked
0      0  A/5 21171   7.2500   NaN        S
1      0    PC 17599  71.2833   C85        C
2      0 STON/O2. 3101282   7.9250   NaN        S
```

```
[ ]: df=df.iloc[:,[2,5,6,7,9,1]]
df.head(3)
```

```
[ ]: Pclass  Age  SibSp  Parch    Fare  Survived
0      3  22.0     1     0   7.2500         0
1      1  38.0     1     0  71.2833         1
2      3  26.0     0     0   7.9250         1
```

```
[ ]: df.dropna(inplace=True)
```

```
[ ]: df.isnull().sum()
```

```
[ ]: Pclass      0
     Age        0
     SibSp      0
     Parch      0
     Fare       0
     Survived    0
     dtype: int64
```

#PCA manually

```
[ ]: X=df.iloc[:, :5]
     y=df['Survived']
```

```
[ ]: #Step-1: Standardization Scaling
     from sklearn.preprocessing import StandardScaler
     ss=StandardScaler()
     new_x=ss.fit_transform(X)
     new_x
```

```
[ ]: array([[ 0.91123237, -0.53037664,  0.52457013, -0.50589515, -0.51897787],
            [-1.47636364,  0.57183099,  0.52457013, -0.50589515,  0.69189675],
            [ 0.91123237, -0.25482473, -0.55170307, -0.50589515, -0.50621356],
            ...,
            [-1.47636364, -0.73704057, -0.55170307, -0.50589515, -0.08877362],
            [-1.47636364, -0.25482473, -0.55170307, -0.50589515, -0.08877362],
            [ 0.91123237,  0.15850313, -0.55170307, -0.50589515, -0.50952283]])
```

```
[ ]: #step2: Co-Varinace Matrix
     cov=np.cov(new_x.T)
```

```
[ ]: #setp3: Eigen value and Eigen Vector
     eig=np.linalg.eig(cov)
     eig
```

```
[ ]: EigResult(eigenvalues=array([1.74380104, 1.6159263 , 0.36447732, 0.69209424,
 0.59071373]), eigenvectors=array([[ -0.62133317,  0.2742927 , -0.71116258,
 -0.16677988,  0.0716998 ],
 [ 0.54592049,  0.19719823, -0.28190116, -0.66731845, -0.37188909],
 [-0.31151744, -0.53986787, -0.02187925,  0.03015686, -0.7810963 ],
 [-0.20582771, -0.56301483,  0.15922655, -0.64819931,  0.44173954],
 [ 0.42012825, -0.52671942, -0.62365674,  0.32526724,  0.2265224 ]]))
```

```
[ ]: eig.eigenvalues
```

```
[ ]: array([1.74380104, 1.6159263 , 0.36447732, 0.69209424, 0.59071373])
```

```
[ ]: #step4:Choose No. of Principle Component(PC)  
W=eig.eigenvectors[:2,]  
W
```

```
[ ]: array([[ -0.62133317,  0.2742927 , -0.71116258, -0.16677988,  0.0716998 ],  
          [ 0.54592049,  0.19719823, -0.28190116, -0.66731845, -0.37188909]])
```

```
[ ]: #setp5: Projection of Scaled Data on PCs  
pca_matrix=np.dot(new_x,np.transpose(W))  
pca_matrix
```

```
[ ]: array([[ -1.03754947,  0.77558953],  
          [ 0.83509012, -0.76080572],  
          [-0.19564717,  1.12858364],  
          ...,  
          [ 1.18550751, -0.42518742],  
          [ 1.3177758 , -0.33009531],  
          [-0.08251163,  1.21132184]])
```

```
[ ]: New_df=pd.DataFrame(pca_matrix,columns=['pc1','pc2'])  
New_df['Survived']=y  
New_df.head()
```

```
#5D to 2D te converted
```

```
[ ]:      pc1      pc2  Survived  
0 -1.037549  0.775590        0.0  
1  0.835090 -0.760806        1.0  
2 -0.195647  1.128584        1.0  
3  0.753750 -0.673686        1.0  
4 -0.025418  1.249966        0.0
```

```
[ ]: New_df.isnull().sum()
```

```
[ ]: pc1      0  
pc2      0  
Survived  147  
dtype: int64
```

```
[ ]: ex.scatter_3d(X,x='Age',y='Fare',z='Pclass',color=df['Survived'].astype('str'))
```

```
[ ]: ex.scatter(New_df,x='pc1',y='pc2',color=New_df['Survived'].astype('str'))
```