

## **United** International **University** School of Science and Engineering

Assignment-2(Mid-term Examination) Trimester: Summer-2024 Course Title: Calculus and Linear Algebra

Course Code: MATH 2183 Submission deadline: 3 weeks

1. Find the solution of the given differential equations

$$i) ty' - y = t^2 e^{2t},$$

$$y(1) = \frac{1}{2}$$

ii) 
$$y' = \frac{(1-x^2)y^3}{x}$$
,

$$y(1)=2$$

iii) 
$$x \frac{dy}{dx} - y = \sin x$$

i) 
$$ty'-y=t^2e^{2t}$$
,  $y(1)=\frac{1}{2}$   
ii)  $y'=\frac{(1-x^2)y^3}{x}$ ,  $y(1)=2$   
iii)  $x\frac{dy}{dx}-y=sinx$   
iv)  $y'-5y=cos(2x)+4x$ 

a) The initial temperature of a cake when it is removed from an oven was measured as 250°F. Five minutes later the temperature of the cake was recorded as 200°F.

- Construct a first order differential equation with initial conditions. i)
- ii) Find the decay constant.
- How long will the cake take to cool down to the room temperature of 75°F? iii)
- Graph the solution of the IVP in (i) iv)

b) The population of a community is known to increase at rate proportional to the number of people present at time t. If an **initial** population  $A_0$  has **doubled** in 5 years, how long will it take to **triple**?