



**Course Title: Theory of Computation**  
**Trimester & Year: Fall 2021**

**Course Code: CSE 2233**  
**Section: A**

**Credit Hours: 3.0**  
**AZ**

## **CT-04**

Total Marks: 20

Time: 45 min

In the Question the value of x and y will be as follows and you must write on the first page of your answer script clearly:

$$\mathbf{x} = [ \{ (\text{last digit of your ID number} + 1) * 8 \} \% 3 ] + 1$$

$$\mathbf{y} = [ \{ (\text{last digit of your ID number} + 1) * 5 \} \% 4 ] + 1$$

1. Construct Pushdown Automata (PDA) that recognizes following languages 5+5

(a)  $L = \{ a^i b^{2j} c^k \mid i, j, k \geq 0 \text{ and } i=j \text{ or } i=k \}$

(b)  $L = \{ 1^{2n} 0^{\mathbf{x}n} \cup 0^{\mathbf{y}n} 1^{3n} \mid n \geq 0 \}$

2. Construct Pushdown Automata (PDA) that recognizes following language and show a PDA tree traversal of the input  $\mathbf{xyy\#yyx}$  to determine it's acceptability. 5

$$L = \{ W\#W^R \mid W \in \{ \mathbf{x}, \mathbf{y} \} \}$$

3. Draw the state diagram of TM for deciding the following Language and show a tape traversal of the input  $\mathbf{yz\#yx}$  to determine it's acceptability. 5

$$L = \{ W\#W \mid W \in \{ \mathbf{x}, \mathbf{y}, \mathbf{z} \} \text{ where } z = y+2 \}$$