



United International University (UIU)

Dept. of Computer Science & Engineering (CSE)

Mid Exam Spring 2022.

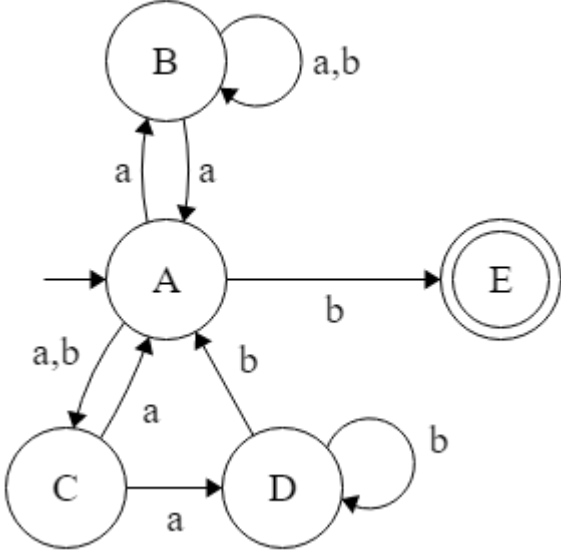
CSE 2233/CSI 233: Theory of Computation/Theory of Computing

Total Marks: 30

Duration: 105 Minutes

Answer all questions. Figures are in the right-hand margin indicates full marks. **Any examinee found adopting unfair means will be expelled from the trimester / program as per UIU disciplinary rules.**

1.	Design DFAs that accepts the following languages: a) $L = \text{starts with '0' and contains '110' and ends with '01'}$ $\Sigma = \{0,1,2\}$ <i>Sample Valid: 011001, 001101</i> <i>Sample Invalid: 111001, 0110100</i> b) $L = \text{starts with 'c' and contains 'abc' or 'bca' and ends with 'b'}$ $\Sigma = \{a,b,c\}$ <i>Sample Valid: ccabcb, cbcabb</i> <i>Sample Invalid: cabbbb, abcac</i> c) $L = \text{does not contain 'xyz' and ends with 'yy'}$ $\Sigma = \{x,y,z\}$ <i>Sample Valid: xyy, yy</i> <i>Sample Invalid: xyzyy, xyxy</i>	3x3
2.	Design NFAs that accepts the following languages: a) $L = \text{starts and ends with the same symbol with total length at least 2}$ $\Sigma = \{0,1\}$ <i>Sample Valid: 00,11,010,1010101</i> <i>Sample Invalid: 100, 0</i> b) $L = \text{contains 'xx' or 'yx' or 'zz' and ends with 'yz' or 'y'}$ $\Sigma = \{x,y,z\}$ <i>Sample Valid: zyxy, zxxzzy</i> <i>Sample Invalid: xyzyz, yxxz</i> c) $L = \text{starts with '0x0' and contains '0' or 'x' and ends with '0'}$ $\Sigma = \{0,x,y\}$ <i>Sample Valid: 0x0,0x0yyy0</i> <i>Sample Invalid: 0xx0, 0xy0x</i>	3x3
3.	Consider the following NFA, and show with the help of NFA-tree whether the string "0011001" is accepted or not. <pre> graph LR Start(()) --> A((A)) A -- 0 --> A A -- 1 --> B((B)) B -- "0,1" --> B B -- 0 --> C(((C))) C -- 1 --> B C -- 0 --> C </pre>	3

4.	<p>Convert the following NFA over alphabet $\Sigma = \{a, b\}$ to an equivalent DFA.</p>  <pre> graph TD A((A)) -- a --> B((B)) B -- a --> A B -- "a,b" --> B A -- b --> E(((E))) A -- "a,b" --> C((C)) C -- a --> A C -- a --> D((D)) D -- b --> A D -- b --> D style A fill:#fff,stroke:#000,stroke-width:1px style B fill:#fff,stroke:#000,stroke-width:1px style C fill:#fff,stroke:#000,stroke-width:1px style D fill:#fff,stroke:#000,stroke-width:1px style E fill:#fff,stroke:#000,stroke-width:2px </pre>	6
5.	<p>Develop Regular expression over $\Sigma = \{x,y,z\}$ for following languages:</p> <ul style="list-style-type: none"> a) Contains at least three x b) Number of y is multiple of 4 c) Even length if the string starts with x and Odd length if the string starts with y or z 	3x1