



Modélisations de foules dans un contexte et un environnement donné

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SCEI : 48160 ; MPI 2022-2023

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- > Présentation de la méthode de modélisation
- > Programmation
- > Comparaison avec le réel

Conclusion

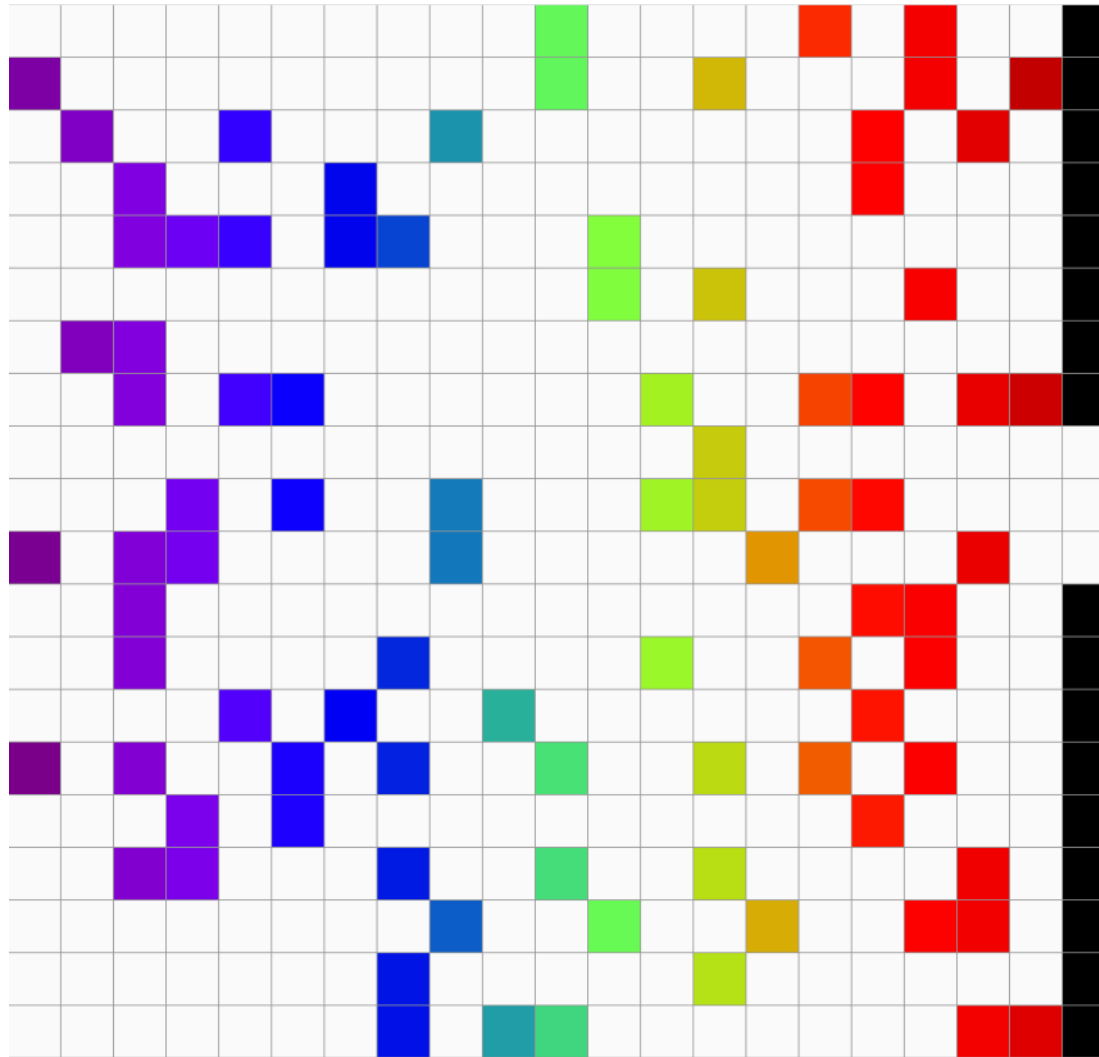
Introduction & rapport à la ville

Permet de prévoir :

- comment se déroulera l'évacuation d'un futur bâtiment
- comment se déplaceront les personnes dans les espaces publics

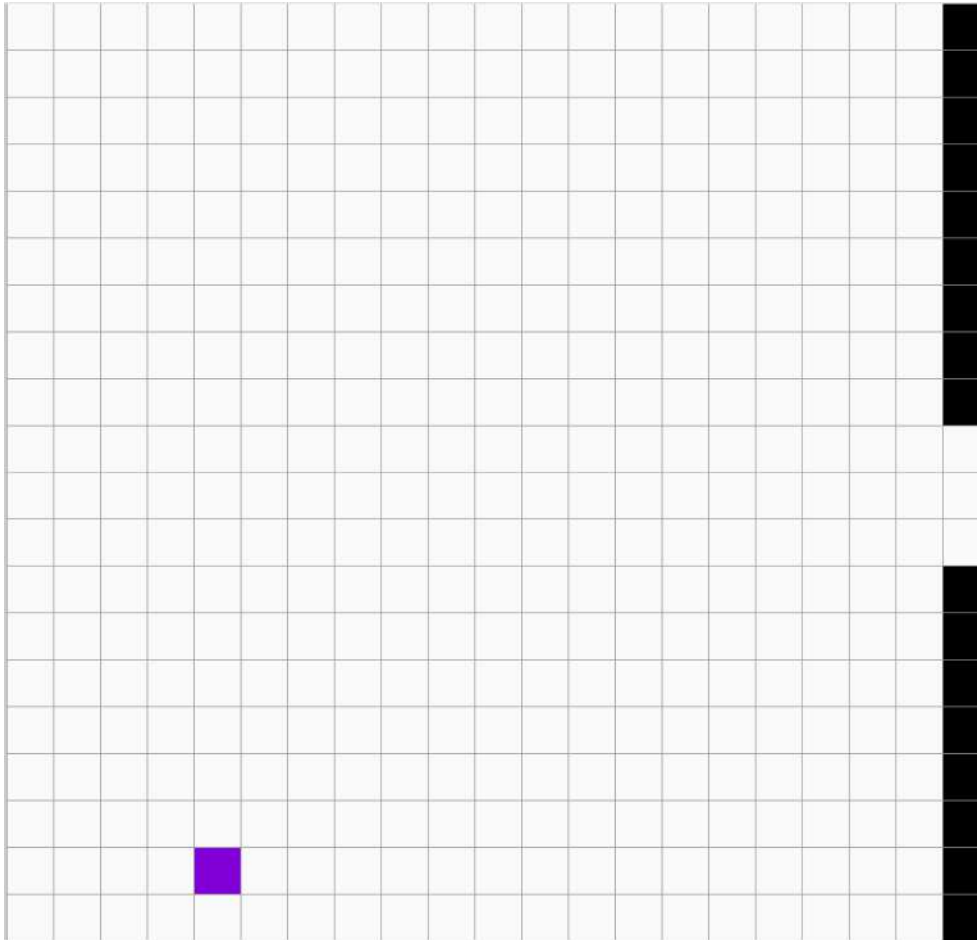
I-1) Modélisation multi-agent sur grille

Présentation de la méthode



I-2) Programmation

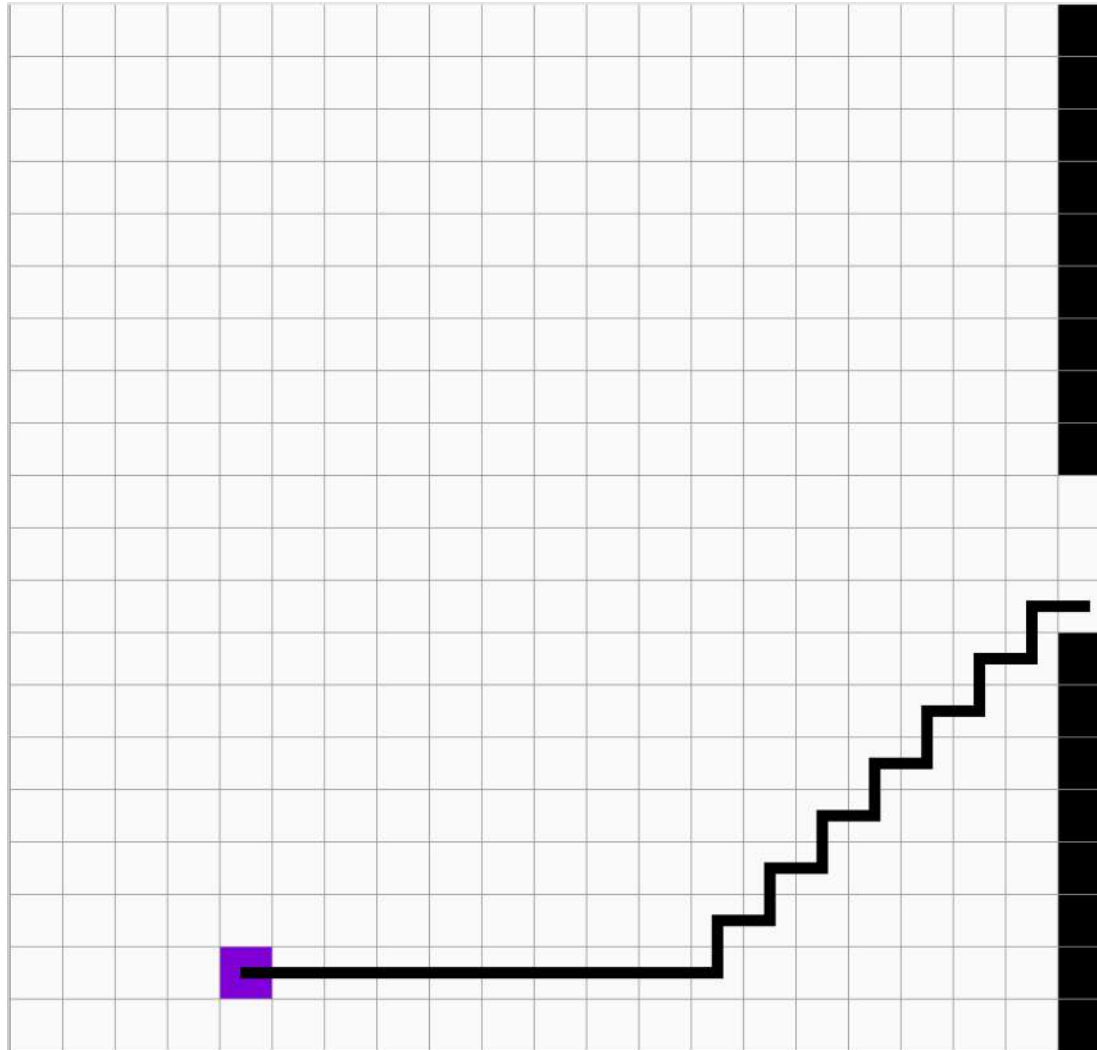
Programme trouve_chemin



Utilisation de Best First

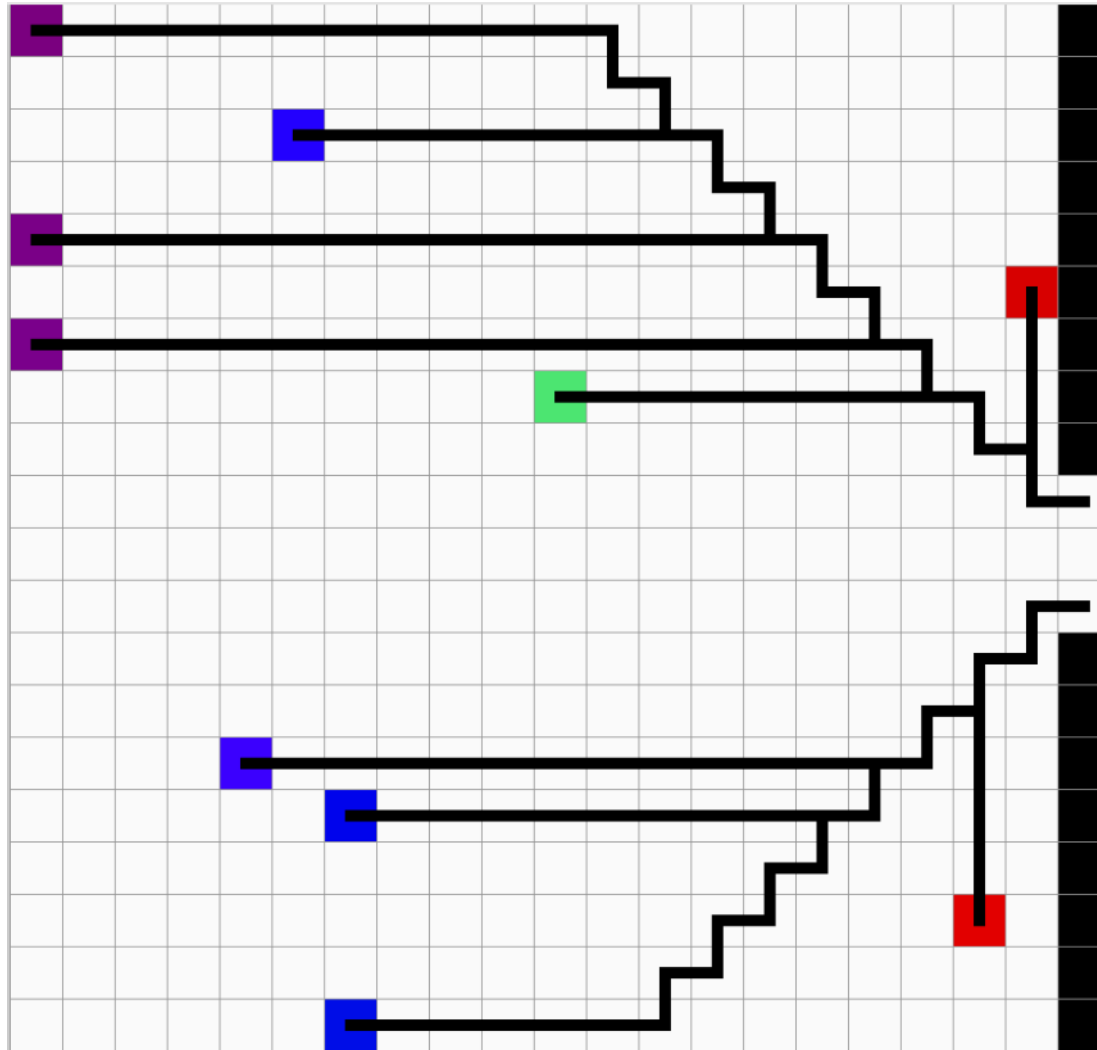
I-2) Programmation

Programme trouve_chemin



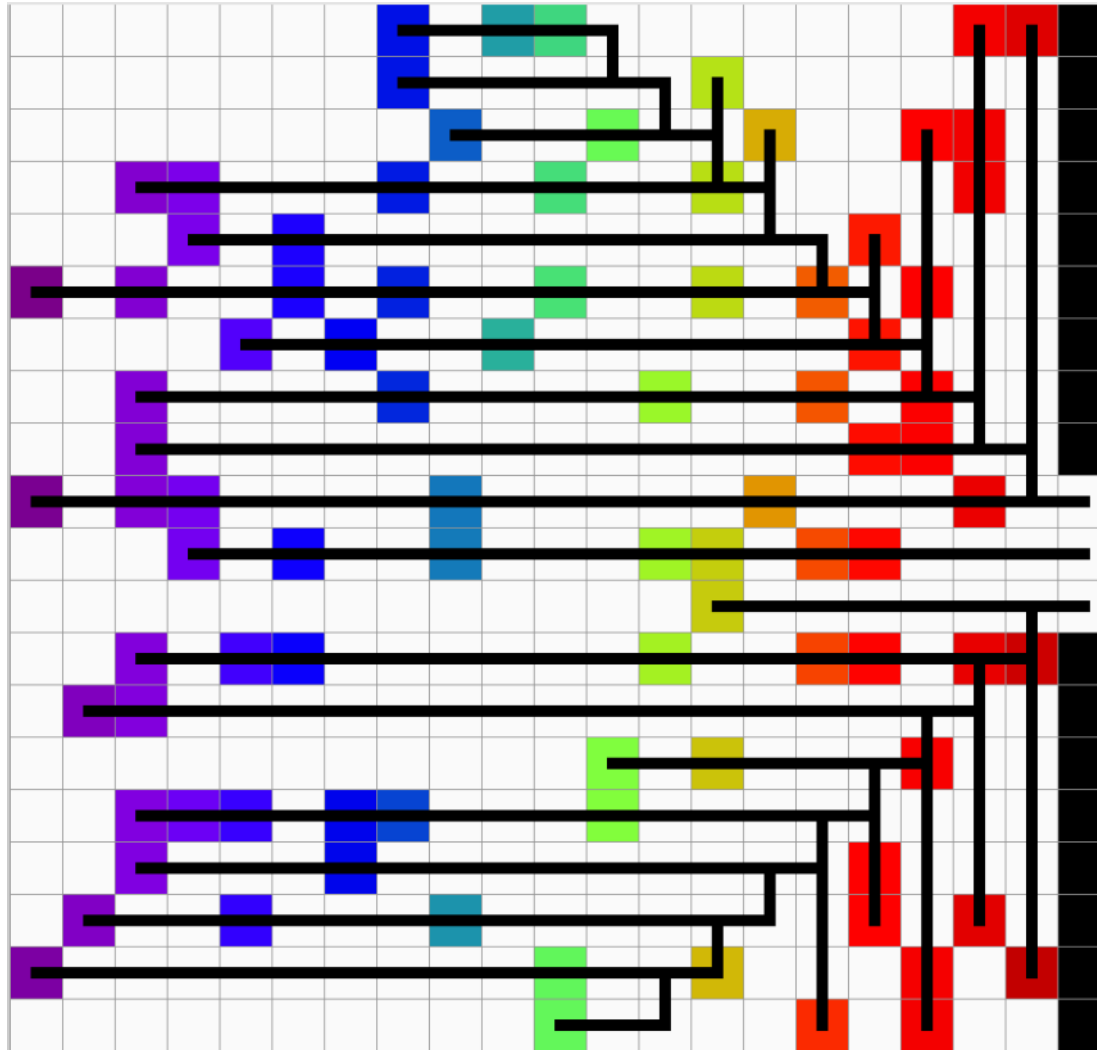
I-2) Programmation

Déroulé de l'algorithme



I-2) Programmation

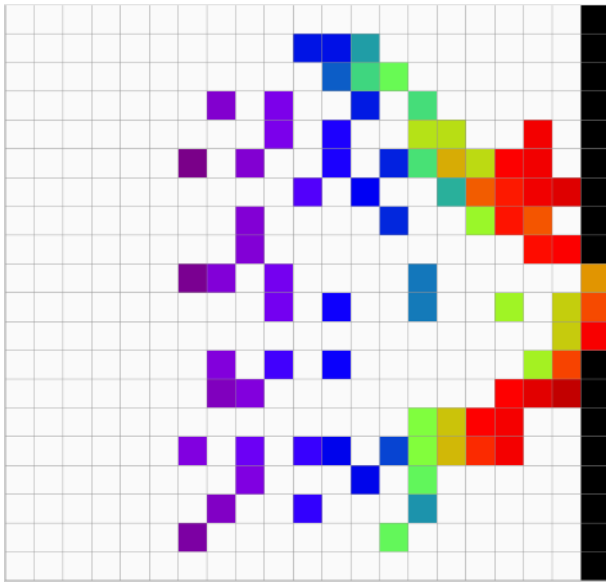
Déroulé de l'algorithme



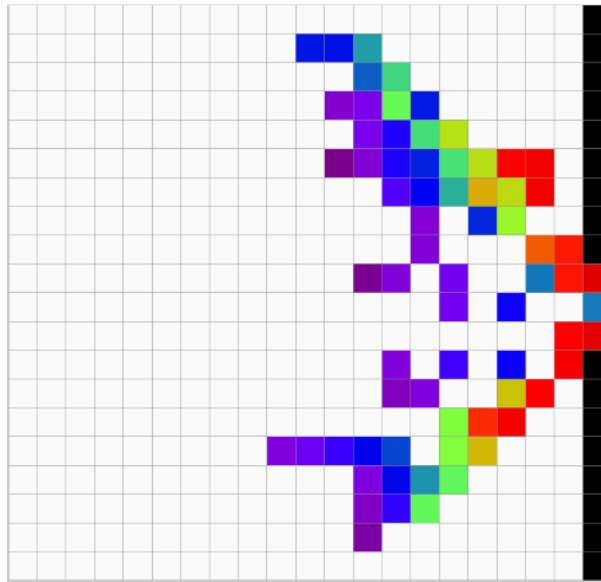
I-2) Programmation

Réglage du défaut apparent

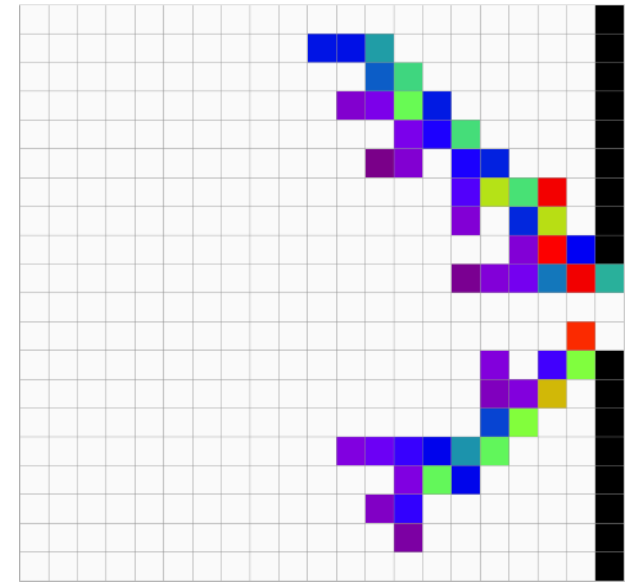
Embouteillage qui n'a pas lieu d'être



Grille au tour 6



Grille au tour 12

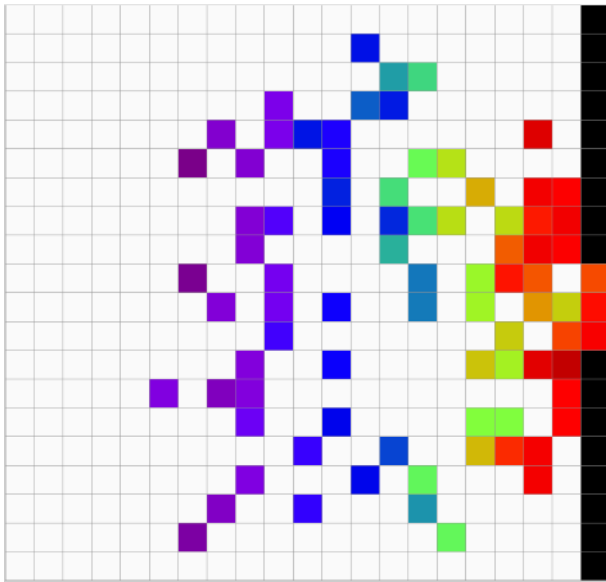


Grille au tour 20

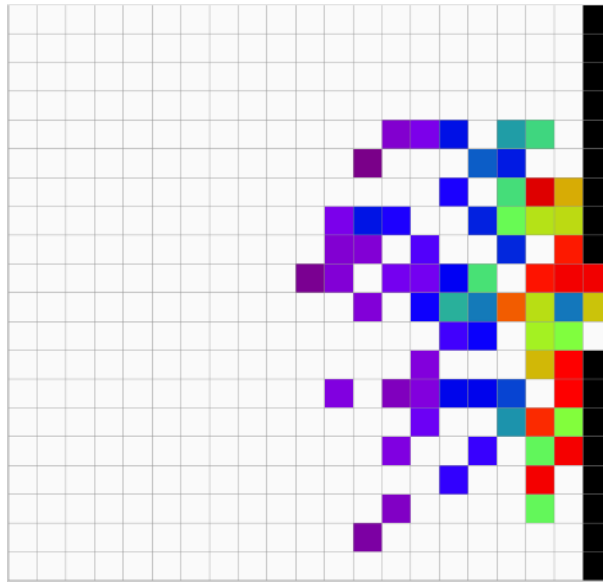
I-2) Programmation

Réglage du défaut apparent

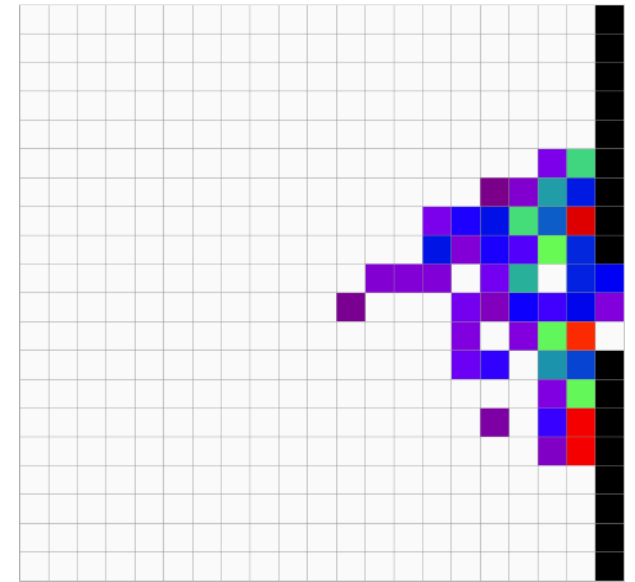
A* et recalcul



Grille au tour 6



Grille au tour 12



Grille au tour 20

I-3) Confrontation avec le réel

Évacuation de 90 personnes à $t = 20s$

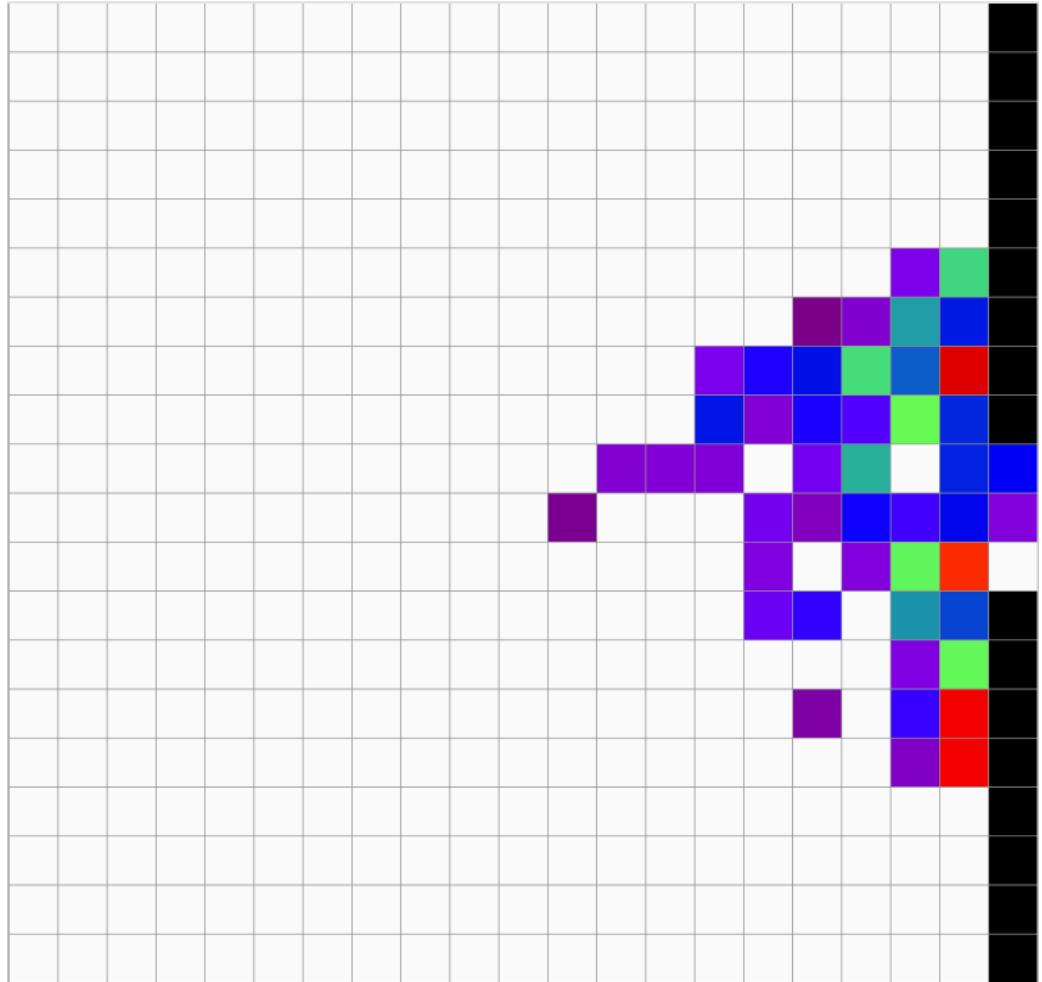


Image du papier Redefining the role of obstacles in pedestrian evacuation

Prise sur : <https://iopscience.iop.org/article/10.1088/1367-2630/aaf4ca/meta#njpaaf4caf1>

I-3) Confrontation avec le réel

Défaut du modèle : exemple du silo

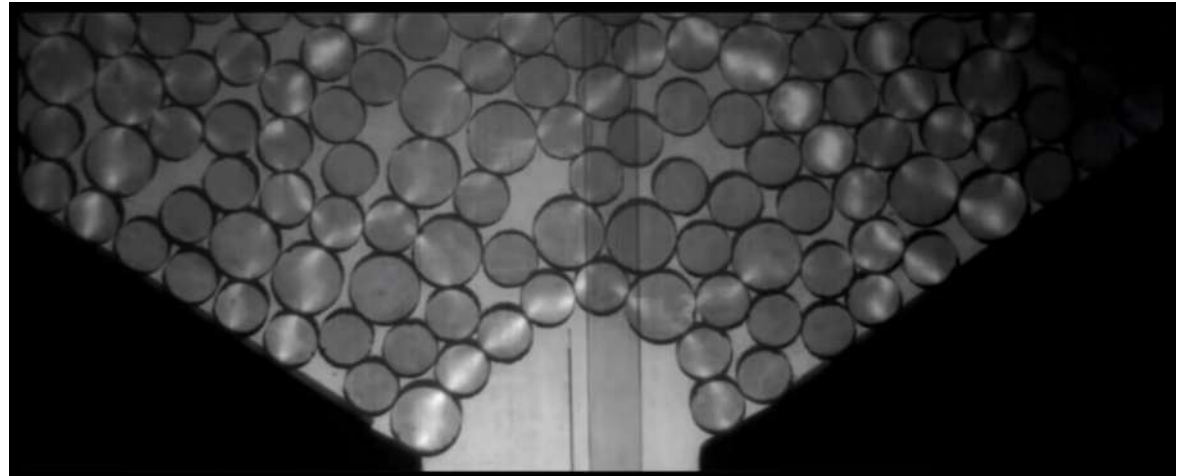
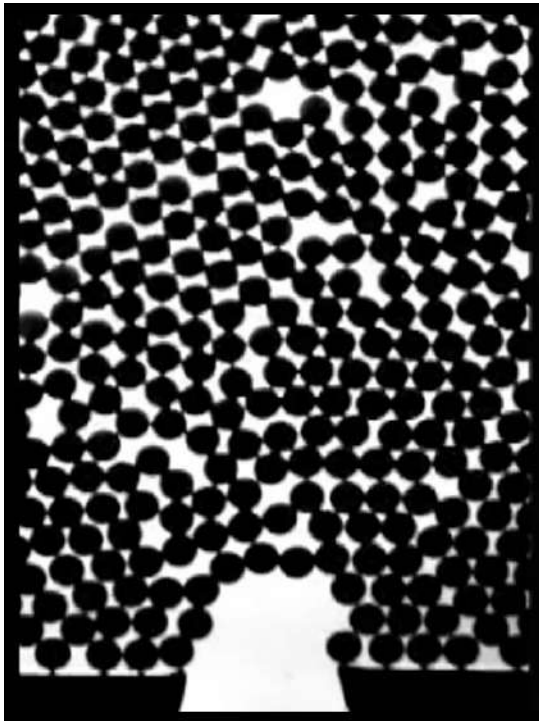


Image du papier Redefining the role of obstacles in pedestrian evacuation

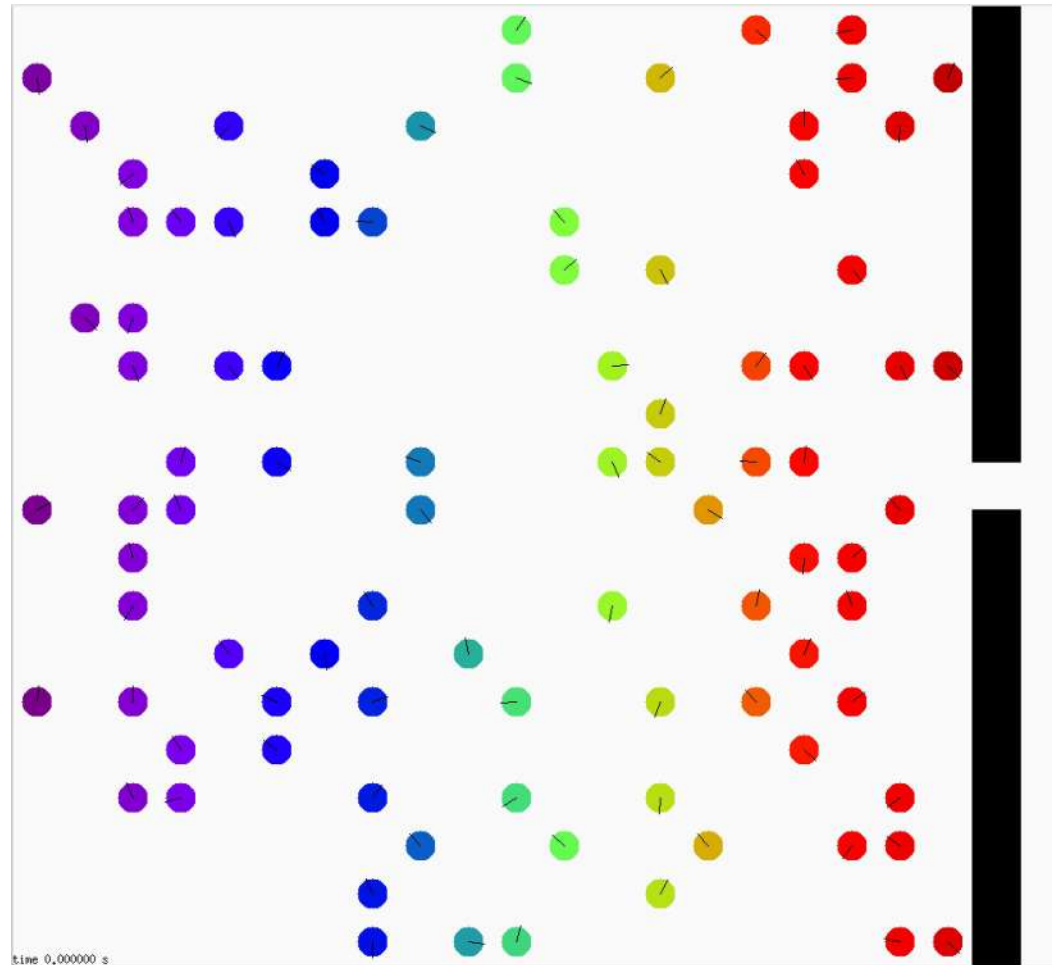
Prise sur : <https://iopscience.iop.org/article/10.1088/1367-2630/aaf4ca/meta#njpaa4caf1>

Tiré de « Le dilemme de l'évacuation » écrit par

Mehdi Moussaid, chercheur en science cognitive à l'institut Max Planck de Berlin

II-1) Modélisation en deux dimensions

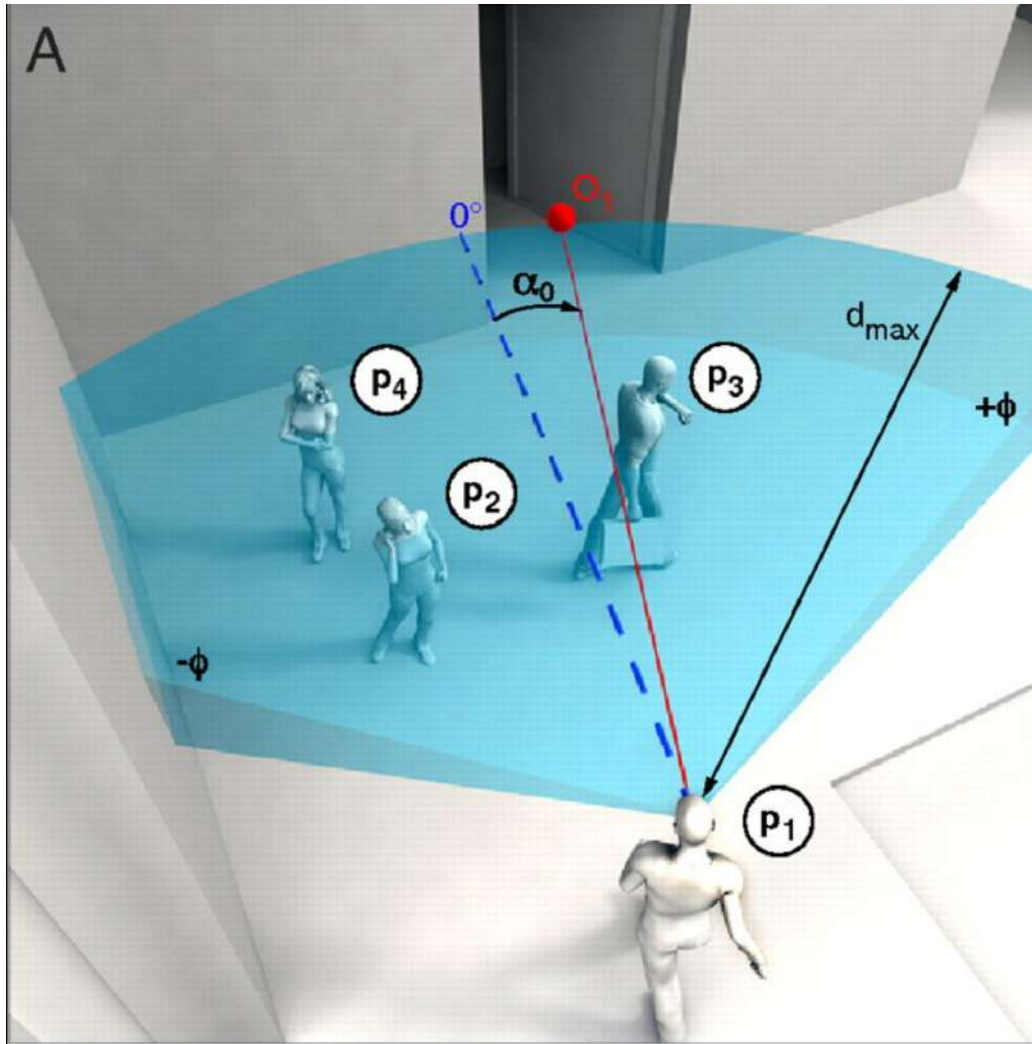
Présentation



How simple rules determine pedestrian behavior and crowd disasters
De Mehdi Moussaïd, Dirk Helbing, et Guy Theraulaz

II-2) Programmation

Méthode de choix de l'orientation

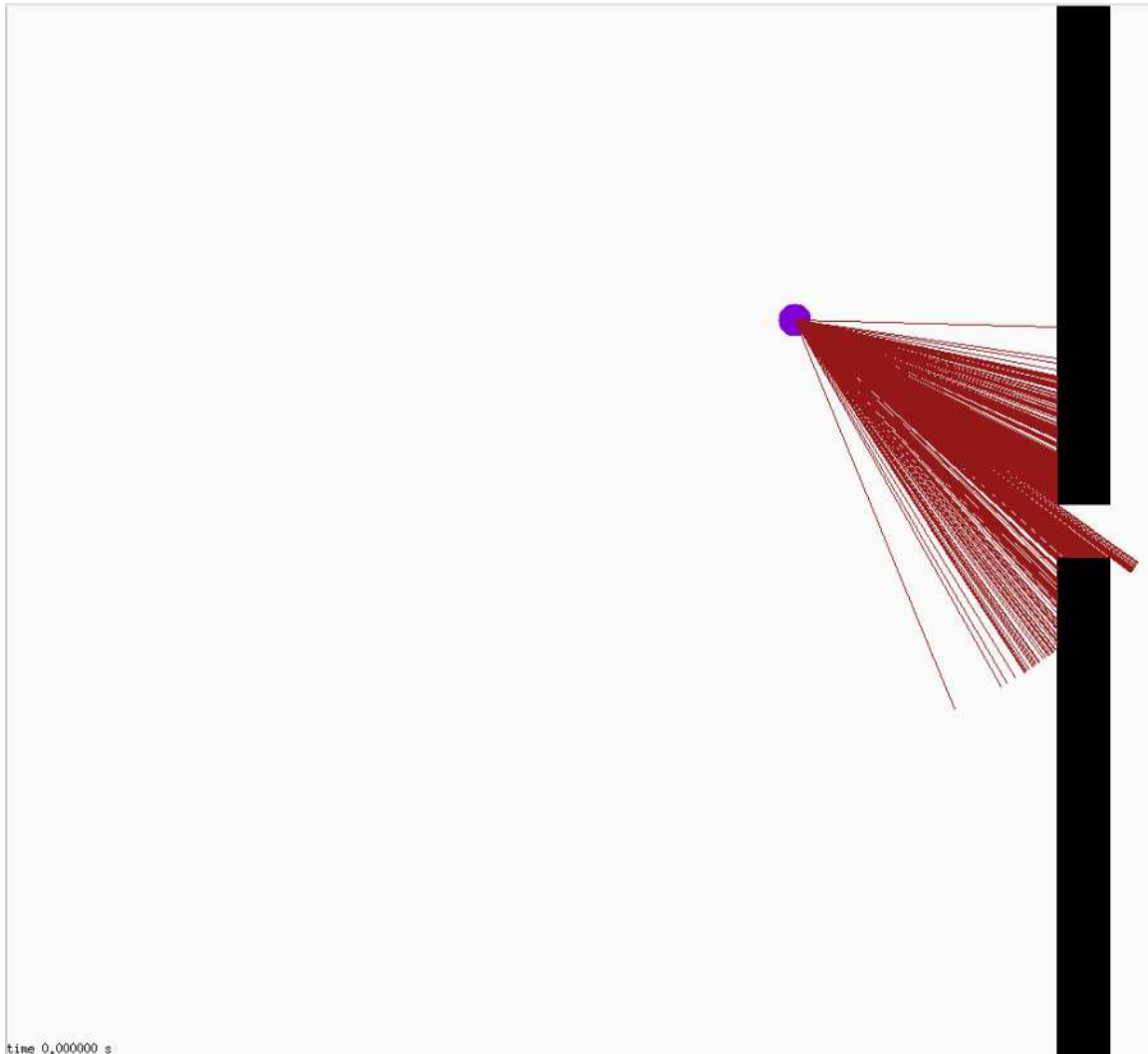


$$d(\alpha_{\text{des}}) = \min (d(\alpha), \alpha \in [-\pi, \pi])$$

$$d(\alpha) = (d_{\text{max}})^2 + f(\alpha)^2 - 2d_{\text{max}}f(\alpha)\cos(\alpha_0 - \alpha)$$

II-2) Programmation

Programmer une « vision » avec du raytracing



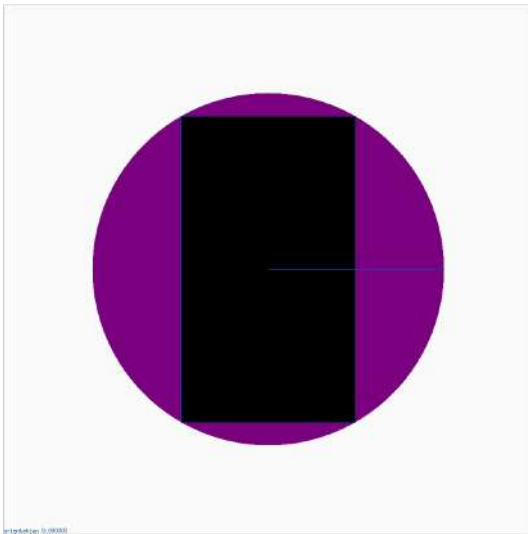
Box-Muller transformation

$$z = \sqrt{-2 \ln(u_1)} \cos(2\pi u_2)$$

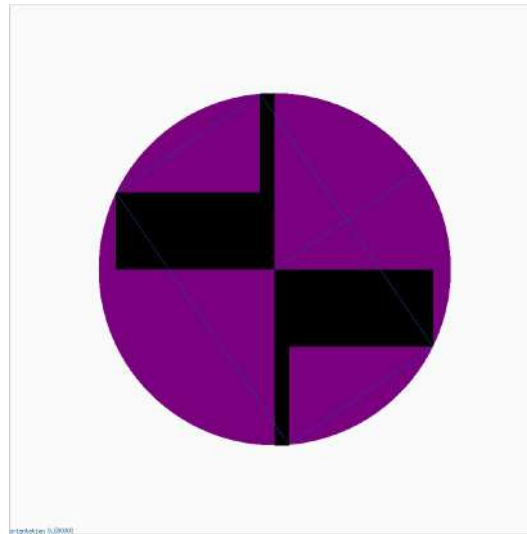
u_1, u_2 , deux variables issues
d'une fonction aléatoire
uniforme sur $[0; 1]$

II-2) Programmation

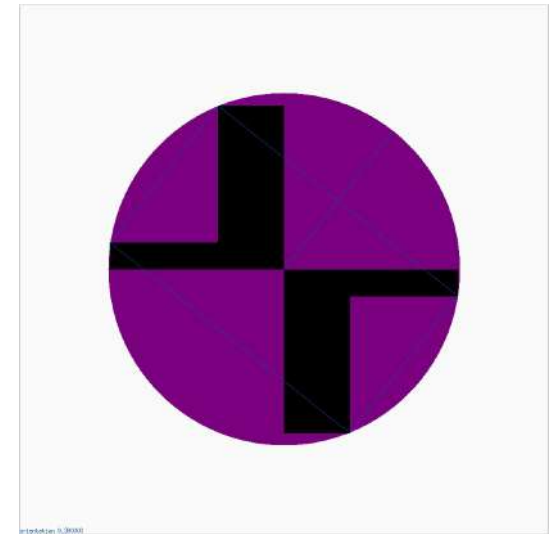
Découpage en rectangles suivant les axes



Pour direction = 0 rad



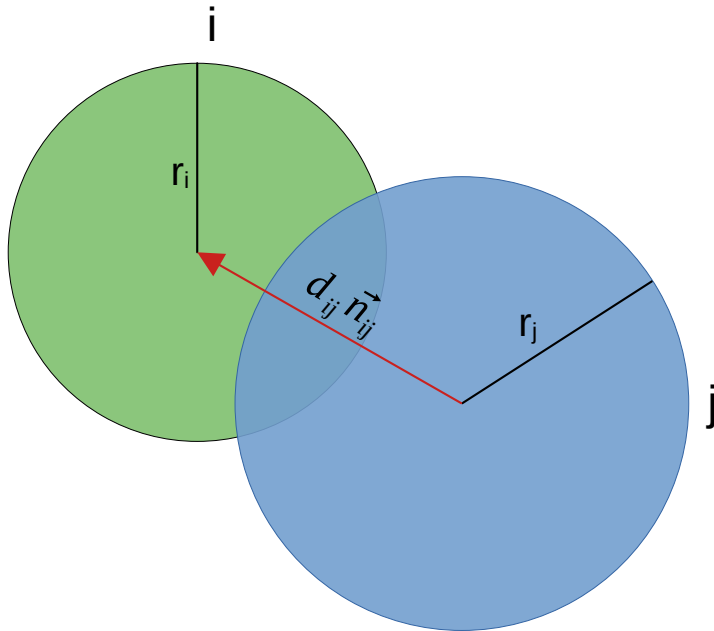
0,6 rad



0,9 rad

II-2) Programmation

Calcul du vecteur vitesse choisi



$$\vec{f}_{ij} = kg(r_i + r_j - d_{ij})\vec{n}_{ij}$$

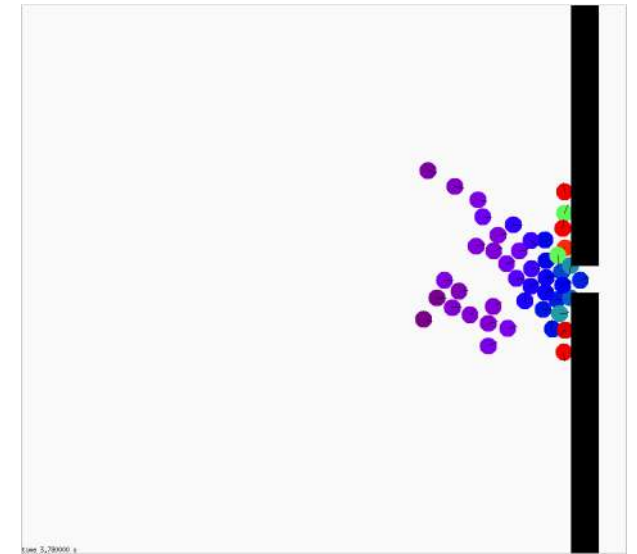
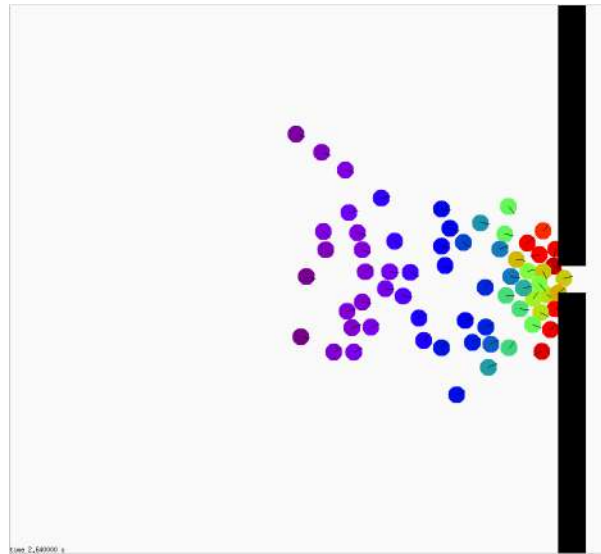
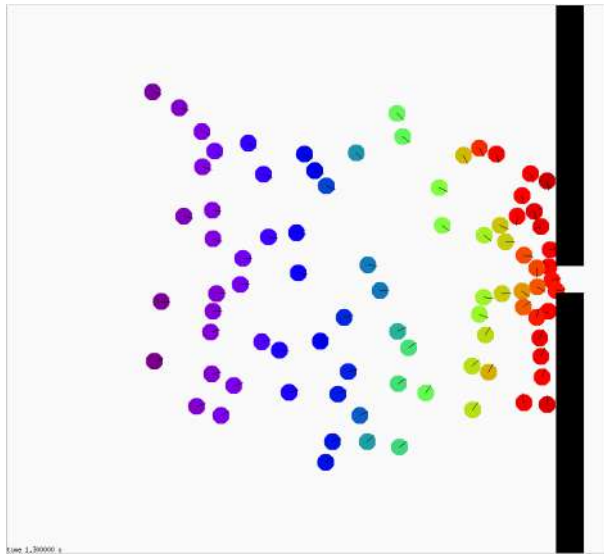
$$\vec{f}_{iW} = kg(r_i - d_{iW})\vec{n}_{iW}$$

$$\vec{v}_{des}(t) = \min(v_i^0, d_h) \cdot (u_x \cos(\alpha_{des}) + u_y \sin(\alpha_{des}))$$

$$\frac{d\vec{v}_{des}}{dt} = (\vec{v}_{des} - \vec{v}_i) + \sum_{j, j \neq i}^n \vec{f}_{ij}/m_i + \sum_W^m \vec{f}_{iW}/m_i$$

II-3) Comparaison avec le réel

Déroulement de l'évacuation



II-3) Comparaison avec le réel

Déroulement de l'évacuation

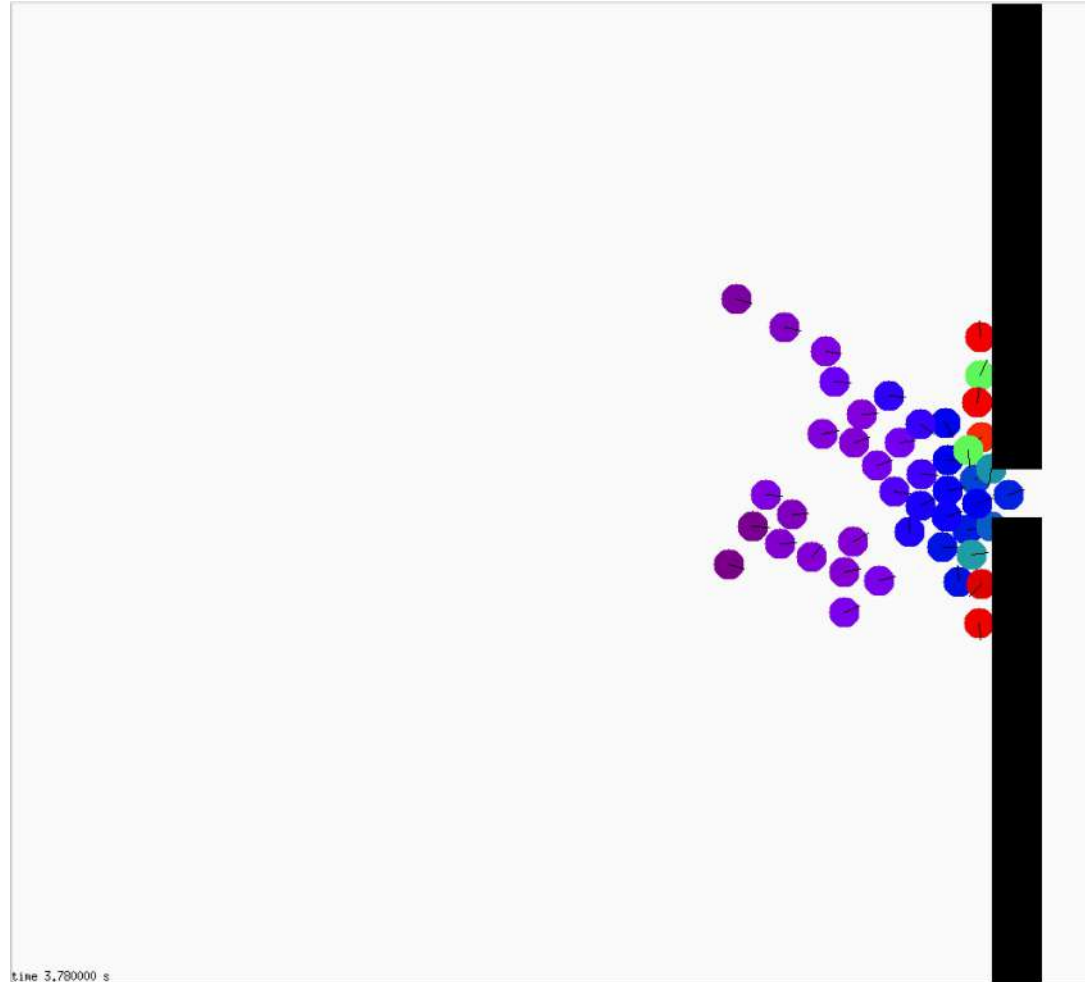


Image du papier Redefining the role of obstacles in pedestrian evacuation

Prise sur : <https://iopscience.iop.org/article/10.1088/1367-2630/aaf4ca/meta#njpaaf4caf1>

Conclusion

Modélisation multi-agents sur grille :

Qualités :

- Rapide ($O(nm)$ ou n = nombre de personnes, m = taille du chemin le plus long)

Défauts :

- S'approche du modèle réel seulement lors des situations non-urgentes

Modélisation en deux dimensions :

Qualités :

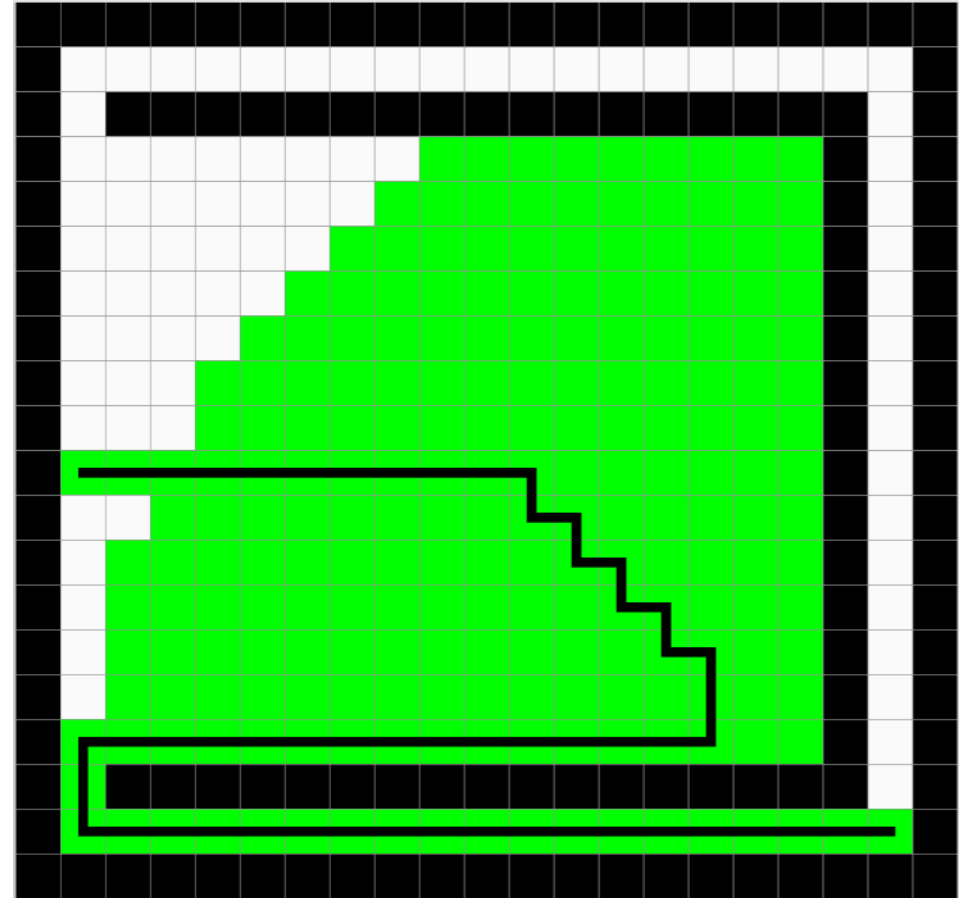
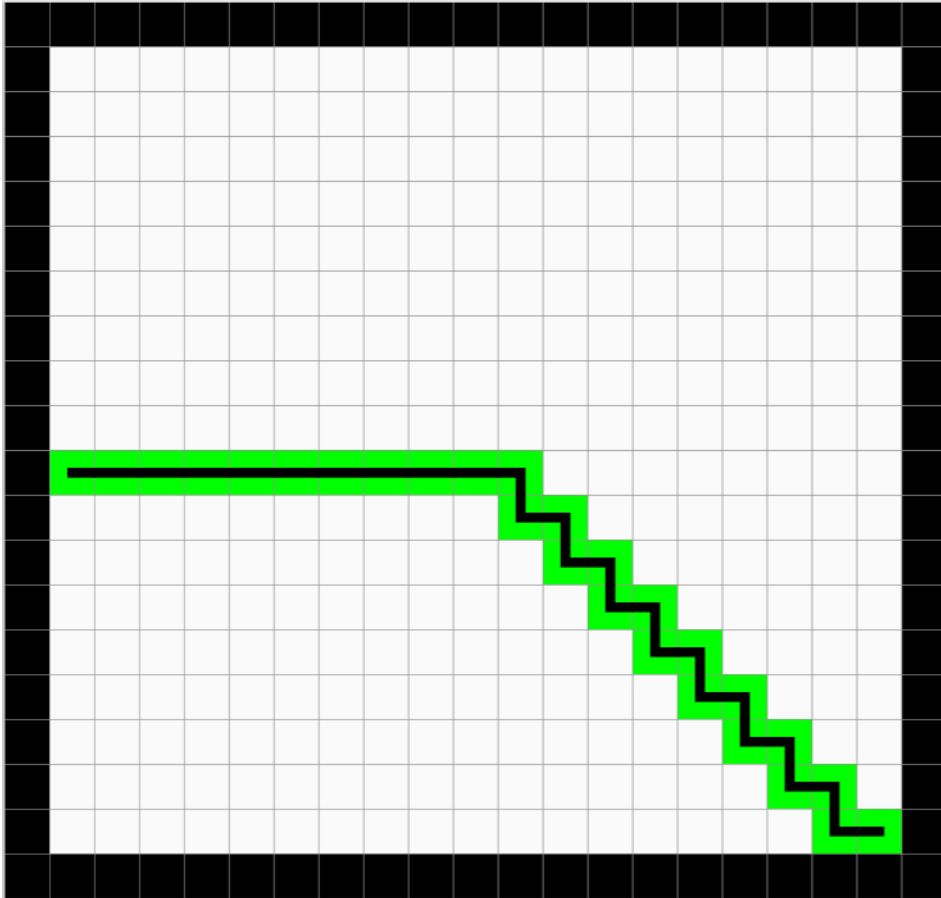
- Une meilleure modélisation

Défauts :

- Bien plus lourde en complexités temporelle ($O(n^2+nm)$ avec n = le nombre de personnes et m le nombre d'obstacles)

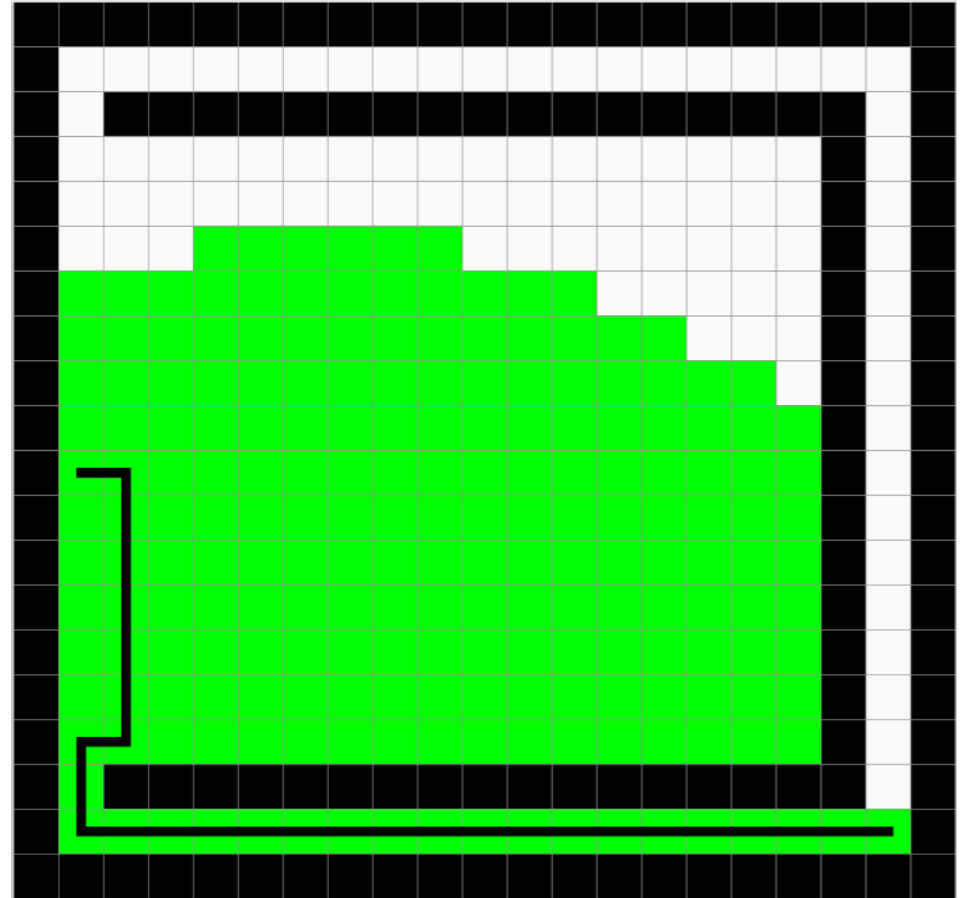
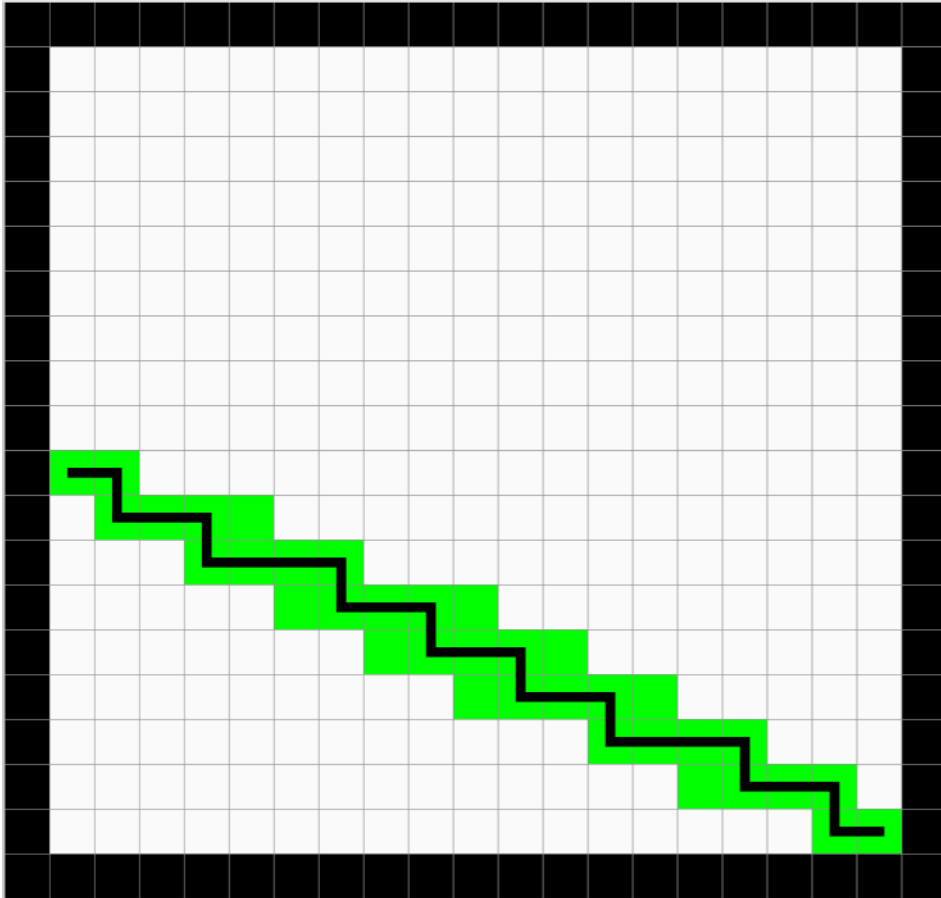
Annexe

Dijkstra pondéré



Annexe

A^*



Annexe

Bvh_tree

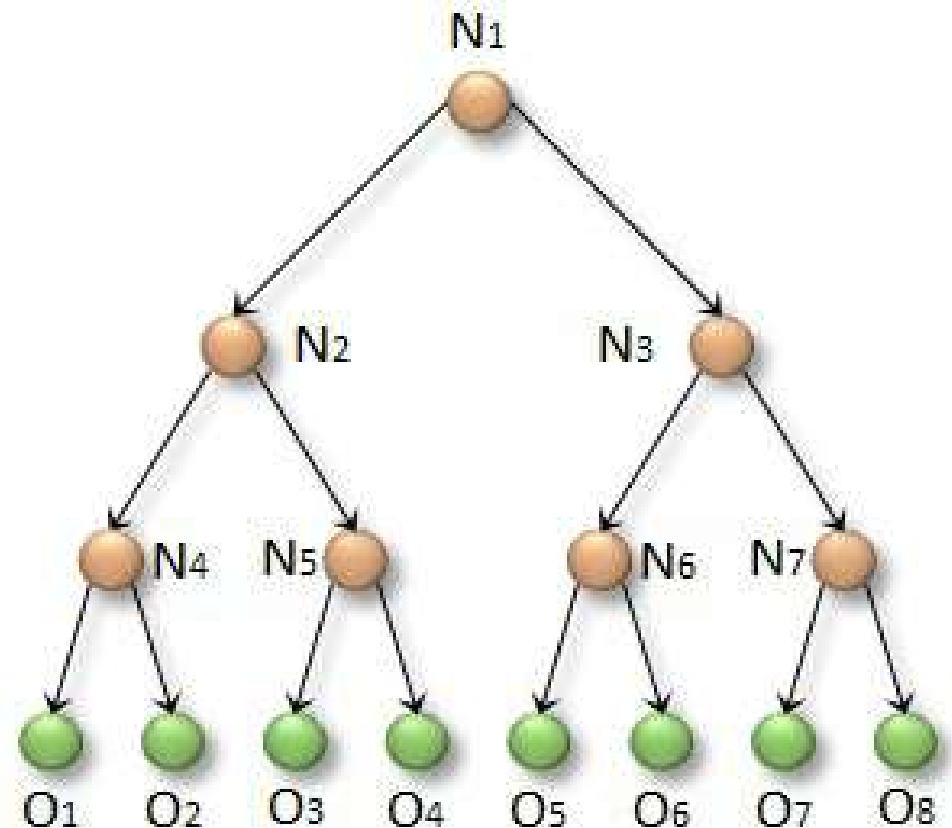
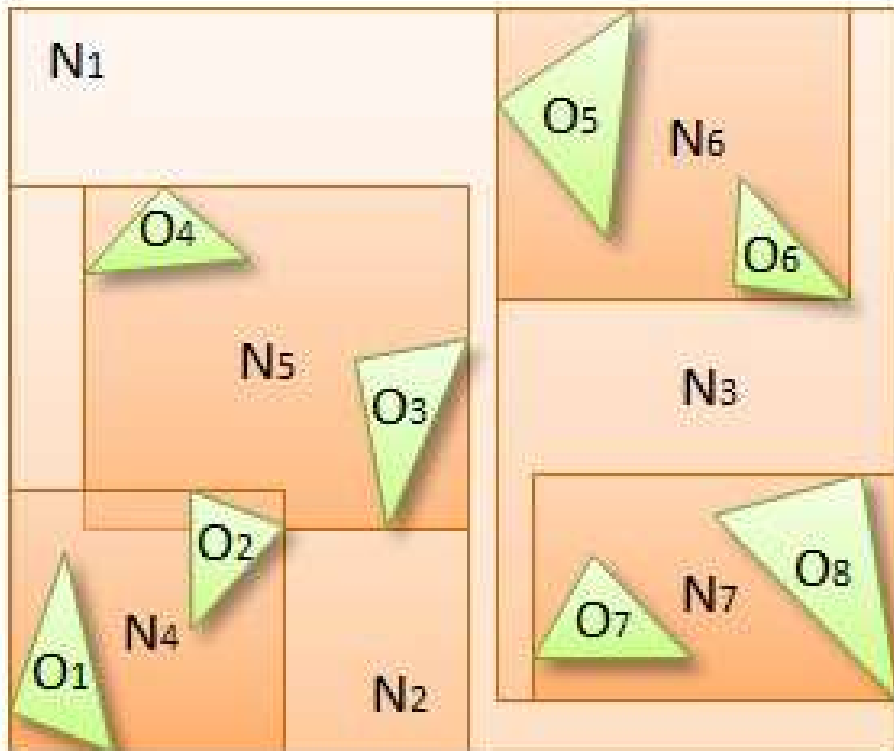
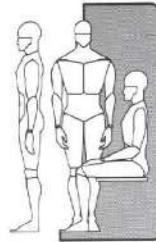


Image venant de <https://developer.nvidia.com/blog/thinking-parallel-part-ii-tree-traversal-gpu/>
écrit par Tero Karras

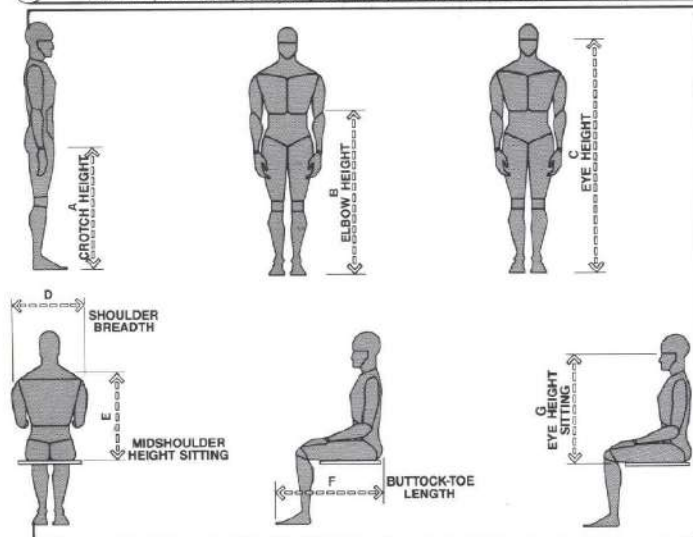
Annexe

Dimensions moyenne d'un homme

3 MISCELLANEOUS STRUCTURAL BODY DIMENSIONS

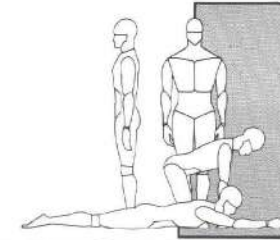


Adult Male and Female Miscellaneous Structural Body Dimensions in Inches and Centimeters by Age and Selected Percentiles															
		A		B		C		D		E		F		G	
		in	cm	in	cm	in	cm	in	cm	in	cm	in	cm	in	cm
95 5	MEN	36.2	91.9	47.3	120.1	68.6	174.2	20.7	52.6	27.3	69.3	37.0	94.0	33.9	86.1
	WOMEN	32.0	81.3	43.6	110.7	64.1	162.8	17.0	43.2	24.6	62.5	37.0	94.0	31.7	80.5
	MEN	30.8	78.2	41.3	104.9	56.8	143.4	17.4	44.2	23.7	60.2	32.0	81.3	30.0	76.2
	WOMEN	26.6	68.1	38.6	98.0	50.5	128.0	14.9	37.8	21.2	53.8	27.0	68.6	25.1	71.4

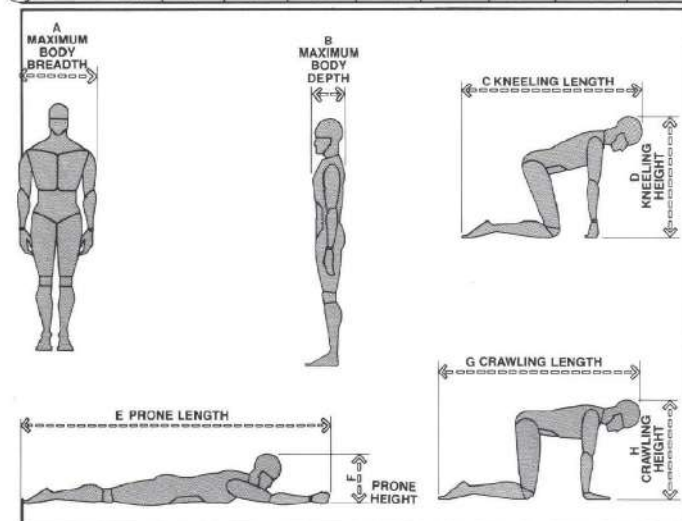


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6 WORKING POSITIONS



Adult Male Working Positions in Inches and Centimeters and by Selected Percentiles*		A	B	C	D	E	F	G	H
		in	in	in	in	in	in	in	in
95	in	22.0	13.0	48.1	34.5	95.6	16.4	58.2	30.5
5	cm	57.9	33.0	122.2	87.6	243.3	41.7	147.8	77.5
	in	18.8	10.1	37.5	29.7	84.7	12.3	49.3	26.2
	cm	47.8	25.7	95.5	75.4	215.1	31.2	125.2	66.5



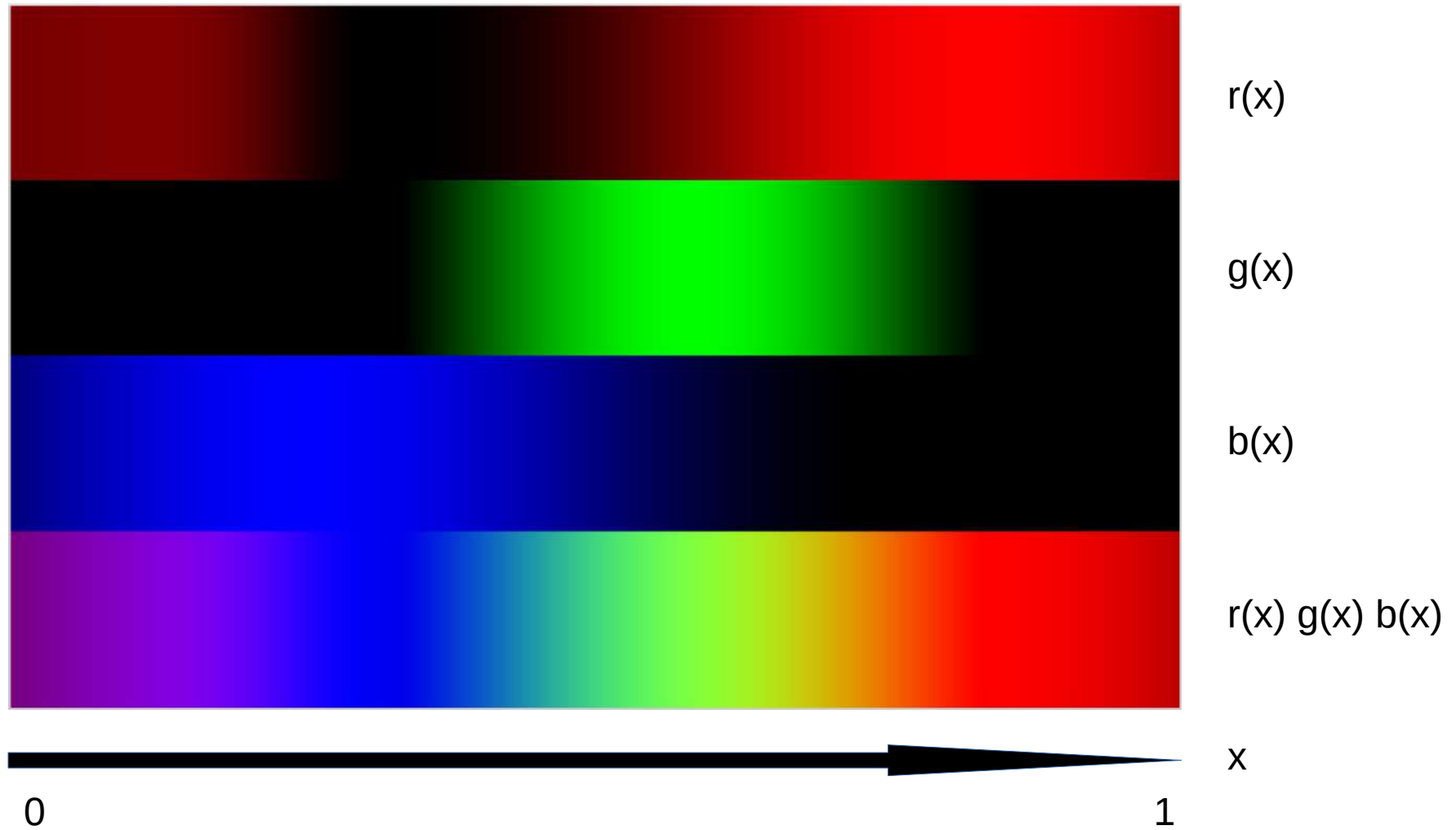
*A and B from Damon, Sloudt, McFarland, *The Human Body in Equipment Design*. C through H from *Human Factors Engineering*.

104 HUMAN DIMENSION/ANTHROPOMETRIC TABLES

Human dimension & interior space ; Chapitre B Human Dimension / Anthropometric Tables

Annexe

Couleur



Annexe

Couleur

```
let pi = Float.pi

let r x =
  let r = x *. pi *. 2. in
  if r >= pi *. 4. /. 6. then int_of_float ((cos (r +. pi *. 2. /. 6.) +. 1.) *. 255. /. 2.)
  else begin
    if r >= 3. *. pi /. 5.
    then 0
    else let tmp = cos (r *. r -. pi /. 6.) in int_of_float ((tmp +. 1.) *. 131. /. 2.)
  end

let g x =
  let r = x *. pi *. 2. in
  if r >= pi /. 3. then let tmp = sin (r -. 4. *. pi /. 6.) in int_of_float ((Float.pow tmp 1.2) *. 255.)
  else 0

let b x =
  let r = x *. pi *. 2. in
  if r >= pi +. pi /. 2. then 0
  else int_of_float ((sin r +. 1.) *. 255. /. 2.)
```

Annexe

Code multi-agents sur grille 01

```
open Graphics
open Couleur
```

```
type case = Obstacle | Exit | Empty | People of int
```

```
type plateau = case array array
```

```
exception Solution
```

```
type etat = Traite | Traitement | Inconnu
```

```
let print_pere (p : (int * int) array array) : unit =
  for j = 0 to Array.length p - 1 do
    for i = 0 to Array.length p.(0) - 1 do
      match p.(j).(i) with
      | (x, y) when x = -1 && y = -1 -> Printf.printf "| "
      | (x, y) when x = i-1 && y = j -> Printf.printf "|<"
      | (x, y) when x = i+1 && y = j -> Printf.printf "|>"
      | (x, y) when x = i && y = j-1 -> Printf.printf "|^"
      | _ -> Printf.printf "|v"
    done;
    Printf.printf "|\n";
  done;
  Printf.printf "\n";
  flush stdout
```

Annexe

Code multi-agents sur grille 02

```
let print_graph (p : plateau) c prop : unit =
  let n = Array.length p.(0) - 1 in
  for j = 0 to Array.length p - 1 do
    for i = 0 to n do
      set_color (rgb 150 150 150);
      draw_rect (i*prop) ((n-j-1)*prop) prop prop;
      (match p.(j).(i) with
      | Obstacle -> set_color (rgb 0 0 0)
      | People n -> set_color c.(n)
      | _ -> set_color (rgb 250 250 250));
      fill_rect (i*prop+1) ((n-j-1)*prop+1) (prop-2) (prop-2)
    done;
  done
```

Annexe

Code multi-agents sur grille 03

```
let print_graph_chemin (p : plateau) c prop acoord achemin : unit =
  let n = Array.length p.(0) - 1 in
  for j = 0 to Array.length p - 1 do
    for i = 0 to n do
      set_color (rgb 150 150 150);
      draw_rect (i*prop) ((n-j-1)*prop) prop prop;
      (match p.(j).(i) with
      | Obstacle -> set_color (rgb 0 0 0)
      | People n -> set_color c.(n)
      | _ -> set_color (rgb 250 250 250));
      fill_rect (i*prop+1) ((n-j-1)*prop+1) (prop-2) (prop-2)
    done;
  done;
  set_color (rgb 0 0 0);
  let t1 = 10 in
  (*let t2 = 4 in*)
  for i = 0 to Array.length achemin - 1 do
    let xt = ref (fst acoord.(i)) in
    let yt = ref (snd acoord.(i)) in
    List.iter (fun (x, y) ->
      set_color (rgb 0 0 0);
      fill_rect ((min !xt x) * prop + prop/2 - t1/2) ((n-1-(max !yt y)) * prop + prop/2 - t1/2)
        (t1 + (abs (!xt - x)) * prop) (t1 + (abs (!yt - y)) * prop);
      xt := x;
      yt := y) achemin.(i)
    done
```


Annexe

Code multi-agents sur grille 04

```
let valide (p : plateau) (x : int) (y : int) : bool =
  p.(y).(x) == Empty || p.(y).(x) == Exit

let mouvement (x : int) (y : int) =
  [(x+1,y); (x-1,y); (x,y+1); (x,y-1)]

let mouvement_valide (p : plateau) (pp : etat array array) (x : int) (y : int) : (int * int) list =
  List.filter
    (fun (x,y) ->
      x >= 0 && y >= 0 && y < Array.length p && x < Array.length p.(0) && (valide p x y) && pp.(y).(x) == Inconnu)
    (mouvement x y)

let trouve_chemin pere xe ye x y =
  let chemin = ref [] in
  (try
    while (!xe,!ye) <> (x, y) do
      chemin := (!xe, !ye) :: !chemin;
      let x_tmp, y_tmp = pere.(!ye).(!xe) in
      xe := x_tmp;
      ye := y_tmp
    done;
  with
    | Invalid_argument _ -> chemin := List.init (Array.length pere * Array.length pere.(0)) (fun _ -> (0, 0));
  !chemin
```

Annexe

Code multi-agents sur grille 05

```
let dis_to_exit ld (a,b) =
  let minab = ref (Float.infinity) in
  List.iter (fun (xd,yd) ->
    let tmp1 = sqrt (float_of_int ((xd-a)*(xd-a) + (yd-b)*(yd-b))) in
    if tmp1 < !minab then minab := tmp1) ld;
  !minab

let enleve_min l =
  let mini = List.fold_left (fun (a,x) (b,y) -> if a = min a b then (a,x) else (b,y))
    (Float.infinity, (0,0)) l in
  let rec aux l =
    match l with
    | [] -> []
    | t::q -> if t = mini then q else t :: (aux q) in
  (snd mini, aux l)
```

Annexe

Code multi-agents sur grille 06

```
let resolution (p : plateau) (x : int) (y : int) (ld : (int * int) list) : (int* int) list =
  let pere = Array.make_matrix (Array.length p) (Array.length p.(0)) (-1,-1) in
  try
    let map_deplacement = Array.make_matrix (Array.length p) (Array.length p.(0)) Inconnu in
    let f = ref [(dis_to_exit ld (x,y), (x,y))] in
    let n = List.length ld in
    let m = ref 0 in
    map_deplacement.(y).(x) <- Traitement;
    while !f <> [] do
      let tmp = enleve_min !f in
      f := snd tmp;
      let i,j = fst tmp in
      if map_deplacement.(j).(i) == Traitement
      then begin
        if p.(j).(i) = Exit then begin
          m := !m +1;
          if !m = n
          then
            raise Solution
          end;
        map_deplacement.(j).(i) <- Traite;
        List.iter (fun (ip, jp) ->
          f := (dis_to_exit ld (ip, jp), (ip, jp)) :: !f;
          if map_deplacement.(jp).(ip) == Inconnu
          then begin
            pere.(jp).(ip) <- (i, j);
            map_deplacement.(jp).(ip) <- Traitement end)
            (mouvement_valide p map_deplacement i j)
          end
        done;
        if !m > 0 then raise Solution
        else begin
          []
        end
      end
```


Annexe

Code multi-agents sur grille 07

```
with Solution ->
  print_pere pere;
  let rep = ref (List.init (Array.length p * Array.length p) (fun _ -> (0, 0))) in
  List.iter (fun (xd,yd) ->
    let xe, ye = ref xd, ref yd in
    let tmp = trouve_chemin pere xe ye x y in
    if List.length tmp < List.length !rep then rep := tmp) ld;
  !rep

let init_matrix (leny : int) (lenx : int) (f : (int * int) -> 'a) : 'a array array =
  let rep = Array.make_matrix leny lenx (f (0, 0)) in
  for i = 0 to Array.length rep -1 do
    for j = 0 to Array.length rep.(0) -1 do
      rep.(i).(j) <- f (j,i)
    done
  done;
  rep

let randomarray n max =
  if max < n then failwith "max < n";
  let rep = Array.make n (-1) in
  for i = 0 to n-1 do
    let tmp = ref (Random.int max) in
    while Array.exists (fun i -> i = !tmp) rep do
      tmp := Random.int max
    done;
    rep.(i) <- !tmp
  done;
  rep
```

Annexe

Code multi-agents sur grille 08

```
let _ =
  Random.init 90;
  let my = 20 in
  let mx = my +1 in
  let p = init_matrix my mx (fun (x,y) -> match x, y with
    |_, _ when x = mx-1 && y < my/2 -1 -> Obstacle
    |_, _ when x = mx-1 && y > my/2 +1 -> Obstacle
    |_, _ -> Empty) in
  let ld = [(mx-1, my/2); (mx-1, my/2 -1); (mx-1, my/2 +1)] in
  List.iter (fun (xd, yd) -> p.(yd).(xd) <- Exit) ld;
  let n = 90 in
  let tmp = randomarray n (my*my) in
  let acoord = Array.init n (fun i -> tmp.(i)/my, tmp.(i) mod my) in
  let apeople = Array.init n (fun i -> i) in
  let acouleur = Array.init n (fun i ->
    let c = float_of_int (tmp.(i)) /. float_of_int (my*my) in
    rgb (r c) (g c) (b c)) in
  let achemin = Array.init (Array.length acoord)
    (fun i -> resolution p (fst acoord.(i)) (snd acoord.(i)) ld) in
  let plateau = Array.init (Array.length p) (fun i -> Array.copy p.(i)) in
  for i = 0 to n-1 do
    p.(snd acoord.(i)).(fst acoord.(i)) <- People apeople.(i)
  done;

  let prop_i = 50 in
  open_graph (Printf.sprintf " %dx%d" (prop_i*mx) (prop_i*my));
  set_window_title "test";
  print_graph_chemin p acouleur prop_i acoord achemin;
```

Annexe

Code multi-agents sur grille 09

```
while Array.fold_left (+) 0 apeople <> -n do
  temp := !temp -1;
  let start_time = Sys.time () in
  for i = 0 to n-1 do
    if apeople.(i) <> -1
    then begin
      (match achemin.(i) with
      | _ when List.mem acoord.(i) ld ->
        p.(snd acoord.(i)).(fst acoord.(i)) <- Exit;
        apeople.(i) <- -1
      | [] -> achemin.(i) <- resolution plateau (fst acoord.(i)) (snd acoord.(i)) ld;
        if achemin.(i) <> []
        then begin
          let nx, ny = List.hd achemin.(i) in
          if valide p nx ny
          then begin
            p.(snd acoord.(i)).(fst acoord.(i)) <- Empty;
            p.(ny).(nx) <- People apeople.(i);
            achemin.(i) <- List.tl achemin.(i);
            acoord.(i) <- (nx,ny)
          end
        end
      | (x,y)::q when valide p x y ->
        p.(snd acoord.(i)).(fst acoord.(i)) <- Empty;
        p.(y).(x) <- People apeople.(i);
        achemin.(i) <- q;
        acoord.(i) <- (x,y)
    end
  end
end
```

Annexe

Code multi-agents sur grille 10

```
| (x,y)::_ ->
  plateau.(y).(x) <- Obstacle;
  achemin.(i) <- resolution plateau (fst acoord.(i)) (snd acoord.(i)) ld;
  plateau.(y).(x) <- Empty;
  if achemin.(i) <> []
  then
    let nx, ny = List.hd achemin.(i) in
    if valide p nx ny
    then begin
      p.(snd acoord.(i)).(fst acoord.(i)) <- Empty;
      p.(ny).(nx) <- People apeople.(i);
      achemin.(i) <- List.tl achemin.(i);
      acoord.(i) <- (nx,ny)
    end
  )
end
done;
while Sys.time () < start_time +. 0.5 do () done;
print_graph p acouleur prop_i
done;
close_graph ()
```


Code raytracing 01

```
let rec float_mod orient =
  if orient > pi then float_mod (orient -. 2. *. pi)
  else if orient < 0. -. pi then float_mod (orient +. 2. *. pi)
  else orient
```

```
let dist_euclidienne (x,y) (x',y') =  
  sqrt ((x-.x')*.(x-.x') +. (y-.y')*.(y-.y'))
```

```
let regarde_bonne_dir dx (dy : float) (o : float) : bool =
  ((dx >= 0. && cos o >= 0.) || (dx <= 0. && cos o <= 0.)) &&
  ((dy >= 0. && sin o >= 0.) || (dy <= 0. && sin o <= 0.))
```

f

d

c

e

*)

obj

Annexe

Code raytracing 02

```
(*verification de l'intersection avec les segments verticaux*)
(*verif de l'intersection
  verif que l'intersection se face du bon cote (droite si l'humain regarde a droite et gauche si non)
  verif que l'intersection se face sur la bonne hauteur (haut si l'humain regarde en haut et bas si non) *)
if (min d f) <= a *. c +. b && a *. c +. b <= (max d f) && regarde_bonne_dir (c-.xp) (a *. c +. b -. yp) o &&
  dist_euclidienne (c,a*. c +. b) (xp, yp) > rp && dist_euclidienne (c,a*. c +. b) (xp, yp) < dmax
then begin
  if (!x <> None &&
    dist_euclidienne (c,a*. c +. b) (xp, yp) <= dist_euclidienne (Option.get !x, Option.get !y) (xp, yp))
    || !x = None
  then begin
    x := Some c;
    y := Some (a *. c +. b);
    rep := Some obji
  end
end;
if (min d f) <= a *. e +. b && a *. e +. b <= (max d f) && regarde_bonne_dir (e -. xp) (a *. e +. b -. yp) o &&
  dist_euclidienne (e,a*. e +. b) (xp, yp) > rp && dist_euclidienne (e,a*. e +. b) (xp, yp) < dmax
then begin
  if (!x <> None &&
    dist_euclidienne (e,a*. e +. b) (xp, yp) <= dist_euclidienne (Option.get !x, Option.get !y) (xp, yp))
    || !x = None
  then begin
    x := Some e;
    y := Some (a *. e +. b);
    rep := Some obji
  end
end;
end;
```

Annexe

Code raytracing 03

```
(*verification de l'intersection avec les segments horizontaux*)
if (min c e) <= (d -. b) /. a && (d -. b) /. a <= (max c e) && regarde_bonne_dir ((d -. b) /. a -. xp) (d -. yp) o &&
    dist_euclidienne ((d -. b) /. a,d) (xp, yp) > rp && dist_euclidienne ((d -. b) /. a,d) (xp, yp) < dmax
then begin
    if (!x <> None &&
        dist_euclidienne ((d -. b) /. a,d) (xp, yp) <= dist_euclidienne (Option.get !x, Option.get !y) (xp, yp))
        || (!x = None && !y = None)
    then begin
        x := Some ((d -. b) /. a);
        y := Some d;
        rep := Some obji
    end
end;
if (min c e) <= (f -. b) /. a && (f -. b) /. a <= (max c e) && regarde_bonne_dir ((f -. b) /. a -. xp) (f -. yp) o &&
    dist_euclidienne ((f -. b) /. a,f) (xp, yp) > rp && dist_euclidienne ((f -. b) /. a,f) (xp, yp) < dmax
then begin
    if (!x <> None &&
        dist_euclidienne ((f -. b) /. a,f) (xp, yp) <= dist_euclidienne (Option.get !x, Option.get !y) (xp, yp))
        || (!x = None && !y = None)
    then begin
        x := Some ((f -. b) /. a);
        y := Some f;
        rep := Some obji
    end
end;
let tmp = tmp_xy <> (!x, !y) in
if tmp && not change
then begin
    x := fst tmp_xy;
    y := snd tmp_xy
end;
tmp
```

Annexe

Code raytracing 04

```
let raytracing_vecteur (orient : float) (xp : float) (yp : float) (rp : float) (dmax : float)
    (obj : ((float * float) * (float * float)) list) =
  (*orient = angle du rayon sur le cercle trigo
    (xp, yp) = position a partir de la quelle le rayon est tire
    rp = rayon a partir du quel les colition sont possible
    obj = liste des objets (rectangle) sur le terrain *)
  let o = float_mod orient in
  let a = tan o in
  let b = yp -. a *. xp in
  let rep = ref (Some ((0., 0.), (0., 0.))) in
  let x = ref (Some (xp +. dmax *. cos o)) in
  let y = ref (Some (yp +. dmax *. sin o)) in
  (*Printf.printf "orient = %f;\ta = %f;\tb = %f" o a b;*)
  let rec aux obj a b =
    match obj with
    |[] -> ()
    |obji::q ->
      ignore (intersection_droite_rect a b o x y rep xp yp rp obji dmax true);
      aux q a b
  in
  aux obj a b;
  if !x = None || Option.get !x = Float.infinity || Option.get !x = Float.neg_infinity then begin
    failwith "raytracing error"
  end;
  !rep, (Option.get !x, Option.get !y)
```


Annexe

Code 2D 01

```
open Graphics
open Bvh_tree
open Couleur
```

```
let dt : float = 1.0 /. 50.0
let dmax : float = 8. (*m*)
let k : float = 1000.
```

```
let maxX : float = 22. (*largeur de la carte en metre*)
let maxY : float = 20. (*hauteur de la carte en metre*)
let maxX_i : int = (int_of_float maxX)
let maxY_i : int = (int_of_float maxY)
let prop_i : int = 1000 / maxX_i (*affichage proportionnel 1 metre = prop pixel*)
let prop : float = (float_of_int prop_i)
let vitesse_max_humain : float = 8.3 (*m.s-1*)
let acceleration_max_humain : float = 2. (*m.s-2*)
```

```
type people = {
  largeur : float; (*en metre represente la largeur de la personne epaule droite à epaule gauche*)
  epaisseur : float; (*en metre represente l'epaisseur de la personne la profondeur du corp*)
  rayon : float; (*en metre*)
  masse : float; (*en kilogramme represente la masse de la personne*)
  allure_voulue : float; (*en m/s*)
  pos_voulue : float * float; (*en m, m*)
  mutable position : float * float; (*en m, m*)
  mutable allure : float; (*en m/s*)
  mutable direction : float; (*en radiant*)
}
```

Annexe

Code 2D 02

```
let people_init (l : float) (ep : float) (m : float) (allure : float) (pos : float * float) (allure_voulue : float)
  (pos_voulue : float * float) (dir : float) : people =
{
  largeur = l;
  epaisseur = ep;
  rayon = dist_euclidienne (l, ep) (0., 0.) /. 2.;
  masse = m; allure_voulue = allure_voulue;
  pos_voulue = pos_voulue;
  position = pos;
  allure = allure;
  direction = dir
}

let set_allure (p : people) a = p.allure <- min a vitesse_max_humain

let set_dir (p : people) d = p.direction <- float_mod d

let print_people (lp : people list) lcouleur : unit =
  let rec aux lp lcouleur j n =
    match lp, lcouleur with
    | p::qp, couleur::qcouleur ->
      (let x, y = p.position in
       set_color couleur;
       fill_circle (int_of_float (x *. prop)) (int_of_float (y *. prop)) (int_of_float (p.rayon *. prop));
       set_color (rgb 0 0 0);
       moveto (int_of_float (x *. prop)) (int_of_float (y *. prop));
       lineto (int_of_float ((x +. cos p.direction *. p.rayon) *. prop))
              (int_of_float ((y +. sin p.direction *. p.rayon) *. prop));
       aux qp qcouleur (j +. 1.) n)
    | _, _ -> () in
  aux lp lcouleur 0. (float_of_int (List.length lp))
```

Annexe

Code 2D 03

```
let random_diff0 f =
  let temp = ref (Random.float f) in
  while !temp < 0.000001 do
    temp := Random.float f
  done;
  !temp

let set_pos lp t =
  let rec aux lp t (acc : ((float * float) * (float * float)) list) : ((float * float) * (float * float)) list =
    match lp with
    | [] -> List.rev acc
    | p::q ->
      let dis_p = p.allure *. t in
      let x, y = p.position in
      let newx = x +. (cos p.direction)*.dis_p in
      let newy = y +. (sin p.direction)*.dis_p in
      p.position <- (newx, newy);
      let a1 = asin (p.largeur /. (2. *. p.rayon)) in
      let a2 = pi/.2. +. asin (p.epaisseur /. (2. *. p.rayon)) in
      aux q t (
        ((newx, newy +. (sin (float_mod (p.direction -. a2))) *. p.rayon),
          (newx +. (cos (float_mod (p.direction -. a2))) *. p.rayon, newy))::
        ((newx, newy -. (sin (float_mod (p.direction -. a1))) *. p.rayon),
          (newx -. (cos (float_mod (p.direction -. a1))) *. p.rayon, newy))::
        ((newx -. (cos (float_mod (p.direction +. a2))) *. p.rayon, newy),
          (newx, newy -. (sin (float_mod (p.direction +. a2))) *. p.rayon))::
        ((newx +. (cos (float_mod (p.direction +. a1))) *. p.rayon, newy),
          (newx, newy +. (sin (float_mod (p.direction +. a1))) *. p.rayon))::acc) in
  aux lp t []
```


Annexe

Code 2D 04

```
let min_abs a b = if min (Float.abs a) (Float.abs b) = Float.abs a then a else b
```

```
let print_bvh_tree a =  
  let rec aux a =  
    match a with  
    | Nil -> ()  
    | Noeud (g,o,d) ->  
      set_color (rgb 65 0 125);  
      fill_rect  
        (int_of_float ((fst (fst o)) *. prop))  
        (int_of_float ((snd (fst o)) *. prop))  
        (abs(int_of_float (((fst (fst o))-.(fst (snd o))) *. prop)))  
        (abs(int_of_float (((snd (fst o))-.(snd (snd o))) *. prop)));  
      aux g;  
      aux d;  
    | Feuille o ->  
      set_color (rgb 125 0 0);  
      fill_rect  
        (int_of_float ((fst (fst o)) *. prop))  
        (int_of_float ((snd (fst o)) *. prop))  
        (abs(int_of_float (((fst (fst o))-.(fst (snd o))) *. prop)))  
        (abs(int_of_float (((snd (fst o))-.(snd (snd o))) *. prop))) in  
    aux a
```

Annexe

Code 2D 05

```
let print_obj l =
  let rec aux l =
    set_color (rgb 0 0 0);
    match l with
    | [] -> ()
    | o::q ->
      let x = min (fst (fst o)) (fst (snd o)) in
      let y = min (snd (fst o)) (snd (snd o)) in
      let w = max (fst (fst o)) (fst (snd o)) -. x in
      let h = max (snd (fst o)) (snd (snd o)) -. y in
      fill_rect (int_of_float (x *. prop)) (int_of_float (y *. prop))
                (int_of_float (w *. prop)) (int_of_float (h *. prop));
      aux q
  in
  aux l
```

```
let rm lp lc =
  let rec aux lp lc acclp acclc accn =
    match lp, lc with
    | p::qp, c::qc ->
      (*if dist_euclidienne p.position p.pos_voulue < p.rayon*)
      if fst p.position >= fst p.pos_voulue
      then
        aux qp qc acclp acclc accn
      else
        aux qp qc (p::acclp) (c::acclc) (1+accn)
    | _, _ -> ((acclp, acclc), accn) in
  aux lp lc [] [] 0
```

Annexe

Code 2D 06

```
let new_orient (l : ('a * 'b * float) list) (dmax : float) (alpha0 : float) =
  let rec aux l min acc =
    match l with
    | [] -> acc
    | (dist, _, alpha)::q ->
      let tmp = dmax *. dmax +. dist *. dist
        -. 2. *. dmax *. dist *. cos (alpha0 -. alpha)
        +. dmax *. Float.abs (tan ((alpha0 -. alpha) /. 2.)) in
      if tmp < min
      then aux q tmp alpha
      else aux q min acc in
  aux l Float.infinity 0.

let changement_direction_allure (lp : people list) (ll : (float * (float * float) * float) list list)
  (obj : ((float * float) * (float * float)) list) (completobj : ((float * float) * (float * float)) list) : unit =
  (* lp : liste des personne presente
    ll : liste de (liste des point vu par une personne) par personne
    obj : liste des objets sur le terrain *)
  let rec somme_fij lp ri mi posi i j accx accy =
    match lp with
    | [] -> (k *. accx /. mi, k *. accy /. mi)
    | p::qlp -> if i = j
      then
        somme_fij qlp ri mi posi i (j+1) accx accy
      else begin
        let g = ri +. p.rayon -. dist_euclidienne posi p.position in
        if g <= 0.
        then
          somme_fij qlp ri mi posi i (j+1) accx accy
        else begin
          let alphasij = atan2 (snd posi -. snd p.position) (fst posi -. fst p.position) in
          somme_fij qlp ri mi posi i (j+1) (accx +. g *. cos alphasij) (accy +. g *. sin alphasij)
        end
      end
  end
  in
```

Annexe

Code 2D 07

```
let rec somme_fiw obj ri mi xi yi (accx: float) accy =
  match obj with
  | [] -> (k *. accx /. mi, k *. accy /. mi)
  | ((x1, y1), (x2, y2))::qobj ->
    let gx = min x1 x2 in
    let dx = max x1 x2 in
    let by = min y1 y2 in
    let hy = max y1 y2 in
    let x = ref xi in
    let y = ref yi in
    if dx < xi then x := dx;
    if xi < gx then x := gx;
    if hy < yi then y := hy;
    if yi < by then y := by;
    let g = ri -. dist_euclidienne (xi, yi) (!x, !y) in
    if g <= 0.
    then
      somme_fiw qobj ri mi xi yi accx accy
    else begin
      let alhaij = atan2 (yi -. !y) (xi -. !x) in
      somme_fiw qobj ri mi xi yi (accx +. g *. cos alhaij) (accy +. g *. sin alhaij)
    end
  in
```


Annexe

Code 2D 08

```
let rec aux auxlp ll acc =
  match auxlp, ll with
  | p::qp, l::ql ->
    let alpha0 = 0. -. p.direction +.
      atan2 (snd p.pos_voulue -. snd p.position) (fst p.pos_voulue -. fst p.position) in
    let alpha_des = p.direction +. new_orient 1 dmax alpha0 in
    let (vix, viy) = p.allure *. (cos p.direction), p.allure *. (sin p.direction) in
    let tmp = raytracing_vecteur
      alpha_des
      (fst p.position)
      (snd p.position)
      p.rayon
      (sqrt (maxX *. maxX +. maxY *. maxY))
      completobj in
    let dh = dist_euclidienne p.position (snd tmp) in
    let v_des = min p.allure_voulue (dh /. dt) in
    let (vx_des, vy_des) = (v_des *. cos alpha_des, v_des *. sin alpha_des) in
    let (afijx, afijy) = somme_fij lp p.rayon p.masse p.position acc 0 0. 0. in
    let (afiwX, afiwy) = somme_fiw obj p.rayon p.masse (fst p.position) (snd p.position) 0. 0. in
    let vx = vix +. (vx_des -. vix) *. 0.5 +. afijx +. afiwX in
    let vy = viy +. (vy_des -. viy) *. 0.5 +. afijy +. afiwy in
    let new_allure = sqrt (vx *. vx +. vy *. vy) in
    set_allure p (new_allure);
    set_dir p (atan2 vy vx);
    aux qp ql (acc+1)
  | _, _ -> () in
aux lp ll 0
```


Annexe

Code 2D 09

```
let rec detection_pt_physique (lpeople : people list) (obj : ((float*float)*(float*float)) list)
    : (float * (float * float) * float) list list =
  (*lpeople : liste des humains presents
  obj : tableau contenant les objets qu'il y a sur le terrain*)
  match lpeople with
  | [] -> []
  | p::q ->
    let orient_ray = ref 0. in
    let pt_vu = ref [] in
    moveto (int_of_float(fst p.position *. prop)) (int_of_float(snd p.position *. prop));
    set_color (rgb 150 25 25);
    for _ = 0 to 255 do
      let r1 = random_diff0 1. in
      let r2 = Random.float 1. in
      let z = (sqrt((-2.) *. log(r1)) /. 3.899) *. cos(2. *. pi *. r2) /. 1.348172 in
      orient_ray := asin (z);
      set_color (rgb 150 25 25);
      (match raytracing_vecteur (p.direction +. !orient_ray) (fst p.position) (snd p.position) p.rayon dmax obj with
      | Some (_,x,y) ->
          let dist = dist_euclidienne (x,y) p.position in
          pt_vu := (dist, (x,y), !orient_ray) :: !pt_vu
      | None,_ -> ());
      (match raytracing_vecteur (p.direction -. !orient_ray) (fst p.position) (snd p.position) p.rayon dmax obj with
      | Some (_,x,y) ->
          let dist = dist_euclidienne (x, y) p.position in
          pt_vu := (dist, (x,y), 0. -. !orient_ray) :: !pt_vu
      | None,_ -> ());
    done;
    !pt_vu :: (detection_pt_physique q obj)
```

Annexe

Code 2D 10

```
let randomarray n max =
  if max < n then failwith "max < array length";
  let rep = Array.make n (-1) in
  for i = 0 to n-1 do
    let tmp = ref (Random.int max) in
    while Array.exists (fun i -> i = !tmp) rep do
      tmp := Random.int max
    done;
    rep.(i) <- !tmp
  done;
  rep

let test_prog () =
  Random.init 90;
  let pause = 1000 in
  let nbboucle = ref 0 in

  open_graph (Printf.sprintf " %dx%d" (prop_i*maxX_i) (prop_i*maxY_i));
  set_window_title "Deplacement test";
  set_color (rgb 0 0 0);
  fill_rect 0 0 (maxX_i*prop_i) (maxY_i*prop_i);
  set_color (rgb 255 255 255);
```

Annexe

Code 2D 11

```
let n = ref 90 in
let tab = randomarray !n (maxY_i * maxY_i) in
let ltest = ref (List.init !n (fun i -> people_init 0.579 0.33 70.
  0. (float_of_int (tab.(i)/maxY_i) +. 0.5, float_of_int (tab.(i) mod maxY_i) +. 0.5)
  1. (maxX -. 1.5, maxY /. 2.) (Random.float (2. *. pi)))) in
let lcouleur = ref (List.init !n (fun i ->
  let c = float_of_int (tab.(i)) /. float_of_int (maxY_i * maxY_i) in
  rgb (r c) (g c) (b c))) in

let obj = [((-1., Float.neg_infinity), (0., Float.infinity));
  ((maxX, Float.neg_infinity), (maxX+.1., Float.infinity));
  ((Float.neg_infinity, -1.), (Float.infinity, 0.));
  ((Float.neg_infinity, maxY), (Float.infinity, maxY+.1.));
  (((maxX -. 2.), 0.), ((maxX -. 1.), (maxY /. 2.) -. 0.5));
  (((maxX -. 2.), (maxY /. 2.) +. 0.5), ((maxX -. 1.), maxY));] in

let people_block = ref [] in
```

Annexe

Code 2D 12

```
while !n > 0 && !nbboucle < pause do
  let time = Sys.time() in
  set_color (rgb 250 250 250);
  fill_rect 0 0 (maxX_i*prop_i) (maxY_i*prop_i);
  set_color (rgb 0 0 0);
  moveto 0 0;
  draw_string (Printf.sprintf "time %f s" (float_of_int (!nbboucle) *. dt));

  let tmp = rm !ltest !lcouleur in
  ltest := fst (fst tmp);
  lcouleur := snd (fst tmp);
  n := snd tmp;

  people_block := set_pos !ltest dt; (*O(n)*)

  print_people !ltest !lcouleur; (*O(n)*)
  print_obj obj; (*O(m)*)

  let lo = detection_pt_physique !ltest (!people_block @ obj) in (*O(n*510*(4n+m)*)
  changement_direction_allure !ltest lo obj (!people_block @ obj); (*O(n*(4n+m+n+m)*)
  nbboucle := !nbboucle +1;
  while Sys.time () < time +. (dt *. 1.) do () done;
done;
while true do () done;
close_graph ()
```