HW3SDS

Bailey Brady, Andrew Chen, Cristian Sigala, Cherry Sun

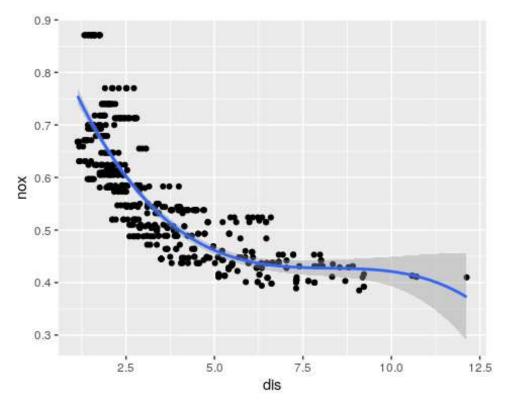
4/11/2021

Question 9 Secttion 7.9

```
rm(list = ls())
library(MASS)
##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
       select
library(boot)
library(gridExtra)
##
## Attaching package: 'gridExtra'
## The following object is masked from 'package:randomForest':
##
##
       combine
## The following object is masked from 'package:dplyr':
##
##
       combine
data("Boston")
attach(Boston)
cubic <- lm(nox~poly(dis,3), data = Boston)</pre>
summary(cubic)
##
## Call:
## lm(formula = nox ~ poly(dis, 3), data = Boston)
##
## Residuals:
                    1Q
                           Median
                                         3Q
                                                   Max
## -0.121130 -0.040619 -0.009738 0.023385 0.194904
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
```

```
## (Intercept) 0.554695 0.002759 201.021 < 2e-16 ***
## poly(dis, 3)1 -2.003096 0.062071 -32.271 < 2e-16 ***
## poly(dis, 3)2 0.856330 0.062071 13.796 < 2e-16 ***
## poly(dis, 3)3 -0.318049 0.062071 -5.124 4.27e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.06207 on 502 degrees of freedom
## Multiple R-squared: 0.7148, Adjusted R-squared: 0.7131
## F-statistic: 419.3 on 3 and 502 DF, p-value: < 2.2e-16

ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method = "lm", formula = y~poly(x,3))</pre>
```



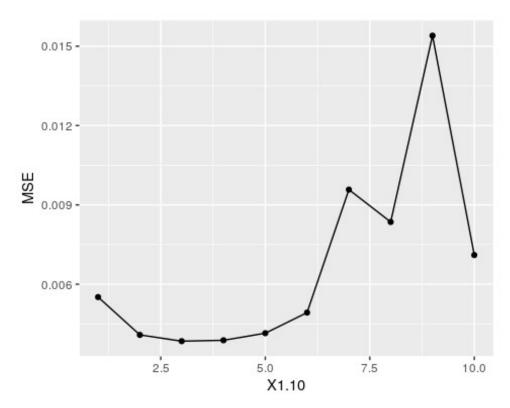
```
set.seed(1000)

residuallist = rep(NA,10)
for (i in 1:10) {
   cubic <- lm(nox~poly(dis,i), data = Boston)
     residuallist[i] = sum(cubic$residuals^2)
}

residuallist
## [1] 2.768563 2.035262 1.934107 1.932981 1.915290 1.878257 1.849484
1.835630
## [9] 1.833331 1.832171</pre>
```

```
a <- ggplot(Boston, aes(dis,nox)) + geom point()+ stat smooth(method = "lm",
formula = y \sim poly(x,1))
b <- ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method = "lm",</pre>
formula = y \sim poly(x,2))
c <- ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method = "lm",</pre>
formula = y \sim poly(x,3))
d <- ggplot(Boston, aes(dis,nox)) + geom point()+ stat smooth(method = "lm",</pre>
formula = y \sim poly(x,4))
e <-ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method = "lm",
formula = y \sim poly(x,5))
f<-ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method = "lm",</pre>
formula = y \sim poly(x,6))
g<-ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method = "lm",</pre>
formula = y \sim poly(x,7))
h<-ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method = "lm",
formula = y \sim poly(x, 8))
i<-ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method = "lm",</pre>
formula = y \sim poly(x,9))
j<-ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method = "lm",</pre>
formula = y \sim poly(x, 10)
grid.arrange(a,b,c,d,e,f,g,h,i,j, ncol = 3)
 O.7 - 0.5 - 0.3 -
                                                Nox
        2.5 5.0 7.510.012.5
                                                       2.5 5.0 7.510.012.5
                               2.5 5.0 7.510.012.5
             dis
                                     dis
                                                            dis
                                                  0.8
                                                NOX
                                                  0.4 -
                                                       2.5 5.0 7.510.012.5
        2.5 5.0 7.510.012.5
                               2.5 5.0 7.510.012.5
             dis
                                    dis
                                                            dis
                                                  0.75
                                                NO.
                                                  0.50
                                                  0.25 -
        2.5 5.0 7.510.012.5
                               2.5 5.0 7.510.012.5
                                                        2.5 5.0 7.510.012.5
             dis
                                     dis
                                                             dis
   0.5
   0.0 -
        2.5 5.0 7.510.012.5
             dis
set.seed(1000)
MSE \leftarrow rep(NA, 10)
for (i in 1:10) {
cubic <- glm(nox~poly(dis,i), data = Boston)
```

```
MSE[i] <- cv.glm(Boston, cubic, K = 10)$delta[2]
}
cv.plot <- data.frame(1:10,MSE)
ggplot(cv.plot, aes(X1.10,MSE))+geom_point()+geom_line()</pre>
```



```
which.min(MSE)
## [1] 3
```

The model with degree 3 on the polynomial has the smallest MSE so it is most optimal one.

```
library(splines)
quantile(dis)

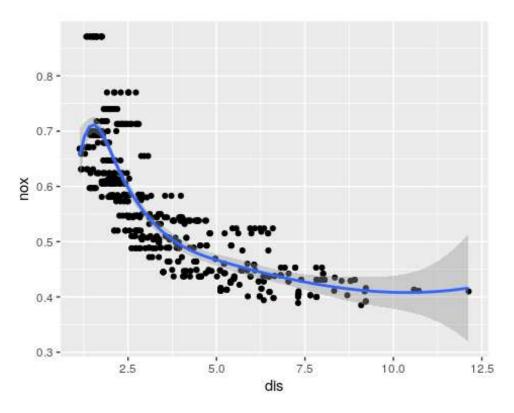
## 0% 25% 50% 75% 100%
## 1.129600 2.100175 3.207450 5.188425 12.126500
```

The 25th 50th and 75th qunatiles of dis is used for the knots

```
splinemodel <- lm(nox~bs(dis, df = 4, knots=c(2.100175,3.20745,5.188425)))
summary(splinemodel)

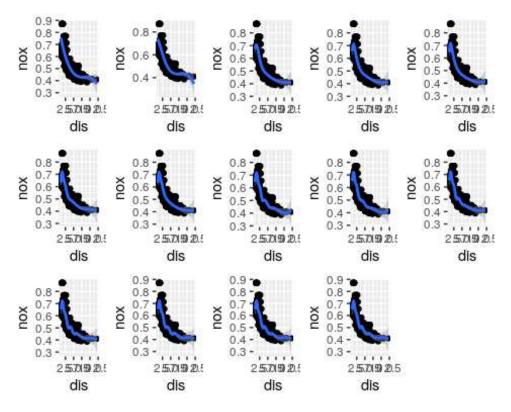
##
## Call:
## lm(formula = nox ~ bs(dis, df = 4, knots = c(2.100175, 3.20745,
## 5.188425)))
##
## Residuals:</pre>
```

```
Min 1Q
                         Median
                                       30
                                                Max
## -0.128538 -0.037813 -0.009987 0.022644 0.195494
##
## Coefficients:
                                                           Estimate Std.
##
Error
## (Intercept)
                                                            0.65622
0.02370
## bs(dis, df = 4, knots = c(2.100175, 3.20745, 5.188425))1 0.10222
0.03516
## bs(dis, df = 4, knots = c(2.100175, 3.20745, 5.188425))2 - 0.02963
0.02338
## bs(dis, df = 4, knots = c(2.100175, 3.20745, 5.188425))3 - 0.15959
0.02791
## bs(dis, df = 4, knots = c(2.100175, 3.20745, 5.188425))4 - 0.22815
0.03324
## bs(dis, df = 4, knots = c(2.100175, 3.20745, 5.188425))5 - 0.26272
0.04930
## bs(dis, df = 4, knots = c(2.100175, 3.20745, 5.188425))6 - 0.24002
0.05434
##
                                                           t value Pr(>|t|)
                                                            27.689 < 2e-16
## (Intercept)
***
## bs(dis, df = 4, knots = c(2.100175, 3.20745, 5.188425))1
                                                            2.907
                                                                    0.00381
**
## bs(dis, df = 4, knots = c(2.100175, 3.20745, 5.188425))2 -1.267 0.20571
## bs(dis, df = 4, knots = c(2.100175, 3.20745, 5.188425))3 -5.718 1.86e-08
***
## bs(dis, df = 4, knots = c(2.100175, 3.20745, 5.188425))4 -6.864 1.99e-11
## bs(dis, df = 4, knots = c(2.100175, 3.20745, 5.188425))5 -5.329 1.50e-07
## bs(dis, df = 4, knots = c(2.100175, 3.20745, 5.188425))6 -4.417 1.23e-05
***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.06062 on 499 degrees of freedom
## Multiple R-squared: 0.7295, Adjusted R-squared: 0.7263
## F-statistic: 224.3 on 6 and 499 DF, p-value: < 2.2e-16
ggplot(Boston, aes(dis,nox))+geom_point()+stat_smooth(method = "lm", formula
= y \sim bs(x,4,knots=c(2.100175,3.20745,5.188425)))
```



```
set.seed(1000)
residuals = rep(NA, 16)
for (i in 3:16) {
  splinemodel \leftarrow lm(nox \sim bs(dis, df = i), data = Boston)
  residuals[i] <- sum(splinemodel$residuals^2)</pre>
}
plot1 = ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method =
"lm", formula = y \sim bs(x, df = 3))
plot2 = ggplot(Boston, aes(dis,nox)) + geom point()+ stat smooth(method =
"lm", formula = y \sim bs(x, df = 4))
plot3 = ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method =
"lm", formula = y \sim bs(x, df = 5))
plot4 = ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method =
"lm", formula = y \sim bs(x, df = 6))
plot5 = ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method =
"lm", formula = y \sim bs(x, df = 7))
plot6 = ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method =
"lm", formula = y \sim bs(x, df = 8))
plot7 = ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method =
"lm", formula = y \sim bs(x, df = 9))
plot8 = ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method =
"lm", formula = y \sim bs(x, df = 10))
plot9 = ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method =
"lm", formula = y \sim bs(x, df = 11))
plot10 = ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method =
```

```
"lm", formula = y~bs(x, df = 12))
plot11 = ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method =
"lm", formula = y~bs(x, df = 13))
plot12 = ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method =
"lm", formula = y~bs(x, df = 14))
plot13 = ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method =
"lm", formula = y~bs(x, df = 15))
plot14 = ggplot(Boston, aes(dis,nox)) + geom_point()+ stat_smooth(method =
"lm", formula = y~bs(x, df = 16))
grid.arrange(plot1,plot2,plot3,plot4,plot5,plot6,plot7,plot8,plot9,plot10,plot11,plot12,plot13,plot14, ncol = 5)
```

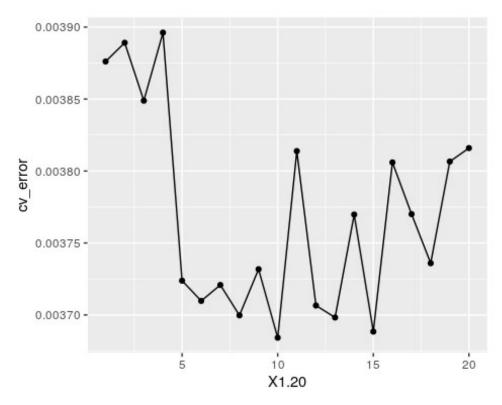


```
residuals
## [1] NA NA 1.934107 1.922775 1.840173 1.833966 1.829884
1.816995
## [9] 1.825653 1.792535 1.796992 1.788999 1.782350 1.781838 1.782798
1.783546
```

Th resulting RSS's are pretty close together with 1.93 at degree one being the biggest and 1.781 being the smallest at degree 14

```
set.seed(1000)
cv_error <- rep(0,20)
for (i in 1:20){
  splinemodel <- glm(nox~bs(dis, df = i), data = Boston)</pre>
```

```
cv_error[i] <- cv.glm(Boston, splinemodel, K = 10)$delta[1]</pre>
cv.plot2 <- data.frame(1:20,cv_error)</pre>
cv.plot2
##
      X1.20
               cv_error
## 1
          1 0.003876104
## 2
          2 0.003889102
          3 0.003848859
## 3
## 4
          4 0.003896136
## 5
          5 0.003723802
## 6
          6 0.003709755
## 7
          7 0.003720826
## 8
          8 0.003699725
## 9
          9 0.003731784
## 10
         10 0.003684162
## 11
         11 0.003813839
## 12
         12 0.003706551
## 13
         13 0.003698232
## 14
         14 0.003769753
## 15
         15 0.003688437
## 16
         16 0.003805985
## 17
         17 0.003770049
## 18
         18 0.003735931
## 19
         19 0.003806571
## 20
         20 0.003815923
ggplot(cv.plot2, aes(X1.20,cv_error))+geom_point()+geom_line()
```



```
which.min(cv_error)
## [1] 10
```

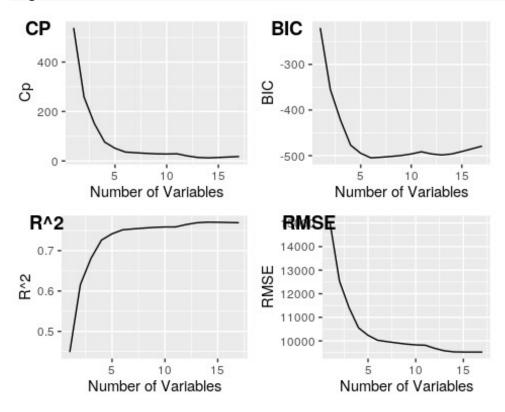
The best degree to use is 10 degrees of freedom. It has the lowest error.

detach(Boston)

Question 10 in Section 7.9

```
set.seed(1)
data <- College
n <- length(data$Outstate)
train <- sample(n, n/2)
trainset <- College[train, ]
testset <- College[-train, ]
lm <- regsubsets(Outstate ~ ., data = trainset, nvmax = 17, method =
"forward")
lm.summary <- summary(lm)

cp <- data.frame(cp =lm.summary$cp, y=1:17)
bic <- data.frame(bic =lm.summary$bic, y=1:17)
adjr2 <- data.frame(adjr2 =lm.summary$adjr2, y=1:17)
RMSE <- data.frame(RMSE = sqrt(lm.summary$rss/17), y=1:17)</pre>
var1 <- ggplot(cp,aes(x=y, y=cp))+xlab("Number of Variables") + ylab("Cp") +</pre>
```



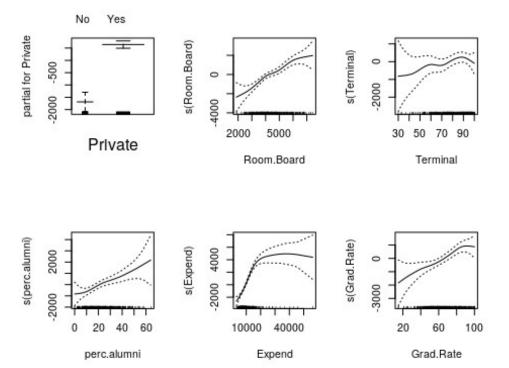
```
which.min(lm.summary$bic)
## [1] 6

coef <- coef(lm, id = 6)
names(coef)
## [1] "(Intercept)" "PrivateYes" "Room.Board" "Terminal" "perc.alumni"
## [6] "Expend" "Grad.Rate"</pre>
```

While looking at the different plots, we can tell that the BIC model is the best to fit the data because it has the least variance with the lowest amount of variables affecting the fit. After conducting coef tests on the BIC model, we find the variables are "Private", "Room.Board", "Terminal", "perc.alumni", "Expend", and "Grad.Rate" that interact with the "outstate" variable.

```
gamlm <- gam(Outstate ~ Private + s(Room.Board) + s(Terminal) +
    s(perc.alumni) + s(Expend) + s(Grad.Rate), data = trainset)

par(mfrow = c(2, 3))
plot(gamlm, se = T)</pre>
```



After plotting our

gam model, we can see the data is more on a exponential type of curve rather than linear. All the variables are able to explain out of state tuition but Room.Board has the least variance and the straightest line making the relationship almost direct between the two. Terminal and perc.alumni on the other hand has large variance at the ends so although the model fits, it is not the best variable to find a relationship with out of state tuition.

```
Predi <- predict(gamlm, testset)
RSS <- sum((Predi-testset$Outstate)^2)
TSS <- sum((testset$Outstate - mean(testset$Outstate))^2)
RS2_Test <- 1- (RSS/TSS)
RS2_Test
## [1] 0.7656864</pre>
```

```
Predi2 <- predict(gamlm, trainset)
RSS <- sum((Predi2-trainset$Outstate)^2)
TSS <- sum((trainset$Outstate - mean(trainset$Outstate))^2)
RS2_Train <- 1- (RSS/TSS)

RS2_Train
## [1] 0.8049801</pre>
```

After calculating the r^2 value of the train and test set, we find out that both are good fits for the data. However, when comparing the two we find the train set has a greater fit than the test which is expected.

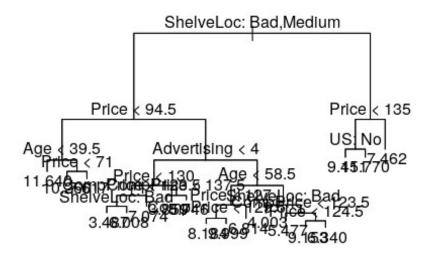
```
summary(gamlm)
##
## Call: gam(formula = Outstate ~ Private + s(Room.Board) + s(Terminal) +
       s(perc.alumni) + s(Expend) + s(Grad.Rate), data = trainset)
## Deviance Residuals:
       Min
                      Median
##
                  10
                                    30
                                            Max
## -7128.62 -1133.86
                       -74.25
                              1231.50 7369.50
##
## (Dispersion Parameter for gaussian family taken to be 3724586)
##
       Null Deviance: 6989966760 on 387 degrees of freedom
## Residual Deviance: 1363197370 on 365.9997 degrees of freedom
## AIC: 6995.069
##
## Number of Local Scoring Iterations: NA
##
## Anova for Parametric Effects
##
                  Df
                                   Mean Sq F value
                         Sum Sa
                                                       Pr(>F)
## Private
                   1 1764398916 1764398916 473.717 < 2.2e-16 ***
                   1 1616561254 1616561254 434.024 < 2.2e-16 ***
## s(Room.Board)
## s(Terminal)
                   1 287918343 287918343 77.302 < 2.2e-16 ***
## s(perc.alumni)
                   1 354690429 354690429 95.230 < 2.2e-16 ***
                      601731164 601731164 161.556 < 2.2e-16 ***
## s(Expend)
                    1
## s(Grad.Rate)
                                   90312393 24.248 1.284e-06 ***
                   1
                       90312393
## Residuals
                 366 1363197370
                                   3724586
## ---
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## Anova for Nonparametric Effects
##
                 Npar Df Npar F
                                      Pr(F)
## (Intercept)
## Private
## s(Room.Board)
                       3 1.9107
                                     0.1274
## s(Terminal)
                       3 1.4636
                                     0.2241
## s(perc.alumni)
                      3 0.3498
                                     0.7893
               3 26.1184 2.442e-15 ***
## s(Expend)
```

```
## s(Grad.Rate) 3 0.9075 0.4375
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

When looking at our anova nonperametric effects, we see that only the expend variable is significant in explaining out of state tuition with a nonlinear relationship. Although the rest of the variables have some effect it is not enough to be significant.

Section 8.4 Question 8

```
set.seed(1)
train = sample(1:nrow(Carseats), nrow(Carseats)/2)
Cartrain <- Carseats[train, ]</pre>
Cartest <- Carseats[-train, ]</pre>
tree.carseats <- tree(Sales ~ ., data = Cartrain)</pre>
summary(tree.carseats)
##
## Regression tree:
## tree(formula = Sales ~ ., data = Cartrain)
## Variables actually used in tree construction:
## [1] "ShelveLoc"
                                    "Age"
                                                  "Advertising" "CompPrice"
## [6] "US"
## Number of terminal nodes: 18
## Residual mean deviance: 2.167 = 394.3 / 182
## Distribution of residuals:
       Min.
             1st Qu.
##
                       Median
                                   Mean 3rd Qu.
                                                     Max.
## -3.88200 -0.88200 -0.08712 0.00000 0.89590 4.09900
plot(tree.carseats)
text(tree.carseats, pretty = 0)
```



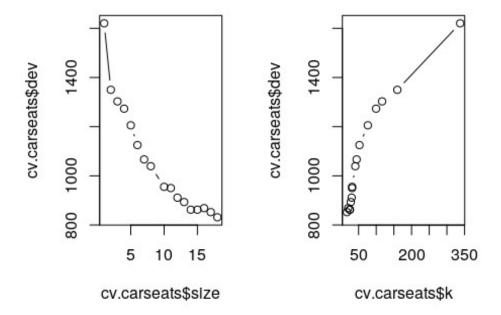
```
predicty <- predict(tree.carseats, newdata = Cartest)
mean((predicty - Cartest$Sales)^2)

## [1] 4.922039

We get a MSE of 4.922.

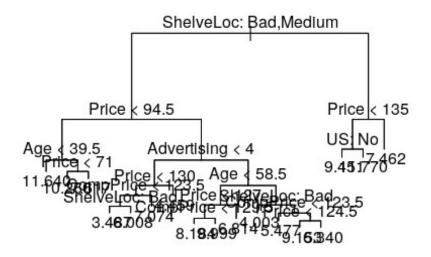
cv.carseats = cv.tree(tree.carseats)

par(mfrow = c(1,2))
plot(cv.carseats$size, cv.carseats$dev, type="b")
plot(cv.carseats$k, cv.carseats$dev, type="b")</pre>
```



```
par(mfrow = c(1,1))

prune.carseats <- prune.tree(tree.carseats, best = 17)
plot(prune.carseats)
text(prune.carseats, pretty = 0)</pre>
```



```
predicty <- predict(prune.carseats, newdata = Cartest)
mean((predicty - Cartest$Sales)^2)
## [1] 4.827162</pre>
```

We get a MSE of 4.827. In this case pruning the tree improved the MSE by about 0.1.

```
bagcarseats <- randomForest(Sales ~ ., data = Cartrain, mtry = 10, importance</pre>
= TRUE)
y.bag <- predict(bagcarseats, newdata = Cartest)</pre>
mean((y.bag - Cartest$Sales)^2)
## [1] 2.657296
importance(bagcarseats)
##
                   %IncMSE IncNodePurity
## CompPrice
               23.07909904
                               171.185734
## Income
                2.82081527
                                94.079825
## Advertising 11.43295625
                                99.098941
## Population -3.92119532
                                59.818905
## Price
               54.24314632
                               505.887016
## ShelveLoc
               46.26912996
                               361.962753
## Age
               14.24992212
                               159.740422
## Education
               -0.07662320
                                46.738585
## Urban
                0.08530119
                                 8.453749
## US
                4.34349223
                                15.157608
```

The MSE found is 2.62.

We see that Price and ShelveLoc are the most important and followed by CompPrice.

```
rfcarseats <- randomForest(Sales ~ ., data = Cartrain, mtry = 3, importance =
TRUE)
y.rf <- predict(rfcarseats, newdata = Cartest)</pre>
mean((y.rf - Cartest$Sales)^2)
## [1] 3.049406
importance(rfcarseats)
##
                  %IncMSE IncNodePurity
## CompPrice
               12.9489323
                              158.48521
## Income
                2.2754686
                              129.59400
## Advertising 8.9977589
                              111.94374
## Population -2.2513981
                              102.84599
## Price
               33.4226950
                              391.60804
                              290.56502
## ShelveLoc
               34.0233545
## Age
               12.2185108
                              171.83302
## Education
                0.2592124
                               71.65413
## Urban
                1.1382113
                               14.76798
## US
                4.1925335
                               33.75554
```

The MSE found is 3.00.

We see that Price and ShelveLoc are the most important again and CompPrice and Age are followed after.

Question 10 in Section 8.4

```
Hitters <- Hitters
Hitters = na.omit(Hitters)
Hitters$Salary = log(Hitters$Salary)
Hitters$League <- as.factor(Hitters$League)</pre>
Hitters$Division <- as.factor(Hitters$Division)</pre>
Hitters$NewLeague <- as.factor(Hitters$NewLeague)</pre>
head(Hitters)
##
                     AtBat Hits HmRun Runs RBI Walks Years CAtBat CHits
CHmRun
## -Alan Ashby
                                            38
                                                   39
                       315
                             81
                                     7
                                         24
                                                         14
                                                               3449
                                                                      835
69
## -Alvin Davis
                       479 130
                                         66 72
                                                               1624
                                                                      457
                                    18
                                                   76
                                                          3
63
                                         65
## -Andre Dawson
                       496 141
                                    20
                                            78
                                                   37
                                                         11
                                                               5628 1575
225
## -Andres Galarraga
                             87
                                         39 42
                                                   30
                                                          2
                                                                396
                                                                      101
                       321
                                    10
12
## -Alfredo Griffin
                                                         11
                       594 169
                                    4
                                         74 51
                                                   35
                                                               4408 1133
```

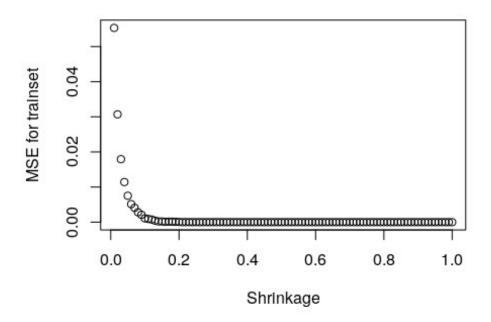
```
19
                                                       21
                                                                    214
                                                                            42
## -Al Newman
                         185
                                37
                                       1
                                            23
                                                 8
                                                               2
1
##
                       CRuns CRBI CWalks League Division PutOuts Assists Errors
## -Alan Ashby
                         321
                              414
                                      375
                                                Ν
                                                          W
                                                                 632
                                                                           43
                                                                                   10
## -Alvin Davis
                               266
                                                                 880
                                                                           82
                                                                                   14
                         224
                                      263
                                                Α
                                                          W
## -Andre Dawson
                         828
                              838
                                      354
                                                Ν
                                                          Ε
                                                                 200
                                                                           11
                                                                                    3
## -Andres Galarraga
                                                          Ε
                                                                 805
                                                                           40
                                                                                   4
                          48
                               46
                                       33
                                                Ν
## -Alfredo Griffin
                                                                                   25
                         501
                               336
                                      194
                                                                 282
                                                                          421
                                                Α
                                                          W
## -Al Newman
                                                                                    7
                          30
                                 9
                                       24
                                                Ν
                                                          Ε
                                                                  76
                                                                          127
##
                         Salary NewLeague
                       6.163315
## -Alan Ashby
## -Alvin Davis
                       6.173786
                                          Α
## -Andre Dawson
                       6.214608
                                          Ν
## -Andres Galarraga 4.516339
                                          N
## -Alfredo Griffin
                      6.620073
                                          Α
## -Al Newman
                       4.248495
train_set <- Hitters[1:200,]</pre>
dim(train_set)
## [1] 200 20
head(train_set)
                       AtBat Hits HmRun Runs RBI Walks Years CAtBat CHits
##
CHmRun
## -Alan Ashby
                         315
                                81
                                       7
                                            24
                                                38
                                                       39
                                                              14
                                                                   3449
                                                                           835
69
## -Alvin Davis
                         479
                               130
                                      18
                                                72
                                                                   1624
                                                                           457
                                            66
                                                       76
                                                               3
63
## -Andre Dawson
                         496
                               141
                                      20
                                            65
                                                78
                                                       37
                                                              11
                                                                   5628
                                                                          1575
225
## -Andres Galarraga
                                87
                                            39
                                                42
                                                       30
                                                               2
                                                                    396
                                                                           101
                         321
                                      10
12
## -Alfredo Griffin
                         594
                               169
                                       4
                                            74
                                                51
                                                       35
                                                              11
                                                                   4408
                                                                          1133
19
## -Al Newman
                         185
                                37
                                       1
                                            23
                                                 8
                                                       21
                                                               2
                                                                    214
                                                                            42
1
##
                       CRuns CRBI CWalks League Division PutOuts Assists Errors
## -Alan Ashby
                              414
                                                N
                                                                           43
                                                                                   10
                         321
                                      375
                                                          W
                                                                 632
## -Alvin Davis
                         224
                               266
                                      263
                                                Α
                                                          W
                                                                 880
                                                                           82
                                                                                   14
## -Andre Dawson
                         828
                              838
                                      354
                                                Ν
                                                          Ε
                                                                 200
                                                                           11
                                                                                    3
                                                          Ε
                                                                 805
                                                                           40
                                                                                   4
## -Andres Galarraga
                          48
                                46
                                       33
                                                Ν
## -Alfredo Griffin
                         501
                               336
                                      194
                                                Α
                                                                 282
                                                                          421
                                                                                   25
                                                          W
## -Al Newman
                          30
                                 9
                                       24
                                                Ν
                                                          Ε
                                                                  76
                                                                          127
                                                                                    7
##
                         Salary NewLeague
## -Alan Ashby
                       6.163315
                                          Ν
## -Alvin Davis
                       6.173786
                                          Α
## -Andre Dawson
                                          N
                       6.214608
## -Andres Galarraga 4.516339
                                          Ν
```

```
## -Alfredo Griffin 6.620073
                                         Α
## -Al Newman
                      4.248495
test_set <- Hitters[-(1:200),]
dim(test set)
## [1] 63 20
head(test set)
                     AtBat Hits HmRun Runs RBI Walks Years CAtBat CHits CHmRun
##
                             101
                                          65
                                              58
                                                     92
                                                           20
                                                                 9528
                                                                       2510
                                                                                548
## -Reggie Jackson
                       419
                                     18
## -Ron Kittle
                        376
                              82
                                     21
                                          42
                                              60
                                                     35
                                                            5
                                                                 1770
                                                                        408
                                                                                115
                                              76
## -Ray Knight
                       486
                             145
                                     11
                                          51
                                                     40
                                                           11
                                                                 3967
                                                                       1102
                                                                                 67
## -Rick Leach
                        246
                              76
                                      5
                                          35
                                              39
                                                     13
                                                                  912
                                                                         234
                                                                                 12
                                                            6
                                              27
                        205
                              52
                                      8
                                          31
                                                     17
                                                           12
                                                                 5134
                                                                       1323
                                                                                 56
## -Rick Manning
## -Rance Mulliniks
                        348
                              90
                                     11
                                          50
                                              45
                                                     43
                                                           10
                                                                 2288
                                                                         614
                                                                                 43
##
                     CRuns CRBI CWalks League Division PutOuts Assists Errors
## -Reggie Jackson
                      1509 1659
                                    1342
                                              Α
                                                        W
                                                                 0
                                                                          0
                                                                                 0
## -Ron Kittle
                        238
                             299
                                     157
                                              Α
                                                        W
                                                                 0
                                                                          0
                                                                                 0
                                                        Ε
## -Ray Knight
                       410
                            497
                                     284
                                              N
                                                                88
                                                                        204
                                                                                16
                                      80
                                                        Ε
## -Rick Leach
                       102
                              96
                                              Α
                                                                44
                                                                          0
                                                                                 1
                                                        Ε
                                                                          3
                                                                                 2
## -Rick Manning
                       643
                            445
                                     459
                                              Α
                                                               155
                                                        Ε
## -Rance Mulliniks
                       295
                             273
                                     269
                                              Α
                                                                60
                                                                       176
                                                                                 6
##
                       Salary NewLeague
## -Reggie Jackson
                     6.189290
## -Ron Kittle
                     6.052089
                                        Α
## -Ray Knight
                     6.214608
                                        Α
## -Rick Leach
                     5.521461
                                        Α
## -Rick Manning
                     5.991465
                                        Α
## -Rance Mulliniks 6.109248
                                        Α
```

shows 200, which means that training set consist of first 200 observations shows 63, the rest of data are assigned to test set

```
set.seed(100)
pows \leftarrow seq(0.01, 1, by = 0.01)
range <- pows
train_error <- rep(0, length(range))</pre>
for (i in 1: length(range)){
  my_boost <- gbm(Salary~., data = train_set, distribution = "gaussian",</pre>
n.trees= 1000, interaction.depth = 5, shrinkage = range[i])
  pred <- predict(my boost, newdata = train set, n.trees = 1000)</pre>
  train error[i] <- MSE(pred, train set$Salary)</pre>
}
train_error
##
     [1] 5.531229e-02 3.070116e-02 1.793041e-02 1.141311e-02 7.515446e-03
##
     [6] 5.135847e-03 4.089155e-03 2.829888e-03 2.107375e-03 1.090970e-03
    [11] 9.143186e-04 7.527424e-04 4.438250e-04 2.107033e-04 2.084422e-04
## [16] 1.275705e-04 1.564862e-04 1.481893e-04 1.122995e-04 4.508664e-05
```

```
[21] 6.669702e-06 1.632212e-05 1.089263e-05 1.868700e-06 4.964248e-06
##
    [26] 1.141003e-06 6.565694e-07 2.394964e-06 4.514636e-08 3.121725e-07
##
    [31] 6.639143e-08 2.024619e-08 4.573450e-07 3.784828e-09 2.050641e-08
    [36] 5.068387e-08 4.006767e-09 2.628265e-09 1.003464e-09 3.465420e-09
##
    [41] 5.803472e-09 4.233554e-09 6.757971e-10 1.205403e-08 1.816530e-11
    [46] 1.157308e-09 5.552622e-11 4.077847e-09 1.506577e-10 2.791922e-10
##
    [51] 8.232659e-12 1.485731e-10 6.286405e-12 2.730091e-12 1.224742e-12
    [56] 1.205243e-12 2.151287e-13 2.859646e-12 1.600019e-13 2.264890e-13
    [61] 2.532185e-14 2.721992e-12 4.726114e-14 1.251975e-16 1.276339e-14
##
    [66] 1.387579e-15 5.746383e-14 5.599344e-17 5.966583e-17 1.391327e-15
    [71] 6.460855e-16 3.188759e-15 1.395992e-16 7.268948e-16 5.488075e-17
    [76] 1.568662e-17 6.096367e-18 1.258339e-17 1.650647e-16 1.253426e-17
##
    [81] 9.068014e-19 5.372179e-16 2.473670e-18 3.337819e-18 1.435766e-18
    [86] 3.410540e-18 2.484255e-17 2.448975e-17 1.391628e-17 1.586695e-16
    [91] 3.882708e-17 2.305812e-17 8.095739e-18 1.055980e-16 3.387161e-16
##
    [96] 3.070941e-16 1.862369e-16 1.169657e-15 7.427585e-15 3.361751e-14
plot(range, train_error, xlab = "Shrinkage", ylab = "MSE for trainset")
```



we are seeing this

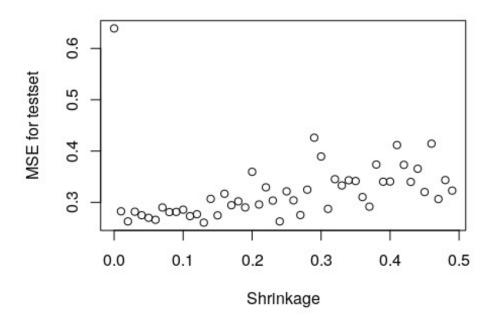
behavior on the graph because we don't have enough number of trees, we should be using a larger number for trees

```
set.seed(100)
pows <- seq(0.00001, 0.5, by = 0.01)
range <- pows
train_error <- rep(0, length(range))
for (i in 1: length(range)){
   my_boost <- gbm(Salary~., data = train_set, distribution = "gaussian",</pre>
```

```
n.trees= 1000, interaction.depth = 4, shrinkage = range[i])
  pred <- predict(my_boost, newdata = test_set, n.trees = 1000)
  train_error[i] <- MSE(pred, test_set$Salary)
}
train_error

## [1] 0.6390523 0.2825796 0.2629287 0.2818142 0.2749321 0.2699292 0.2660277
## [8] 0.2900506 0.2810656 0.2814218 0.2857974 0.2732245 0.2768972 0.2605141
## [15] 0.3068412 0.2747142 0.3168417 0.2945322 0.3020256 0.2902090 0.3595950
## [22] 0.2958914 0.3293535 0.3035305 0.2628832 0.3214829 0.3039472 0.2753221
## [29] 0.3247932 0.4260514 0.3894280 0.2873221 0.3452304 0.3330359 0.3431202
## [36] 0.3417009 0.3103887 0.2916457 0.3737698 0.3403540 0.3406864 0.4117370
## [43] 0.3731936 0.3399068 0.3656035 0.3202130 0.4144441 0.3065400 0.3435098
## [50] 0.3229746

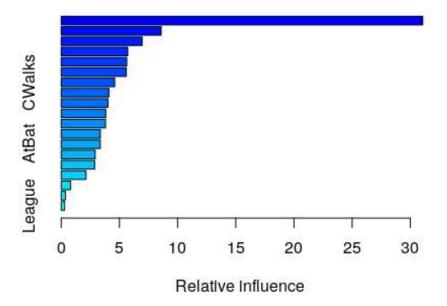
plot(range, train_error, xlab = "Shrinkage", ylab = "MSE for testset")</pre>
```



```
fit = lm(Salary ~ ., data = train_set)
pred = predict(fit, test_set)
error <- MSE(pred, test_set$Salary)
error

## [1] 0.4917959

min_test_error <- min(error)
my_boost <- gbm(Salary~., data = train_set, distribution = "gaussian",
n.trees= 1000, interaction.depth = 4, shrinkage = min_test_error)
summary(my_boost)</pre>
```



```
##
                    var
                            rel.inf
## CAtBat
                 CAtBat 31.0630258
## CRBI
                   CRBI
                         8.5887495
## PutOuts
                PutOuts
                         6.9515029
## Assists
                Assists
                         5.7110593
## Runs
                         5.6274573
                   Runs
## Walks
                  Walks
                         5.5930638
## CWalks
                 CWalks
                         4.5922161
## Years
                  Years
                         4.1059768
                         4.0195358
## CRuns
                  CRuns
## Hits
                   Hits
                         3.8284619
## CHmRun
                 CHmRun
                         3.8056729
## HmRun
                  HmRun
                         3.3645642
## AtBat
                  AtBat
                         3.3568675
## CHits
                  CHits
                         2.9192027
## RBI
                    RBI
                         2.8748625
## Errors
                 Errors
                         2.1324180
## Division
               Division
                          0.8089888
## NewLeague NewLeague
                          0.3674487
                 League
                         0.2889254
## League
train <- model.matrix(Salary~ ., data=train_set)</pre>
test <- model.matrix(Salary~., data= test_set)</pre>
fit <- glmnet(train, train_set$Salary, alpha=1)</pre>
pred <- predict(fit,s=0.1,test)</pre>
error <- MSE(pred, test_set$Salary)</pre>
error
```

```
## [1] 0.4389054
```

CatBat seems to be the most important predictors in the boosted model the MSE is lower compare to these regression methods.

```
set.seed(100)
my_bagging <- randomForest(Salary ~ ., data = train_set, mtry = 10)
pred <- predict(my_bagging, newdata = test_set)
test_error <- MSE(pred, test_set$Salary)
test_error
## [1] 0.2232362</pre>
```

This is the test MSE bagging compare to regressions gives an lower MSE