

# Lecture 4: Exploratory Data Analysis

Intro to Data Science for Public Policy, Spring 2016

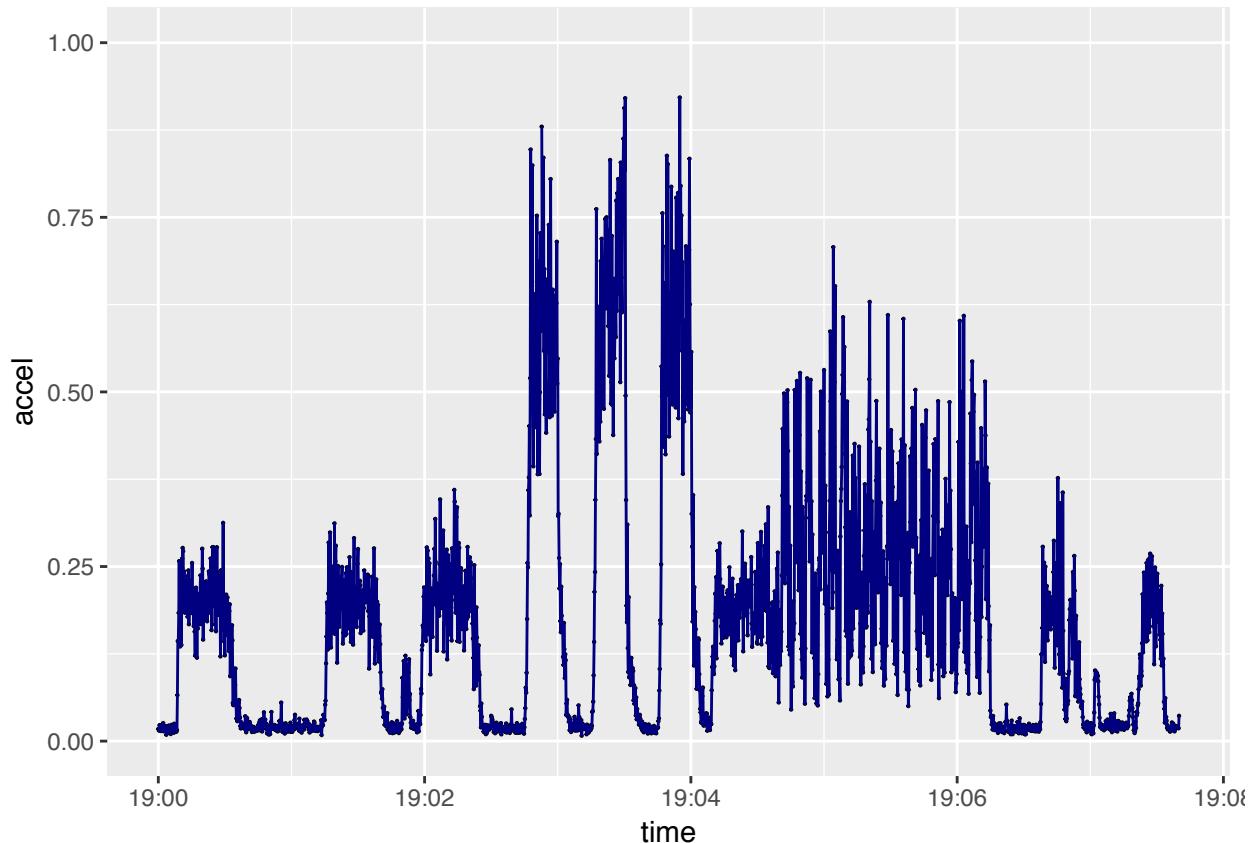
by Jeff Chen & Dan Hammer, Georgetown University McCourt School of Public Policy

## Contents

Structure . . . . .	3
Univariate data analysis . . . . .	5
Multivariate Data . . . . .	11
Assignments . . . . .	16

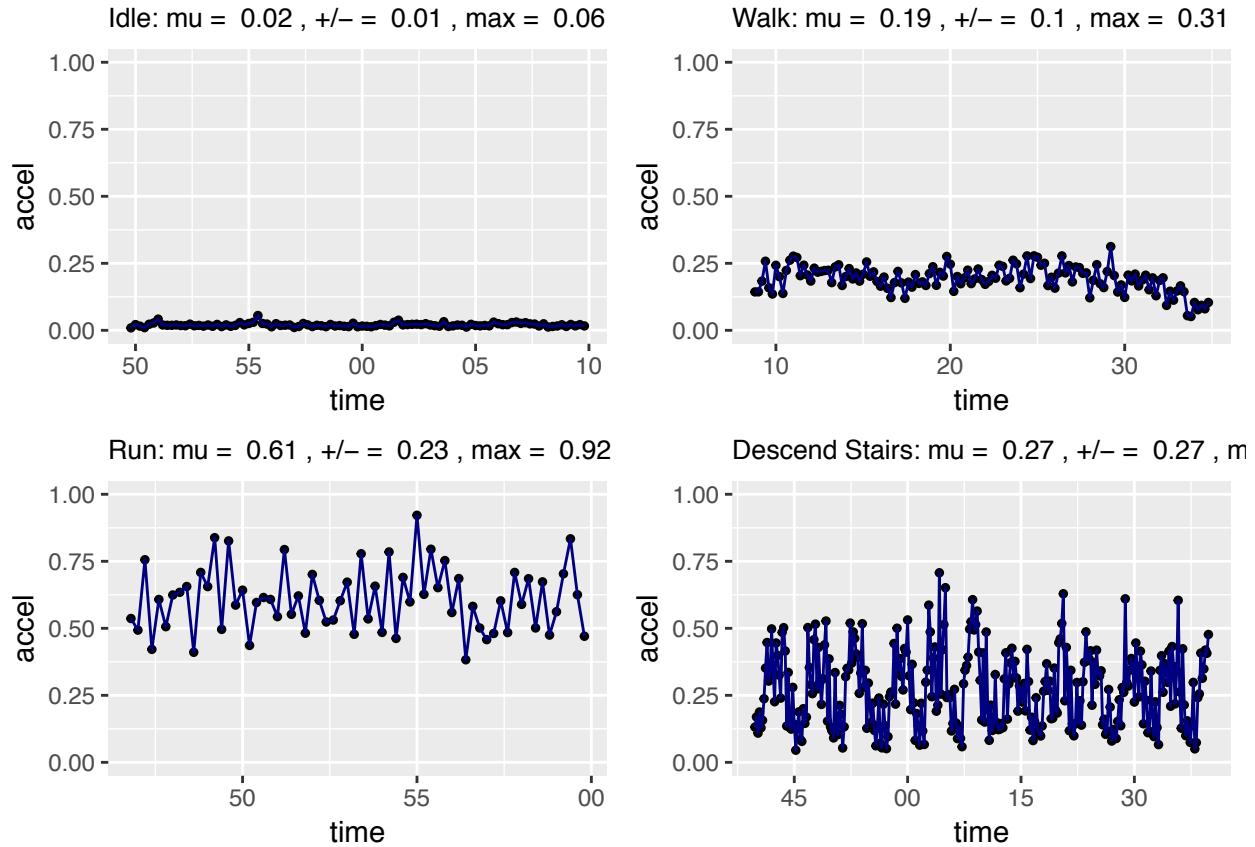
Mobile technologies have lowered the bar to using lightweight sensors that measure the physical world and have opened new applications of data in daily life. From a smart phone's accelerometer, it's possible to track distinct patterns in one's activity based on the fluctuations in acceleration ( $\frac{m}{s^2}$ ). In fact, many of these technologies have become commonly available, enabling physical fitness activity monitoring to characterizing transportation quality. Below is a set of exercise measurements from an smartphone accelerometer that lasted approximately 6.5 minutes and graphed at a frequency of 5 hertz (five readings per second).

Can you visually identify distinct patterns? What makes those patterns distinct?



Over the short time sample, the graphs indicate four distinct types of acceleration patterns. If we manually extract samples from these periods, we can quantify the patterns in terms of their central tendencies. Idle periods have near zero acceleration, walking periods have acceleration around 0.2 with tight dispersion, running periods hover around 0.6 +/- 0.2, and descending stairs vary widely. Given how these basic insights, we can experiment with various methods of *feature extraction*, or ways to distill and represent useful signal

from the raw data. We can also begin to formulate hypotheses for how to model and represent the patterns and relationships in the data.



This is the basis of *exploratory data analysis* or *EDA* – the first look at a dataset. Much of exploratory data analysis is focused on formulating hypotheses, assessing data structures, and understanding the quirks and tolerances of data in order to develop useful and insightful data-driven applications. This is achieved by using visual techniques (e.g. histograms, other graphs) to identify outliers and assess the distribution of variables as well as statistical measures help to understand central tendency among other properties of the data. A well-conducted EDA would yield critical insights into how the data can and should be processed, methods for feature extraction to represent usable signal in the data, and options for operationalizing a strategy for solving the problem at hand.

We can break EDA into a series of high-level goals, each of which is associated with analytical tasks that help piece together a clearer picture of what is contained in the data. Each of these questions can be answered through a graphical or numerical technical approach.

Goal	Common Questions
Assess the data types	- Are the data categorical, numerical, factor, strings, other? - What manipulations will you need to perform to get the data into usable shape?
Understand the empirical distributions	- Does the data fall into a commonly recognized shape? - Is it unimodal, bimodal? - Is there any indication of time-dependence?
Detect outliers, missingness and errors	- Are there anomalous values? - Do records spike or occur during odd times? - How complete is the data? - Which variables need to be standardized and cleaned?
Check the assumptions	- How exactly is the data collected? - Does the data reflect what would be expected?

Goal	Common Questions
Identify important variables	-Which variables are correlated with one another?
Formulate data-bounded hypotheses	- Which variables are most correlated?

This chapter will equip you with the skills to explore the data in an efficient and thoughtful manner. There are three considerations that underlie effective discovery: data structure, statistical measures, and graphical summaries. We begin with an overview of elements of EDA, then reinforce by walking through an example workflow.

## Structure

The structure of the data dictates the amount and type of processing required to make data usable and wieldy. Typically, data should be in matrix or tabular form – a basic requirement for data to be manipulated and analyzed. However, at times, the raw data may be in an unstructured format (e.g. raw text) or in different structured formats (e.g. satellite imagery, long form), requiring processing, reshaping and/or feature extraction so that the data is usable.

### Where to start

To start, we'll create a simulated dataset, containing five variables: sex, age, weight, program, and status.

```
num_recs <- 1200
```

```
long = expand.grid(seq(1,num_recs), c("sex","age", "weight", "program", "status"))
colnames(long) <- c("person_id", "field")
long$values <- c( round(runif(num_recs)),
                 round(rnorm(num_recs,40,10)),
                 sample(c(rep(-9999, num_recs), round(rnorm(num_recs,120,20))),num_recs),
                 rep(c("a","b"),num_recs/2),
                 rep(c("in",NA,"out"),num_recs/3))
long <- long[order(long$person_id),]

head(long, 10)
```

```
##      person_id  field values
## 1           1    sex     0
## 1201        1    age    23
## 2401        1  weight -9999
## 3601        1  program    a
## 4801        1  status    in
## 2           2    sex     0
## 1202        2    age    44
## 2402        2  weight   121
## 3602        2  program    b
## 4802        2  status   <NA>
```

Using the `str()` method (below), we can produce a structural summary of each variable in a dataset. There are a few common things to keep in mind:

- Is the data in the right *shape*? The data is ‘stacked’ or in ‘long’ form, which means that each row contains a value (**values**) that corresponds to a person-variable combination (**person\_id** and **field**). Notice that while there are numeric and character values, all variables are coded as characters. In order to analyze the data, each field should be represented in a separate column. This process is known as *reshaping* from *long* to *wide* form and is pre-requisite.
- Are there discrete variables that are coded as integers? Numeric codes often are used in order to keep the data files smaller. For example, **sex** is coded as a binary integer, but represents two values: 0 = Female, 1 = Male. In some case, it may be helpful to recode using the text value for ease of interpretation
- Are there missing values? Missing values are often coded as **NA** or a large negative number in cases where values should be non-zero positive such as -9999. This will require some cleaning to standardize values and at times imputation.
- Which variables should be numeric? At times, numeric variables will be formatted as strings and factors.

```
str(long)
```

```
## 'data.frame': 6000 obs. of 3 variables:
## $ person_id: int 1 1 1 1 2 2 2 2 ...
## $ field     : Factor w/ 5 levels "sex","age","weight",...: 1 2 3 4 5 1 2 3 4 5 ...
## $ values    : chr "0" "23" "-9999" "a" ...
## - attr(*, "out.attrs")=List of 2
##   ..$ dim      : int 1200 5
##   ..$ dimnames:List of 2
##     ...$ Var1: chr "Var1= 1" "Var1= 2" "Var1= 3" "Var1= 4" ...
##     ...$ Var2: chr "Var2=sex" "Var2=age" "Var2=weight" "Var2=program" ...
```

### Example of structural fixes

Data should be in wide form. To do so, we can rely on the **reshape()** method to create a column for each of the **field** variables.

```
head(long)
```

```
##   person_id   field values
## 1           1   sex     0
## 1201        1   age    23
## 2401        1 weight -9999
## 3601        1 program   a
## 4801        1 status    in
## 2           2   sex     0
wide <- reshape(long, idvar = c("person_id"), timevar="field", direction="wide")
head(wide)

##   person_id values.sex values.age values.weight values.program
## 1           1         0        23       -9999          a
## 2           2         0        44        121          b
## 3           3         0        36       -9999          a
## 4           4         0        35        162          b
## 5           5         1        37        110          a
## 6           6         0        36        121          b
##   values.status
## 1             in
## 2            <NA>
## 3            out
```

```

## 4           in
## 5           <NA>
## 6           out

## [1] "person_id"      "values.sex"       "values.age"       "values.weight"
## [5] "values.program"  "values.status"

#rename by removing "values."
colnames(wide) <- gsub("values.", "", colnames(wide))

## [1] "person_id" "sex"        "age"         "weight"      "program"    "status"

```

Lastly, variables should be recoded and reformatted into the appropriate format. These basic fixes help ensure the usability of the dataset.

```

#re-code sex
wide$sex[wide$sex=="1"] <- "male"
wide$sex[wide$sex=="0"] <- "female"

#Character to numeric
wide$age <- as.numeric(wide$age)
wide$weight <- as.numeric(wide$weight)

#Recode -9999 to NA
wide$weight[wide$weight== -9999] <- NA

```

## Univariate data analysis

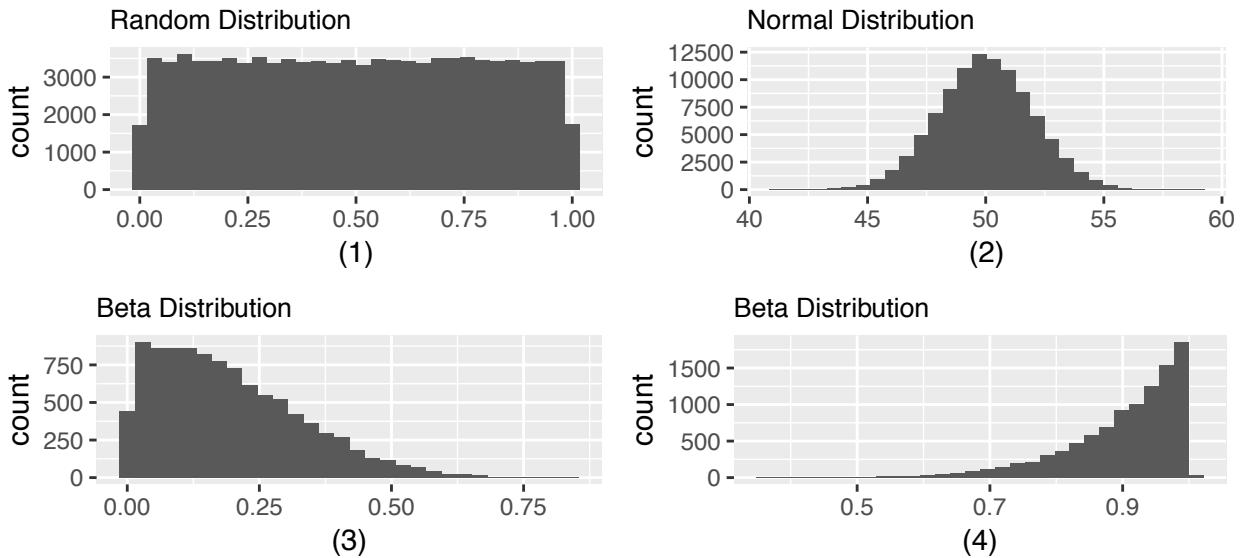
The tools and techniques used to analyze can be distinguished into univariate (concerning one data series at a time) or multivariate (concerning two or more data series at a time). To start, we will focus on univariate techniques, starting with statistics, then moving into graphical methods.

### Statistics for continuous variables

The shape and properties of a continuous variables will vary greatly. These *moments*, or common attributes of data, should influence how an analyst will treat the data. Four continuous distributions are plotted below:

- The first graph looks similar to a box, indicating that there is an equal chance that a value can take on any value between 0 and 1.
- The second graph follows a bell curve ( also known as a ‘normal distribution’ or ‘Gaussian distribution’) with a central peak and symmetrical tails.
- The third graph peaks to the left with a longer tail to the right.
- The fourth graph peaks to the right with a longer tail to the left.

While graphical techniques are useful, and are the topic of the next section in this chapter, sample statistics can concisely summarize the contents of data in a way that are insightful and comparable.



How can we quantitatively tell these variables apart? Sample statistics are particularly helpful with characterizing central tendency, spread, skewness and kurtosis.

### Central tendency

Data with any amount of signal typically tends towards a central value or location. This means that values will *peak* or *cluster* around a central point, but need not be symmetrically distributed around that central point. There are two common measures that are used to characterize central tendency: the mean and the median.

The mean, also known as the *arithmetic mean* or *average*, is simply the sum of all values in  $x$  divided by the sample size  $n$ . Since the calculation takes into account *all* values in  $x$ , means are sensitive to outliers and extreme values. Often times, the mean is the main statistic used to describe what is typical of a sample or population as it is considered to be the *expected value*. For example:

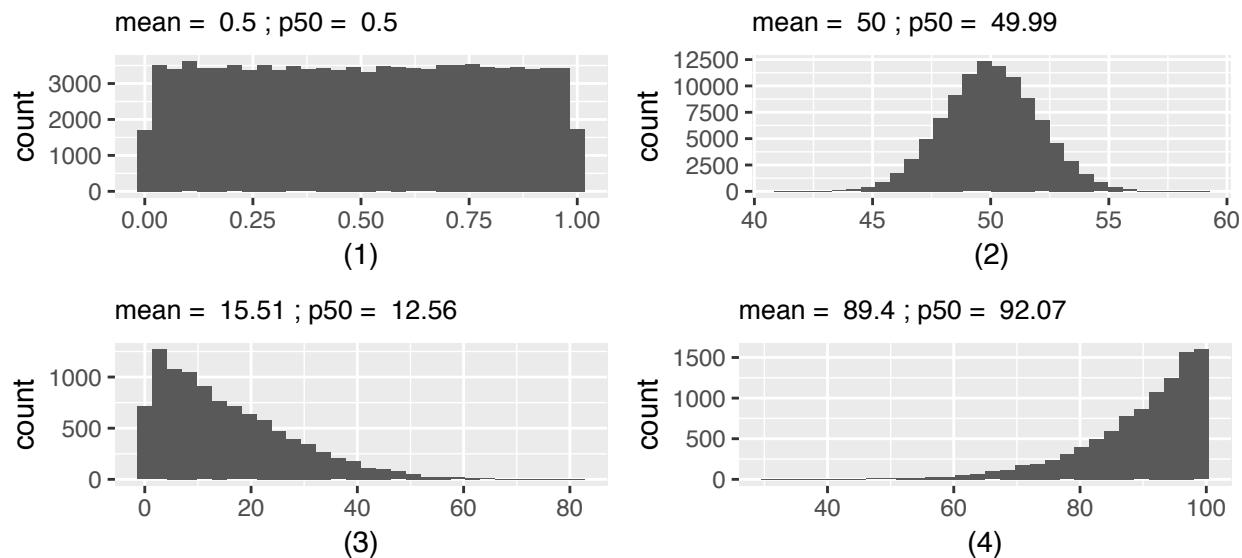
- Average age of a cohort entering graduate school
- Average speed of vehicles traveling down a highway segment
- Average number of days to close a complaint

The median or  $P50$  is also used as a method of indicate central tendency based on indexed position in a variable. It is computed as the 50th percentile value: sort all values from lowest to highest, then find the value at the  $(\frac{n+1}{2})^{th}$  position. Essentially, the median is denotes the position at which 50% of values are above and below. Medians are robust to outliers, meaning that the change in the magnitude of values above or below the 50th percentile point may change, but the median may stay the same.

Measure	Formula	Definition	When to use	R Function	Example
Mean or Average	$\mu = \frac{1}{n} \sum_{i=1}^n x_i$	A measure of central tendency formulated as the sum of all values. Also known as the 'expected value'.	The general de facto choice	mean()	mean(c(1,3,5,7,9)) = 5

Measure	Formula	Definition	When to use	R Function	Example
Median	Value at $(\frac{n+1}{2})^{th}$ position	A measure of central tendency based on the 'middle value' or 50th percentile of a random variable.	When data appears to be skewed or asymmetrical	median()	median(c(1,3,5,7,9)) = 5

Typically, it's helpful to consider and compare both median and mean values as they provide context. Revisiting the four distributions, we can compare the means and medians. In graphs 1 and 2, the distributions are symmetrical, thus one would expect the mean to be approximately equal to the median. In graph 3, the longer tail to the right pulls the mean above the median, whereas in graph 4, the left tail pulls the mean below the median.



## Spread

Just as important as central tendency is the spread or dispersion, or measures that gauge the variability of data relative to a central point. There are a number of measures that commonly are focused upon, such as variance and the interquartile range, and all help piece together a comprehensive understanding of a given data series.

Perhaps the simplest measures are those that are based on positions of records. The *minimum* and *maximum* are the smallest and largest values of a continuous variable. The minimum and maximum are also known as the *P0* and *P100*. The arithmetic difference between those values is the *range*. Similar to the range is the *Interquartile Range* or *IQR*, which is the arithmetic difference in values between the *P75* and *P25*. Examining the IQR gives a sense of the density of the center mass of a distribution, or the middle 50%. Together, these basic measures can contextualize the shape and density of a variable, especially comparing between subpopulations. For example, the income range of group A is \$100,000 and group B is \$2,000,000, indicating that the top and bottom of group A are closely distributed whereas there are large outliers in group B.

In addition, the *variance* of a data series contains key information about variability around the mean. Variance is defined as the *average squared difference between each value of a series and its mean*. The differences are squared in order to (1) preserve the information as simply adding the differences would net to zero, (2) emphasize differences from the mean. While the variance is a key part of statistics, it's not particularly

interpretable without some additional transformations. The *standard deviation* is the square-root of the variance, which has the same units as the original data and can be used to contextualize dispersion of data relative to the mean. In fact, standard deviations are used as a unit of analysis. Under a normal distribution using the mean as a point of reference, +/- 1.96 standard deviations should contain 95% of records and +/- 3 standard deviations should contain 99.7% of records. These benchmarks are commonly used to identify outliers.

Measure	Formula	Definition	R Function	Example
Minimum	$\text{argmin}(x_i)$	The smallest value of a random variable.	<code>min()</code>	<code>min(c(1,3,5,7,9))</code>
Maximum	$\text{argmax}(x_i)$	The largest value of a random variable.	<code>max()</code>	<code>max(c(1,3,5,7,9))</code>
Range	$\text{argmax}(x_i) - \text{argmin}(x_i)$	Difference of its largest and smallest data values	<code>range()</code>	<code>range(c(1,3,5,7,9))</code>
IQR	P75 - P50	Difference of the 75th percentile and 25th percentile value	<code>IQR()</code>	<code>IQR(c(1,3,5,7,9))</code>
Variance	$s^2 = \frac{1}{n} \sum_{i=1}^n (x_i - \mu)^2$	A measure of dispersion around the mean.	<code>var()</code>	<code>var(c(1,3,5,7,9))</code>
Standard Deviation	$s = \sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \mu)^2}$	The square root of the variance.	<code>sd()</code>	<code>sd(c(1,3,5,7,9))</code>

## Skewness + Kurtosis

[Debating if this should be used]

Measure	Formula	Definition	R Function	Example
Skewness	$\mu = \frac{1}{n} \sum_{i=1}^n x_i$	Measure of symmetry	<code>library(e1071)</code> <code>kurtosis()</code>	<code>example</code>

Measure	Formula	Definition	R Function	Example
Kurosis	$\mu = \frac{1}{n} \sum_{i=1}^n x_i$	Measure of peakedness relative to Gaussian distribution	library(e1071) <code>skewness()</code>	

## Graphical Approaches

While sample statistics help to determine expected values and overall trends of continuous variables, graphical and visual approaches help to identify unexpected values – where are there outliers and unusual quirks of the data. In this section, we will explore univariate and bivariate graphs and their application in EDA.

### Univariate graphs

```
temp <- tempfile()
download.file("https://www2.census.gov/programs-surveys/acs/data/pums/2015/1-Year/csv_pia.zip", temp, mode = "wb")
unz <- unzip(temp, exdir=getwd())
df <- read.csv(unz[1])
```

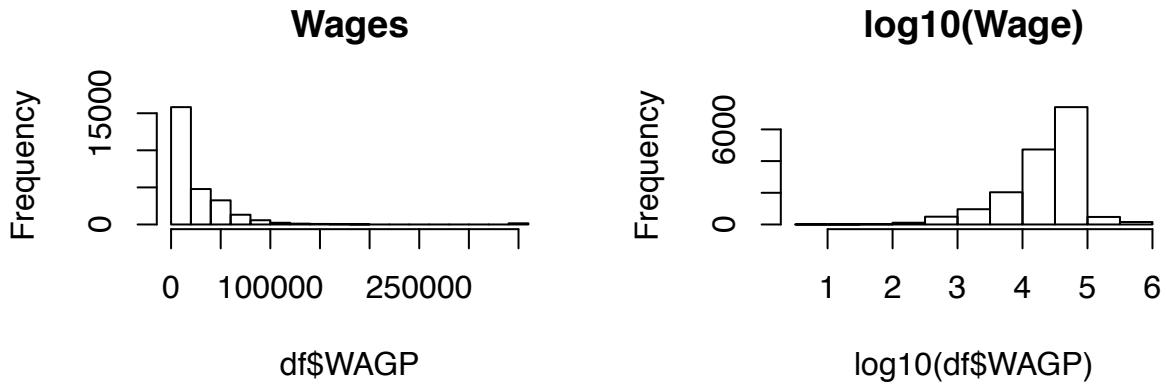
### Histograms and kernel density graphs

The most commonly used graph to visualize univariate data is the histogram. Essentially, histograms will break a continuous variable into equal sized *bins* based on the range of values, then graph the number of observations in each bin. This practice of *binning* or *discretizing* add a second dimension to a continuous variable that is needed to visualize patterns. Typically the number of bins is determined automatically when using functions such as `hist()`.

While normal distributions are the best known probability distribution, a pure normal distribution is fairly rare in the wild. In social data, it's more common to see long tails as seen below. Thus, data is often times *transformed* using mathematical functions in order to reshape the distribution of values. For data with large peaks to the left and long tails, common transformations include the natural logarithm (`log()`), logarithm base 2 (`log2()`) or logarithm base 10 (`log10()`). In the graph below, we use the `log10()` transformation to *stretch* the data to the right so that it is more normally or symmetrically distributed.

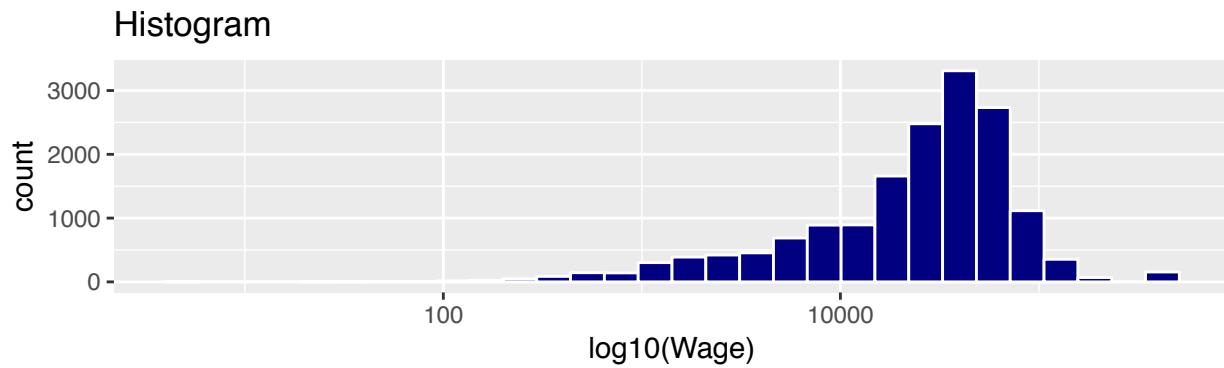
```
#Set up format
par(mfrow=c(1,2))

#Basic histogram
hist(df$WAGP, main = "Wages")
hist(log10(df$WAGP), main = "log10(Wage)")
```



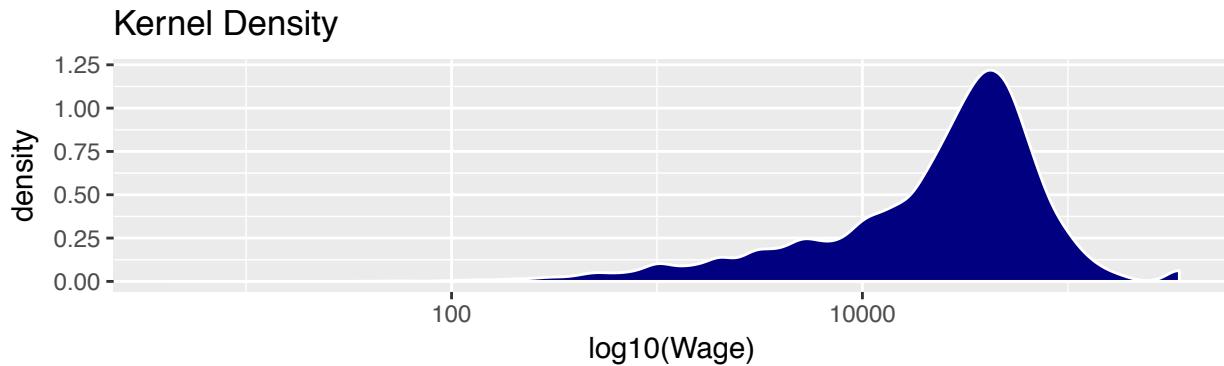
The `hist()` function provides rudimentary stylings for histograms. For more advanced stylings, the `ggplot2` library offers more convenient and easier to use stylistic options. In the example below, the `log10` transformation is applied using `scale_x_log10()`.

```
#Histogram using ggplot2
ggplot(df, aes(WAGP)) +
  ggtitle("Histogram") +
  geom_histogram(colour = "white", fill = "navy") +
  labs(x = "log10(Wage)") +
  scale_x_log10()
```



An alternative to histograms is the *kernel density plot*, which applies a technique known as *kernel-density estimation* as opposed to binning. Using `ggplot2`, we can apply the `geom_density()` argument to use the kernel density plot. The plot is notably smoother and organic when compared to histograms.

```
#K-density
ggplot(df, aes(WAGP)) +
  ggtitle("Kernel Density") +
  geom_density(colour = "white", fill = "navy") +
  labs(x = "log10(Wage)") +
  scale_x_log10()
```



Both histograms and kernel density graphs are helpful for developing a notional understanding of the shape of data. Due to binning, the individual bins of a histograms correspond to an actual number of observations whereas kernel densities can be used to illustrate the organic shape of the distribution. However, neither provide quantitative benchmarks such as the mean or quantiles.

## Multivariate Data

Much of data analysis focuses on the possibilities of combining two or more data series in order to uncover relationships and patterns as well as inform modeling hypotheses. In this section, we will focus on using correlation statistics and bivariate graphs to identify patterns.

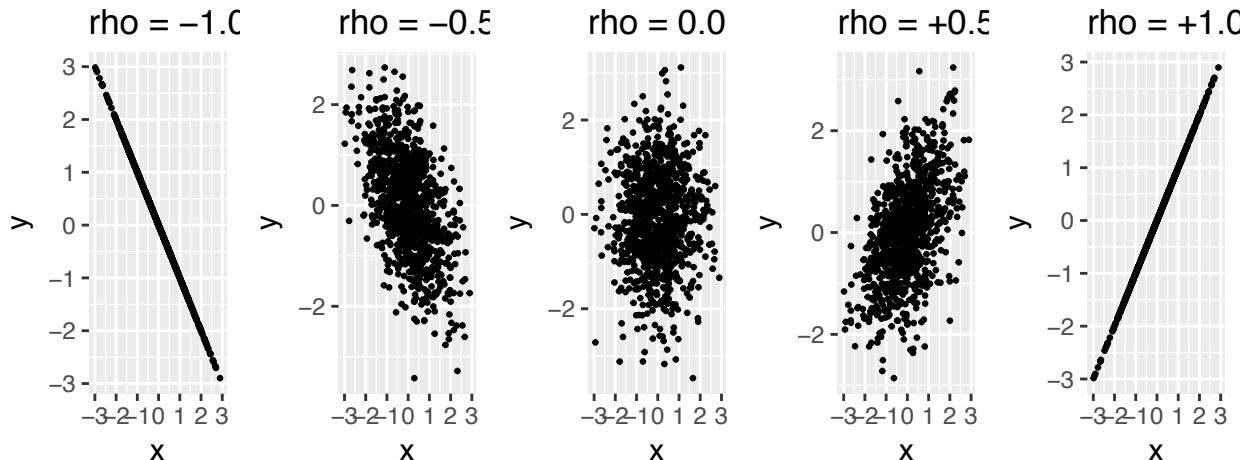
### Correlation of continuous variables

In everyday rhetoric, the term *correlation* is relatively loosely used. In statistics, it commonly has a specific definition, specifically, the *Pearson Product-Moment Correlation Coefficient* or *Correlation Coefficient* for short – a measure of relatedness. It is defined as:

$$\rho(X, Y) = \frac{\text{cov}(X, Y)}{\sigma_X \sigma_Y}$$

where  $\rho$  denotes the correlation coefficient,  $\text{cov}$  is the covariance of two variables ( $X$  and  $Y$ ) as defined as  $(X - \mu_X)(Y - \mu_Y)$ , and  $\sigma$  is the standard deviation of each  $X$  and  $Y$ . The correlation coefficient is bound between -1 and 1, where:

- -1 indicates perfectly negative linear relationship (as  $X$  increases,  $Y$  decreases proportionally)
- 0 indicates no relationship ( $X$  and  $Y$  are not related)
- +1 indicates perfectly positive linear relationship (as  $X$  increases,  $Y$  increases proportionally)



In practice, it's fairly simple to calculate and explore relationships by using `cor()`. For example, what if we were to compare age (AGEP) with retirement income (RETP). Notice that we use the `complete.obs` option to use only records that have values for both AGEPE and RETP. The correlation coefficient is +0.226 indicating only a slight correlation.

```
cor(df$AGEP, df$RETP, use="complete.obs")
```

```
## [1] 0.2262218
```

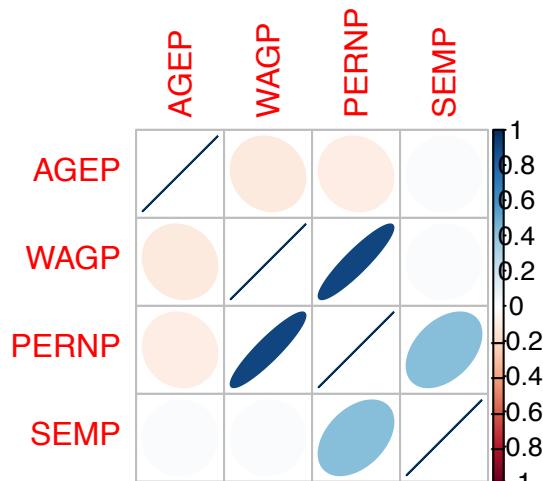
How do we examine a much broader set of variables such as WAGP - wage income, PERNP - personal income, RETP - retirement income, SSIP - supplemental security income, PAP - public assistance income, SEMP - self-employment income, and OIP - all other income. The `cor()` function can accept a dataframe or matrix of continuous variables and outputs a  $k \times k$  matrix of pairwise correlation coefficients. The diagonal will always be filled with 1 as a correlation of a variable with itself will be the highest possible value. Values above the diagonal are identical to values below.

```
select <- df[, c("AGEP", "WAGP", "PERNP", "SEMP")]
cor(select, use="complete.obs")
```

```
##          AGEP        WAGP        PERNP        SEMP
## AGEP  1.00000000 -0.11366644 -0.09416775  0.02141612
## WAGP -0.11366644  1.00000000  0.91511883  0.02645639
## PERNP -0.09416775  0.91511883  1.00000000  0.42725385
## SEMP   0.02141612  0.02645639  0.42725385  1.00000000
```

The correlation matrix may be a bit overwhelming to decipher. We may use the `corrplot` package to visualize the size of correlations. In this case, we can see that the strongest correlations are PERNP, WAGP, and SEMP.

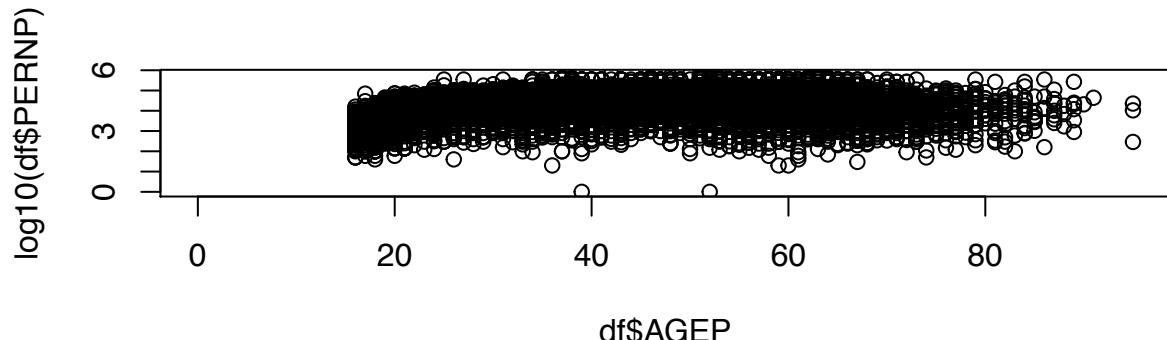
```
library(corrplot)
M <- cor(select, use="complete.obs")
corrplot(M, method="ellipse")
```



### Bivariate plots: continuous vs continuous

The simplest bivariate graph is the scatter plot, which graphs points placing one variable on the horizontal axis and another on the vertical axis. The intersection of the values fall on a two-dimensional canvas, exposing relationships between variables. Below, a simple scatter plot shows the non-linear relationship between log-transformed personal income and age, suggesting that wages may reach a ceiling as one gets older.

```
plot(df$AGEP, log10(df$PERNP))
```



In data science, often times, the amount of the data will push the limits of traditional graphs and require more stylized ways to derive empirical insight:

- Graph (a) plots a traditional scatter plot with much of the plot saturated with points. This is generally good when strong linear trends are present or with relatively few data points.
- Graph (b) is another scatter plot with an adjusted `alpha`, also known as opacity. In graphs, changing the opacity in a graph without any overlapping points makes the entire image look faint. In cases where points overlap, the opacity values add up, thereby darkening areas with overlapping points. This style is particularly useful when there is a high volume of points.
- Graph (c) is a scatter plot, but uses a *locally weighted smoother* to show the direction of local relationships and the variability around the trend line. This style can be used to find candidate transformations and non-linear specifications for the modeling phase.
- Graph (d) is a hexbin plot, which converts a graphical canvas into equal hexagonal bins, counts the number of values in each discrete bin and color codes based on the counts. This style is particularly useful when there is a high volume of points.
- Graph (e) is a contour graph that bins the graph into distinct regions where concentric regions towards the middle are larger values. This is useful for geographic or spatial data, particularly for terrain data.

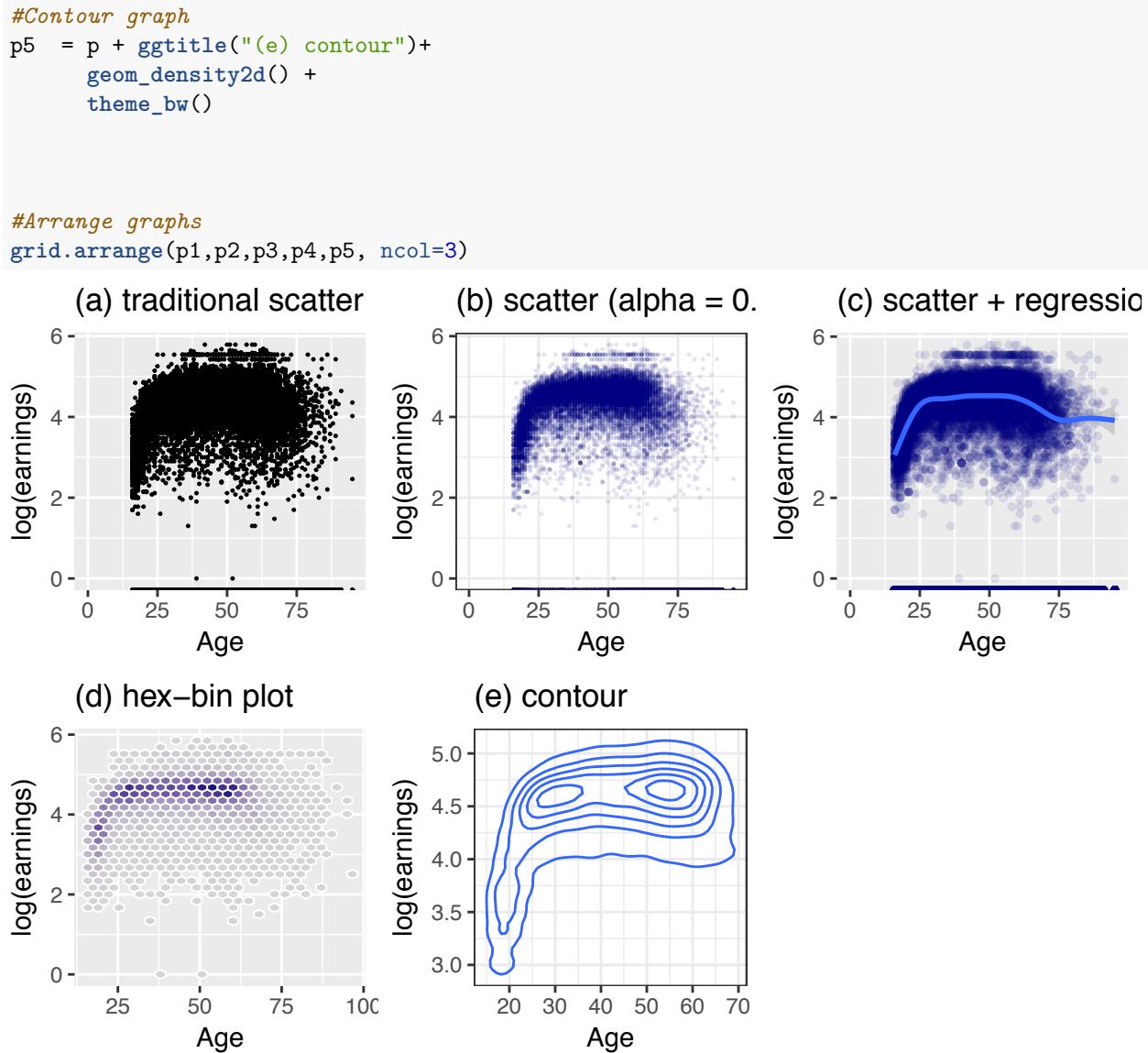
```
#Base data for plot
p = ggplot(df,aes(x=AGEP,y=log10(PERNP))) +
  xlab("Age") +
  ylab("log(earnings)")

##Scatter plot
p1 = p + geom_point(size=0.2) +
  ggtitle("(a) traditional scatter")

##Scatter plot with transparency
p2 = p + geom_point(alpha = 0.1, colour="navy", size=0.2) +
  theme_bw() +
  ggtitle("(b) scatter (alpha = 0.1)")

##Scatter plot with regression line (locally weighted smoother)
p3 = p + ggtitle("(c) scatter + regression line")+
  geom_point(alpha = 0.1, colour="navy",size=1) +
  geom_smooth() + xlab("Age") + ylab("log(earnings)")

##Hexbin
p4 = p + stat_bin_hex(colour="white", na.rm=TRUE,alpha=0.9) +
  scale_fill_gradientn(colours=c("lightgrey","navy"), name = "Frequency") +
  guides(fill=FALSE) + ggtitle("(d) hex-bin plot")
```



### Comparing subpopulations

A common task in EDA is the search for *separability* – when data cluster in such a way that can help distinguish one group from another. This helps with identifying qualities that distinguish one subpopulation from another and factors that may be included in a modeling strategy. Side-by-side graphical comparisons, such as violin and boxplots, and graph overlays are powerful tools in showing differences.

To illustrate this, let's create a variable for whether a respondent holds a bachelor's degree. These two levels can be used to stratify a dataset into subpopulations for comparison.

```

df$college <- NA
df$college[df$SCHL<21] <- "Less than bachelor's"
df$college[df$SCHL>=21] <- "With bachelor's"

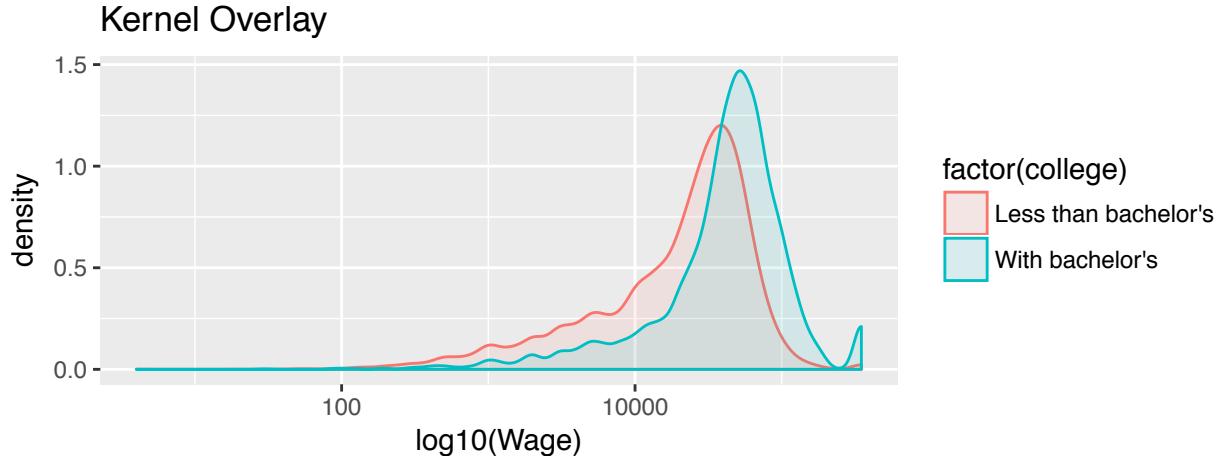
```

The natural shape of kernel density plots lend themselves to easier comparison. As seen below, we two kernel density plots are overlaid. Using the `fill` and `colour` parameters, the kernel densities are color-coded for ease of inspection. Notice that distributions are differently distributed, with college graduates generally

earning higher wages.

```
ggplot(df, aes(WAGP, fill = factor(college), colour = factor(college))) +
  geom_density(alpha = 0.1) + ##alpha controls opacity
  labs(x = "log10(Wage)") +
  ggtitle("Kernel Overlay") +
  scale_x_log10()

## Warning: Transformation introduced infinite values in continuous x-axis
## Warning: Removed 15516 rows containing non-finite values (stat_density).
```



What if there are many subpopulations? If there are more than a couple of sub-groups, other side-by-side comparisons lend themselves for easier interpretation and reduce clutter.

```
df$SCHL2[df$SCHL<16] <- "1 - Less than HS"
df$SCHL2[df$SCHL>=16 & df$SCHL<21] <- "2 - HS"
df$SCHL2[df$SCHL==21] <- "3 - Undergraduate Degree"
df$SCHL2[df$SCHL>21] <- "4 - Graduate Degree"
```

Two data scientist favorites are the violin plot and the boxplot. The *violin plot* (left) is a kernel density graph rotated onto a vertical axis with the probability density plotted symmetrically across the vertical axis. *Boxplots* display the distribution of the data following key summary statistics, namely the median, 25th percentile/first quartile and the 75th percentile/third quartile. On the right, the median is denoted by the gray horizontal line in each blue box, and the upper and lower edges of the box are the 75th and 25th percentiles, respectively, also referred to as the shoulders of the distribution. Points to the top and the bottom are outliers, which are points located outside the body of the distribution (usually a distance of over 1.5-times the IQR above 75th percentile and below the 25th percentile). Both graphs are quite useful. The violin plot shows the shape of the distribution, whereas the boxplot allows for comparison of center mass.

```
#Violin
vio <- ggplot(df, aes(factor(SCHL2), WAGP)) +
  geom_violin(colour = "navy", fill = "navy") +
  labs(x = "log10(Wage)") +
  ggtitle("Violin Plot") +
  scale_y_log10()
```

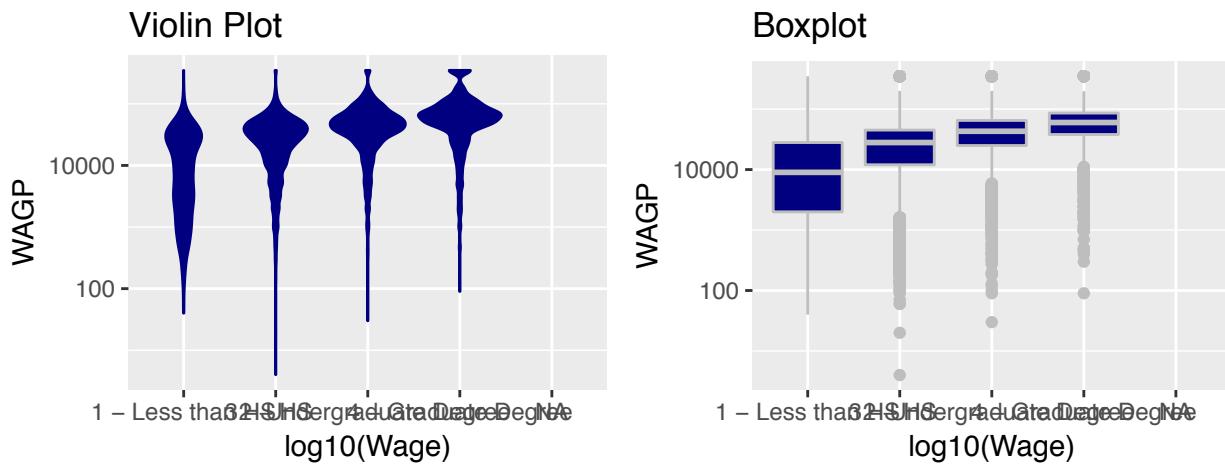
```
#Boxplot
box <- ggplot(df, aes(factor(SCHL2), WAGP)) +
  geom_boxplot(colour = "grey", fill = "navy") +
  labs(x = "log10(Wage)") +
  ggtitle("Boxplot") +
```

```

  scale_y_log10()

#Plot side by side
grid.arrange(vio, box, ncol = 2)

```



## Assignments

- Play the *Guess The Correlation Game* for 5 minutes. This game challenges players to guess the coefficient correlation based on randomly assigned scatter plots of two continuous variables.