

Carlos Arguedas Barahona

Ing. Eléctrica

Análisis de Sistemas Lineales

Respuesta de V_L , V_C y V_R en un circuito RLC, ante la entrada de V_{in} señales de impulso, rampa y escalón unitario.

Componente	Tiempo	Frecuencia
Resistencia	$V_R = I * R$	$V_R = I_{(s)} * R$
Capacitor	$V_C = \frac{1}{C} \int_0^T I_C dt$	$V_C = \frac{I_{(s)}}{C * S}$
Inductor	$V_L = L \frac{di}{dt}$	$V_L = L * S * I_{(s)}$

Debemos calcular las funciones de transmisión para cada voltaje de salida.

Aplicando LVK obtenemos:

$$-V_{in}(t) + V_R(t) + V_C(t) + V_L(t) = 0$$

Aplicando Laplace.

$$L \left(-V_{in}(t) + I * R + \frac{1}{C} \int_0^T I_C dt + L \frac{di}{dt} = 0 \right)$$

$$-V_{in}(s) + I_{(s)} * R + \frac{I_{(s)}}{C * S} + L * S * I_{(s)} = 0$$

o **Inductor:**

$$\frac{I_{(s)}}{V_{in}(s)} = \frac{1}{R + L * S + \frac{1}{CS}} = \frac{S}{R * S + L * S^2 + \frac{1}{C}}$$

$$\frac{I_{(s)} * L * S}{V_{in}(s)} = \frac{S * L * S}{R * S + L * S^2 + \frac{1}{C}}$$

$$\frac{V_L(s)}{V_{in}(s)} = \frac{L * S^2}{R * S + L * S^2 + \frac{1}{C}}$$

○ **Resistencia:**

$$\frac{I_{(s)}}{V_{in}(s)} = \frac{1}{R + L * S + \frac{1}{CS}} = \frac{S}{R * S + L * S^2 + \frac{1}{C}}$$

$$\frac{I_{(s)} * R}{V_{in}(s)} = \frac{S * R}{R * S + L * S^2 + \frac{1}{C}}$$

$$\frac{V_R(s)}{V_{in}(s)} = \frac{S * R}{R * S + L * S^2 + \frac{1}{C}}$$

○ **Capacitor:**

$$\frac{I_{(s)}}{V_{in}(s)} = \frac{1}{R + L * S + \frac{1}{CS}} = \frac{S}{R * S + L * S^2 + \frac{1}{C}}$$

$$\frac{\frac{I_{(s)}}{CS}}{V_{in}(s)} = \frac{\frac{S}{CS}}{R * S + L * S^2 + \frac{1}{C}} = \frac{S}{CS \left(R * S + L * S^2 + \frac{1}{C} \right)} = \frac{S}{CR * S^2 + CL * S^3 + S}$$

$$\frac{V_C(s)}{V_{in}(s)} = \frac{S}{CR * S^2 + CL * S^3 + S}$$

- Respuesta a impulso del inductor:



laplace inverse $(1 \cdot 10^{-6} s^2) / (1 \cdot 10^3 s + 1 \cdot 10^{-6} s^2 + (1 / 1 \cdot 10^{-6}))$



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Assuming "s" is a variable | Use "s^2" as a [unit](#) instead

Input interpretation:

$$\mathcal{L}_s^{-1} \left[\frac{1 \times 10^{-6} s^2}{1 \times 10^3 s + 1 \times 10^{-6} s^2 + \frac{1}{1 \times 10^{-6}}} \right] (t)$$

[Open code](#)

$\mathcal{L}_s^{-1}[f(s)](t)$ is the inverse Laplace transform of $f(s)$ with real variable t

Result:

$$\frac{1}{1000000} \left(1000000 \delta(t) - \left(50000000000 e^{-\frac{1000000t}{500 + \sqrt{249999}}} \right. \right. \\ \left. \left(499998500 e^{\frac{1000000t}{500 + \sqrt{249999}}} + (-500000000 - 1000000 \sqrt{249999}) t \right. \right. \\ \left. \left. 999999 \sqrt{249999} e^{\frac{1000000t}{500 + \sqrt{249999}}} + (-500000000 - 1000000 \sqrt{249999}) t \right. \right. \\ \left. \left. 500 + \sqrt{249999} \right) \right) / (249999 + 500 \sqrt{249999}) \right)$$

- Respuesta a escalón unitario del inductor:



laplace inverse $(1 \times 10^{-6} s^2) / (1 \times 10^3 s + 1 \times 10^{-6} s^2 + (1/1 \times 10^{-6})) (1/s)$



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Assuming "s" is a variable | Use "s^2" as a unit instead

Input interpretation:

$$\mathcal{L}_s^{-1} \left[\frac{1 \times 10^{-6} s^2}{1 \times 10^3 s + 1 \times 10^{-6} s^2 + \frac{1}{1 \times 10^{-6}}} \times \frac{1}{s} \right] (t)$$

[Open code](#)

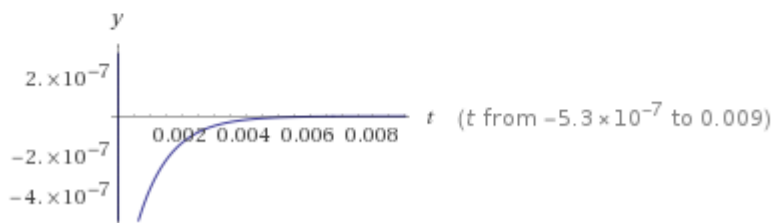
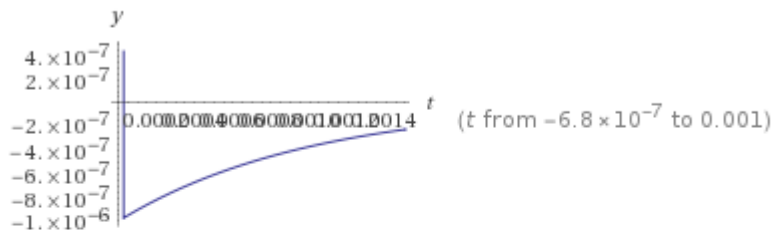
$\mathcal{L}_s^{-1} [f(s)] (t)$ is the inverse Laplace transform of $f(s)$ with real variable t

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Result:

$$\left(e^{\frac{-1000000t}{500 + \sqrt{249999}}} \left(499999 e^{\frac{1000000t}{500 + \sqrt{249999}}} + (-500000000 - 1000000\sqrt{249999})t + 1000\sqrt{249999} e^{\frac{1000000t}{500 + \sqrt{249999}}} + (-500000000 - 1000000\sqrt{249999})t - 1 \right) \right) / \left(2(249999 + 500\sqrt{249999}) \right)$$

Plots:



- Respuesta a rampa del inductor:



laplace inverse $(1 \cdot 10^{-6} s^2) / (1 \cdot 10^3 s + 1 \cdot 10^{-6} s^2 + (1 / 1 \cdot 10^{-6})) (1 / s^2)$



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Assuming "s" is a variable | Use "s^2" as a unit instead

Input interpretation:

$$\mathcal{L}_s^{-1} \left[\frac{1 \times 10^{-6} s^2}{1 \times 10^3 s + 1 \times 10^{-6} s^2 + \frac{1}{1 \times 10^{-6}}} \times \frac{1}{s^2} \right] (t)$$

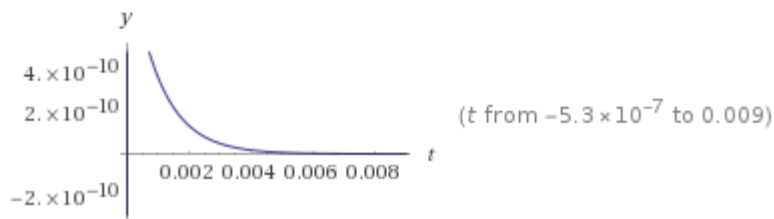
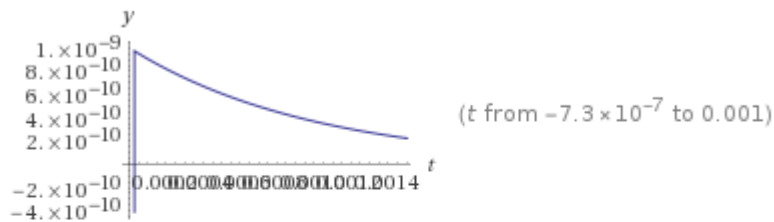
[Open code](#)

$\mathcal{L}_s^{-1}[f(s)](t)$ is the inverse Laplace transform of $f(s)$ with real variable t

Result:

$$\frac{(500 + \sqrt{249999}) e^{-\frac{1000000 t}{500 + \sqrt{249999}}} \left(\frac{1000000 t}{e^{500 + \sqrt{249999}}} + (-500000000 - 1000000 \sqrt{249999}) t - 1 \right)}{2000000 (249999 + 500 \sqrt{249999})}$$

Plots:



- Respuesta a impulso de la resistencia:



laplace inverse $(1 \times 10^3 s) / (1 \times 10^3 s + 1 \times 10^{-6} s^2 + (1 / 1 \times 10^{-6}))$



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Assuming "s" is a variable | Use as a [unit](#) instead

Input interpretation:

$$\mathcal{L}_s^{-1} \left[\frac{1 \times 10^3 s}{1 \times 10^3 s + 1 \times 10^{-6} s^2 + \frac{1}{1 \times 10^{-6}}} \right] (t)$$

[Open code](#)

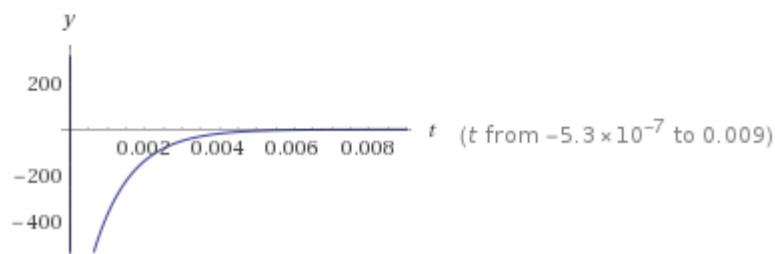
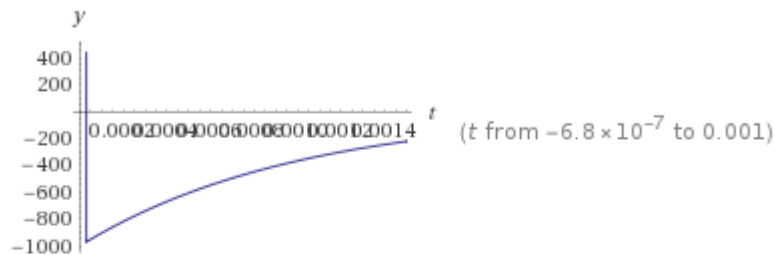
$\mathcal{L}_s^{-1}[f(s)](t)$ is the inverse Laplace transform of $f(s)$ with real variable t

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Result:

$$\left(500\,000\,000 e^{-\frac{1\,000\,000 t}{500 + \sqrt{249\,999}}} \left(499\,999 e^{\frac{1\,000\,000 t}{500 + \sqrt{249\,999}}} + (-500\,000\,000 - 1\,000\,000 \sqrt{249\,999}) t \right) + \right. \\ \left. 1000 \sqrt{249\,999} e^{\frac{1\,000\,000 t}{500 + \sqrt{249\,999}}} + (-500\,000\,000 - 1\,000\,000 \sqrt{249\,999}) t - 1 \right) / \\ (249\,999 + 500 \sqrt{249\,999})$$

Plots:



- Respuesta a escalón unitario de la resistencia:



laplace inverse $(1 \times 10^3 s) / (1 \times 10^3 s + 1 \times 10^{-6} s^2 + (1 / 1 \times 10^{-6})) (1/s)$



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Input interpretation:

$$\mathcal{L}_s^{-1} \left[\frac{1 \times 10^3 s}{1 \times 10^3 s + 1 \times 10^{-6} s^2 + \frac{1}{1 \times 10^{-6}}} \times \frac{1}{s} \right] (t)$$

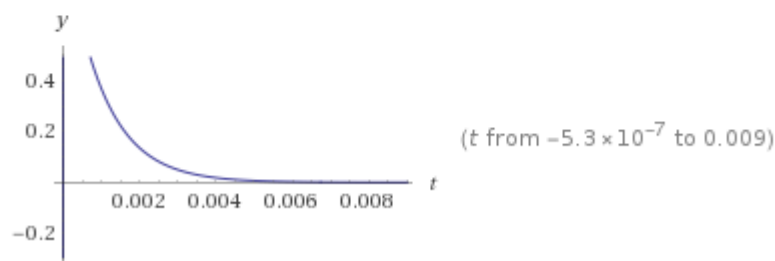
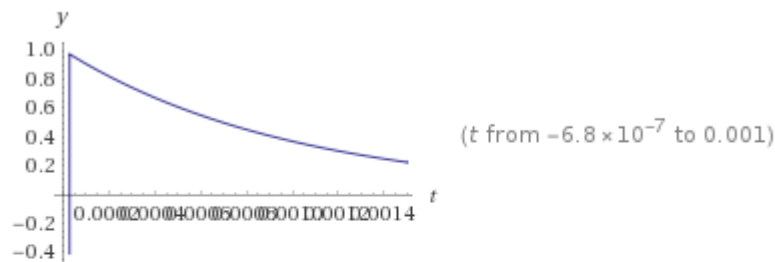
[Open code](#)

$\mathcal{L}_s^{-1}[f(s)](t)$ is the inverse Laplace transform of $f(s)$ with real variable t

Result:

$$-\left(\left(500 \left(500 + \sqrt{249999} \right) e^{-\frac{1000000 t}{500 + \sqrt{249999}}} \right. \right. \\ \left. \left. \left(e^{\frac{1000000 t}{500 + \sqrt{249999}}} + \left(-500000000 - 1000000 \sqrt{249999} \right) t - 1 \right) \right) \right) / \\ \left(249999 + 500 \sqrt{249999} \right)$$

Plots:



- Respuesta a rampa de la resistencia:



laplace inverse $(1 \cdot 10^3 s) / (1 \cdot 10^3 s + 1 \cdot 10^{-6} s^2 + (1/1 \cdot 10^{-6})) (1/s^2)$



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Assuming "s" is a variable | Use as a [unit](#) instead

Input interpretation:

$$\mathcal{L}_s^{-1} \left[\frac{1 \times 10^3 s}{1 \times 10^3 s + 1 \times 10^{-6} s^2 + \frac{1}{1 \times 10^{-6}}} \times \frac{1}{s^2} \right] (t)$$

[Open code](#)

$\mathcal{L}_s^{-1} [f(s)] (t)$ is the inverse Laplace transform of $f(s)$ with real variable t

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Result:

$$1000 \left(\frac{1}{1000000} - \left(e^{-\frac{1000000t}{500 + \sqrt{249999}}} \left(-\frac{1000000t}{500 + \sqrt{249999}} + (-500000000 - 1000000\sqrt{249999})t \right) + 499999 + 1000\sqrt{249999} \right) \right) / \left(2000000(249999 + 500\sqrt{249999}) \right)$$

- Respuesta a impulso del capacitor:



laplace inverse (s)/(1*10^-3*s^2+1*10^-12*s^3+s)



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Assuming "s" is a variable | Use as a [unit](#) instead

Input interpretation:

$$\mathcal{L}_s^{-1}\left[\frac{s}{1 \times 10^{-3} s^2 + 1 \times 10^{-12} s^3 + s}\right](t)$$

[Open code](#)

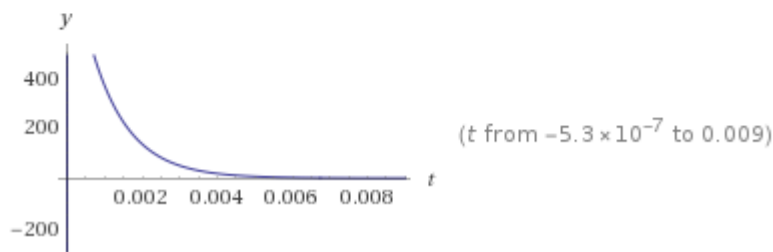
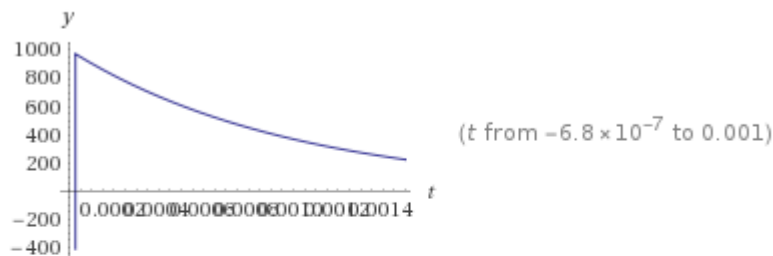
$\mathcal{L}_s^{-1}[f(s)](t)$ is the inverse Laplace transform of $f(s)$ with real variable t

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Result:

$$\frac{-\left(\left(500000\left(500+\sqrt{249999}\right)e^{-\frac{1000000t}{500+\sqrt{249999}}}\right.\right. \\ \left.\left.\left(e^{\frac{1000000t}{500+\sqrt{249999}}}+(-500000000-1000000\sqrt{249999})t-1\right)\right)\right)}{(249999+500\sqrt{249999})}$$

Plots:



- *Respuesta a escalón unitario del capacitor:*



laplace inverse (s)/(1*10^-3*s^2+1*10^-12*s^3+s)(1/s)



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Assuming "s" is a variable | Use as [a unit](#) instead

Input interpretation:

$$\mathcal{L}_s^{-1}\left[\frac{s}{1 \times 10^{-3} s^2 + 1 \times 10^{-12} s^3 + s} \times \frac{1}{s}\right](t)$$

[Open code](#)

$\mathcal{L}_s^{-1}[f(s)](t)$ is the inverse Laplace transform of $f(s)$ with real variable t

Result:

$$1 - \left(e^{-\frac{1000000t}{500 + \sqrt{249999}}} \left(\frac{1000000t}{-e^{\frac{1000000t}{500 + \sqrt{249999}}} + (-500000000 - 1000000\sqrt{249999})t} + 499999 + 1000\sqrt{249999} \right) \right) / \left(2(249999 + 500\sqrt{249999}) \right)$$

- Respuesta a rampa del capacitor:



laplace inverse (s)/(1*10^-3*s^2+1*10^-12*s^3+s)(1/s^2)



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Assuming "s" is a variable | Use as [a unit](#) instead

Input interpretation:

$$\mathcal{L}_s^{-1}\left[\frac{s}{1 \times 10^{-3} s^2 + 1 \times 10^{-12} s^3 + s} \times \frac{1}{s^2}\right](t)$$

[Open code](#)

$\mathcal{L}_s^{-1}[f(s)](t)$ is the inverse Laplace transform of $f(s)$ with real variable t

Result:

$$\left(e^{-\frac{1000000t}{500+\sqrt{249999}}} \left(-500 e^{\frac{1000000t}{500+\sqrt{249999}}} + (-500000000 - 1000000\sqrt{249999})t + \sqrt{249999} e^{\frac{1000000t}{500+\sqrt{249999}}} + (-500000000 - 1000000\sqrt{249999})t + 499998500 + 999999\sqrt{249999} \right) \right) / \left(2000000(249999 + 500\sqrt{249999}) + t - \frac{1}{1000} \right)$$