



Classification (Short Version)

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Classification

- To learn more

2016年



<https://youtu.be/fZAZUYEeIMg>
(in Mandarin)

Classification

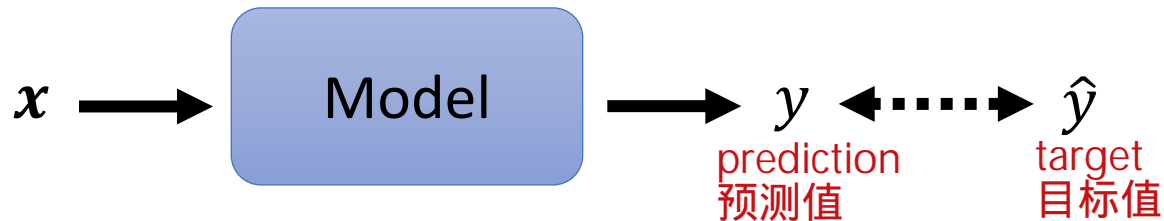


<https://youtu.be/hSXFuypLukA>
(in Mandarin)

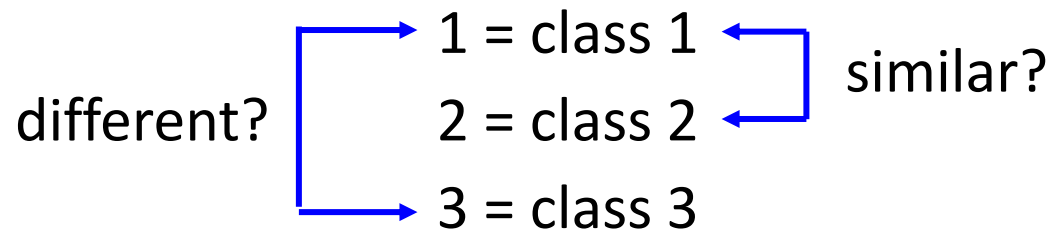
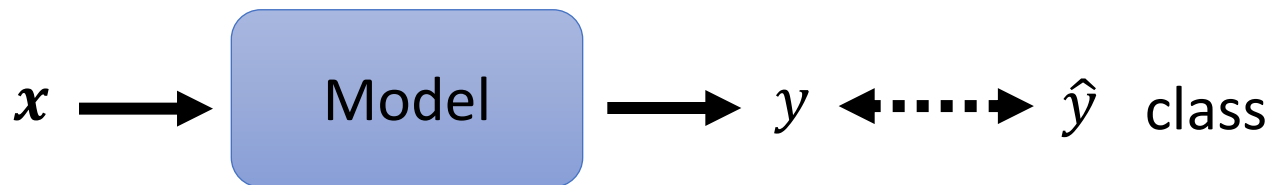
Logistic Regression

Classification as Regression?

- Regression



- Classification as regression?



这种分类有时可以，有时不行

Class as one-hot vector

one-hot vector 独热码来表示class

Class 1

Class 2

Class 3

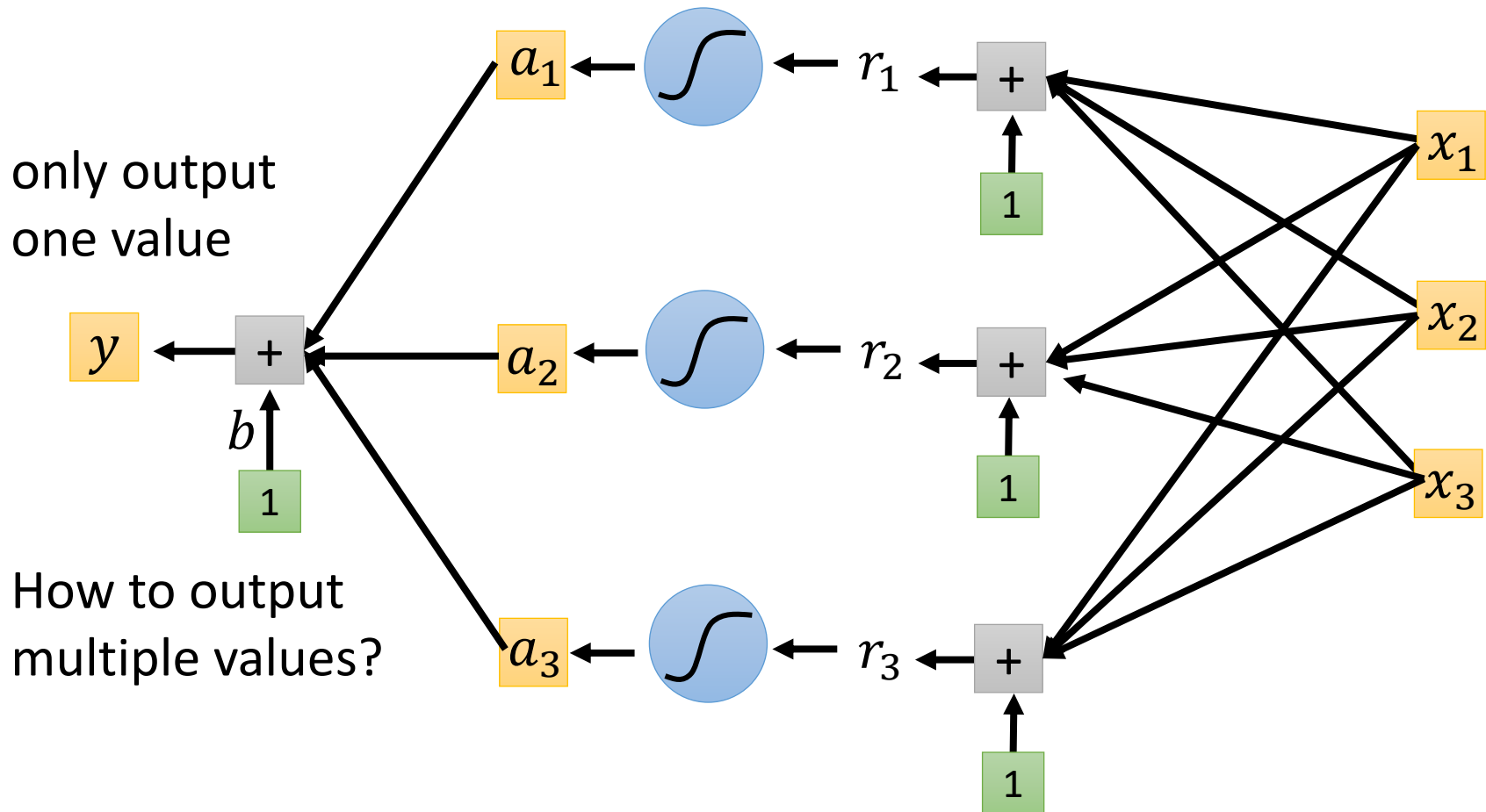
$$\hat{y} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

or

$$\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$$

or

$$\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$



Class as one-hot vector

Class 1

Class 2

Class 3

$$\hat{y} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

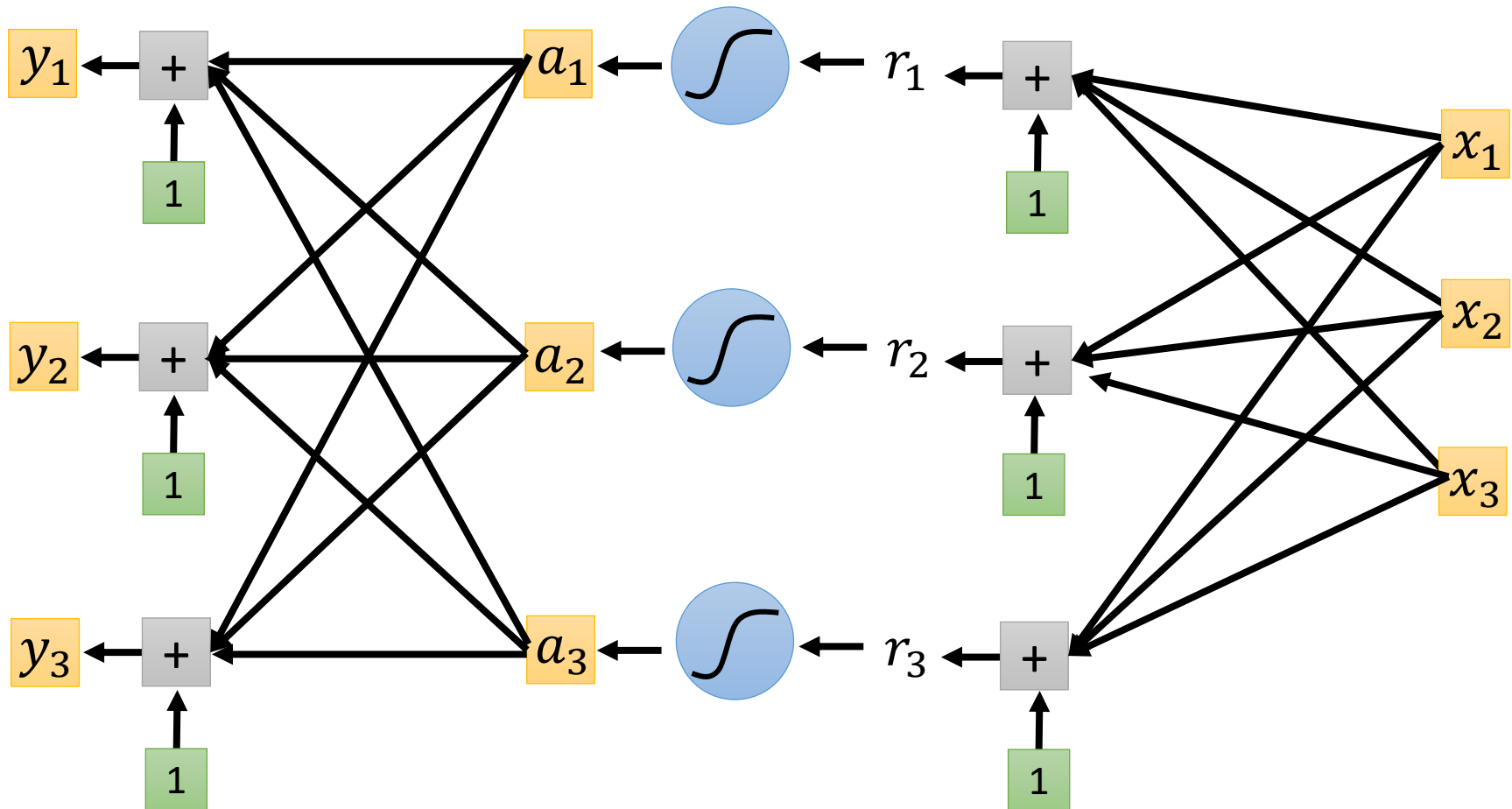
or

$$\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$$

or

$$\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

output multiple values



Regression

label

$$\hat{y} \longleftrightarrow y = b + c^T \sigma(\underset{\text{feature}}{b} + W x)$$

Classification

feature

$$y = b' + W' \sigma(b + W x)$$

label

$$\hat{y} \longleftrightarrow y' = \text{softmax}(y)$$

0 or 1

Make all values between 0 and 1
骗小孩的解释

Can have any value
为什么要用softmax

Soft-max

1. $0 < \text{值} < 1$
2. 大小值的差距会更大

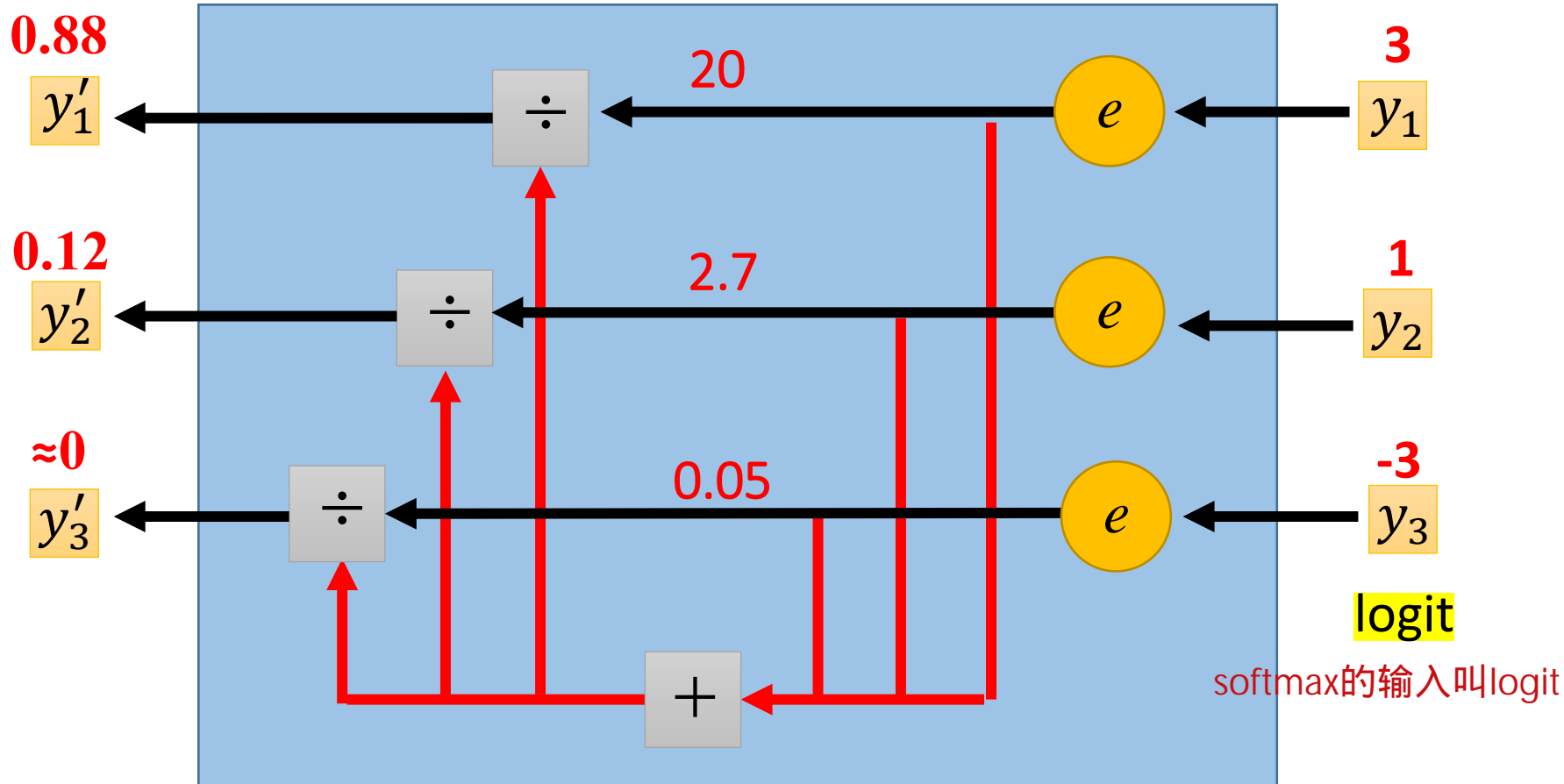
Softmax

(都变正)

$$y'_i = \frac{\exp(y_i)}{\sum_j \exp(y_j)}$$

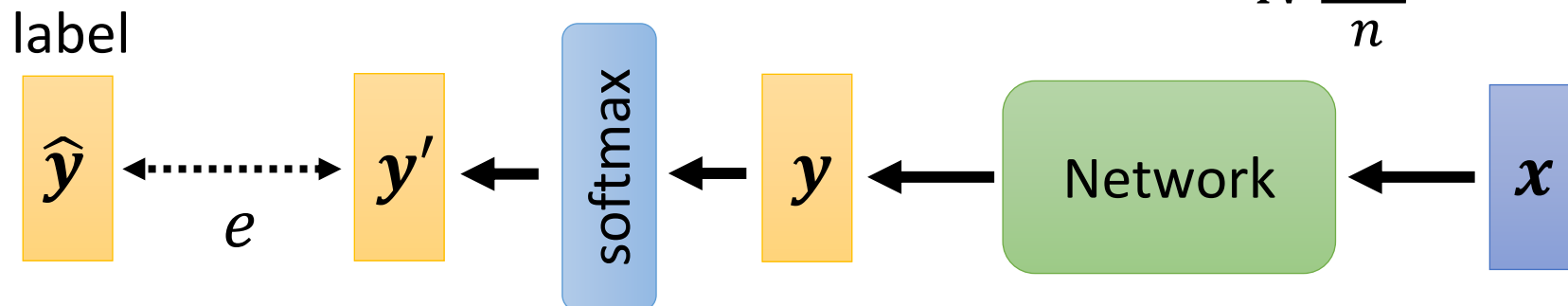
- $1 > y'_i > 0$
- $\sum_i y'_i = 1$

How about **binary classification**? ☺ **sigmoid**
sigmoid和softmax是同一件事情



Loss of Classification

$$L = \frac{1}{N} \sum_n e_n$$



Mean Square Error (MSE)

$$e = \sum_i (\hat{y}_i - y'_i)^2$$

Cross-entropy

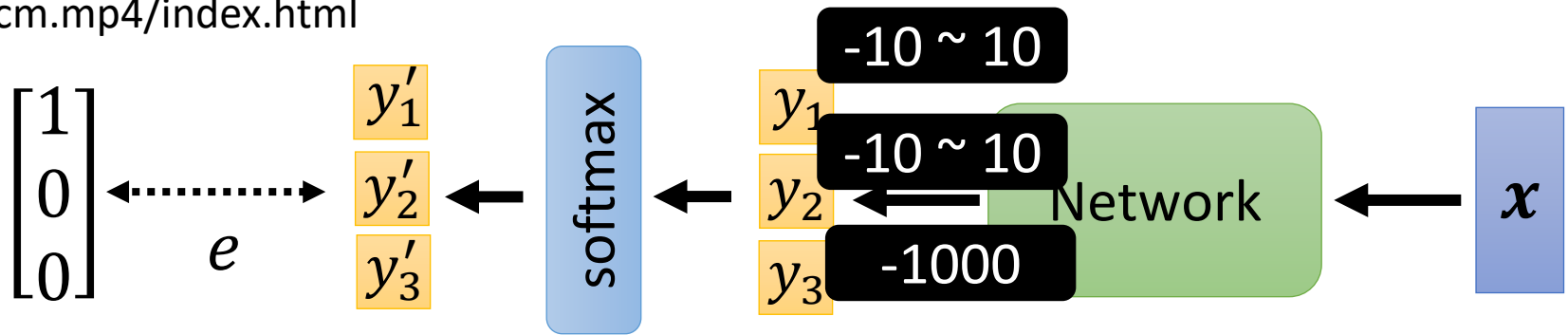
交叉熵



$$e = - \sum_i \hat{y}_i \ln y'_i$$

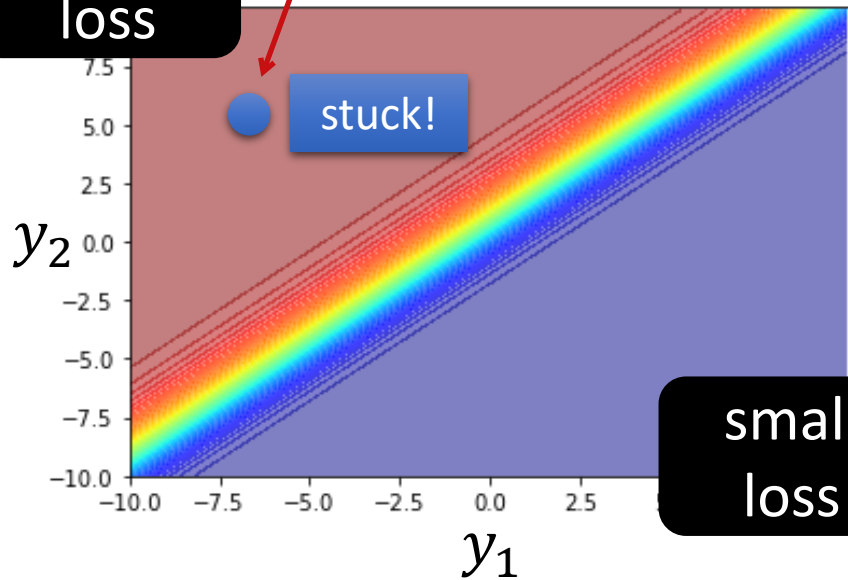
Minimizing cross-entropy is equivalent to **maximizing likelihood**.

Pytorch内部cross-entropy和softmax绑在一起了

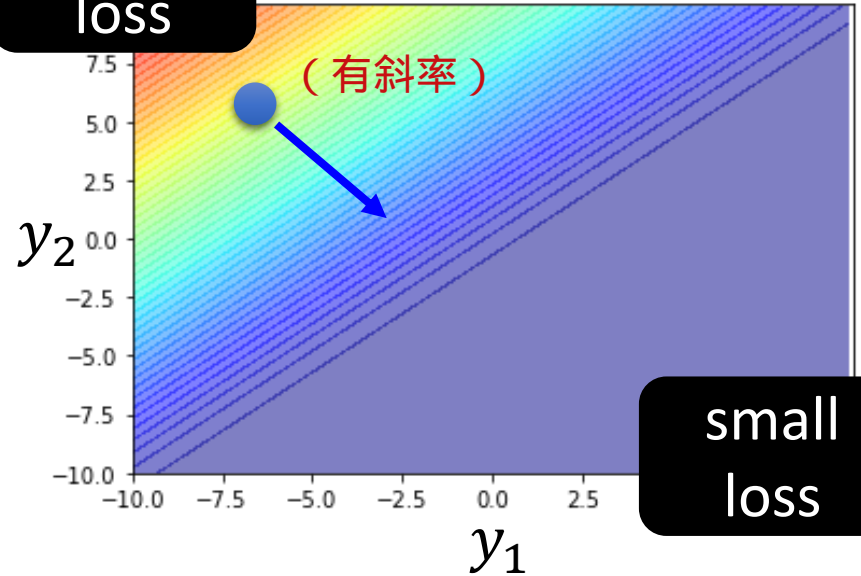


(gradient很小 , train不起来)

large loss Mean Square Error (MSE)



large loss Cross-entropy



Changing the loss function can change the difficulty of optimization.