

CS2134 Homework 1

Fall 2016

Due* 11:00 p.m. Sat. Sept 17, 2016

Your first assignment includes a programming portion and a written portion. The programming portion *must* compile and should consist of a single file called `hw01.cpp`, and the written portion should consist of a single file called `hw01written` saved in a `.pdf` format. Be sure to include your name at the beginning of each file! You must hand in both files via NYU Classes.

Programming Part:

1. You will compare the time it takes to solve the Max Contiguous Subsequence sum problem, using the three algorithms provided in the file called `MaxSubsequenceSum` and `Timer Class`. You will run all three algorithms with the following values of `n`: $2^7 = 128$, $2^8 = 256$, $2^9 = 512$, $2^{10} = 1024$, $2^{11} = 2048$, and $2^{12} = 4096$.

What you will need to do:

- (a) Look at the code for the `timer` class in the file `MaxSubsequenceSum` and `Timer Class`, and then apply it in your own code.¹
- (b) Fill a `vector` with `n` random integers in the range from -1000 to 1000. There is a function² from the standard library called `rand()` that returns a value from 0 to `RAND_MAX`; (`RAND_MAX` is at least 32767.) The code `x = (rand() % 2001) - 1000` puts a random number in the range `[-1000, 1000]` into the variable `x`.
- (c) Time how long it takes the function `maxSubSum1` to find the maximum subsequence sum. The code might look like the following

```
timer t;
double nuClicks;
// other code to fill in the vector with n items, etc.
t.reset();
maxSubsequenceSum1( items );
```

*Early submissions 5:00 p.m. Fri. Sept 16, 2016 for 5% bonus.

¹Some compilers require `#include <ctime>` or `#include <time.h>` to be included in your code for this class to work.

²The function `rand()` is not cryptographically strong, and our use of the mod function will not create a uniform distribution in the range -1000 to 1000. You do not need to "seed" the random number generator for this assignment. C++11 has introduced a library for producing "good" random numbers, but using it is more complicated and the better quality random numbers provided by the library is not needed for this assignment.

```
nuClicks = t.elapsed();
```

- (d) Time how long it takes the function `maxSubSum2` to find the maximum subsequence sum, using the same n elements.
- (e) Time how long it takes the function `maxSubSum4` to find the maximum subsequence sum, again using the same n elements. (Yes, this is function number 4; I am using the textbook's name for the functions.)

Note: Here are three suggestions to help you:

First, after debugging your code, turn off your debugger. Do not run any other program while solving this problem. Your program should take no more than 20 min. (My code took much less.)

Second, make sure when you print the running times you are printing enough significant digits. Here are two choices for how to do this:

```
cout.setf( ios::fixed, ios::floatfield );  
cout.precision( 6 );
```

or

```
cout.precision(numeric_limits<double>::digits10 + 1);
```

Third, we are using the clock function (you need to add the header `ctime` or `time.h`) that allows us to get an estimate of the CPU time spent on the program. The problem is, different systems keep track of the time differently. My computer's clock function returns a value in units of (approx) 1,000,000 of a second. Other computers have a clock that returns a value of (approx) 1000 of a second. Therefore, some short time intervals are distinguishable from zero on my computer, but not on other computers.

To determine the resolution used on your computer type:

```
cout << CLOCKS_PER_SEC << endl;
```

For the written homework problem 7, if you get a running time of 0 when you run the linear time algorithm, then run that particular function with the same input multiple times³ and then divide by the number of times you ran the program.

Be aware that the measurements you are getting are "rough" because other factors will influence the time. If you wanted a more accurate time estimate you would run each algorithm on for a fixed value of n several times and average the results.

2. For the code snippets 2b through 2e determine the running time for the following values of n : $2^8 = 256$, $2^9 = 512$, $2^{10} = 1024$, $2^{11} = 2048$, and $2^{12} = 4096$.

³E.g. clock how long it takes to run the algorithm 10,000 times and then divide by 10,000 to get an estimate that is sufficient for this assignment.

Written Part:

1. Write each of the following functions in Big-Oh notation:

(a) $T(n) = 12n - 204$

(b) $T(n) = \frac{3}{2}n^2 + \frac{5}{2}n + 0.24$

(c) $T(n) = 2n^3 + 2n + 2n \cdot \log(n)$

(d) $T(n) = 10 \cdot n^2 + 0.002n + 82$

(e) $T(n) = (2n^2 + 4 \cdot \log n) \cdot 10n$

(f) $T(n) = 34 \log(n^5) + \frac{2}{3}n$

(g) $T(n) = \frac{4n \cdot \log(n)(3n \cdot \log(n) + 2n^2)}{n}$

(h) $T(n) = \binom{n}{2}$ (This means n choose 2)

(i) $T(n) = \binom{n}{3}$ (This means n choose 3)

2. For each of the following code fragments⁴, determine the worst case running time using Big-Oh notation as a function of n .

(a)

```
// a, b, c, d, e are integers
a = b + c;
d = b + e;
```

(b)

```
int sum = 0;
for (int i = 0; i < n; i++)
    ++sum;
```

(c)

```
int sum = 0;
for(int i = 0; i < n; i++)
    for(int j = 0; j < n; ++j)
        ++sum;
```

⁴Some of these problems are from Weiss' book.

- (d)

```
int sum = 0;
for(int i = 0; i < n; i++)
    for(int j = 0; j < i; ++j)
        ++sum;
```
- (e)

```
int sum = 0;
for(int i = 0; i < n; i++)
    for(int j = 0; j < n; ++j)
        for(int k = 0; k < n; ++k)
            ++sum;
```
- (f)

```
int sum = 0;
for (int i = 0; i < n; i++)
    sum += i;
for (int j = 0; j < n; j++)
    sum += j;
for (int k = 0; k < n; k++)
    sum += k;
```
- (g)

```
int sum = 0;
for (int i = 0; i < n; i++)
{
    sum += i;
    for (int j = 0; j < n; j++)
        sum += j;
}
```
- (h)

```
int sum = 0;
for (int i = 0; i < n; i++)
{
    sum += i;
    for (int j = 0; j < n; j++)
    {
        sum += j;
        for (int k = 0; k < n; k++)
            sum += k;
    }
}
```
- (i)

```
int sum = 0;
for (int i = 1; i < n; i*=2)
{
    sum += i;
}
```

```

(j)   int sum = 0;
      for (int i = 1; i < n; i*=2)
      {
          sum += i;
          for (int j = 0; j < n; j++)
          {
              sum += j;
          }
      }

```

```

(k)   int sum = 0;
      while (n>0)
      {
          cout<< n%2;
          sum += n%2;
          n/=2;
      }

```

3. For the following functions, order them by their rates of growth from fastest to slowest: $n, \sqrt{n}, n^{1.5}, n^2, n \log n, n \log^2 n, n/2, n^3$. Indicate which functions grow at the same rate.
4. Suppose a program takes 0.05 seconds to run on input size of 2048. Estimate how long it would run for an input size of 2^{13} if:
 - (a) the program had an $O(n)$ running time.
 - (b) the program had an $O(n^2)$ running time.
 - (c) the program had an $O(n^4)$ running time.
5. Suppose you had a very complicated code that was difficult to analyze. To get a quick idea of your algorithm's running time you ran your program on different sized inputs. Suppose the following are the timing results for your algorithm. Using the timing results below, indicate the most likely running time in big-Oh notation; choose one from the following list. $O(1), O(n), O(n^2), O(n^3), O(n^4)$.

n	time
2^7	0.002094
2^8	0.00834
2^9	0.033412
2^{10}	0.133054
2^{11}	0.532501
2^{12}	2.12835

- Using the definition of *Big-Oh*, show that $3n^2 + 2n \log(n) + 6n + 19 = O(n^2)$.
- Look at the output from the programming part 1 of this assignment. Create a chart of your answers including times for all three algorithms and for all the specified input sizes, e.g.

Actual Times:

n	maxSubsequenceSum1 $O(n^3)$	maxSubsequenceSum2 $O(n^2)$	maxSubsequenceSum4 $O(n)$
128	0.00228	6.2e-05	3e-06
256	0.01676	0.000237	2e-06
.			
.			
.			

- Create another chart that estimates the running time for each of the algorithms using the method presented in class, and using the time your computer took for the algorithms when $n = 2^7$. (If you did not receive valid answers, use the run times from question 7.) Display your answer in a chart, e.g.

Predicted Times:

n	Exp. maxSubseq. 1 $O(n^3)$	Exp. maxSubseq. 2 $O(n^2)$	Exp. maxSubseq. 4 $O(n)$
256	0.01824	0.000248	6e-06
512	0.14592	0.000992	1.2e-05
1024	...		
2048			
4096			

- Using the method given in class, predict how long each algorithm would take if $n = 2^{18}$. Show how you made your prediction by providing the formula (presented in class), and then evaluate your formula.
- Using your answer from the previous question, rewrite your answer cumulatively in seconds, minutes, hours, days, and weeks. (To clarify: you are not going to re-express that time in terms of weeks and then again in terms of days and then again in terms of hours. You should only express it once, using weeks, days, hours, minutes, and seconds.)

11. Look at the output⁵ from the programming part 2 of this assignment. Create a chart of your answers including times for all four algorithms and for all the specified input sizes, e.g.

Actual Times:

n	a	b	c	d
-----	-----	-----	-----	-----
256	0.000002	0.000169	0.000072	0.046341
.				
.				
.				

Look at your output and see if it matches your predictions.

12. Circle **True** or **False**. I understand that if I don't submit a *.pdf* file for the written portion of this assignment, I will receive no credit for the written part of this assignment.
13. Circle **True** or **False**. I understand that if I don't submit code that *compiles* for the programming portion of this assignment, I will receive no credit for the programming part of this assignment.

⁵Note: the table should be filled with values from running the code, not prediction values