

- 1) +4 a) the energy of a positron / electron is $0.511 \text{ MeV}/c^2$,
So the particle is obviously relativistic.

$$\lambda = \frac{h}{p} = \frac{hc}{\sqrt{E^2 - (mc^2)^2}} = \frac{hc}{\sqrt{(k + mc^2)^2 - (mc^2)^2}}$$

$$m = 0.511 \text{ MeV}/c^2 \quad k = 450 \text{ MeV}$$

$$\lambda = 2.752 \times 10^{-6} \text{ nm} = \boxed{2.75 \text{ fm}} \quad \checkmark$$

- b) Using the same math, at this will also be relativistic:

$$m = 938.27 \text{ MeV}/c^2 \quad k = 450 \text{ MeV}$$

$$\lambda = 1.211 \times 10^{-6} \text{ nm} = \boxed{1.2 \text{ fm}} \quad \checkmark$$

- c) This one is not relativistic, but I already have the values coded in:

$$m = 3727 \text{ MeV}/c^2 \quad k = 450 \text{ MeV}$$


$$\lambda = 6.575 \times 10^{-7} \text{ nm} = \boxed{0.66 \text{ fm}} \quad \checkmark$$

Photon: $\lambda = \frac{hc}{E} = \boxed{2.76 \text{ fm}} \quad \checkmark$

All these values are less than the photon.

The only one able to probe will be the alpha particle, as:
The hydrogen nucleus is 1.7 fm across,
so the proton would work too.

 Positron / Proton

alpha.


The hydrogen nucleus can actually stop the
Alpha particle.

2.

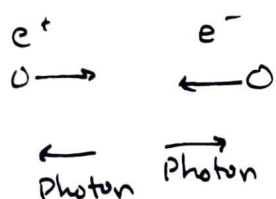
+4

$$\theta_2 = \sin^{-1}\left(\frac{n\lambda}{E}\right) \Rightarrow \sin^{-1}\left(\frac{2(0.167)\text{nm}}{0.215\text{nm}}\right) = \sin^{-1}\left(\frac{0.334\text{nm}}{0.215\text{nm}}\right)$$

arc sin is ~~only~~ defined for -1 to 1, so θ_2 is undefined. What this reflects is the electron being reflected back into the material, thus it's not detected outside the material.

3.

+2



a) $3 \times 10^6 \text{ m/s} < 0.1 c \rightarrow \text{Non-relativistic} \checkmark$

$$\lambda = \frac{h}{p} = \frac{hc}{mvc} = \frac{hc}{mc^2(\frac{v}{c})}$$

$$= 0.243 \text{ nm} \checkmark$$

$$m = 0.511 \text{ MeV}/c^2$$

$$\frac{v}{c} = 0.01$$

b) the energy will be evenly split for everything, so:
(non-relativistic)

$$K = \frac{1}{2}mv^2 = \frac{1}{2}mc^2\left(\frac{v}{c}\right) = E_{\text{photon}} = \cancel{25\text{eV}}$$

$$E = hf = \frac{hc}{\lambda} \rightarrow \lambda = \frac{hc}{E} = \frac{hc}{\frac{1}{2}mc^2\left(\frac{v}{c}\right)^2} = \frac{2hc}{mc^2\left(\frac{v}{c}\right)^2} = \cancel{485\text{nm}}$$

$$P = \frac{E}{c} \Rightarrow \cancel{25\text{eV}/c}$$

The electron and positrons TOTAL energy goes into the photons, including their mass energy.

c) Wavelength is not conserved.

$$\lambda_c = \frac{mc}{mc^2(\frac{v}{c})} = \frac{hc}{mc^2(\frac{v}{c})}$$

$$\lambda_{\text{photon}} = \frac{2hc}{(mc^2)(\frac{v}{c})^2} \quad \text{Consistent}$$

ratio of $2(\frac{c}{v})^2 \rightarrow$ this is not a pure conservation of ~~momentum~~ wavelength.