# Critique of Right for the Right Reasons: Training Neural Networks to be Interpretable, Robust, and Consistent with Expert Knowledge

#### William Jardee

WILLJARDEE@GMAIL.COM

Physics Department Montana State University Bozeman, MT 59715, USA

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$$\mathcal{L}(\theta, \mathbf{X}, y, A) = \underbrace{\sum_{n=1}^{N} \sum_{k=1}^{K} -y_{nk} \log(\hat{y}_{nk})}_{\text{Right Reason (Cross-Entropy)}} + \underbrace{\lambda_{1} \sum_{n=1}^{N} \sum_{d=1}^{D} \left[ A_{nd} \frac{\partial}{\partial x_{nd}} \sum_{k=1}^{K} \log(\hat{y}_{nk}) \right]^{2}}_{\text{Right Reasons}} + \underbrace{\lambda_{2} \sum_{i} \theta_{i}^{2}}_{\text{Regularizer}}$$
(Equation 1)

$$\mathcal{L}(\{\theta_{m}\}) = \underbrace{\sum_{m} \mathbb{E}_{p(x,y)} \left[ -\log(p(y|f(x;\theta_{m}))) \right]}_{\text{Predictive Term (Cross-Entropy)}} + \underbrace{\lambda \sum_{l \neq m} \mathbf{IndepErr} \left( f(\cdot;\theta_{m}), f(\cdot;\theta_{l}) \right)}_{\text{Diversity Measurement}}$$

$$\approx \underbrace{\sum_{m} \mathbb{E}_{p(x,y)} \left[ -\log(p(y|f(x;\theta_{m}))) \right]}_{\text{Predictive Term (Cross-Entropy)}} + \underbrace{\lambda \sum_{l \neq m} \mathbf{CosIndepErr} \left( f(\cdot;\theta_{m}), f(\cdot;\theta_{l}) \right)}_{\text{Diversity Measurement}}$$
(Equation 3)

where

$$\mathbf{IndepErr}(f,g) = \mathbb{E}\left[\left(f(x_{g_{\max}}) - f(x)\right)^2\right] \approx \left(\epsilon \, \boldsymbol{\nabla} f(x) \cdot \boldsymbol{\nabla} g(x)\right)^2 \left(\frac{\boldsymbol{\nabla} f(x) \cdot \boldsymbol{\nabla} g(x)}{|f(x)|_2 |g(x)|_2}\right)^2 \equiv \cos^2(\boldsymbol{\nabla} f(x), \boldsymbol{\nabla} g(x)) \equiv \cos^2(\boldsymbol{\nabla} f(x), \boldsymbol{\nabla} g(x)) = \cos^2(\boldsymbol{\nabla} f(x), \boldsymbol{\nabla} g(x))$$

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## Equation (1)

- 4. Algorithm Experiments
- 5. Application of Algorithm in Adversarial Context
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