

Introduction to Logic Programming – WS 2022 Programming project

1 Submission and evaluation

It is sufficient if your submission passes all tests and benchmarks reasonably to be admitted to write the final exam. The runtime of your submission is not important. Of course, it is not acceptable to hard code any test.

You should work on the project alone. You can of course exchange information with one another, but please do not share any code.

Please contact us early if you have any problems or questions. You can either send an email to joshua.schmidt@hhu.de, visit the tutorials or use the forum in the ILIAS.

Deadline: February 8, 2023

Exam: February 15, 2023

Submit your solution as a zip archive in the ILIAS.

2 Task: SAT Solver

The goal is to implement a Prolog programm that is able to transform propositional logic formulas into conjunctive normalform and solve them afterwards using the DPLL algorithm as discussed in the lecture. Please use the file sat_solver.pl for your implementation.

The input is a syntax tree that is built recursively from the following Prolog terms:

- literals lit(...)
 - the constants lit(true) and lit(false)
 - Prolog variables such as lit(X)
- the equivalence $\rho \Leftrightarrow \phi$, in Prolog equivalence (ρ, ϕ)
- the implication $\rho \Rightarrow \phi$, in Prolog implies (ρ, ϕ)
- the conjunction $\rho \wedge \phi$, in Prolog and (ρ, ϕ)
- the disjunction $\rho \vee \phi$, in Prolog or (ρ, ϕ)

- the negation $\neg \rho$, in Prolog not(ρ)
- exactly_one_pos(ListOfVars): exactly one variable in ListOfVars is true
- min_one_pos(ListOfVars): at least one variable in ListOfVars has to be true

The terms can be nested arbitrarily.

Your SAT solver should provide three Prolog predicates:

- normalise(+Formula, -NFormula) The first argument is a propositional logic formula using the terms described above. This predicate should normalise the input formula to only use constants, variables, conjunction, disjunction, and negation. Your implementation thus has to rewrite equivalences, implications, and the terms exactly_one_pos/1 and min_one_pos/1.
- to_cnf(+Formula, -CNF). The first argument is a propositional logic formula using the terms described above. Your implemenation should call normalise/2 for the input formula first. The conjunctive normalform should be returned as a list of lists in the second argument. Hereby, each inner list is a clause (a disjunction) while the list of lists is connected by a conjunction.

Examples:

- and(lit(X),lit(true)) is transformed to [[X],[true]]
- and(lit(X), or(lit(true), lit(false)) is transformed to [[X],[true,false]]

The negation is still represented as the term not/1: and(not(lit(X)),lit(true)) is transformed to [[not(X)],[true]].

• solve(+CNF). The predicate receives a CNF as returned by to_cnf/2 and tries to find an assignment of variables occurring in CNF that make the formula satisfiable. The variables (X in the above example) should be assigned with either true or false. The predicate should fail if there exists no satisfiable assignment of variables for a propositional logic formula. Implement the DPLL algorithm for this as discussed in the lecture. That means, you should implement unit propagation, clause simplification, and variable branching.

The benchmarks can be found in resources/sat_benchmarks/ and can be run using run_benchmarks/0 in sat_benchmarks.pl.

Note that the problem of satisfiability solving is NP-completeness.

The file large_formula_example.cnf contains a more complex propositional logic formula which your solver can probably not solve in a reasonable amount of time. In order to do so, we need more sophisticated techniques of SAT solving such as conflict-driven clause learning or a watched literals scheme. Such techniques are not discussed in the lecture since they are beyond the scope of this introductory course.