## July 10, 2012 Room 5.4 (2 pm to 7 pm):

## **Introduction to Combinatorial Optimization**

(tailored for students who did not follow an Operations Research course):

### Contents

- 1. Introduction: Some easy examples
- 2. Linear Programming
- 3. Optimization problems
- 4. Integer Linear Programming

**July 17, 2012** Room 5.1, with possible change to room 4.2 (2 pm to 7 pm):

# **Approximate Solution of Optimization Problems**

#### Contents

- 1. Mathematical model of combinatorial optimization problems
- 2. Approximation algorithms
- 3. Heuristic algorithms
- 4. Metaheuristic algorithms

**October 29, November 5, November 12, November 19, 2012** Room 5.5 (2 pm to 7 pm):

# Models and Algorithms for Matching and Assignment Problems (4 lectures, 5 hours each) Contents

- 1. Introduction: matching, assignment, graphs, bipartite graphs, adjacency matrix, incidence matrix;
- **2.** Theoretical foundations: matching problems, Hall's marriage theorem, Koenig's algorithm, augmenting path, complexity, stable marriage problem;
- **3. Maximum matching applications**: vehicle scheduling, time slot assignment (TDMA), open shop scheduling;
- **4. Linear sum assignment problem**: weighted matching, constraint matrix, unimodularity, duality, Egervary's theorem, initialization algorithms;
- **5. The Hungarian algorithm:** main structure, rooted alternating tree, complexity, Kuhn's algorithm, Jacobi's theorem;
- **6. Non-Hungarian algorithms:** Dinic-Kronrod's algorithm, primal simplex algorithms, Egervary's algorithm, Birkhoff-Von Neumann theorem;
- **7. Other linear assignment problems:** k-cardinality assignment, bottleneck assignment, threshold algorithm , balanced assignment ;
- **8. Quadratic assignment problems:** combinatorial formulation, complexity, integer quadratic formulation, inner product formulation, trace formulation, exact solution, heuristics.

The slides of each lecture will be available few days in advance at my site: http://www.or.deis.unibo.it/staff\_pages/martello/cvitae.html --> Courses --> PhD courses