

P1. $\bar{x} = 21$; $G = \sqrt{437}$; $a, b \in \mathbb{R} / b > a$

$$\frac{a+b}{2} = 21, \sqrt{ab} = \sqrt{437}$$

$$a = 42 - b, ab = 437$$

$$(42-b)(b) = 437 \Rightarrow b^2 - 42b + 437 = 0$$

$$(b-19)(b-23) = 0$$

$$b_1 = 19 ; b_2 = 23$$

$$\underline{b = 23}$$

P2. $\frac{x+21}{n+1} = \frac{x}{n} + 2$; $\frac{x+3}{n+1} = \frac{x}{n} - 1$

$$\textcircled{1} n(x+21) = (n+1)(x+2n) ; n(x+3) = (n+1)(x-n) \textcircled{2}$$

$$\textcircled{1} - \textcircled{2}$$

$$n(x+21-x-3) = (n+1)(x+2n-x+n)$$

$$18n = 3n^2 + 3n$$

$$5n = n^2$$

$$5 = n$$

$$\underline{n = 5}$$

P3. $\bar{x}_1 = 75 ; n = 1 ; \bar{x}_2 = 85 ; n = 2 ; \bar{x}_3 = 70 ; n = 3 ;$

$$\bar{x}_4 = 60 ; n = 4 ; \bar{x}_5 = 55 ; n = 5$$

$$a+b+c+d+e \rightarrow \Sigma \text{ califs.}$$

$$\bar{x}_1 = a$$

$$\bar{x}_5 = \frac{4\bar{x}_4 + e}{5}$$

$$\bar{x}_2 = \frac{a+b}{2}$$

$$\bar{x}_5 = 55 = \frac{4(60) + e}{5}$$

$$\bar{x}_3 = \frac{a+b+c}{3}$$

$$55(5) = 4(60) + e$$

$$\bar{x}_4 = \frac{a+b+c+d}{4}$$

$$e = 35$$

$$\bar{x}_5 = \frac{a+b+c+d+e}{5}$$

$$\underline{\text{Ultima calificación} = 35}$$

P4.

x	f	$f \cdot x$	$\Sigma(f \cdot x) = \bar{x}$	$n = 20$
5	1	5	$5 \cdot 1 + 6 \cdot 2 + 7 \cdot 4 + 8 \cdot 7 + 9 \cdot 4 + 10 \cdot 2 = 157$	$\therefore \frac{157}{20} = 7.85$
6	2	12		
7	4	28		
8	7	56		
9	4	36		
10	2	20		
Σ	20	157	$\bar{x} = 7.85$	

P5.

x	f	$f \cdot x$	$f \cdot x^2$	$n = 20 \Rightarrow n < 31 \Rightarrow s^2$
5	1	5	25	$\bar{x} = \frac{157}{20} = 7.85$
6	2	12	72	$s^2 = \frac{\Sigma(f \cdot x^2)}{n-1} - \frac{\Sigma^2(f \cdot x)}{n^2 - n}$
7	4	28	196	$s^2 = \frac{1265}{19} - \frac{157^2}{20^2 - 20}$
8	7	56	448	$s^2 = \frac{651}{380} = 1.7132$
9	4	36	324	
10	2	20	200	
	20	157	1265	$s^2 = \frac{651}{380}$

P6.

#	Close	int. d/close	F	x_i	F/x_i	LRI - LRS	F	$F \cdot x$
1	1.0-3.0	0.9	1	2	1/2	0.95-3.05	1	2
2	3.1-5.1		3	4.1	30/41	3.05-5.15	4	12.3
3	5.2-7.2		6	6.2	30/31	5.15-7.25	10	37.2
Mo Md	7.3-9.3		25	8.3	250/83	7.25-9.35	35	207.5
5	9.4-11.4		17	10.4	85/152	9.35-11.45	52	176.8
P95	11.5-13.5		8	12.5	16/25	11.45-13.55	60	100
Σ			60	43.5	7.4861			535.8

$$H = n \Sigma^{-1} (F/x_i) = 60(7.4861)^{-1} = 8.0149$$

$$Md: Md_m = \frac{60+1}{2} = 30.5 \rightarrow 30$$

$$Md = 7.25 + \left[\frac{30-10}{29} \right] (2.1) = 8.93$$

$$Mo: 7.25 + \left[\frac{25-6}{2(25)-6-17} \right] (2.1) = 8.7278$$

$$P_{95}: P_{95\text{ pos}} = \frac{60(95)}{100} = 57 \Rightarrow P_{95} = 11.45 + \left[\frac{57-52}{8} \right] (2.1) = 12.7625$$

$$n > 30 \Rightarrow \sigma^2 = \frac{\Sigma x_i^2}{n} - \bar{x}^2 = \frac{5096.09}{60} - (8.93)^2 = 5.1891$$

a) $H = 8.0149$; b) $Md = 8.93$; c) $Mo = 8.7278$; d) 12.7625 ; e) 5.1891