Waveguide Solver

2.1

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Chapter 1

Shape-Optimization of a 3D waveguide using dealii, transformation optics and the finite element method

1.1 Topics of this project

This project began as the implementation used in the thesis for the title of Master of Science by Pascal Kraft at the KIT. It is continued for his PHD studies and possibly as an introduction to dealii for other students in the same research group. This project, apart from mathematical goals, aims at creating a clear and reusable implementation of the the finite element method for Maxwell's equaations in a range of performance values, that enable the inclusion of an optimization-scheme without crippling time- or CPU-time consumption. Therefore the code should fullfill the following criteria:

- 1. The code should be readable to starters (educational purpose),
- 2. The code should be maintainable (reusability),
- 3. The code should be paralellizable via MPI or CUDA (both will be tested as a part of the phd-proceedings),
- 4. The code should perform well under the given circumstances,
- 5. The code should give scientific results and not only operate on marginal domains of parameter-values,
- 6. The code should be portable to other hardware-specifications then those on the given computer at the workspace (i.e. the performance should be usable in large-scale computations for example in Super← Computers of the KIT"s SCC.

These demands led to the introduction of a software development scheme for the work on the code based on agile-development and git.

1.2 Prerequisites of this project

In order to be able to work with this code it is important to first achieve a fundamental understanding of the following topics: First and foremost, an understanding of the finite element method is required and completely unreplacable. There exists extensive documentation on this topic and the reader should be aware of the fact, that the mathematical background cannot be understood without this knowledge. However, there are further demands. The programming-language of both this project and dealii itself is C++. This language also forms the backbone id CUDA and manu other, relevant libraries. It is to be considered inevitable in this field. "The vhoice of this language in a wau reduces the importance of the need for a performanc implementation on the code level *on the functional or theoretical level this obviously has a very miimal influence on the performanc.(. Also it should be noted that there exists a very large documentation about dealii which might help the reader understand this code. Lastly dealii is basically only available on Linux since it nearly always requires a build-process which would not be possible with out enormous problems on different OS. As far as mathematical knowledge is concerned, a basic education in linear algebra, krylov subspace methods, transformation-optics, functional analysis, optics and optimization theory will further the understanding of both the code and this documentation of it.

2 Shane-Ontimization	n of a 3D wavequide using deal	i transformation ontics an	d the finite element method
2 Onupe Optimizatio	in or a ob waveguide asing dean	i, transformation optics an	nd the finite element method
Author			
Pascal Kraft			

Version

2.1

Chapter 2

Hierarchical Index

2.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

FaceSurfaceComparator
FaceSurfaceComparatorZ
Function
ExactSolution
SolutionWeight < dim >
GradientTable
HSIE_Dof_Type < hsie_order >
Inhomogenous Transformation Rectangle
MeshGenerator 98
RoundMeshGenerator
SquareMeshGenerator
ModeManager
Optimization
AdjointOptimization
OptimizationAlgorithm< datatype >
OptimizationAlgorithm< double >
OptimizationCG
OptimizationSteepestDescent
$Optimization Algorithm < std::complex < double >> \dots \dots$
Optimization1D
Parameters
PointVal
PreconditionBase
HSIEPreconditionerBase< hsie_order >
PreconditionerSweeping
Sector < Dofs_Per_Sector >
Sector < 2 >
Sector < 3 >
ShapeDescription
SpaceTransformation
DualProblemTransformationWrapper
Homogenous Transformation Circular
Homogenous Transformation Rectangular
InhomogenousTransformationCircular

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ParameterReader		 			 							. 119
tagGSPHERE		 										169
Wayaquida												160

Chapter 3

Class Index

3.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

AdjointOptimization	
Derived from the Optimization class, this class implements an Optimization-scheme based on	
an adjoint method	7
DualProblemTransformationWrapper	
If we do an adjoint computation, we need a SpaceTransformation, which has the same properties	
as the primal one but measures in transformed coordinates	10
ExactSolution	
This class is derived from the Function class and can be used to estimate the L2-error for a	
straight waveguide	25
FaceSurfaceComparator	29
FaceSurfaceComparatorZ	30
GradientTable	
The Gradient Table is an OutputGenerator, intended to write information about the shape gradient	
to the console upon its computation	31
HomogenousTransformationCircular	
For this transformation we try to achieve a situation in which tensorial material properties from	
the coordinate transformation and PML-regions dont overlap	32
Homogenous Transformation Rectangular	
For this transformation we try to achieve a situation in which tensorial material properties from	
the coordinate transformation and PML-regions dont overlap	47
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Inhomogenous Transformation Circular	
In this case we regard a tubular waveguide and the effects on the material tensor by the space	
transformation and the boundary condition PML may overlap (hence inhomogenous space trans-	
formation)	68
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This class is an abstract interface to describe the general workings of an optimization scheme .	102

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This class implements the computation of an optimization step by doing 1D optimization based	
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This class is used to gather all the information from the input file and store it in a static object available to all processes	119
Parameters	119
This structure contains all information contained in the input file and some values that can simply	
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This class implements the DeallI preconditioner interface and offers a sweeping preconditioning	
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RoundMeshGenerator	,
This class generates meshes, that are used to discretize a rectangular Waveguide	133
Sector Soft Per Sector	
Sectors are used, to split the computational domain into chunks, whose degrees of freedom are	
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SolutionWeight< dim >	
This function has internal usage to execute a function only on the interior of the Waveguide	149
Space Transformation 5	
Encapsulates the coordinate transformation used in the simulation	152
SquareMeshGenerator	
This class generates meshes, that are used to discretize a rectangular Waveguide	163
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This class encapsulates all important mechanism for solving a FEM problem	169

Chapter 4

Class Documentation

4.1 AdjointOptimization Class Reference

Derived from the Optimization class, this class implements an Optimization-scheme based on an adjoint method.

```
#include <AdjointOptimization.h>
```

Inheritance diagram for AdjointOptimization:



Public Member Functions

- AdjointOptimization (Waveguide *waveguide_primal, MeshGenerator *mg, SpaceTransformation *st_← primal, SpaceTransformation *st_dual, OptimizationAlgorithm< std::complex< double >> *Oa)
- std::vector< std::complex< double >> compute_small_step (double step)
- double compute_big_step (std::vector< double > step)
- void run ()

This function is the core implementation of an optimization algorithm.

Public Attributes

- · const int type
- Waveguide * waveguide
- SpaceTransformation * primal_st
- SpaceTransformation * dual_st
- MeshGenerator * mg
- OptimizationAlgorithm< std::complex< double >> * oa

4.1.1 Detailed Description

Derived from the Optimization class, this class implements an Optimization-scheme based on an adjoint method.

This method should prove to be far superior to a finite difference approach as soon as the shape has more then 2 degrees of freedom since its effort is always a total of 2 forward problems to solve.

Author

Pascal Kraft

Date

29.11.2016

Definition at line 20 of file AdjointOptimization.h.

4.1.2 Member Function Documentation

```
4.1.2.1 run()
void AdjointOptimization::run ( ) [virtual]
```

This function is the core implementation of an optimization algorithm.

Currently it is very fundamental in its technical prowess which can be improved upon in later versions. Essentially, it calculates the signal quality for a configurations and for small steps in every one of the dofs. After that, the optimization-step is estimated based on difference-quotients. Following this step, a large step is computed based upon the approximation of the gradient of the signal-quality functional and the iteration starts anew. If a decrease in quality is detected, the optimization-step is undone and the step-width is reduced. This function controls both the Waveguide- and the Waveguide-structure object.

Implements Optimization.

Definition at line 201 of file AdjointOptimization.cpp.

```
201
202
       Convergence_Table.set_auto_fill_mode(true);
203
       bool run = true;
204
        int counter = 0;
205
       double quality = 0;
206
207
        while (run) {
208
          int small steps = 0;
209
          while (oa->perform_small_step_next(small_steps)) {
             deallog << "Performing a small step." << std::endl;
double temp_step_width = oa->get_small_step_step_width(small_steps);
210
211
212
             oa->pass_result_small_step(compute_small_step(temp_step_width));
213
             small_steps++;
214
215
216
           if (oa->perform_big_step_next(small_steps)) {
             deallog << "Performing a big step." << std::endl;
std::vector<double> step = oa->get_big_step_configuration();
217
218
             deallog << "Got the following big step configuration: ";
for (unsigned int i = 0; i < step.size(); i++) {
  deallog << step[i] << " , ";</pre>
219
220
221
```

```
223
         deallog << std::endl;</pre>
224
         quality = compute_big_step(step);
         oa->pass_result_big_step(
225
             primal_st->evaluate_for_z(GlobalParams.M_R_ZLength / 2.0, waveguide));
226
2.2.7
228
229
       counter++;
230
       231
232
233
234
         run = false:
235
236
237
       if ((GlobalParams.O_C_D_ConvergenceFirst ||
           GlobalParams.O_C_D_ConvergenceAll) &&
(GlobalParams.MPI_Rank == 0)) {
238
239
240
         std::ofstream result_file;
         result_file.open((solutionpath + "/convergence_rates.dat").c_str(),
241
242
                         std::ios_base::openmode::_S_trunc);
243
244
         Convergence_Table.write_text(
         result_file,
245
             dealii::TableHandler::TextOutputFormat::table_with_headers);
246
247
         result_file.close();
248
        result_file.open((solutionpath + "/convergence_rates.tex").c_str(),
249
                          std::ios_base::openmode::_S_trunc);
250
         Convergence_Table.write_tex(result_file);
2.51
         result_file.close();
252
        result_file.open((solutionpath + "/steps.dat").c_str(),
253
254
                         std::ios_base::openmode::_S_trunc);
255
         oa->WriteStepsOut(result_file);
256
         result_file.close();
2.57
258 }
259 }
```

4.1.3 Member Data Documentation

4.1.3.1 type

const int AdjointOptimization::type

Initial value:

=

Definition at line 22 of file AdjointOptimization.h.

The documentation for this class was generated from the following files:

- · Code/OptimizationStrategies/AdjointOptimization.h
- Code/OptimizationStrategies/AdjointOptimization.cpp

4.2 DualProblemTransformationWrapper Class Reference

If we do an adjoint computation, we need a SpaceTransformation, which has the same properties as the primal one but measures in transformed coordinates.

#include <DualProblemTransformationWrapper.h>

Inheritance diagram for DualProblemTransformationWrapper:



Public Member Functions

DualProblemTransformationWrapper (SpaceTransformation *non dual st, int rank)

Since this object encapsulates another Space Transformation, the construction is straight forward.

Point< 3 > math_to_phys (Point< 3 > coord) const

One of the core functionalities of a SpaceTransformation is to map a mathematical coordinate to a physical one (so an transformed to an untransformed coordinate).

• Point < 3 > phys to math (Point < 3 > coord) const

This function does the same as math_to_phys only in the opposit direction.

bool is_identity (Point< 3 > coord) const

In order to test implementation, this function was added to check, if the transformation-tensor at a given coordinate is the identity or not.

- Tensor< 2, 3, std::complex< double > > get_Tensor (Point< 3 > &coordinate) const
- Tensor < 2, 3, std::complex < double >> get_Preconditioner_Tensor (Point < 3 > &coordinate, int block)
 const
- Tensor< 2, 3, std::complex< double >> **Apply_PML_To_Tensor** (Point< 3 > &coordinate, Tensor< 2, 3, double > Tensor input) const
- Tensor< 2, 3, std::complex< double > > Apply_PML_To_Tensor_For_Preconditioner (Point< 3 > &coordinate, Tensor< 2, 3, double > Tensor input, int block) const
- Tensor < 2, 3, double > get Space Transformation Tensor (Point < 3 > &coordinate) const
- Tensor< 2, 3, double > **get_Space_Transformation_Tensor_Homogenized** (Point< 3 > &coordinate) const
- bool PML_in_X (Point< 3 > &position) const

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the x-axis.

bool PML in Y (Point < 3 > &position) const

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the y-axis.

bool PML in Z (Point < 3 > &position) const

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the *z*-axis.

double Preconditioner_PML_Z_Distance (Point < 3 > &p, unsigned int block) const

This function fulfills the same purpose as those with similar names but it is supposed to be used together with Preconditioner_PML_in_Z instead of the versions without "Preconditioner".

double PML_X_Distance (Point< 3 > &position) const

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

double PML_Y_Distance (Point< 3 > &position) const

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

double PML Z Distance (Point < 3 > &position) const

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

· void estimate and initialize ()

At the beginning (before the first solution of a system) only the boundary conditions for the shape of the waveguide are known.

• double get Q1 (double z) const

This member calculates the value of Q1 for a provided *z*-coordinate.

• double get Q2 (double z) const

This member calculates the value of Q2 for a provided *z*-coordinate.

double get_Q3 (double z) const

This member calculates the value of Q3 for a provided *z*-coordinate.

• double get_dof (int dof) const

This is a getter for the values of degrees of freedom.

· void set dof (int dof, double value)

This function sets the value of the dof provided to the given value.

· double get free dof (int dof) const

This is a getter for the values of degrees of freedom.

void set_free_dof (int dof, double value)

This function sets the value of the dof provided to the given value.

• std::pair< int, double > Z to Sector and local z (double in z) const

Using this method unifies the usage of coordinates.

double System_Length () const

Returns the complete length of the computational domain.

• double Sector_Length () const

Returns the length of one sector.

· double Layer_Length () const

Returns the length of one layer.

double get_r (double in_z) const

Returns the radius for a system-coordinate;.

• double get_m (double in_z) const

Returns the shift for a system-coordinate;.

• double get_v (double in_z) const

Returns the tilt for a system-coordinate;.

- int Z_to_Layer (double) const
- Vector< double > Dofs () const

Other objects can use this function to retrieve an array of the current values of the degrees of freedom of the functional we are optimizing.

· unsigned int NFreeDofs () const

This function returns the number of unrestrained degrees of freedom of the current optimization run.

unsigned int NDofs () const

This function returns the total number of DOFs including restrained ones.

• bool IsDofFree (int) const

Since Dofs() also returns restrained degrees of freedom, this function can be applied to determine if a degree of freedom is indeed free or restrained.

· void Print () const

Console output of the current Waveguide Structure.

std::complex< double > evaluate_for_z (double z_in, Waveguide *)

Since the Wavegudie itself may be circular or rectangular now, the evaluation routines should be moved to a point in the code where this information is included in the code.

- std::complex < double > evaluate for z with sum (double, double, Waveguide *)
- std::complex< double > gauss_product_2D_sphere (double z, int n, double R, double Xc, double Yc, Waveguide *in_w)

Public Attributes

- · const double XMinus
- · const double XPlus
- · const double YMinus
- · const double YPlus
- · const double ZMinus
- · const double ZPlus
- std::vector< Sector< 3 > > case sectors

This member contains all the Sectors who, as a sum, form the complete Waveguide.

const double epsilon_K

The material-property ϵ_r has a different value inside and outside of the waveguides core.

· const double epsilon_M

The material-property ϵ_r has a different value inside and outside of the waveguides core.

· const int sectors

Since the computational domain is split into subdomains (called sectors), it is important to keep track of the amount of subdomains.

const double deltaY

This value is initialized with the value Delta from the input-file.

Vector< double > InitialDofs

This vector of values saves the initial configuration.

SpaceTransformation * st

4.2.1 Detailed Description

If we do an adjoint computation, we need a SpaceTransformation, which has the same properties as the primal one but measures in transformed coordinates.

This Wrapper contains the space transformation of the primal version but maps input parameters to their dual equivalent.

Essentially this class enables us to write a waveguide class which is unaware of its being primal or dual. Using this wrapper makes us compute the solution of the inverse order shape parametrization.

Author

Pascal Kraft

Date

1.12.2016

Definition at line 26 of file DualProblemTransformationWrapper.h.

4.2.2 Constructor & Destructor Documentation

4.2.2.1 DualProblemTransformationWrapper()

```
\label{lem:polem:non_dual_st} \mbox{DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::DualProblemTransformationWrapper::Du
```

Since this object encapsulates another Space Transformation, the construction is straight forward.

Parameters

non_dual⇔	This pointer points to the actual transformation that is being wrapped.
_st	

Definition at line 22 of file DualProblemTransformationWrapper.cpp.

```
: SpaceTransformation(3, inner_rank),
25
          XMinus(-(GlobalParams.M_R_XLength * 0.5 - GlobalParams.M_BC_XMinus)),
26
          XPlus(GlobalParams.M_R_XLength * 0.5 - GlobalParams.M_BC_XPlus),
          YMinus(-(GlobalParams.M_R_YLength * 0.5 - GlobalParams.M_BC_YMinus)),
YPlus(GlobalParams.M_R_YLength * 0.5 - GlobalParams.M_BC_YPlus),
2.7
28
          ZMinus (-GlobalParams.M_R_ZLength * 0.5),
29
          ZPlus(GlobalParams.M_R_ZLength * 0.5),
30
          epsilon_K(GlobalParams.M_W_epsilonin),
32
          epsilon_M(GlobalParams.M_W_epsilonout),
33
          {\tt sectors} \, ({\tt GlobalParams.M\_W\_Sectors}) \, ,
34
          deltaY(GlobalParams.M_W_Delta) {
     st = in_st;
35
36
    homogenized = st->homogenized;
```

4.2.3 Member Function Documentation

4.2.3.1 Dofs()

```
Vector< double > DualProblemTransformationWrapper::Dofs ( ) const [virtual]
```

Other objects can use this function to retrieve an array of the current values of the degrees of freedom of the functional we are optimizing.

This also includes restrained degrees of freedom and other functions can be used to determine this property. This has to be done because in different cases the number of restrained degrees of freedom can vary and we want no logic about this in other functions.

Implements SpaceTransformation.

Definition at line 246 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::Dofs().

```
246 {
247     return st->Dofs();
248 }
```

4.2.3.2 estimate_and_initialize()

```
void DualProblemTransformationWrapper::estimate_and_initialize ( ) [virtual]
```

At the beginning (before the first solution of a system) only the boundary conditions for the shape of the waveguide are known.

Therefore the values for the degrees of freedom need to be estimated. This function sets all variables to appropriate values and estimates an appropriate shape based on averages and a polynomial interpolation of the boundary conditions on the shape.

Implements SpaceTransformation.

Definition at line 188 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::estimate_and_initialize().

4.2.3.3 evaluate_for_z()

Since the Wavegudie itself may be circular or rectangular now, the evaluation routines should be moved to a point in the code where this information is included in the code.

Since I dont want to create derived classes from waveguide (which I should do eventually) I will for now include this functionality into the space transformation which is shape-sensitive. The waveguide only offers the evaluation at a point. The quadrature-rule has to be imposed by the space transformation.

Implements SpaceTransformation.

Definition at line 183 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::evaluate_for_z().

```
184
185    return st->evaluate_for_z(in_z, in_w);
186 }
```

4.2.3.4 get_dof()

This is a getter for the values of degrees of freedom.

A getter-setter interface was introduced since the values are estimated automatically during the optimization and non-physical systems should be excluded from the domain of possible cases.

Parameters

dof The index of the degree of freedom to be retrieved from the structure of the modelled waveguide.

Returns

This function returns the value of the requested degree of freedom. Should this dof not exist, 0 will be returnd.

Implements SpaceTransformation.

Definition at line 205 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::get_dof().

Referenced by HomogenousTransformationCircular::Dofs().

```
205
206    return st->get_dof(dof);
207 }
```

4.2.3.5 get_free_dof()

This is a getter for the values of degrees of freedom.

A getter-setter interface was introduced since the values are estimated automatically during the optimization and non-physical systems should be excluded from the domain of possible cases.

Parameters

dof The index of the degree of freedom to be retrieved from the structure of the modelled waveguide.

Returns

This function returns the value of the requested degree of freedom. Should this dof not exist, 0 will be returnd.

Implements SpaceTransformation.

Definition at line 213 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::get_free_dof().

```
213
214   return st->get_free_dof(dof);
215 }
```

4.2.3.6 get_Q1()

```
\label{lem:const} \begin{tabular}{ll} \begin
```

This member calculates the value of Q1 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q1 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implements SpaceTransformation.

Definition at line 193 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::get_Q1().

```
193
194    return st->get_Q1(z);
195 }
```

4.2.3.7 get_Q2()

```
double DualProblemTransformationWrapper::get_Q2 ( double z ) const [virtual]
```

This member calculates the value of Q2 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q2 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implements SpaceTransformation.

Definition at line 197 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::get_Q2().

```
197
198    return st->get_Q2(z);
199 }
```

4.2.3.8 get_Q3()

```
double DualProblemTransformationWrapper::get_Q3 ( \label{eq:const} \mbox{double $z$ ) const [virtual]}
```

This member calculates the value of Q3 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q3 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implements SpaceTransformation.

Definition at line 201 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::get_Q3().

```
201 {
202    return st->get_Q3(z);
203 }
```

4.2.3.9 is_identity()

In order to test implementation, this function was added to check, if the transformation-tensor at a given coordinate is the identity or not.

Parameters

```
coord This is the coordinate to test.
```

4.2.3.10 IsDofFree()

Since Dofs() also returns restrained degrees of freedom, this function can be applied to determine if a degree of freedom is indeed free or restrained.

"restrained" means that for example the DOF represents the radius at one of the connectors (input or output) and therefore we forbid the optimization scheme to vary this value.

Implements SpaceTransformation.

Definition at line 258 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::IsDofFree().

```
258
259   return st->IsDofFree(input);
260 }
```

4.2.3.11 math_to_phys()

```
Point<br/>< 3 > DualProblemTransformationWrapper::math_to_phys (<br/> Point<br/>< 3 > coord ) const [virtual]
```

One of the core functionalities of a SpaceTransformation is to map a mathematical coordinate to a physical one (so an transformed to an untransformed coordinate).

Parameters

coord the coordinate to be transformed. In this class we simply pass the

Implements SpaceTransformation.

Definition at line 39 of file DualProblemTransformationWrapper.cpp.

```
39
40 return st->math_to_phys(coord);
41 }
```

4.2.3.12 NDofs()

```
unsigned int DualProblemTransformationWrapper::NDofs ( ) const [virtual]
```

This function returns the total number of DOFs including restrained ones.

This is the lenght of the array returned by Dofs().

Implements SpaceTransformation.

Definition at line 254 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::NDofs().

Referenced by HomogenousTransformationCircular::Dofs(), HomogenousTransformationCircular::get_dof(), HomogenousTransformationCircular::get_free_dof(), HomogenousTransformationCircular::IsDofFree(), Homogenous \leftarrow TransformationCircular::Set_dof(), and Homogenous \leftarrow TransformationCircular::set_free_dof().

```
254 {
255    return st->NDofs();
256 }
```

4.2.3.13 phys_to_math()

```
Point<br/>< 3 > DualProblemTransformationWrapper::phys_to_math (<br/> Point<br/>< 3 > coord) const [virtual]
```

This function does the same as math_to_phys only in the opposit direction.

Parameters

```
coord the coordinate to be transformed.
```

 $Implements\ Space Transformation.$

Definition at line 43 of file DualProblemTransformationWrapper.cpp.

```
43 {
44 return st->phys_to_math(coord);
45 }
```

4.2.3.14 PML_in_X()

```
bool DualProblemTransformationWrapper::PML_in_X (  Point < 3 > \& position \ ) \ const \ [virtual]
```

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the x-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

position Stores the position in which to test for presence of a PML-Material.

Implements SpaceTransformation.

Definition at line 47 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::PML_in_X().

 $Referenced \ by \ Homogenous Transformation Circular :: PML_Z_Distance ().$

```
47 {
48     return st->PML_in_X(p);
49 }
```

4.2.3.15 PML_in_Y()

```
bool DualProblemTransformationWrapper::PML_in_Y (  Point < 3 > \& position \ ) \ const \ [virtual]
```

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the y-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

position	Stores the position in which to test for presence of a PML-Material.
----------	--

Implements SpaceTransformation.

Definition at line 51 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::PML_in_Y().

Referenced by HomogenousTransformationCircular::PML_Z_Distance().

4.2.3.16 PML_in_Z()

```
bool DualProblemTransformationWrapper::PML_in_Z (  Point < 3 > \& position ) const [virtual]
```

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the z-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

	position	Stores the position in which to test for presence of a PML-Material.	
--	----------	--	--

Implements SpaceTransformation.

Definition at line 55 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::PML_in_Z().

Referenced by HomogenousTransformationCircular::PML Z Distance().

4.2.3.17 PML_X_Distance()

```
double DualProblemTransformationWrapper::PML_X_Distance ( \label{eq:point} \mbox{Point} < \mbox{3 > \& position ) const [virtual]}
```

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

Implements SpaceTransformation.

Definition at line 64 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::PML_X_Distance().

Referenced by HomogenousTransformationCircular::PML Z Distance().

```
64
65  return st->PML_X_Distance(p);
66 }
```

4.2.3.18 PML_Y_Distance()

```
double DualProblemTransformationWrapper::PML_Y_Distance ( Point< 3 > & position ) const [virtual]
```

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

position Stores the position from which to calculate the distance to the PML-surface.

Implements SpaceTransformation.

Definition at line 68 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::PML_Y_Distance().

Referenced by HomogenousTransformationCircular::PML_Z_Distance().

```
69  return st->PML_Y_Distance(p);
70 }
4.2.3.19  PML_Z_Distance()
double DualProblemTransformationWrapper::PML_Z_Distance (
```

Point< 3 > & position) const [virtual]

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

р	osition	Stores the position from which to calculate the distance to the PML-surface.
---	---------	--

Implements SpaceTransformation.

Definition at line 72 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::PML_Z_Distance().

 $Referenced \ by \ Homogenous Transformation Circular :: PML_Z_Distance ().$

```
72
73 return st->PML_Z_Distance(p);
74 }
(75)
```

4.2.3.20 set_dof()

This function sets the value of the dof provided to the given value.

It is important to consider, that some dofs are non-writable (i.e. the values of the degrees of freedom on the boundary, like the radius of the input-connector cannot be changed).

Parameters

dof	The index of the parameter to be changed.
value	The value, the dof should be set to.

Implements SpaceTransformation.

Definition at line 209 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::set_dof().

int dof,

```
209
210   return st->set_dof(dof, value);
211 }

4.2.3.21   set_free_dof()

void DualProblemTransformationWrapper::set_free_dof (
```

This function sets the value of the dof provided to the given value.

double value) [virtual]

It is important to consider, that some dofs are non-writable (i.e. the values of the degrees of freedom on the boundary, like the radius of the input-connector cannot be changed).

Parameters

dof	The index of the parameter to be changed.
value	The value, the dof should be set to.

Implements SpaceTransformation.

Definition at line 217 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::set_free_dof().

```
217
218   return st->set_free_dof(dof, value);
219 }
```

```
4.2.3.22 Z_to_Sector_and_local_z()
```

```
\label{local_z} $$ std::pair< int, double > DualProblemTransformationWrapper::Z_to_Sector_and_local_z ( double $in_z$) const $$ $$
```

Using this method unifies the usage of coordinates.

This function takes a global z coordinate (in the computational domain) and returns both a Sector-Index and an internal z coordinate indicating which sector this coordinate belongs to and how far along in the sector it is located.

Parameters

double	in_z global system z coordinate for the transformation.
--------	---

Definition at line 222 of file DualProblemTransformationWrapper.cpp.

References SpaceTransformation::Z_to_Sector_and_local_z().

Referenced by HomogenousTransformationCircular::get_m(), HomogenousTransformationCircular::get_Q1(), HomogenousTransformationCircular::get_Q3(), HomogenousTransformationCircular::get_Q3(), HomogenousTransformationCircular::get_v(), and HomogenousTransformationCircular::PML Z Distance().

```
222
223   return st->Z_to_Sector_and_local_z(in_z);
224 }
```

4.2.4 Member Data Documentation

4.2.4.1 case_sectors

```
std::vector<Sector<3> > DualProblemTransformationWrapper::case_sectors
```

This member contains all the Sectors who, as a sum, form the complete Waveguide.

These Sectors are a partition of the simulated domain.

Definition at line 151 of file DualProblemTransformationWrapper.h.

Referenced by HomogenousTransformationCircular::estimate_and_initialize(), HomogenousTransformation \leftarrow Circular::get_dof(), HomogenousTransformationCircular::get_free_dof(), HomogenousTransformationCircular \leftarrow ::get_m(), HomogenousTransformationCircular::get_Q1(), HomogenousTransformationCircular::get_Q2(), Homogenous \leftarrow TransformationCircular::get_Q3(), HomogenousTransformationCircular::get_r(), HomogenousTransformationCircular::PML_Z_Distance(), HomogenousTransformationCircular \leftarrow ::set_dof(), and HomogenousTransformationCircular::set_free_dof().

4.2.4.2 epsilon_K

```
const double DualProblemTransformationWrapper::epsilon_K
```

The material-property ϵ_r has a different value inside and outside of the waveguides core.

This variable stores its value inside the core.

Definition at line 158 of file DualProblemTransformationWrapper.h.

4.2.4.3 epsilon_M

const double DualProblemTransformationWrapper::epsilon_M

The material-property ϵ_r has a different value inside and outside of the waveguides core.

This variable stores its value outside the core.

Definition at line 164 of file DualProblemTransformationWrapper.h.

4.2.4.4 sectors

const int DualProblemTransformationWrapper::sectors

Since the computational domain is split into subdomains (called sectors), it is important to keep track of the amount of subdomains.

This member stores the number of Sectors the computational domain has been split into.

Definition at line 170 of file DualProblemTransformationWrapper.h.

Referenced by HomogenousTransformationCircular::estimate_and_initialize(), HomogenousTransformation Circular::get_dof(), HomogenousTransformationCircular::det_dof(), HomogenousTransformationCircular::set dof(), and HomogenousTransformationCircular::set free dof().

The documentation for this class was generated from the following files:

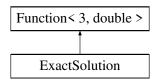
- · Code/SpaceTransformations/DualProblemTransformationWrapper.h
- Code/SpaceTransformations/DualProblemTransformationWrapper.cpp

4.3 ExactSolution Class Reference

This class is derived from the Function class and can be used to estimate the L2-error for a straight waveguide.

#include <ExactSolution.h>

Inheritance diagram for ExactSolution:



Public Member Functions

- ExactSolution (bool in rectangular=false, bool in dual=false)
- double value (const Point < 3 > &p, const unsigned int component) const

This function calculates one single component of the solution vector.

void vector value (const Point< 3 > &p, Vector< double > &value) const

This function is the one that gets called from external contexts and calls the value-function to calculate the individual components.

- std::vector< std::string > split (std::string) const
- Tensor< 1, 3, std::complex< double >> curl (const Point< 3 > &in p) const
- Tensor< 1, 3, std::complex< double >> val (const Point< 3 > &in p) const

4.3.1 Detailed Description

This class is derived from the Function class and can be used to estimate the L2-error for a straight waveguide.

In the case of a completely cylindrical waveguide, an analytic solution is known (the modes of the input-signal themselves) and this class offers a representation of this analytical solution. If the waveguide has any other shape, this solution does not lose its value completely - it can still be used as a starting-vector for iterative solvers.

The structure of this class is defined by the properties of the Function-class meaning that we have two functions:

- 1. virtual double value (const Point<dim> &p, const unsigned int component) calculates the value for a single component of the vector-valued return-value.
- 2. virtual void vector_value (const Point<dim> &p, Vector<double> &value) puts these individual components into the parameter value, which is a reference to a vector, handed over to store the result.

Author

Pascal Kraft

Date

23.11.2015

Definition at line 36 of file ExactSolution.h.

4.3.2 Member Function Documentation

4.3.2.1 value()

This function calculates one single component of the solution vector.

To calculate this, we do the following: We know the input on the boundary of the computational domain for $z=z_{in}$. So for a given position p=(x,y,z) we calculate

$$f_c(x, y, z) = \sum_{j=0}^{N} (a_j \, \phi_j(x, y, z_{in})) \cdot \boldsymbol{e_c} \, e^{i\omega(z - z_{in})}.$$

Here, ϕ_j is the j-th mode of the waveguide which is induced with the intensity a_j . e_c is the c-th unit-vector with c being the index of the component we want to compute.

Parameters

p	This value contains the position for which we want to calculate the exact solution.
component	This integer holds the index of the component we want to compute. Keep in mind that these are
	not coordinates in the physical sense. The components 0 to 2 are the real parts of the
	solution-vector and the components 3-5 are the imaginary parts.

Definition at line 13 of file ExactSolution.cpp.

```
14
15
       Point<3, double> p = in_p;
       if (is_dual) p[2] = -in_p[2];
17
       bool zero = false;
1.8
      if (p[0] > GlobalParams.M_R_XLength / 2.0 - GlobalParams.M_BC_XPlus)
19
         zero = true;
      if (p[0] < -GlobalParams.M_R_XLength / 2.0 + GlobalParams.M_BC_XMinus)</pre>
20
21
         zero = true;
       if (p[1] > GlobalParams.M_R_YLength / 2.0 - GlobalParams.M_BC_YPlus)
23
          zero = true;
        \  \  \  \text{if } \  \  (p[1] \ < \  \  -\text{GlobalParams.M\_R\_YLength} \ / \ 2.0 \ + \  \  \text{GlobalParams.M\_BC\_YMinus}) 
2.4
25
         zero = true;
       if (p[2] > GlobalParams.M_R_ZLength / 2.0) zero = true;
26
       if (zero) {
28
         return 0.0;
29
30
       if (is_rectangular) {
31
         std::complex<double> ret val(0.0, 0.0);
32
          const double delta = abs(mesh_points[0] - mesh_points[1]);
33
                  int mesh_number = mesh_points.size();
35
          if (!(abs(p(1)) >= mesh_points[0] || abs(p(0)) >= mesh_points[0])) {
            int ix = 0;
int iy = 0;
36
37
            while (mesh_points[ix] > p(0) && ix < mesh_number) ix++;
while (mesh_points[iy] > p(1) && iy < mesh_number) iy++;
if (ix == 0 || iy == 0 || ix == mesh_number || iy == mesh_number) {</pre>
38
39
40
               return 0.0;
42
            } else {
               double dx = (p(0) - mesh\_points[ix]) / delta; double dy = (p(1) - mesh\_points[iy]) / delta;
43
44
               double m1m1 = dx * dy;
45
               double m1p1 = dx * (1.0 - dy);
46
               double plp1 = (1.0 - dx) * (1.0 - dy);
double plm1 = (1.0 - dx) * dy;
47
48
49
                switch (component % 3) {
                  case 0:
50
51
                     ret_val.real(p1p1 * vals[ix][iy].Ex.real() +
                                        plm1 * vals[ix][iy - 1].Ex.real() +
mlm1 * vals[ix - 1][iy - 1].Ex.real() +
mlp1 * vals[ix - 1][iy].Ex.real());
52
                     ret_val.imag(plp1 * vals[ix][iy].Ex.imag() +
55
                                       plm1 * vals[ix][iy - 1].Ex.imag() +
mlm1 * vals[ix - 1][iy - 1].Ex.imag() +
mlp1 * vals[ix - 1][iy].Ex.imag());
56
57
58
                     // ret_val *= -1.0;
60
                     break;
61
                  case 1:
62
                     ret_val.real(p1p1 * vals[ix][iy].Ey.real() +
                                        plm1 * vals[ix][iy - 1].Ey.real() +
mlm1 * vals[ix - 1][iy - 1].Ey.real() +
mlp1 * vals[ix - 1][iy].Ey.real());
63
64
65
                     ret_val.imag(plp1 * vals[ix][iy].Ey.imag() + plm1 * vals[ix][iy - 1].Ey.imag() +
66
67
                                        mlm1 * vals[ix - 1][iy - 1].Ey.imag() + mlp1 * vals[ix - 1][iy].Ey.imag());
68
69
70
                     break;
71
                  case 2:
72
                     ret_val.real(p1p1 * vals[ix][iy].Ez.real() +
                                        plm1 * vals[ix][iy - 1].Ez.real() +
mlm1 * vals[ix - 1][iy - 1].Ez.real() +
mlp1 * vals[ix - 1][iy].Ez.real());
73
74
75
                     ret_val.imag(plp1 * vals[ix][iy].Ez.imag() +
76
                                        plm1 * vals[ix][iy - 1].Ez.imag() +
mlm1 * vals[ix - 1][iy - 1].Ez.imag() +
mlp1 * vals[ix - 1][iy].Ez.imag());
78
79
                    break;
80
81
                  default:
                     ret val.real(0.0);
82
83
                     ret_val.imag(0.0);
```

```
}
87
          double n;
         if (abs(p(0)) <= GlobalParams.M_C_Dim1In / 2.0 &&
    abs(p(1)) <= GlobalParams.M_C_Dim2In / 2.0) {</pre>
88
89
           n = std::sqrt(GlobalParams.M_W_epsilonin);
90
91
         } else {
           n = std::sqrt(GlobalParams.M_W_epsilonout);
93
         double k = n * 2 * GlobalParams.C_Pi / GlobalParams.M_W_Lambda;
94
         std::complex<double> phase(0.0, (p(2) - GlobalParams.Minimum_Z) * k);
95
96
         ret_val *= std::exp(phase);
         if (component > 2) {
98
            return ret_val.imag();
99
         } else {
            return ret_val.real();
100
101
102
        } else {
103
          return 0.0;
104
105
      } else {
106
        return ModeMan.get_input_component(component, p, 0);
      }
107
108 }
```

4.3.2.2 vector_value()

This function is the one that gets called from external contexts and calls the value-function to calculate the individual components.

The real solution looks as follows:

$$f(x,y,z) = \begin{pmatrix} \text{value}(x,y,z,0) \\ \text{value}(x,y,z,1) \\ \text{value}(x,y,z,2) \end{pmatrix} + i \begin{pmatrix} \text{value}(x,y,z,3) \\ \text{value}(x,y,z,4) \\ \text{value}(x,y,z,5) \end{pmatrix}.$$

Definition at line 110 of file ExactSolution.cpp.

 $Referenced \ by \ Waveguide::estimate_solution(), \ and \ Waveguide::evaluate_for_Position().$

```
Point<3, double> p = in_p;
if (is_dual) p[2] = -in_p[2];
112
113
114
      bool zero = false;
      if (p[0] > GlobalParams.M_R_XLength / 2.0 - GlobalParams.M_BC_XPlus)
115
116
        zero
               = true;
117
       \  \  \, \text{if} \  \, (p[0] \ < \  \, \text{GlobalParams.M\_R\_XLength} \  \, / \  \, 2.0 \  \, + \  \, \text{GlobalParams.M\_BC\_XMinus}) 
118
        zero = true;
      if (p[1] > GlobalParams.M_R_YLength / 2.0 - GlobalParams.M_BC_YPlus)
119
120
        zero = true;
      if (p[1] < -GlobalParams.M_R_YLength / 2.0 + GlobalParams.M_BC_YMinus)</pre>
121
122
        zero = true;
123
      if (p[2] > GlobalParams.M_R_ZLength / 2.0) zero = true;
124
      if (zero) {
        for (unsigned int i = 0; i < values.size(); i++) {</pre>
125
          values[i] = 0.0;
126
127
128
        return;
129
130
      if (is_rectangular) {
131
        const double delta = abs(mesh_points[0] - mesh_points[1]);
132
        const int mesh_number = mesh_points.size();
133
        if (!(abs(p(1)) >= mesh_points[0] || abs(p(0)) >= mesh_points[0])) {
134
         int ix = 0;
135
           int iy = 0;
```

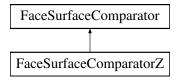
```
while (mesh_points[ix] > p(0) && ix < mesh_number) ix++;</pre>
            while (mesh_points[iy] > p(1) && iy < mesh_number) iy++;
if (ix == 0 || iy == 0 || ix == mesh_number || iy == mesh_number) {</pre>
137
138
             for (unsigned int i = 0; i < values.size(); i++) {</pre>
139
140
                values[i] = 0.0;
141
142
              return;
143
              double dx = (p(0) - mesh_points[ix]) / delta;
double dy = (p(1) - mesh_points[iy]) / delta;
144
145
              double mlm1 = dx * dy;
double mlm1 = dx * (1.0 - dy);
146
147
              double plp1 = (1.0 - dx) * (1.0 - dy);
double plm1 = (1.0 - dx) * dy;
148
149
150
              values[0] = p1p1 * vals[ix][iy].Ex.real() +
                             plm1 * vals[ix][iy - 1].Ex.real() +
mlm1 * vals[ix - 1][iy - 1].Ex.real() +
mlp1 * vals[ix - 1][iy].Ex.real();
151
152
153
              values[1] = p1p1 * vals[ix][iy].Ey.real() +
154
                             plm1 * vals[ix][iy - 1].Ey.real() +
mlm1 * vals[ix - 1][iy - 1].Ey.real() +
mlp1 * vals[ix - 1][iy].Ey.real();
156
157
              158
159
160
161
162
              values[3] = p1p1 * vals[ix][iy].Ex.imag() +
                             plm1 * vals[ix][iy - 1].Ex.imag() +
mlm1 * vals[ix - 1][iy - 1].Ex.imag() +
mlp1 * vals[ix - 1][iy].Ex.imag();
163
164
165
              166
167
168
169
              170
171
172
173
174
             if (abs(p(0)) <= GlobalParams.M_C_Dim1In / 2.0 &&
    abs(p(1)) <= GlobalParams.M_C_Dim2In / 2.0) {</pre>
175
176
                n = std::sqrt(GlobalParams.M_W_epsilonin);
177
178
              } else {
                n = std::sqrt(GlobalParams.M_W_epsilonout);
181
              double k = n * 2 * GlobalParams.C_Pi / GlobalParams.M_W_Lambda;
182
             std::complex<double> phase(
183
                   0.0, -(p(2) + GlobalParams.M_R_ZLength / 2.0) * k);
              phase = std::exp(phase);
for (unsigned int komp = 0; komp < 3; komp++) {</pre>
184
185
186
                std::complex<double> entr(values[0 + komp], values[3 + komp]);
187
                 entr *= phase;
188
                 values[0 + komp] = entr.real();
189
                values[3 + komp] = entr.imag();
190
191
              // values[0] *= -1.0;
              // values[3] *= -1.0;
193
194
195
         } else {
196
           for (unsigned int i = 0; i < values.size(); i++) {</pre>
197
              values[i] = 0.0;
198
199
           return;
200
201
       } else {
         for (unsigned int c = 0; c < 6; ++c)
202
203
            values[c] = ModeMan.get_input_component(c, p, 0);
204
205 }
```

The documentation for this class was generated from the following files:

- · Code/Helpers/ExactSolution.h
- Code/Helpers/ExactSolution.cpp

4.4 FaceSurfaceComparator Class Reference

Inheritance diagram for FaceSurfaceComparator:



Public Member Functions

• virtual bool **check_face** (const dealii::parallel::distributed::Triangulation< 3, 3 >::face_iterator)

4.4.1 Detailed Description

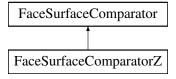
Definition at line 12 of file FaceSurfaceComparator.h.

The documentation for this class was generated from the following files:

- · Code/HSIE/FaceSurfaceComparator.h
- · Code/HSIE/FaceSurfaceComparator.cpp

4.5 FaceSurfaceComparatorZ Class Reference

Inheritance diagram for FaceSurfaceComparatorZ:



Public Member Functions

- FaceSurfaceComparatorZ (double in_z=0, double in_tol=0.0001)
- virtual bool **check_face** (const dealii::parallel::distributed::Triangulation< 3, 3 >::face_iterator)

4.5.1 Detailed Description

Definition at line 14 of file FaceSurfaceComparatorZ.h.

The documentation for this class was generated from the following files:

- · Code/HSIE/FaceSurfaceComparatorZ.h
- Code/HSIE/FaceSurfaceComparatorZ.cpp

4.6 GradientTable Class Reference

The Gradient Table is an OutputGenerator, intended to write information about the shape gradient to the console upon its computation.

#include <GradientTable.h>

Public Member Functions

- **GradientTable** (unsigned int in_step, dealii::Vector< double > in_configuration, double in_quality, dealii::

 Vector< double > in_last_configuration, double in_last_quality)
- void SetInitialQuality (double in_quality)
- void AddComputationResult (int in_component, double in_step, double in_quality)
- void AddFullStepResult (dealii::Vector< double > in_step, double in_quality)
- void PrintFullLine ()
- · void PrintTable ()
- void WriteTableToFile (std::string in_filename)

Public Attributes

- · const int ndofs
- · const int nfreedofs
- const unsigned int GlobalStep

4.6.1 Detailed Description

The Gradient Table is an OutputGenerator, intended to write information about the shape gradient to the console upon its computation.

Date

28.11.2016

Author

Pascal Kraft

Definition at line 11 of file GradientTable.h.

The documentation for this class was generated from the following files:

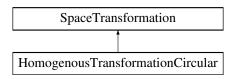
- · Code/OutputGenerators/Console/GradientTable.h
- Code/OutputGenerators/Console/GradientTable.cpp

4.7 HomogenousTransformationCircular Class Reference

For this transformation we try to achieve a situation in which tensorial material properties from the coordinate transformation and PML-regions dont overlap.

#include <HomogenousTransformationCircular.h>

Inheritance diagram for Homogenous Transformation Circular:



Public Member Functions

- HomogenousTransformationCircular (int)
- Point< 3 > math_to_phys (Point< 3 > coord) const
- Point< 3 > phys_to_math (Point< 3 > coord) const
- Point< 3 > math_to_phys_hom (Point< 3 > coord) const
- Point < 3 > phys_to_math_hom (Point < 3 > coord) const
- bool is_identity (Point< 3 > coord) const
- Tensor < 2, 3, std::complex < double > > get_Tensor (Point < 3 > &coordinate) const
- Tensor < 2, 3, std::complex < double >> get_Preconditioner_Tensor (Point < 3 > &coordinate, int block)
 const
- Tensor< 2, 3, std::complex< double >> Apply_PML_To_Tensor (Point< 3 > &coordinate, Tensor< 2, 3, double > Tensor_input) const
- Tensor< 2, 3, std::complex< double >> Apply_PML_To_Tensor_For_Preconditioner (Point< 3 > &coordinate, Tensor< 2, 3, double > Tensor_input, int block) const
- Tensor< 2, 3, double > get_Space_Transformation_Tensor (Point< 3 > &coordinate) const
- Tensor< 2, 3, double > get_Space_Transformation_Tensor_Homogenized (Point< 3 > &coordinate) const
- bool PML in X (Point < 3 > &position) const

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the x-axis.

bool PML in Y (Point < 3 > &position) const

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the *y*-axis.

bool PML in Z (Point < 3 > &position) const

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the *z*-axis.

double Preconditioner_PML_Z_Distance (Point< 3 > &p, unsigned int block) const

Similar to the PML_in_Z only this function is used to generate the artificial PML used in the Preconditioner.

double PML_X_Distance (Point< 3 > &position) const

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

double PML_Y_Distance (Point< 3 > &position) const

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

double PML_Z_Distance (Point< 3 > &position) const

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

void estimate_and_initialize ()

At the beginning (before the first solution of a system) only the boundary conditions for the shape of the waveguide are known.

• double get Q1 (double z) const

This member calculates the value of Q1 for a provided z-coordinate.

• double get_Q2 (double z) const

This member calculates the value of Q2 for a provided z-coordinate.

double get_Q3 (double z) const

This member calculates the value of Q3 for a provided *z*-coordinate.

double get dof (int dof) const

This is a getter for the values of degrees of freedom.

void set_dof (int dof, double value)

This function sets the value of the dof provided to the given value.

double get_free_dof (int dof) const

This is a getter for the values of degrees of freedom.

void set_free_dof (int dof, double value)

This function sets the value of the dof provided to the given value.

• double System Length () const

Returns the complete length of the computational domain.

· double Sector_Length () const

Returns the length of one sector.

· double Layer Length () const

Returns the length of one layer.

• double get_r (double in_z) const

Returns the radius for a system-coordinate;.

• double get_m (double in_z) const

Returns the shift for a system-coordinate;.

• double get_v (double in_z) const

Returns the tilt for a system-coordinate;.

Vector< double > Dofs () const

Other objects can use this function to retrieve an array of the current values of the degrees of freedom of the functional we are optimizing.

· unsigned int NFreeDofs () const

This function returns the number of unrestrained degrees of freedom of the current optimization run.

· unsigned int NDofs () const

This function returns the total number of DOFs including restrained ones.

bool IsDofFree (int) const

Since Dofs() also returns restrained degrees of freedom, this function can be applied to determine if a degree of freedom is indeed free or restrained.

· void Print () const

Console output of the current Waveguide Structure.

std::complex < double > evaluate for z (double z in, Waveguide *)

Since the Wavegudie itself may be circular or rectangular now, the evaluation routines should be moved to a point in the code where this information is included in the code.

- std::complex < double > evaluate for z with sum (double, double, Waveguide *)
- std::complex< double > gauss_product_2D_sphere_primal (double z, int n, double R, double Xc, double Yc, Waveguide *in_w)

Public Attributes

- · const double XMinus
- · const double XPlus
- · const double YMinus
- · const double YPlus
- · const double ZMinus
- · const double ZPlus
- std::vector< Sector< 3 >> case_sectors

This member contains all the Sectors who, as a sum, form the complete Waveguide.

· const double epsilon_K

The material-property ϵ_r has a different value inside and outside of the waveguides core.

· const double epsilon_M

The material-property ϵ_r has a different value inside and outside of the waveguides core.

· const int sectors

Since the computational domain is split into subdomains (called sectors), it is important to keep track of the amount of subdomains.

· const double deltaY

This value is initialized with the value Delta from the input-file.

Vector< double > InitialDofs

This vector of values saves the initial configuration.

4.7.1 Detailed Description

For this transformation we try to achieve a situation in which tensorial material properties from the coordinate transformation and PML-regions dont overlap.

The usage of a coordinate transformation which is identity on the domain containing our PML is a strong restriction however it ensures lower errors since the quality of the PML is harder to estimate otherwise. Also it limits us in how we model the waveguide essentially forcing us to have no bent between the wavguides-connectors.

Author

Pascal Kraft

Date

28.11.2016

Definition at line 33 of file HomogenousTransformationCircular.h.

4.7.2 Member Function Documentation

4.7.2.1 Dofs()

```
Vector< double > HomogenousTransformationCircular::Dofs ( ) const [virtual]
```

Other objects can use this function to retrieve an array of the current values of the degrees of freedom of the functional we are optimizing.

This also includes restrained degrees of freedom and other functions can be used to determine this property. This has to be done because in different cases the number of restrained degrees of freedom can vary and we want no logic about this in other functions.

Implements SpaceTransformation.

Definition at line 586 of file HomogenousTransformationCircular.cpp.

References DualProblemTransformationWrapper::get_dof(), and DualProblemTransformationWrapper::NDofs().

```
586
587     Vector<double> ret;
588     const int total = NDofs();
589     ret.reinit(total);
590     for (int i = 0; i < total; i++) {
591         ret[i] = get_dof(i);
592     }
593     return ret;
594 }</pre>
```

4.7.2.2 estimate_and_initialize()

```
\verb|void HomogenousTransformationCircular::estimate\_and\_initialize () | [virtual]| \\
```

At the beginning (before the first solution of a system) only the boundary conditions for the shape of the waveguide are known.

Therefore the values for the degrees of freedom need to be estimated. This function sets all variables to appropriate values and estimates an appropriate shape based on averages and a polynomial interpolation of the boundary conditions on the shape.

Implements SpaceTransformation.

Definition at line 512 of file HomogenousTransformationCircular.cpp.

References DualProblemTransformationWrapper::case_sectors, DualProblemTransformationWrapper::Sector_ \leftarrow Length(), and DualProblemTransformationWrapper::sectors.

```
512
      case sectors.reserve(sectors);
513
      double m_0 = GlobalParams.M_W_Delta / 2.0;
514
      double m_1 = -GlobalParams.M_W_Delta /
      double r_0 = GlobalParams.M_C_DimlIn;
double r_1 = GlobalParams.M_C_DimlOut;
516
517
518
      if (sectors == 1) {
        Sector<3> temp12(true, true, -GlobalParams.M_R_ZLength / 2,
519
520
                          GlobalParams.M_R_ZLength / 2);
521
        case_sectors.push_back(temp12);
522
        case_sectors[0].set_properties_force(
523
            GlobalParams.M_W_Delta / 2.0, -GlobalParams.M_W_Delta / 2.0,
524
            GlobalParams.M_C_DimlIn, GlobalParams.M_C_DimlOut, 0, 0);
525
     } else {
526
        double length = Sector_Length();
        Sector<3> temp(true, false, -GlobalParams.M_R_ZLength / (2.0),
```

```
-GlobalParams.M_R_ZLength / 2.0 + length);
529
        case_sectors.push_back(temp);
530
        for (int i = 1; i < sectors; i++) {</pre>
          Sector<3> temp2(false, false,
531
532
                           -GlobalParams.M_R_ZLength / (2.0) + length * (1.0 * i),
                            -GlobalParams.M_R_ZLength / (2.0) + length * (i + 1.0));
533
534
          case_sectors.push_back(temp2);
535
536
537
        double length_rel = 1.0 / ((double) (sectors));
        case_sectors[0].set_properties_force(
538
            m_0, InterpolationPolynomialZeroDerivative(length_rel, m_0, m_1), r_0,
539
             InterpolationPolynomialZeroDerivative(length_rel, r_0, r_1), 0, InterpolationPolynomialDerivative(length_rel, m_0, m_1, 0, 0));
540
541
542
        for (int i = 1; i < sectors; i++) {</pre>
         double z_1 = i * length_rel;
double z_r = (i + 1) * length_rel;
case_sectors[i].set_properties_force(
543
544
545
             InterpolationPolynomialZeroDerivative(z_1, m_0, m_1),
546
547
               InterpolationPolynomialZeroDerivative(z_r, m_0, m_1),
548
               InterpolationPolynomialZeroDerivative(z_1, r_0, r_1),
549
               InterpolationPolynomialZeroDerivative(z_r, r_0, r_1),
550
               551
               InterpolationPolynomialDerivative(z_r, m_0, m_1, 0, 0));
552
        }
     }
554 }
```

4.7.2.3 evaluate_for_z()

Since the Wavegudie itself may be circular or rectangular now, the evaluation routines should be moved to a point in the code where this information is included in the code.

Since I dont want to create derived classes from waveguide (which I should do eventually) I will for now include this functionality into the space transformation which is shape-sensitive. The waveguide only offers the evaluation at a point. The quadrature-rule has to be imposed by the space transformation.

Implements SpaceTransformation.

Definition at line 432 of file HomogenousTransformationCircular.cpp.

```
433
434 double r = GlobalParams.M_C_DimlIn + GlobalParams.M_C_DimlOut;
435 return gauss_product_2D_sphere(in_z, 10, r, 0, 0, in_w);
436 }
```

4.7.2.4 get_dof()

This is a getter for the values of degrees of freedom.

A getter-setter interface was introduced since the values are estimated automatically during the optimization and non-physical systems should be excluded from the domain of possible cases.

Parameters

dof The index of the degree of freedom to be retrieved from the structure of the modelled waveguide.

Returns

This function returns the value of the requested degree of freedom. Should this dof not exist, 0 will be returnd.

Implements SpaceTransformation.

Definition at line 438 of file HomogenousTransformationCircular.cpp.

References DualProblemTransformationWrapper::case_sectors, DualProblemTransformationWrapper::NDofs(), and DualProblemTransformationWrapper::sectors.

Referenced by HomogenousTransformationRectangular::Dofs().

```
438
439
     if (dof < (int) NDofs() && dof >= 0) {
       int sector = floor(dof / 3);
440
      if (sector == sectors) {
441
         return case_sectors[sector - 1].dofs_r[dof % 3];
442
      } else {
444
        return case_sectors[sector].dofs_1[dof % 3];
445
446 } else {
      std::cout << "Critical: DOF-index out of bounds in "
447
                    "HomogenousTransformationCircular::get_dof!"
448
                << std::endl;
       return 0.0;
451 }
452 }
```

4.7.2.5 get_free_dof()

This is a getter for the values of degrees of freedom.

A getter-setter interface was introduced since the values are estimated automatically during the optimization and non-physical systems should be excluded from the domain of possible cases.

Parameters

dof The index of the degree of freedom to be retrieved from the structure of the modelled waveguide.

Returns

This function returns the value of the requested degree of freedom. Should this dof not exist, 0 will be returnd.

Implements SpaceTransformation.

Definition at line 454 of file HomogenousTransformationCircular.cpp.

References DualProblemTransformationWrapper::case_sectors, DualProblemTransformationWrapper::NDofs(), and DualProblemTransformationWrapper::sectors.

```
454
      int dof = in_dof + 3;
if (dof < (int) NDofs() - 3 && dof >= 0) {
455
456
        int sector = floor(dof / 3);
if (sector == sectors) {
457
458
           return case_sectors[sector - 1].dofs_r[dof % 3];
459
       } else {
460
          return case sectors[sector].dofs 1[dof % 3];
461
462
463
      } else {
        std::cout << "Critical: DOF-index out of bounds in "
464
                       "{\tt HomogenousTransformationCircular::get\_free\_dof!"}
465
                    << std::endl;
466
467
        return 0.0;
468
469 }
```

4.7.2.6 get_Q1()

```
double HomogenousTransformationCircular::get_Q1 ( \label{eq:const} \mbox{double $z$ ) const [virtual]}
```

This member calculates the value of Q1 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q1 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implements SpaceTransformation.

Definition at line 571 of file HomogenousTransformationCircular.cpp.

References DualProblemTransformationWrapper::case_sectors, and DualProblemTransformationWrapper:: $Z_to \leftarrow _Sector_and_local_z()$.

```
571
572 std::pair<int, double> two = Z_to_Sector_and_local_z(z_in);
573 return case_sectors[two.first].getQ1(two.second);
574 }
```

4.7.2.7 get_Q2()

```
double HomogenousTransformationCircular::get_Q2 ( double z ) const [virtual]
```

This member calculates the value of Q2 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q2 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implements SpaceTransformation.

Definition at line 576 of file HomogenousTransformationCircular.cpp.

References DualProblemTransformationWrapper::case_sectors, and DualProblemTransformationWrapper::Z_to ← __Sector_and_local_z().

```
576
577 std::pair<int, double> two = Z_to_Sector_and_local_z(z_in);
578 return case_sectors[two.first].getQ2(two.second);
579 }
```

4.7.2.8 get_Q3()

```
double HomogenousTransformationCircular::get_Q3 ( double z ) const [virtual]
```

This member calculates the value of Q3 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q3 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implements SpaceTransformation.

Definition at line 581 of file Homogenous Transformation Circular.cpp.

References DualProblemTransformationWrapper::case_sectors, and DualProblemTransformationWrapper:: $Z_{to} \leftarrow S_{cot} - S_{cot}$

4.7.2.9 IsDofFree()

Since Dofs() also returns restrained degrees of freedom, this function can be applied to determine if a degree of freedom is indeed free or restrained.

"restrained" means that for example the DOF represents the radius at one of the connectors (input or output) and therefore we forbid the optimization scheme to vary this value.

Implements SpaceTransformation.

Definition at line 600 of file HomogenousTransformationCircular.cpp.

References DualProblemTransformationWrapper::NDofs().

```
600 {
601 return index > 2 && index < (int) NDofs() - 3;
602 }
```

4.7.2.10 NDofs()

```
unsigned int HomogenousTransformationCircular::NDofs ( ) const [virtual]
```

This function returns the total number of DOFs including restrained ones.

This is the lenght of the array returned by Dofs().

Implements SpaceTransformation.

Definition at line 608 of file HomogenousTransformationCircular.cpp.

References DualProblemTransformationWrapper::sectors.

Referenced by HomogenousTransformationRectangular::Dofs(), HomogenousTransformationRectangular::get_ \leftarrow dof(), HomogenousTransformationRectangular::get_free_dof(), HomogenousTransformationRectangular::lsDof \leftarrow Free(), HomogenousTransformationRectangular::NFreeDofs(), HomogenousTransformationRectangular::set_dof(), and HomogenousTransformationRectangular::set free dof().

```
608
609 return sectors * 3 + 3;
610 }
```

4.7.2.11 PML_in_X()

```
bool HomogenousTransformationCircular::PML_in_X (  Point < 3 \ > \ \& \ position \ ) \ const \ \ [virtual]
```

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the x-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

pos	sition	Stores the position in which to test for presence of a PML-Material.
1 200		

Implements SpaceTransformation.

Definition at line 151 of file HomogenousTransformationCircular.cpp.

Referenced by HomogenousTransformationRectangular::PML_Z_Distance().

```
151 {
152    return p(0) < XMinus || p(0) > XPlus;
153 }
```

4.7.2.12 PML_in_Y()

```
bool HomogenousTransformationCircular::PML_in_Y (  Point < 3 > \& position ) const [virtual]
```

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the y-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

	position	Stores the position in which to test for presence of a PML-Material.
--	----------	--

 $Implements\ Space Transformation.$

Definition at line 155 of file HomogenousTransformationCircular.cpp.

Referenced by HomogenousTransformationRectangular::PML_Z_Distance().

4.7.2.13 PML_in_Z()

```
bool HomogenousTransformationCircular::PML_in_Z (  Point < 3 \ > \ \& \ position \ ) \ const \ \ [virtual]
```

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the z-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

position Stores the position in which to test for presence of a PML-Material.

Implements SpaceTransformation.

Definition at line 159 of file HomogenousTransformationCircular.cpp.

Referenced by HomogenousTransformationRectangular::PML_Z_Distance().

```
159 {
160 return p(2) > ZPlus;
161 }
```

4.7.2.14 PML X Distance()

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

position Stores the position from which to calculate the distance to the PML-surface.

Implements SpaceTransformation.

Definition at line 170 of file HomogenousTransformationCircular.cpp.

Referenced by HomogenousTransformationRectangular::PML_Z_Distance().

4.7.2.15 PML_Y_Distance()

```
double HomogenousTransformationCircular::PML_Y_Distance ( \label{eq:point} \mbox{Point} < \mbox{3 > \& position ) const [virtual]}
```

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

position	Stores the position from which to calculate the distance to the PML-surface.

Implements SpaceTransformation.

Definition at line 178 of file HomogenousTransformationCircular.cpp.

Referenced by HomogenousTransformationRectangular::PML Z Distance().

4.7.2.16 PML Z Distance()

```
double HomogenousTransformationCircular::PML_Z_Distance (
Point < 3 > \& position ) const [virtual]
```

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

Implements SpaceTransformation.

Definition at line 186 of file HomogenousTransformationCircular.cpp.

References DualProblemTransformationWrapper::case_sectors, Waveguide::evaluate_for_Position(), Dual \leftarrow ProblemTransformationWrapper::PML_in_X(), DualProblemTransformationWrapper::PML_in_Y(), DualProblem \leftarrow TransformationWrapper::PML_in_Z(), DualProblemTransformationWrapper::PML_X_Distance(), DualProblem \leftarrow TransformationWrapper::PML_Y_Distance(), DualProblemTransformationWrapper::PML_Z_Distance(), DualCollemTransformationWrapper::Preconditioner_PML_Z_Distance(), and DualProblemTransformationWrapper:: \leftarrow Z_to_Sector_and_local_z().

Referenced by HomogenousTransformationRectangular::PML Z Distance().

```
186 {
187     if (p(2) < 0) {
188         return 0;
189     } else {
190         return p(2) - (GlobalParams.M_R_ZLength / 2.0);
191     }
192 }
```

4.7.2.17 Preconditioner_PML_Z_Distance()

```
double HomogenousTransformationCircular::Preconditioner_PML_Z_Distance ( Point< 3 > & p, unsigned int block ) const [virtual]
```

Similar to the PML_in_Z only this function is used to generate the artificial PML used in the Preconditioner.

These Layers are not only situated at the surface of the computational domain but also inside it at the interfaces of Sectors. This function fulfills the same purpose as those with similar names but it is supposed to be used together with Preconditioner PML in Z instead of the versions without "Preconditioner".

Implements SpaceTransformation.

Definition at line 163 of file HomogenousTransformationCircular.cpp.

Referenced by HomogenousTransformationRectangular::PML Z Distance().

```
164 {
165 double width = GlobalParams.LayerThickness * 1.0;
166 return p(2) + GlobalParams.M_R_ZLength / 2.0 - ((double)rank) * width;
168 }
```

4.7.2.18 set_dof()

This function sets the value of the dof provided to the given value.

It is important to consider, that some dofs are non-writable (i.e. the values of the degrees of freedom on the boundary, like the radius of the input-connector cannot be changed).

Parameters

dof	The index of the parameter to be changed.
value	The value, the dof should be set to.

Implements SpaceTransformation.

Definition at line 471 of file HomogenousTransformationCircular.cpp.

References DualProblemTransformationWrapper::case_sectors, DualProblemTransformationWrapper::NDofs(), and DualProblemTransformationWrapper::sectors.

```
471
472     if (dof < (int)NDofs() && dof >= 0) {
473         int sector = floor(dof / 3);
474         if (sector == sectors) {
475             case_sectors[sector - 1].dofs_r[dof % 3] = in_val;
476         } else if (sector == 0) {
```

```
case_sectors[0].dofs_1[dof % 3] = in_val;
478
479
         case_sectors[sector].dofs_1[dof % 3] = in_val;
480
         case_sectors[sector - 1].dofs_r[dof % 3] = in_val;
481
     } else {
482
      std::cout << "Critical: DOF-index out of bounds in "
483
484
                    "HomogenousTransformationCircular::set_dof!"
485
                 << std::endl;
486
487 }
```

4.7.2.19 set_free_dof()

This function sets the value of the dof provided to the given value.

It is important to consider, that some dofs are non-writable (i.e. the values of the degrees of freedom on the boundary, like the radius of the input-connector cannot be changed).

Parameters

dof	The index of the parameter to be changed.
value	The value, the dof should be set to.

Implements SpaceTransformation.

Definition at line 489 of file HomogenousTransformationCircular.cpp.

References DualProblemTransformationWrapper::case_sectors, DualProblemTransformationWrapper::NDofs(), and DualProblemTransformationWrapper::sectors.

```
489
      int dof = in_dof + 3;
if (dof < (int) NDofs() - 3 && dof >= 0) {
490
491
        int sector = floor(dof / 3);
if (sector == sectors) {
492
493
        case_sectors[sector - 1].dofs_r[dof % 3] = in_val;
} else if (sector == 0) {
494
495
496
          case_sectors[0].dofs_1[dof % 3] = in_val;
        } else {
497
          case_sectors[sector].dofs_1[dof % 3] = in_val;
498
499
           case_sectors[sector - 1].dofs_r[dof % 3] = in_val;
500
501
         std::cout << "Critical: DOF-index out of bounds in "</pre>
502
                       "HomogenousTransformationCircular::set_free_dof!"
503
                    << std::endl;
504
505
      }
506 }
```

4.7.3 Member Data Documentation

4.7.3.1 case_sectors

std::vector<Sector<3> > HomogenousTransformationCircular::case_sectors

This member contains all the Sectors who, as a sum, form the complete Waveguide.

These Sectors are a partition of the simulated domain.

Definition at line 150 of file Homogenous Transformation Circular.h.

Referenced by Homogenous Transformation Rectangular::estimate_and_initialize(), Homogenous Transformation \leftarrow Rectangular::get_dof(), Homogenous Transformation Rectangular::get_free_dof(), Homogenous Transformation \leftarrow Rectangular::get_m(), Homogenous Transformation Rectangular::get_Q1(), Homogenous Transformation Rectangular::get_Q2(), Homogenous Transformation Rectangular::get_v(), Homogenous Transformation Rectangular::PML_Z_Distance(), Homogenous Transformation Rectangular::set_dof(), and Homogenous Transformation Rectangular::set_free_dof().

4.7.3.2 epsilon K

const double HomogenousTransformationCircular::epsilon_K

The material-property ϵ_r has a different value inside and outside of the waveguides core.

This variable stores its value inside the core.

Definition at line 157 of file HomogenousTransformationCircular.h.

4.7.3.3 epsilon_M

 $\verb|const| double | Homogenous Transformation Circular::epsilon_M|$

The material-property ϵ_r has a different value inside and outside of the waveguides core.

This variable stores its value outside the core.

Definition at line 163 of file Homogenous Transformation Circular.h.

4.7.3.4 sectors

```
const int HomogenousTransformationCircular::sectors
```

Since the computational domain is split into subdomains (called sectors), it is important to keep track of the amount of subdomains.

This member stores the number of Sectors the computational domain has been split into.

Definition at line 169 of file Homogenous Transformation Circular.h.

Referenced by Homogenous Transformation Rectangular::estimate_and_initialize(), Homogenous Transformation \leftarrow Rectangular::get_dof(), Homogenous Transformation Rectangular::get_free_dof(), Homogenous Transformation \leftarrow Rectangular::set_dof(), and Homogenous Transformation \leftarrow Rectangular::set_free_dof().

The documentation for this class was generated from the following files:

- Code/SpaceTransformations/HomogenousTransformationCircular.h
- Code/SpaceTransformations/HomogenousTransformationCircular.cpp

4.8 HomogenousTransformationRectangular Class Reference

For this transformation we try to achieve a situation in which tensorial material properties from the coordinate transformation and PML-regions dont overlap.

#include <HomogenousTransformationRectangular.h>

Inheritance diagram for Homogenous Transformation Rectangular:



Public Member Functions

- HomogenousTransformationRectangular (int)
- Point< 3 > math_to_phys (Point< 3 > coord) const
- Point< 3 > phys_to_math (Point< 3 > coord) const
- bool is_identity (Point< 3 > coord) const
- Tensor < 2, 3, std::complex < double > > get_Tensor (Point < 3 > &coordinate) const
- Tensor< 2, 3, std::complex< double >> get_Preconditioner_Tensor (Point< 3 > &coordinate, int block) const
- Tensor< 2, 3, std::complex< double >> Apply_PML_To_Tensor (Point< 3 > &coordinate, Tensor< 2, 3, double > Tensor_input) const
- Tensor< 2, 3, std::complex< double > > Apply_PML_To_Tensor_For_Preconditioner (Point< 3 > &coordinate, Tensor< 2, 3, double > Tensor_input, int block) const
- Tensor < 2, 3, double > get_Space_Transformation_Tensor (Point < 3 > &coordinate) const
- Tensor< 2, 3, double > get_Space_Transformation_Tensor_Homogenized (Point< 3 > &coordinate)
- bool PML_in_X (Point< 3 > &position) const

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the x-axis.

bool PML_in_Y (Point < 3 > &position) const

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the y-axis.

bool PML_in_Z (Point< 3 > &position) const

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the z-axis.

bool Preconditioner_PML_in_Z (Point< 3 > &p, unsigned int block) const

Similar to the PML in Z only this function is used to generate the artificial PML used in the Preconditioner.

double Preconditioner PML Z Distance (Point < 3 > &p, unsigned int block) const

This function fulfills the same purpose as those with similar names but it is supposed to be used together with Preconditioner_PML_in_Z instead of the versions without "Preconditioner".

double PML X Distance (Point < 3 > &position) const

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

double PML_Y_Distance (Point< 3 > &position) const

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

double PML Z Distance (Point < 3 > &position) const

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

void estimate_and_initialize ()

At the beginning (before the first solution of a system) only the boundary conditions for the shape of the waveguide are known.

• double get_Q1 (double z) const

This member calculates the value of Q1 for a provided z-coordinate.

double get_Q2 (double z) const

This member calculates the value of Q2 for a provided z-coordinate.

• double get_Q3 (double z) const

This member calculates the value of Q3 for a provided *z*-coordinate.

double get_dof (int dof) const

This is a getter for the values of degrees of freedom.

void set_dof (int dof, double value)

This function sets the value of the dof provided to the given value.

double get_free_dof (int dof) const

This is a getter for the values of degrees of freedom.

void set_free_dof (int dof, double value)

This function sets the value of the dof provided to the given value.

double System Length () const

Returns the complete length of the computational domain.

double Sector_Length () const

Returns the length of one sector.

· double Layer_Length () const

Returns the length of one layer.

· double get_r (double in_z) const

Returns the radius for a system-coordinate;.

double get_m (double in_z) const

Returns the shift for a system-coordinate;.

double get_v (double in_z) const

Returns the tilt for a system-coordinate;.

- int **Z_to_Layer** (double) const
- Vector< double > Dofs () const

Other objects can use this function to retrieve an array of the current values of the degrees of freedom of the functional we are optimizing.

• unsigned int NFreeDofs () const

This function returns the number of unrestrained degrees of freedom of the current optimization run.

unsigned int NDofs () const

This function returns the total number of DOFs including restrained ones.

• bool IsDofFree (int) const

Since Dofs() also returns restrained degrees of freedom, this function can be applied to determine if a degree of freedom is indeed free or restrained.

· void Print () const

Console output of the current Waveguide Structure.

std::complex< double > evaluate_for_z (double z_in, Waveguide *)

Since the Wavegudie itself may be circular or rectangular now, the evaluation routines should be moved to a point in the code where this information is included in the code.

• std::complex< double > evaluate_for_z_with_sum (double, double, Waveguide *)

Public Attributes

- · const double XMinus
- · const double XPlus
- · const double YMinus
- · const double YPlus
- · const double ZMinus
- · const double ZPlus
- std::vector< Sector< 2 >> case_sectors

This member contains all the Sectors who, as a sum, form the complete Waveguide.

const double epsilon_K

The material-property ϵ_r has a different value inside and outside of the waveguides core.

· const double epsilon_M

The material-property ϵ_r has a different value inside and outside of the waveguides core.

· const int sectors

Since the computational domain is split into subdomains (called sectors), it is important to keep track of the amount of subdomains.

· const double deltaY

This value is initialized with the value Delta from the input-file.

• Vector< double > InitialDofs

This vector of values saves the initial configuration.

4.8.1 Detailed Description

For this transformation we try to achieve a situation in which tensorial material properties from the coordinate transformation and PML-regions dont overlap.

The usage of a coordinate transformation which is identity on the domain containing our PML is a strong restriction however it ensures lower errors since the quality of the PML is harder to estimate otherwise. Also it limits us in how we model the waveguide essentially forcing us to have no bent between the wavguides-connectors.

Author

Pascal Kraft

Date

28.11.2016

Definition at line 28 of file HomogenousTransformationRectangular.h.

4.8.2 Member Function Documentation

4.8.2.1 Dofs()

```
Vector< double > HomogenousTransformationRectangular::Dofs ( ) const [virtual]
```

Other objects can use this function to retrieve an array of the current values of the degrees of freedom of the functional we are optimizing.

This also includes restrained degrees of freedom and other functions can be used to determine this property. This has to be done because in different cases the number of restrained degrees of freedom can vary and we want no logic about this in other functions.

Implements SpaceTransformation.

Definition at line 518 of file HomogenousTransformationRectangular.cpp.

References HomogenousTransformationCircular::get_dof(), and HomogenousTransformationCircular::NDofs().

```
518
519    Vector<double> ret;
520    const int total = NDofs();
521    ret.reinit(total);
522    for (int i = 0; i < total; i++) {
523      ret[i] = get_dof(i);
524    }
525    return ret;
526 }</pre>
```

4.8.2.2 estimate_and_initialize()

```
\verb|void HomogenousTransformationRectangular::estimate\_and\_initialize () | [virtual]| \\
```

At the beginning (before the first solution of a system) only the boundary conditions for the shape of the waveguide are known.

Therefore the values for the degrees of freedom need to be estimated. This function sets all variables to appropriate values and estimates an appropriate shape based on averages and a polynomial interpolation of the boundary conditions on the shape.

Implements SpaceTransformation.

Definition at line 415 of file HomogenousTransformationRectangular.cpp.

 $References \quad Homogenous Transformation Circular:: case_sectors, \quad Homogenous Transformation Circular:: Sector_\leftarrow Length(), \\ Homogenous Transformation Circular:: sectors, \\ and Sector<Dofs_Per_Sector>:: set_properties_force().$

```
415
416
      if (GlobalParams.M PC Use) {
417
        Sector<2> the_first(true, false, GlobalParams.sd.z[0],
418
                              GlobalParams.sd.z[1]);
        the\_first.set\_properties\_force (GlobalParams.sd.m[0], \ GlobalParams.sd.m[1], \\
419
420
                                          GlobalParams.sd.v[0], GlobalParams.sd.v[1]);
        case_sectors.push_back(the_first);
421
        for (int i = 1; i < GlobalParams.sd.Sectors - 2; i++) {</pre>
422
423
          Sector<2> intermediate(false, false, GlobalParams.sd.z[i],
424
                                   GlobalParams.sd.z[i + 1]);
425
           intermediate.set_properties_force(
               GlobalParams.sd.m[i], GlobalParams.sd.m[i + 1], GlobalParams.sd.v[i], GlobalParams.sd.v[i + 1]);
426
42.7
428
          case_sectors.push_back(intermediate);
429
430
        Sector<2> the_last(false, true,
```

```
431
                           GlobalParams.sd.z[GlobalParams.sd.Sectors - 2],
                           GlobalParams.sd.z[GlobalParams.sd.Sectors - 1]);
432
433
       the_last.set_properties_force(
434
            GlobalParams.sd.m[GlobalParams.sd.Sectors - 2],
           GlobalParams.sd.m[GlobalParams.sd.Sectors - 1],
435
           GlobalParams.sd.v[GlobalParams.sd.Sectors - 2],
436
           GlobalParams.sd.v[GlobalParams.sd.Sectors - 1]);
437
438
       case_sectors.push_back(the_last);
       439
440
441
442
443
444
                  << "(m: " << case_sectors[i].get_m(1.0)
                 << " v: " << case_sectors[i].get_v(1.0) << ")" << std::endl;</pre>
445
446
447
     } else {
448
       case sectors.reserve(sectors);
       double m_0 = GlobalParams.M_W_Delta / 2.0;
449
       double m_1 = -GlobalParams.M_W_Delta / 2.0;
451
       <u>if</u> (sectors == 1) {
452
         Sector<2> temp12(true, true, -GlobalParams.M_R_ZLength / 2.0,
453
                          GlobalParams.M_R_ZLength / 2.0);
         case_sectors.push_back(temp12);
454
         case_sectors[0].set_properties_force(
   GlobalParams.M_W_Delta / 2.0, -GlobalParams.M_W_Delta / 2.0,
455
456
457
             GlobalParams.M_C_DimlIn, GlobalParams.M_C_DimlOut, 0, 0);
458
459
         double length = Sector_Length();
         Sector<2> temp(true, false, -GlobalParams.M_R_ZLength / (2.0),
460
                         -GlobalParams.M_R_ZLength / 2.0 + length);
461
462
         case sectors.push back(temp);
         for (int i = 1; i < sectors; i++) {
463
464
           Sector<2> temp2(false, false,
                           -GlobalParams.M_R_ZLength / (2.0) + length * (1.0 * i),
-GlobalParams.M_R_ZLength / (2.0) + length * (i + 1.0));
465
466
467
           case_sectors.push_back(temp2);
468
469
470
         double length_rel = 1.0 / ((double) (sectors));
471
         case_sectors[0].set_properties_force(
             472
473
             InterpolationPolynomialDerivative(length_rel, m_0, m_1, 0, 0));
474
         for (int i = 1; i < sectors; i++) {</pre>
          double z_l = i * length_rel;
475
           double z_r = (i + 1) * length_rel;
476
477
           case_sectors[i].set_properties_force(
478
                InterpolationPolynomialZeroDerivative(z_r, m_0, m_1),
InterpolationPolynomialDerivative(z_1, m_0, m_1, 0, 0),
479
480
481
               InterpolationPolynomialDerivative(z_r, m_0, m_1, 0, 0));
482
483
484
     }
485 }
```

4.8.2.3 evaluate_for_z()

Since the Wavegudie itself may be circular or rectangular now, the evaluation routines should be moved to a point in the code where this information is included in the code.

Since I dont want to create derived classes from waveguide (which I should do eventually) I will for now include this functionality into the space transformation which is shape-sensitive. The waveguide only offers the evaluation at a point. The quadrature-rule has to be imposed by the space transformation.

Implements SpaceTransformation.

Definition at line 334 of file HomogenousTransformationRectangular.cpp.

4.8.2.4 get_dof()

This is a getter for the values of degrees of freedom.

A getter-setter interface was introduced since the values are estimated automatically during the optimization and non-physical systems should be excluded from the domain of possible cases.

Parameters

dof The index of the degree of freedom to be retrieved from the structure of the modelled waveguide.

Returns

This function returns the value of the requested degree of freedom. Should this dof not exist, 0 will be returnd.

Implements SpaceTransformation.

Definition at line 340 of file HomogenousTransformationRectangular.cpp.

References Homogenous Transformation Circular::case_sectors, Homogenous Transformation Circular::NDofs(), and Homogenous Transformation Circular::sectors.

Referenced by InhomogenousTransformationCircular::Dofs().

```
340
341
      if (dof < (int)NDofs() && dof >= 0) {
        int sector = floor(dof / 2);
if (sector == sectors) {
342
343
344
          return case_sectors[sector - 1].dofs_r[dof % 2];
345
        } else {
346
          return case_sectors[sector].dofs_1[dof % 2];
347
348
     } else {
        std::cout << "Critical: DOF-index out of bounds in "</pre>
349
350
                      "HomogenousTransformationRectangular::get_dof!"
351
                   << std::endl;
352
        return 0.0;
353 }
354 }
```

4.8.2.5 get_free_dof()

This is a getter for the values of degrees of freedom.

A getter-setter interface was introduced since the values are estimated automatically during the optimization and non-physical systems should be excluded from the domain of possible cases.

Parameters

dof The index of the degree of freedom to be retrieved from the structure of the modelled waveguide.

Returns

This function returns the value of the requested degree of freedom. Should this dof not exist, 0 will be returnd.

Implements SpaceTransformation.

Definition at line 356 of file HomogenousTransformationRectangular.cpp.

 $References\ Homogenous\ Transformation\ Circular:: case_sectors,\ Homogenous\ Transformation\ Circular:: NDofs(),\ and\ Homogenous\ Transformation\ Circular:: sectors.$

```
int dof = in_dof + 2;
if (dof < (int)NDofs() - 2 && dof >= 0) {
  int sector = floor(dof / 2);
  if (sector == sectors) {
357
358
359
360
361
           return case_sectors[sector - 1].dofs_r[dof % 2];
       } else {
362
          return case_sectors[sector].dofs_1[dof % 2];
363
364
365 } else {
      std::cout << "Critical: DOF-index out of bounds in "
366
367
         << std::endl;</pre>
                        "HomogenousTransformationRectangular::get_free_dof!"
368
        return 0.0;
369
370 }
371 }
```

4.8.2.6 get_Q1()

```
double HomogenousTransformationRectangular::get_Q1 ( \label{eq:const} \mbox{double $z$ ) const [virtual]}
```

This member calculates the value of Q1 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

|z| The value of Q1 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implements SpaceTransformation.

Definition at line 503 of file HomogenousTransformationRectangular.cpp.

References Homogenous Transformation Circular::case_sectors, and Space Transformation:: Z_{to} Sector_and_ \leftarrow local_z().

```
503
504 std::pair<int, double> two = Z_to_Sector_and_local_z(z_in);
505 return case_sectors[two.first].getQ1(two.second);
506 }
```

4.8.2.7 get Q2()

```
double HomogenousTransformationRectangular::get_Q2 ( double z ) const [virtual]
```

This member calculates the value of Q2 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q2 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implements SpaceTransformation.

Definition at line 508 of file HomogenousTransformationRectangular.cpp.

References HomogenousTransformationCircular::case_sectors, and SpaceTransformation::Z_to_Sector_and_ ← local_z().

```
508
509 std::pair<int, double> two = Z_to_Sector_and_local_z(z_in);
510 return case_sectors[two.first].getQ2(two.second);
511 }
```

4.8.2.8 get_Q3()

```
double HomogenousTransformationRectangular::get_Q3 ( double z ) const [virtual]
```

This member calculates the value of Q3 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q3 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implements SpaceTransformation.

Definition at line 513 of file Homogenous Transformation Rectangular.cpp.

References Homogenous Transformation Circular::case_sectors, and Space Transformation:: Z_{to} Sector_and_ \leftarrow local_z().

```
513
514 std::pair<int, double> two = Z_to_Sector_and_local_z(z_in);
515    return case_sectors[two.first].getQ3(two.second);
516 }
```

4.8.2.9 IsDofFree()

Since Dofs() also returns restrained degrees of freedom, this function can be applied to determine if a degree of freedom is indeed free or restrained.

"restrained" means that for example the DOF represents the radius at one of the connectors (input or output) and therefore we forbid the optimization scheme to vary this value.

Implements SpaceTransformation.

Definition at line 532 of file Homogenous Transformation Rectangular.cpp.

References HomogenousTransformationCircular::NDofs().

```
532 {
533    return index > 1 && index < (int) NDofs() - 1;
534 }
```

4.8.2.10 NDofs()

```
unsigned int HomogenousTransformationRectangular::NDofs ( ) const [virtual]
```

This function returns the total number of DOFs including restrained ones.

This is the lenght of the array returned by Dofs().

Implements SpaceTransformation.

Definition at line 540 of file Homogenous Transformation Rectangular.cpp.

References Homogenous Transformation Circular::sectors.

Referenced by Inhomogenous Transformation Circular::Dofs(), Inhomogenous Transformation Circular::get_ \leftarrow dof(), Inhomogenous Transformation Circular::get_free_dof(), Inhomogenous Transformation Circular::IsDof \leftarrow Free(), Inhomogenous Transformation Circular::NFreeDofs(), Inhomogenous Transformation Circular::set_dof(), and Inhomogenous Transformation Circular::set_free_dof().

```
540
541 return sectors * 2 + 2;
542 }
```

4.8.2.11 PML_in_X()

```
bool HomogenousTransformationRectangular::PML_in_X ( Point < 3 > \& \ position \ ) \ const \ \ [virtual]
```

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the x-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

position	Stores the position in which to test for presence of a PML-Material.
1	

Implements SpaceTransformation.

Definition at line 84 of file Homogenous Transformation Rectangular.cpp.

Referenced by InhomogenousTransformationCircular::PML_Z_Distance().

4.8.2.12 PML_in_Y()

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the y-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

position	Stores the position in which to test for presence of a PML-Material.
----------	--

Implements SpaceTransformation.

Definition at line 88 of file HomogenousTransformationRectangular.cpp.

Referenced by InhomogenousTransformationCircular::PML_Z_Distance().

4.8.2.13 PML_in_Z()

```
bool HomogenousTransformationRectangular::PML_in_Z (  Point < ~3~>~\&~position~)~const~[virtual]
```

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the z-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

position	Stores the position in which to test for presence of a PML-Material.
p 0 0	otoreo are producer ar armor to took in processes of a raise material

Implements SpaceTransformation.

Definition at line 92 of file HomogenousTransformationRectangular.cpp.

Referenced by Inhomogenous Transformation Circular:: PML Z Distance().

```
92

93    return p(2) > ZPlus || p(2) < ZMinus;

94 }
```

4.8.2.14 PML X Distance()

```
double HomogenousTransformationRectangular::PML_X_Distance ( Point < \ 3 \ > \ \& \ position \ ) \ const \ \ [virtual]
```

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

```
position Stores the position from which to calculate the distance to the PML-surface.
```

Implements SpaceTransformation.

Definition at line 102 of file Homogenous Transformation Rectangular.cpp.

 $Referenced \ by \ Inhomogenous Transformation Circular:: PML_Z_Distance().$

```
103

104 if (p(0) > 0) {

105 return p(0) - XPlus;

106 } else {

107 return -p(0) + XMinus;

108 }

109 }
```

4.8.2.15 PML_Y_Distance()

```
double HomogenousTransformationRectangular::PML_Y_Distance ( Point < \ 3 \ > \ \& \ position \ ) \ const \ \ [virtual]
```

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

position Stores the position from which to calculate the distance to the PML-surface.

Implements SpaceTransformation.

Definition at line 111 of file HomogenousTransformationRectangular.cpp.

Referenced by Inhomogenous Transformation Circular:: PML Z Distance().

4.8.2.16 PML Z Distance()

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

position Stores the position from which to calculate the distance to the PML-surface.

Implements SpaceTransformation.

Definition at line 120 of file Homogenous Transformation Rectangular.cpp.

 $\label{eq:local_resolution} References & Homogenous Transformation Circular:: case_sectors, & Homogenous Transformation Circular:: PML $ _ in_X(), & Homogenous Transformation Circular:: PML_in_Y(), & Homogenous Transformation Circular:: PML_X_Distance(), & Homogenous Transformation Circular:: PML_Y $ _ Distance(), & Homogenous Transformation Circular:: PML_Z_Distance(), & Homogenous Transformation Circular:: $ _ Preconditioner_PML_Z_Distance(), and Space Transformation:: $ _ Sector_and_local_z(). $ _ Sect$

 $Referenced \ by \ Inhomogenous Transformation Circular :: PML_Z_Distance ().$

```
121 {
122    if (p(2) < 0) {
123       return -(p(2) + (GlobalParams.M_R_ZLength / 2.0));
124    } else {
125       return p(2) - (GlobalParams.M_R_ZLength / 2.0);
126    }
127 }
```

4.8.2.17 Preconditioner_PML_in_Z()

```
bool HomogenousTransformationRectangular::Preconditioner_PML_in_Z ( Point< 3 > & p, unsigned int block) const
```

Similar to the PML_in_Z only this function is used to generate the artificial PML used in the Preconditioner.

These Layers are not only situated at the surface of the computational domain but also inside it at the interfaces of Sectors.

Referenced by InhomogenousTransformationCircular::PML_Z_Distance().

4.8.2.18 set_dof()

```
void HomogenousTransformationRectangular::set_dof ( int \ dof, \\ double \ value \ ) \ \ [virtual]
```

This function sets the value of the dof provided to the given value.

It is important to consider, that some dofs are non-writable (i.e. the values of the degrees of freedom on the boundary, like the radius of the input-connector cannot be changed).

Parameters

dof	The index of the parameter to be changed.
value	The value, the dof should be set to.

Implements SpaceTransformation.

Definition at line 373 of file HomogenousTransformationRectangular.cpp.

References HomogenousTransformationCircular::case_sectors, HomogenousTransformationCircular::NDofs(), and HomogenousTransformationCircular::sectors.

```
373
374
     if (dof < (int) NDofs() && dof >= 0) {
375
      int sector = floor(dof / 2);
      if (sector == sectors) {
377
        case_sectors[sector - 1].dofs_r[dof % 2] = in_val;
      } else if (sector == 0) {
378
379
        case_sectors[0].dofs_1[dof % 2] = in_val;
      } else {
380
381
        case_sectors[sector].dofs_l[dof % 2] = in_val;
382
        case_sectors[sector - 1].dofs_r[dof % 2] = in_val;
383
384
    } else {
      385
386
               << std::endl;
387
388
    }
389 }
```

4.8.2.19 set_free_dof()

This function sets the value of the dof provided to the given value.

It is important to consider, that some dofs are non-writable (i.e. the values of the degrees of freedom on the boundary, like the radius of the input-connector cannot be changed).

Parameters

dof	The index of the parameter to be changed
value	The value, the dof should be set to.

Implements SpaceTransformation.

Definition at line 391 of file Homogenous Transformation Rectangular.cpp.

References HomogenousTransformationCircular::case_sectors, HomogenousTransformationCircular::NDofs(), and HomogenousTransformationCircular::sectors.

```
392
     int dof = in dof + 2;
393
394
      if (dof < (int) NDofs() - 2 && dof >= 0) {
        int sector = floor(dof / 2);
395
        if (sector == sectors) {
397
         case_sectors[sector - 1].dofs_r[dof % 2] = in_val;
398
       } else if (sector == 0) {
         case_sectors[0].dofs_l[dof % 2] = in_val;
399
400
        } else {
401
          case_sectors[sector].dofs_l[dof % 2] = in_val;
402
          case_sectors[sector - 1].dofs_r[dof % 2] = in_val;
403
404
     } else {
        std::cout << "Critical: DOF-index out of bounds in "</pre>
405
                     "HomogenousTransformationRectangular::set_free_dof!"
406
                  << std::endl;
408
     }
409 }
```

4.8.3 Member Data Documentation

4.8.3.1 case_sectors

```
std::vector<Sector<2> > HomogenousTransformationRectangular::case_sectors
```

This member contains all the Sectors who, as a sum, form the complete Waveguide.

These Sectors are a partition of the simulated domain.

Definition at line 141 of file HomogenousTransformationRectangular.h.

Referenced by Inhomogenous Transformation Circular::estimate_and_initialize(), Inhomogenous Transformation \leftarrow Circular::get_dof(), Inhomogenous Transformation Circular::get_free_dof(), Inhomogenous Transformation Circular::get_Q1(), Inhomogenous Transformation Circular::get_Q2(), Inhomogenous Transformation Circular::get_Q3(), Inhomogenous Transformation Circular::get_r(), Inhomogenous Transformation Circular::get_v(), Inhomogenous Transformation Circular::get_v(), Inhomogenous Transformation Circular::get_v(), Inhomogenous Transformation Circular::set_free_dof().

4.8.3.2 epsilon_K

 $\verb|const| double | Homogenous Transformation Rectangular::epsilon_K|$

The material-property ϵ_r has a different value inside and outside of the waveguides core.

This variable stores its value inside the core.

Definition at line 148 of file HomogenousTransformationRectangular.h.

4.8.3.3 epsilon_M

const double HomogenousTransformationRectangular::epsilon_M

The material-property ϵ_r has a different value inside and outside of the waveguides core.

This variable stores its value outside the core.

Definition at line 154 of file HomogenousTransformationRectangular.h.

4.8.3.4 sectors

 $\verb|const| int Homogenous Transformation Rectangular:: sectors|\\$

Since the computational domain is split into subdomains (called sectors), it is important to keep track of the amount of subdomains.

This member stores the number of Sectors the computational domain has been split into.

Definition at line 160 of file Homogenous Transformation Rectangular.h.

Referenced by Inhomogenous Transformation Circular::estimate_and_initialize(), Inhomogenous Transformation \leftarrow Circular::get_dof(), Inhomogenous Transformation Circular::get_free_dof(), Inhomogenous Transformation Circular::set_dof(), and Inhomogenous Transformation Circular::set_free_ \leftarrow dof().

The documentation for this class was generated from the following files:

- · Code/SpaceTransformations/HomogenousTransformationRectangular.h
- Code/SpaceTransformations/HomogenousTransformationRectangular.cpp

4.9 HSIE_Dof_Type< hsie_order > Class Template Reference

Public Member Functions

- HSIE_Dof_Type (unsigned int in_type, unsigned int in_order, unsigned int q_count)
- void set base point (unsigned int)

Base Points are numbered: 0: low x, low y; 1: low x, high y; 2: high x, high y; 3: high x, low y;.

void set_base_edge (unsigned int)

Edges are numbered: 0: y edge from point 0; 1: x edge from point 1; 2: y edge from point 2; 3: x edge from point 3;.

- std::complex< double > eval_base (std::vector< std::complex< double >> *in_base, std::complex< double > in_x)
- unsigned int get_type ()

This describes the properties of a HSIE dof type.

- void set_x_length (double in_length)
- void set_y_length (double in_length)
- unsigned int get_order ()
- void prepare_for_quadrature_points (std::vector< dealii::Point< 2, double >> q_points)
- void compute_IPsik ()
- void compute_dxiPsik ()
- std::vector< std::complex< double >> evaluate_U (dealii::Point< 2, double >, double xi)
- std::vector< std::complex< double >> evaluate_U_for_ACT (dealii::Point< 2, double >, double xi)
- std::complex < double > component_1a (double x, double y, std::complex < double > xhi)
- std::complex< double > component_1b (double x, double y, std::complex< double > xhi)
- std::complex< double > component_2a (double x, double y, std::complex< double > xhi)
- std::complex< double > component_2b (double x, double y, std::complex< double > xhi)
- std::complex< double > component_3a (double x, double y, std::complex< double > xhi)
- std::complex < double > component 3b (double x, double y, std::complex < double > xhi)
- std::vector< std::complex< double >> apply_T_plus (std::vector< std::complex< double >>, double)
- std::vector< std::complex< double >> apply_T_minus (std::vector< std::complex< double >>, double)

4.9.1 Detailed Description

```
template<int hsie_order>
class HSIE_Dof_Type< hsie_order>
```

Definition at line 16 of file HSIEDofType.h.

4.9.2 Member Function Documentation

4.9.2.1 get_type()

```
template<int hsie_order>
unsigned int HSIE_Dof_Type< hsie_order >::get_type ( ) [inline]
```

This describes the properties of a HSIE dof type.

The versions are descirbed in 3.2 of "High order Curl-conforming Hardy space infinite elements for exterior Maxwell problems". Possible types are: 0. edge functions

- 1. surface functions
- 2. ray functions
- 3. infinite face functions type 1
- 4. infinite face functions type 2
- 5. segment functions type 1
- 6. segment functions type 2

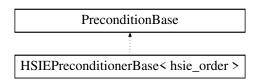
Definition at line 147 of file HSIEDofType.cpp.

The documentation for this class was generated from the following files:

- · Code/HSIE/HSIEDofType.h
- Code/HSIE/HSIEDofType.cpp

4.10 HSIEPreconditionerBase< hsie_order > Class Template Reference

Inheritance diagram for HSIEPreconditionerBase< hsie_order >:



Public Member Functions

• HSIEPreconditionerBase (const dealii::parallel::distributed::Triangulation < 3 > *in tria, double in z)

This constructor of a HSIE Predonditioner works as follows.

• unsigned int n dofs ()

The order of the Hardy-Space polynomials was given as a template argument to an object of this type, so no arguments are required for this function.

unsigned int n_dofs_per_face ()

Similar to the function *n* dofs() this function doesn't currently need any arguments.

void assemble block ()

This function brings the Object-member HSIEPreconditionerBase::system_matrix which is currently supposed to hold all HSIE-dofs (including the Nedelec-elements of the surface elements).

void setup_system ()

This must be called before assemble block since it initializes the HSIEPreconditionerBase::system_matrix.

std::complex < double > a (HSIE_Dof_Type < hsie_order > u, HSIE_Dof_Type < hsie_order > v, bool use ← curl fomulation, dealii::Point < 2, double > x)

This function implements the following equation:

$$a(U,V) := \frac{-2\operatorname{i} \kappa_0}{2\pi} \int_{S_0} U(z) v(\bar{z}) |\mathrm{d}z|$$

which is called from A() which in turn is required to build the HSIEPreconditionerBase::system_matrix.

std::complex < double > A (HSIE_Dof_Type < hsie_order > u, HSIE_Dof_Type < hsie_order > v, dealii::←
Tensor < 2, 3, double > G, bool use curl formulation)

This function implements the following equation:

$$A(U,V) := \int_T \sum_{i,j=1}^3 g_{ij}(\hat{x}) a(U_i(\cdot,\hat{x}), V_j(\cdot,\hat{x})) d\hat{x}$$

where T is a Triangulation of the surface.

Public Attributes

• dealii::TrilinosWrappers::SparseMatrix system_matrix

This matrix contains the couplings between all HSIE-dofs.

4.10.1 Detailed Description

```
template<int hsie_order>
class HSIEPreconditionerBase< hsie_order>
```

Definition at line 20 of file HSIE_Preconditioner_Base.h.

4.10.2 Constructor & Destructor Documentation

4.10.2.1 HSIEPreconditionerBase()

This constructor of a HSIE Predonditioner works as follows.

It takes a given Triangulation and cuts it at a specified z-coordinate and applies infinite elements to the surface generated in this way. This class will be renamed appropriately later since it is not really a Preconditioner as much as it is a general implementation of the HSIE method which can also be employed as part of a preconditioner.

Parameters

in_tria	A handle to the triangulation which contains the surface.
in_z	the z-coordinate at which to attach the infinite Elements.

Definition at line 192 of file HSIE Preconditioner Base.cpp.

```
194
195
      FaceSurfaceComparatorZ fscz = new FaceSurfaceComparatorZ(in_z
      , 0.00001);
196
      association = extract_surface_mesh_at_z(in_tria, &surf_tria, fscz);
      surface_edges = surf_tria.n_active_lines();
surface_faces = surf_tria.n_active_faces();
197
198
199
      surface_vertices = surf_tria.n_vertices();
200
      HSIE_dofs_type_1_factor = dealii::GeometryInfo<2>::lines_per_face * 2;
      HSIE_dofs_type_3_factor =
202
          dealii::GeometryInfo<2>::lines_per_face * 2 * (hsie_order + 1);
203
      HSIE_dofs_type_2_factor =
204
      dealii::GeometryInfo<2>::vertices_per_face * 2 * (hsie_order + 1);
HSIE_degree = hsie_order;
205
206
      fe_nedelec(GlobalParams.So_ElementOrder);
207
      fe_q(1);
208
      quadrature_formula(2);
209
      hsie_dof_handler(surf_tria);
210
      FEValues<3> fev_nedelec(fe_nedelec, quadrature_formula,
211
                                update_values | update_gradients | update_JxW_values |
                                    update_quadrature_points);
212
      FEValues<3> fev_q(fe_q, quadrature_formula,
214
                         update_values | update_gradients | update_JxW_values |
215
                              update_quadrature_points);
216 }
```

4.10.3 Member Function Documentation

4.10.3.1 a()

This function implements the following equation:

$$a(U,V) := \frac{-2\operatorname{i} \kappa_0}{2\pi} \int_{S_0} U(z) v(\bar{z}) |\mathrm{d}z|$$

which is called from A() which in turn is required to build the HSIEPreconditionerBase::system_matrix.

Parameters

и	is an object describing the first type of dof,
V	describes the second dof,
use_curl_formulation	simplifies the usage of this function: It causes the function not to use \$u_1\$ etc. but the terms in A()'s argument list (see equation (30) in the paper High order Curl-conforming Hardy space infinite elements for exterior Maxwell problems.)
Х	is the Point in the surface triangulation where to evaluate the bilinear form.

Definition at line 303 of file HSIE_Preconditioner_Base.cpp.

```
305
```

4.10.3.2 A()

This function implements the following equation:

$$A(U,V) := \int_T \sum_{i,j=1}^3 g_{ij}(\hat{x}) a(U_i(\cdot,\hat{x}), V_j(\cdot,\hat{x})) d\hat{x}$$

where T is a Triangulation of the surface.

For more details see the publication mentioned in the description of a().

Parameters

и	is an object describing the first type of dof,
V	describes the second dof,
G	is the \$3 3\$ matrix consisting of \$g_{ij}\$
use_curl_formulation	has the same purpose as in a().

Definition at line 308 of file HSIE_Preconditioner_Base.cpp.

```
310
311
       dealii::QGauss<2> quadrature_formula(2);
312
       std::complex<double> ret(0, 0);
313
       std::vector<dealii::Point<2>> quad_points
314
           quadrature_formula.quadrature_points;
       for (unsigned int i = 0; i < quad_points.size(); i++) {
   for (unsigned int j = 0; j < 3; j++) {
     for (unsigned int k = 0; k < 3; k++) {</pre>
315
316
317
              ret += quadrature_formula.weight(i) * G[j, k] *
319
                       a(u, v, true, quad_points[i]);
320
321
        }
322
323
      return ret;
```

4.10.3.3 assemble_block()

```
template<int hsie_order>
void HSIEPreconditionerBase< hsie_order >::assemble_block ( )
```

This function brings the Object-member HSIEPreconditionerBase::system_matrix which is currently supposed to hold all HSIE-dofs (including the Nedelec-elements of the surface elements).

This makes coupling the dofs to the interior via dof-constraints necessary.

4.10.3.4 n_dofs()

```
template<int hsie_order>
unsigned int HSIEPreconditionerBase< hsie_order >::n_dofs ( )
```

The order of the Hardy-Space polynomials was given as a template argument to an object of this type, so no arguments are required for this function.

Eventually a version of this function will be added which can deal with higher then lowest order elements in the interior.

Definition at line 285 of file HSIE_Preconditioner_Base.cpp.

```
285
286 unsigned int ret = 0;
287 ret += surface_edges * HSIE_dofs_type_1_factor;
288 ret += surface_vertices * HSIE_dofs_type_2_factor;
289 ret += surface_edges * HSIE_dofs_type_3_factor;
290 return ret;
291 }
```

4.10.3.5 n_dofs_per_face()

```
template<int hsie_order>
unsigned int HSIEPreconditionerBase< hsie_order >::n_dofs_per_face ( )
```

Similar to the function n_dofs() this function doesn't currently need any arguments.

This one however returns the number of HSIE-Dofs per face, which will act as a replacement of dealii's similar functions dofs_per_face etc.

Definition at line 294 of file HSIE_Preconditioner_Base.cpp.

```
294
295 unsigned int ret = 0;
296 ret += 4 * HSIE_dofs_type_1_factor;
297 ret += 4 * HSIE_dofs_type_2_factor;
298 ret += 4 * HSIE_dofs_type_3_factor;
299 return ret;
300 }
```

4.10.4 Member Data Documentation

4.10.4.1 system_matrix

```
template<int hsie_order>
dealii::TrilinosWrappers::SparseMatrix HSIEPreconditionerBase< hsie_order >::system_matrix
```

This matrix contains the couplings between all HSIE-dofs.

This also contains the Nedelec-Elements of the surface triangulation.

Definition at line 122 of file HSIE_Preconditioner_Base.h.

The documentation for this class was generated from the following files:

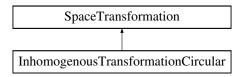
- Code/HSIE/HSIE_Preconditioner_Base.h
- Code/HSIE/HSIE_Preconditioner_Base.cpp

4.11 Inhomogenous Transformation Circular Class Reference

In this case we regard a tubular waveguide and the effects on the material tensor by the space transformation and the boundary condition PML may overlap (hence inhomogenous space transformation)

#include <InhomogenousTransformationCircular.h>

Inheritance diagram for Inhomogenous Transformation Circular:



Public Member Functions

- InhomogenousTransformationCircular (int)
- Point< 3 > math_to_phys (Point< 3 > coord) const
- Point< 3 > phys_to_math (Point< 3 > coord) const
- bool is_identity (Point < 3 > coord) const
- Tensor < 2, 3, std::complex < double > > get_Tensor (Point < 3 > &coordinate) const
- Tensor< 2, 3, std::complex< double >> get_Preconditioner_Tensor (Point< 3 > &coordinate, int block) const
- Tensor< 2, 3, std::complex< double >> Apply_PML_To_Tensor (Point< 3 > &coordinate, Tensor< 2, 3, double > Tensor_input) const
- Tensor< 2, 3, std::complex< double > > Apply_PML_To_Tensor_For_Preconditioner (Point< 3 > &coordinate, Tensor< 2, 3, double > Tensor_input, int block) const
- Tensor < 2, 3, double > get_Space_Transformation_Tensor (Point < 3 > &coordinate) const
- Tensor< 2, 3, double > get_Space_Transformation_Tensor_Homogenized (Point< 3 > &coordinate)
- bool PML_in_X (Point< 3 > &position) const

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the x-axis.

bool PML_in_Y (Point < 3 > &position) const

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the y-axis.

bool PML_in_Z (Point< 3 > &position) const

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the z-axis.

bool Preconditioner_PML_in_Z (Point< 3 > &p, unsigned int block) const

Similar to the PML_in_Z only this function is used to generate the artificial PML used in the Preconditioner.

double Preconditioner PML Z Distance (Point < 3 > &p, unsigned int block) const

This function fulfills the same purpose as those with similar names but it is supposed to be used together with Preconditioner_PML_in_Z instead of the versions without "Preconditioner".

double PML X Distance (Point < 3 > &position) const

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

double PML_Y_Distance (Point< 3 > &position) const

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

double PML Z Distance (Point < 3 > &position) const

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

void estimate_and_initialize ()

At the beginning (before the first solution of a system) only the boundary conditions for the shape of the waveguide are known.

• double get_Q1 (double z) const

This member calculates the value of Q1 for a provided *z*-coordinate.

• double get Q2 (double z) const

This member calculates the value of Q2 for a provided z-coordinate.

• double get_Q3 (double z) const

This member calculates the value of Q3 for a provided *z*-coordinate.

double get dof (int dof) const

This is a getter for the values of degrees of freedom.

void set dof (int dof, double value)

This function sets the value of the dof provided to the given value.

· double get free dof (int dof) const

This is a getter for the values of degrees of freedom.

• void set_free_dof (int dof, double value)

This function sets the value of the dof provided to the given value.

• double System_Length () const

Using this method unifies the usage of coordinates.

double Sector_Length () const

Returns the length of one sector.

double Layer_Length () const

Returns the length of one layer.

double get_r (double in_z) const

Returns the radius for a system-coordinate;.

• double get_m (double in_z) const

Returns the shift for a system-coordinate;.

double get_v (double in_z) const

Returns the tilt for a system-coordinate;.

- int Z_to_Layer (double) const
- Vector< double > Dofs () const

Other objects can use this function to retrieve an array of the current values of the degrees of freedom of the functional we are optimizing.

• unsigned int NFreeDofs () const

This function returns the number of unrestrained degrees of freedom of the current optimization run.

· unsigned int NDofs () const

This function returns the total number of DOFs including restrained ones.

• bool IsDofFree (int) const

Since Dofs() also returns restrained degrees of freedom, this function can be applied to determine if a degree of freedom is indeed free or restrained.

· void Print () const

Console output of the current Waveguide Structure.

std::complex < double > evaluate_for_z (double z_in, Waveguide *)

Since the Wavegudie itself may be circular or rectangular now, the evaluation routines should be moved to a point in the code where this information is included in the code.

- std::complex< double > evaluate_for_z_with_sum (double, double, Waveguide *)
- std::complex< double > gauss_product_2D_sphere (double z, int n, double R, double Xc, double Yc, Waveguide *in_w)

Public Attributes

- · const double XMinus
- · const double XPlus
- · const double YMinus
- · const double YPlus
- · const double ZMinus
- · const double ZPlus
- std::vector< Sector< 3 >> case_sectors

This member contains all the Sectors who, as a sum, form the complete Waveguide.

• const double epsilon_K

The material-property ϵ_r has a different value inside and outside of the waveguides core.

· const double epsilon_M

The material-property ϵ_r has a different value inside and outside of the waveguides core.

· const int sectors

Since the computational domain is split into subdomains (called sectors), it is important to keep track of the amount of subdomains.

· const double deltaY

This value is initialized with the value Delta from the input-file.

• Vector< double > InitialDofs

This vector of values saves the initial configuration.

4.11.1 Detailed Description

In this case we regard a tubular waveguide and the effects on the material tensor by the space transformation and the boundary condition PML may overlap (hence inhomogenous space transformation)

The usage of a coordinate transformation which is identity on the domain containing our PML is a strong restriction however it ensures lower errors since the quality of the PML is harder to estimate otherwise. Also it limits us in how we model the waveguide essentially forcing us to have no bent between the wavguides-connectors.

Author

Pascal Kraft

Date

28.11.2016

Definition at line 28 of file InhomogenousTransformationCircular.h.

4.11.2 Member Function Documentation

4.11.2.1 Dofs()

```
Vector< double > InhomogenousTransformationCircular::Dofs ( ) const [virtual]
```

Other objects can use this function to retrieve an array of the current values of the degrees of freedom of the functional we are optimizing.

This also includes restrained degrees of freedom and other functions can be used to determine this property. This has to be done because in different cases the number of restrained degrees of freedom can vary and we want no logic about this in other functions.

Implements SpaceTransformation.

Definition at line 551 of file InhomogenousTransformationCircular.cpp.

References HomogenousTransformationRectangular::get_dof(), and HomogenousTransformationRectangular::N← Dofs().

```
551
552     Vector<double> ret;
553     const int total = NDofs();
554     ret.reinit(total);
555     for (int i = 0; i < total; i++) {
        ret[i] = get_dof(i);
557     }
558     return ret;
559 }</pre>
```

4.11.2.2 estimate_and_initialize()

```
void InhomogenousTransformationCircular::estimate_and_initialize ( ) [virtual]
```

At the beginning (before the first solution of a system) only the boundary conditions for the shape of the waveguide

Therefore the values for the degrees of freedom need to be estimated. This function sets all variables to appropriate values and estimates an appropriate shape based on averages and a polynomial interpolation of the boundary conditions on the shape.

Implements SpaceTransformation.

 $Definition\ at\ line\ 473\ of\ file\ Inhomogenous Transformation Circular.cpp.$

 $References \ \ Homogenous Transformation Rectangular:: case_sectors, \ \ Homogenous Transformation Rectangular:: \hookleftarrow Sector_Length(), and \ \ Homogenous Transformation Rectangular:: sectors.$

```
474
       case_sectors.reserve(sectors);
       double m_0 = GlobalParams.M_W_Delta / 2.0;
double m_1 = -GlobalParams.M_W_Delta / 2.0;
double r_0 = GlobalParams.M_C_DimlIn;
475
476
477
       double r_1 = GlobalParams.M_C_Dim1Out;
478
       if (sectors == 1)
480
          Sector<3> temp12(true, true, -GlobalParams.M_R_ZLength / 2,
481
                                GlobalParams.M_R_ZLength / 2);
482
          case_sectors.push_back(temp12);
         case_sectors[0].set_properties_force(
    GlobalParams.M_W_Delta / 2.0, -GlobalParams.M_W_Delta / 2.0,
483
484
485
               GlobalParams.M_C_DimlIn, GlobalParams.M_C_DimlOut, 0, 0);
486
```

```
487
       double length = Sector_Length();
       Sector<3> temp(true, false, -GlobalParams.M_R_ZLength / (2.0),
488
489
                       -GlobalParams.M_R_ZLength / 2.0 + length);
490
       case_sectors.push_back(temp);
       for (int i = 1; i < sectors; i++)
  Sector<3> temp2(false, false,
491
492
                         -GlobalParams.M_R_ZLength / (2.0) + length * (1.0 * i),

-GlobalParams.M_R_ZLength / (2.0) + length * (i + 1.0));
493
494
495
         case_sectors.push_back(temp2);
496
497
       double length_rel = 1.0 / ((double) (sectors));
498
499
       case_sectors[0].set_properties_force(
500
            m_0, InterpolationPolynomialZeroDerivative(length_rel, m_0, m_1), r_0,
501
            InterpolationPolynomialZeroDerivative(length_rel, r_0, r_1), 0,
502
            for (int i = 1; i < sectors; i++) {
  double z_l = i * length_rel;
  double z_r = (i + 1) * length_rel;</pre>
503
504
505
         case_sectors[i].set_properties_force(
507
              InterpolationPolynomialZeroDerivative(z_1, m_0, m_1),
508
             InterpolationPolynomialZeroDerivative(z_r, m_0, m_1),
509
             510
511
512
             InterpolationPolynomialDerivative(z_r, m_0, m_1, 0, 0));
513
514
     }
515
516
     // for (unsigned int i = 0; i < NFreeDofs(); ++ i) {</pre>
517
        InitialDofs[i] = this->get_dof(i, true);
```

4.11.2.3 evaluate_for_z()

Since the Wavegudie itself may be circular or rectangular now, the evaluation routines should be moved to a point in the code where this information is included in the code.

Since I dont want to create derived classes from waveguide (which I should do eventually) I will for now include this functionality into the space transformation which is shape-sensitive. The waveguide only offers the evaluation at a point. The quadrature-rule has to be imposed by the space transformation.

Implements SpaceTransformation.

Definition at line 392 of file Inhomogenous Transformation Circular.cpp.

```
393
394    double r = GlobalParams.M_C_DimlIn + GlobalParams.M_C_DimlOut;
395    return gauss_product_2D_sphere(in_z, 10, r, 0, 0, in_w);
396 }

4.11.2.4    get_dof()

double InhomogenousTransformationCircular::get_dof (
```

This is a getter for the values of degrees of freedom.

int dof) const [virtual]

A getter-setter interface was introduced since the values are estimated automatically during the optimization and non-physical systems should be excluded from the domain of possible cases.

Parameters

dof The index of the degree of freedom to be retrieved from the structure of the modelled waveguide.

Returns

This function returns the value of the requested degree of freedom. Should this dof not exist, 0 will be returnd.

Implements SpaceTransformation.

Definition at line 398 of file InhomogenousTransformationCircular.cpp.

References HomogenousTransformationRectangular::case_sectors, HomogenousTransformationRectangular::N← Dofs(), and HomogenousTransformationRectangular::sectors.

Referenced by InhomogenousTransformationRectangular::Dofs().

```
398
399
     if (dof < (int)NDofs() && dof >= 0) {
       int sector = floor(dof / 3);
400
      if (sector == sectors) {
401
         return case_sectors[sector - 1].dofs_r[dof % 3];
402
      } else {
404
        return case_sectors[sector].dofs_1[dof % 3];
405
406 } else {
      std::cout << "Critical: DOF-index out of bounds in "
407
                    "HomogenousTransformationCircular::get_dof!"
408
                << std::endl;
       return 0.0;
411 }
412 }
```

4.11.2.5 get_free_dof()

```
double Inhomogenous
TransformationCircular::get_free_dof ( int\ dof\ )\ const\ [virtual]
```

This is a getter for the values of degrees of freedom.

A getter-setter interface was introduced since the values are estimated automatically during the optimization and non-physical systems should be excluded from the domain of possible cases.

Parameters

dof The index of the degree of freedom to be retrieved from the structure of the modelled waveguide.

Returns

This function returns the value of the requested degree of freedom. Should this dof not exist, 0 will be returnd.

Implements SpaceTransformation.

Definition at line 414 of file InhomogenousTransformationCircular.cpp.

References HomogenousTransformationRectangular::case_sectors, HomogenousTransformationRectangular::N← Dofs(), and HomogenousTransformationRectangular::sectors.

```
414
      int dof = in_dof + 3;
if (dof < (int) NDofs() - 3 && dof >= 0) {
415
416
        int sector = floor(dof / 3);
if (sector == sectors) {
417
418
           return case_sectors[sector - 1].dofs_r[dof % 3];
419
       } else {
420
421
          return case sectors[sector].dofs 1[dof % 3];
422
423
      } else {
        std::cout << "Critical: DOF-index out of bounds in "
424
                       "{\tt HomogenousTransformationCircular::get\_free\_dof!"}
425
                    << std::endl;
42.6
427
        return 0.0;
428
429 }
```

4.11.2.6 get_Q1()

```
double InhomogenousTransformationCircular::get_Q1 ( double z ) const [virtual]
```

This member calculates the value of Q1 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q1 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implements SpaceTransformation.

Definition at line 536 of file Inhomogenous Transformation Circular.cpp.

References Homogenous Transformation Rectangular::case_sectors, and Space Transformation:: Z_{to} Sector_ \leftarrow and local z().

```
536
537 std::pair<int, double> two = Z_to_Sector_and_local_z(z_in);
538 return case_sectors[two.first].getQ1(two.second);
539 }
```

4.11.2.7 get Q2()

```
double InhomogenousTransformationCircular::get_Q2 ( double z ) const [virtual]
```

This member calculates the value of Q2 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q2 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implements SpaceTransformation.

Definition at line 541 of file Inhomogenous Transformation Circular.cpp.

References HomogenousTransformationRectangular::case_sectors, and SpaceTransformation::Z_to_Sector_ and local z().

```
541
542 std::pair<int, double> two = Z_to_Sector_and_local_z(z_in);
543 return case_sectors[two.first].getQ2(two.second);
544 }
```

4.11.2.8 get_Q3()

```
double InhomogenousTransformationCircular::get_Q3 ( double z ) const [virtual]
```

This member calculates the value of Q3 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q3 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implements SpaceTransformation.

Definition at line 546 of file Inhomogenous Transformation Circular.cpp.

References Homogenous Transformation Rectangular::case_sectors, and Space Transformation:: Z_{to} Sector_ \leftarrow and local z().

```
546
547 std::pair<int, double> two = Z_to_Sector_and_local_z(z_in);
548 return case_sectors[two.first].getQ3(two.second);
549 }
```

4.11.2.9 IsDofFree()

Since Dofs() also returns restrained degrees of freedom, this function can be applied to determine if a degree of freedom is indeed free or restrained.

"restrained" means that for example the DOF represents the radius at one of the connectors (input or output) and therefore we forbid the optimization scheme to vary this value.

Implements SpaceTransformation.

Definition at line 565 of file Inhomogenous Transformation Circular.cpp.

References HomogenousTransformationRectangular::NDofs().

```
565 {
566    return index > 2 && index < (int) NDofs() - 3;
567 }
```

4.11.2.10 NDofs()

```
unsigned int InhomogenousTransformationCircular::NDofs ( ) const [virtual]
```

This function returns the total number of DOFs including restrained ones.

This is the lenght of the array returned by Dofs().

Implements SpaceTransformation.

Definition at line 573 of file Inhomogenous Transformation Circular.cpp.

References HomogenousTransformationRectangular::sectors.

Referenced by InhomogenousTransformationRectangular::Dofs(), InhomogenousTransformationRectangular::get dof(), InhomogenousTransformationRectangular::ls DofFree(), InhomogenousTransformationRectangular::NFreeDofs(), InhomogenousTransformationRectangular::NFreeDofs(), InhomogenousTransformationRectangular::set dof(), and InhomogenousTransformationRectangular::set free dof().

```
573 {
574 return sectors * 3 + 3;
575 }
```

4.11.2.11 PML_in_X()

```
bool InhomogenousTransformationCircular::PML_in_X (  Point < ~3 ~> ~\&~position~)~const~[virtual]
```

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the x-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

position	Stores the position in which to test for presence of a PML-Material.
p 0 0	otoreo are producer ar armor to took ior processes or a raise material.

Implements SpaceTransformation.

Definition at line 76 of file Inhomogenous Transformation Circular.cpp.

Referenced by InhomogenousTransformationRectangular::PML_Z_Distance().

4.11.2.12 PML_in_Y()

```
bool InhomogenousTransformationCircular::PML_in_Y (  Point < 3 > \& position \ ) \ const \ [virtual]
```

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the y-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

position	Stores the position in which to test for presence of a PML-Material.
----------	--

Implements SpaceTransformation.

Definition at line 80 of file InhomogenousTransformationCircular.cpp.

Referenced by InhomogenousTransformationRectangular::PML_Z_Distance().

```
80 {
81    return p(1) < YMinus || p(1) > YPlus;
82 }
```

4.11.2.13 PML_in_Z()

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the z-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

position Stores the position in which to test for presence of a PML-Material.

Implements SpaceTransformation.

Definition at line 84 of file InhomogenousTransformationCircular.cpp.

Referenced by InhomogenousTransformationRectangular::PML_Z_Distance().

4.11.2.14 PML_X_Distance()

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

position Stores the position from which to calculate the distance to the PML-surface.

Implements SpaceTransformation.

Definition at line 105 of file Inhomogenous Transformation Circular.cpp.

Referenced by InhomogenousTransformationRectangular::PML_Z_Distance().

4.11.2.15 PML_Y_Distance()

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

position	Stores the position from which to calculate the distance to the PML-surface.
----------	--

Implements SpaceTransformation.

Definition at line 113 of file InhomogenousTransformationCircular.cpp.

Referenced by InhomogenousTransformationRectangular::PML Z Distance().

4.11.2.16 PML Z Distance()

```
double InhomogenousTransformationCircular::PML_Z_Distance (
Point < 3 > \& position ) const [virtual]
```

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

position Stores the position from which to calculate the distance to the PML-surface
--

Implements SpaceTransformation.

Definition at line 121 of file Inhomogenous Transformation Circular.cpp.

References Homogenous Transformation Rectangular::case_sectors, Waveguide::evaluate_for_Position(), Homogenous \leftarrow Transformation Rectangular::PML_in_X(), Homogenous Transformation Rectangular::PML_in_Y(), Homogenous \leftarrow Transformation Rectangular::PML_in_Z(), Homogenous Transformation Rectangular::PML_X_Distance(), Homogenous Transformation Rectangular::PML_Y_Distance(), Homogenous Transformation Rectangular::PML_Z_Distance(), Homogenous Transformation Rectangular::Preconditioner_PML_in_Z(), Homogenous Transformation Rectangular::Preconditioner_PML_Z_Distance(), and Space Transformation::Z_to_Sector_and_local_z().

Referenced by InhomogenousTransformationRectangular::PML Z Distance().

```
121 {
122    if (p(2) < 0) {
123       return 0;
124    } else {
125       return p(2) - (GlobalParams.M_R_ZLength / 2.0);
126    }
127 }
```

4.11.2.17 Preconditioner_PML_in_Z()

```
bool Inhomogenous
TransformationCircular::Preconditioner_PML_in_Z ( Point
< 3 > & p, unsigned int block ) const
```

Similar to the PML_in_Z only this function is used to generate the artificial PML used in the Preconditioner.

These Layers are not only situated at the surface of the computational domain but also inside it at the interfaces of Sectors.

Definition at line 88 of file InhomogenousTransformationCircular.cpp.

4.11.2.18 set_dof()

This function sets the value of the dof provided to the given value.

It is important to consider, that some dofs are non-writable (i.e. the values of the degrees of freedom on the boundary, like the radius of the input-connector cannot be changed).

Parameters

dof	The index of the parameter to be changed.
value	The value, the dof should be set to.

Implements SpaceTransformation.

Definition at line 431 of file InhomogenousTransformationCircular.cpp.

References Homogenous Transformation Rectangular:: case_sectors, Homogenous Transformation Rectangular:: $N \leftarrow Dofs()$, and Homogenous Transformation Rectangular:: sectors.

```
431
     if (dof < (int) NDofs() && dof >= 0) {
432
       int sector = floor(dof / 3);
433
       if (sector == sectors) {
434
435
         case_sectors[sector - 1].dofs_r[dof % 3] = in_val;
436
       } else if (sector == 0) {
         case_sectors[0].dofs_l[dof % 3] = in_val;
437
438
       } else {
439
         case_sectors[sector].dofs_l[dof % 3] = in_val;
440
         case_sectors[sector - 1].dofs_r[dof % 3] = in_val;
441
```

```
442 } else {
443 std::cout << "Critical: DOF-index out of bounds in "
444 "HomogenousTransformationCircular::set_dof!"
445 << std::endl;
446 }
447 }
```

4.11.2.19 set_free_dof()

This function sets the value of the dof provided to the given value.

It is important to consider, that some dofs are non-writable (i.e. the values of the degrees of freedom on the boundary, like the radius of the input-connector cannot be changed).

Parameters

dof	The index of the parameter to be changed.
value	The value, the dof should be set to.

Implements SpaceTransformation.

Definition at line 449 of file Inhomogenous Transformation Circular.cpp.

References HomogenousTransformationRectangular::case_sectors, HomogenousTransformationRectangular::N← Dofs(), and HomogenousTransformationRectangular::sectors.

```
450
                                                                                 {
      int dof = in_dof + 3;
if (dof < (int) NDofs() - 3 && dof >= 0) {
451
452
       int sector = floor(dof / 3);
if (sector == sectors) {
454
      case_sectors[sector - 1].dofs_r[dof % 3] = in_val;
} else if (sector == 0) {
455
456
          case_sectors[0].dofs_l[dof % 3] = in_val;
457
       } else {
458
459
         case_sectors[sector].dofs_1[dof % 3] = in_val;
460
          case_sectors[sector - 1].dofs_r[dof % 3] = in_val;
461
462
      } else {
      std::cout << "Critical: DOF-index out of bounds in "
463
                      "HomogenousTransformationCircular::set_free_dof!"
464
         << std::endl;
465
466 }
467 }
```

4.11.2.20 System_Length()

```
double InhomogenousTransformationCircular::System_Length ( ) const
```

Using this method unifies the usage of coordinates.

This function takes a global z coordinate (in the computational domain) and returns both a Sector-Index and an internal z coordinate indicating which sector this coordinate belongs to and how far along in the sector it is located.

Parameters

double	in_z global system z coordinate for the transformation. Returns the complete length of the	1
	computational domain.	

4.11.3 Member Data Documentation

4.11.3.1 case_sectors

```
std::vector<Sector<3> > InhomogenousTransformationCircular::case_sectors
```

This member contains all the Sectors who, as a sum, form the complete Waveguide.

These Sectors are a partition of the simulated domain.

Definition at line 141 of file Inhomogenous Transformation Circular.h.

Referenced by Inhomogenous Transformation Rectangular::estimate_and_initialize(), Inhomogenous Transformation \leftarrow Rectangular::get_dof(), Inhomogenous Transformation Rectangular::get_free_dof(), Inhomogenous Transformation Rectangular::get_Q1(), Inhomogenous Transformation Inhomogenous Inhomoge

4.11.3.2 epsilon_K

```
const double InhomogenousTransformationCircular::epsilon_K
```

The material-property ϵ_r has a different value inside and outside of the waveguides core.

This variable stores its value inside the core.

Definition at line 148 of file Inhomogenous Transformation Circular.h.

4.11.3.3 epsilon_M

```
const double InhomogenousTransformationCircular::epsilon_M
```

The material-property ϵ_r has a different value inside and outside of the waveguides core.

This variable stores its value outside the core.

Definition at line 154 of file Inhomogenous Transformation Circular.h.

4.11.3.4 sectors

const int InhomogenousTransformationCircular::sectors

Since the computational domain is split into subdomains (called sectors), it is important to keep track of the amount of subdomains.

This member stores the number of Sectors the computational domain has been split into.

Definition at line 160 of file Inhomogenous Transformation Circular.h.

Referenced by Inhomogenous Transformation Rectangular::estimate_and_initialize(), Inhomogenous Transformation \leftarrow Rectangular::get_dof(), Inhomogenous Transformation Rectangular::get_free_dof(), Inhomogenous Transformation \leftarrow Rectangular::NDofs(), Inhomogenous Transformation Rectangular::set_dof(), and Inhomogenous Transformation \leftarrow Rectangular::set_free_dof().

The documentation for this class was generated from the following files:

- Code/SpaceTransformations/InhomogenousTransformationCircular.h
- Code/SpaceTransformations/InhomogenousTransformationCircular.cpp

4.12 Inhomogenous Transformation Rectangle Class Reference

In this case we regard a rectangular waveguide and the effects on the material tensor by the space transformation and the boundary condition PML may overlap (hence inhomogenous space transformation)

#include <InhomogenousTransformationRectangular.h>

4.12.1 Detailed Description

In this case we regard a rectangular waveguide and the effects on the material tensor by the space transformation and the boundary condition PML may overlap (hence inhomogenous space transformation)

If this kind of boundary condition works stably we will also be able to deal with more general settings (which might for example incorporate angles in between the output and input connector.

Author

Pascal Kraft

Date

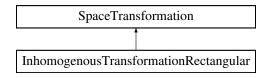
28.11.2016

The documentation for this class was generated from the following file:

• Code/SpaceTransformations/InhomogenousTransformationRectangular.h

4.13 Inhomogenous Transformation Rectangular Class Reference

Inheritance diagram for InhomogenousTransformationRectangular:



Public Member Functions

- InhomogenousTransformationRectangular (int)
- Point< 3 > math_to_phys (Point< 3 > coord) const
- Point< 3 > phys_to_math (Point< 3 > coord) const
- bool is_identity (Point< 3 > coord) const
- Tensor < 2, 3, std::complex < double > > get_Tensor (Point < 3 > &coordinate) const
- Tensor < 2, 3, std::complex < double > > get_Preconditioner_Tensor (Point < 3 > &coordinate, int block)
- Tensor< 2, 3, std::complex< double >> Apply_PML_To_Tensor (Point< 3 > &coordinate, Tensor< 2, 3, double > Tensor_input) const
- Tensor< 2, 3, std::complex< double > > Apply_PML_To_Tensor_For_Preconditioner (Point< 3 > &coordinate, Tensor< 2, 3, double > Tensor_input, int block) const
- Tensor < 2, 3, double > get Space Transformation Tensor (Point < 3 > &coordinate) const
- Tensor< 2, 3, double > get_Space_Transformation_Tensor_Homogenized (Point< 3 > &coordinate) const
- bool PML_in_X (Point< 3 > &position) const

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the x-axis.

bool PML_in_Y (Point < 3 > &position) const

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the y-axis.

bool PML in Z (Point < 3 > &position) const

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the z-axis.

bool Preconditioner_PML_in_Z (Point< 3 > &p, unsigned int block) const

Similar to the PML in Z only this function is used to generate the artificial PML used in the Preconditioner.

double Preconditioner PML Z Distance (Point < 3 > &p, unsigned int block) const

This function fulfills the same purpose as those with similar names but it is supposed to be used together with Preconditioner_PML_in_Z instead of the versions without "Preconditioner".

double PML_X_Distance (Point< 3 > &position) const

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

double PML_Y_Distance (Point< 3 > &position) const

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

double PML_Z_Distance (Point< 3 > &position) const

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

· void estimate and initialize ()

At the beginning (before the first solution of a system) only the boundary conditions for the shape of the waveguide are known.

double get Q1 (double z) const

This member calculates the value of Q1 for a provided z-coordinate.

double get_Q2 (double z) const

This member calculates the value of Q2 for a provided z-coordinate.

• double get_Q3 (double z) const

This member calculates the value of Q3 for a provided z-coordinate.

· double get dof (int dof) const

This is a getter for the values of degrees of freedom.

• void set_dof (int dof, double value)

This function sets the value of the dof provided to the given value.

· double get free dof (int dof) const

This is a getter for the values of degrees of freedom.

void set_free_dof (int dof, double value)

This function sets the value of the dof provided to the given value.

· double System_Length () const

Returns the complete length of the computational domain.

• double Sector_Length () const

Returns the length of one sector.

· double Layer_Length () const

Returns the length of one layer.

• double get_r (double in_z) const

Returns the radius for a system-coordinate;.

• double get_m (double in_z) const

Returns the shift for a system-coordinate;.

• double get v (double in z) const

Returns the tilt for a system-coordinate;.

- int Z to Layer (double) const
- Vector< double > Dofs () const

Other objects can use this function to retrieve an array of the current values of the degrees of freedom of the functional we are optimizing.

• unsigned int NFreeDofs () const

This function returns the number of unrestrained degrees of freedom of the current optimization run.

• unsigned int NDofs () const

This function returns the total number of DOFs including restrained ones.

• bool IsDofFree (int) const

Since Dofs() also returns restrained degrees of freedom, this function can be applied to determine if a degree of freedom is indeed free or restrained.

· void Print () const

Console output of the current Waveguide Structure.

- std::complex < double > evaluate for z with sum (double, double, Wavequide *)
- std::complex< double > evaluate_for_z (double z_in, Waveguide *)

Since the Wavegudie itself may be circular or rectangular now, the evaluation routines should be moved to a point in the code where this information is included in the code.

Public Attributes

- · const double XMinus
- const double XPlus
- · const double YMinus
- · const double YPlus
- · const double ZMinus
- const double ZPlus
- std::vector< Sector< 2 > > case sectors

This member contains all the Sectors who, as a sum, form the complete Waveguide.

· const double epsilon_K

The material-property ϵ_r has a different value inside and outside of the waveguides core.

· const double epsilon M

The material-property ϵ_r has a different value inside and outside of the waveguides core.

· const int sectors

Since the computational domain is split into subdomains (called sectors), it is important to keep track of the amount of subdomains.

const double deltaY

This value is initialized with the value Delta from the input-file.

Vector< double > InitialDofs

This vector of values saves the initial configuration.

4.13.1 Detailed Description

Definition at line 26 of file InhomogenousTransformationRectangular.h.

4.13.2 Member Function Documentation

4.13.2.1 Dofs()

```
Vector< double > InhomogenousTransformationRectangular::Dofs ( ) const [virtual]
```

Other objects can use this function to retrieve an array of the current values of the degrees of freedom of the functional we are optimizing.

This also includes restrained degrees of freedom and other functions can be used to determine this property. This has to be done because in different cases the number of restrained degrees of freedom can vary and we want no logic about this in other functions.

Implements SpaceTransformation.

Definition at line 445 of file Inhomogenous Transformation Rectangular.cpp.

References InhomogenousTransformationCircular::get dof(), and InhomogenousTransformationCircular::NDofs().

4.13.2.2 estimate_and_initialize()

```
void InhomogenousTransformationRectangular::estimate_and_initialize ( ) [virtual]
```

At the beginning (before the first solution of a system) only the boundary conditions for the shape of the waveguide are known.

Therefore the values for the degrees of freedom need to be estimated. This function sets all variables to appropriate values and estimates an appropriate shape based on averages and a polynomial interpolation of the boundary conditions on the shape.

Implements SpaceTransformation.

Definition at line 342 of file Inhomogenous Transformation Rectangular.cpp.

References InhomogenousTransformationCircular::case_sectors, InhomogenousTransformationCircular::Sector_ Length(), InhomogenousTransformationCircular::sectors, and Sector< Dofs_Per_Sector >::set_properties_force().

```
342
                                                                             {
343
         (GlobalParams.M_PC_Use) {
344
        Sector<2> the_first(true, false, GlobalParams.sd.z[0],
345
                             GlobalParams.sd.z[1]);
346
        the\_first.set\_properties\_force (GlobalParams.sd.m[0], \ GlobalParams.sd.m[1], \\
347
                                         GlobalParams.sd.v[0], GlobalParams.sd.v[1]);
        case_sectors.push_back(the_first);
348
        for (int i = 1; i < GlobalParams.sd.Sectors - 2; i++) {
   Sector<2> intermediate(false, false, GlobalParams.sd.z[i],
349
351
                                  GlobalParams.sd.z[i + 1]);
352
          \verb|intermediate.set_properties_force||\\
              GlobalParams.sd.m[i], GlobalParams.sd.m[i + 1], GlobalParams.sd.v[i],
GlobalParams.sd.v[i + 1]);
353
354
355
          case_sectors.push_back(intermediate);
356
357
        Sector<2> the_last(false, true,
358
                            GlobalParams.sd.z[GlobalParams.sd.Sectors - 2],
                            GlobalParams.sd.z[GlobalParams.sd.Sectors - 1]);
359
360
        the_last.set_properties_force(
361
            GlobalParams.sd.m[GlobalParams.sd.Sectors - 2],
362
            GlobalParams.sd.m[GlobalParams.sd.Sectors - 1],
363
            GlobalParams.sd.v[GlobalParams.sd.Sectors - 2],
364
            GlobalParams.sd.v[GlobalParams.sd.Sectors - 1]);
365
        case_sectors.push_back(the_last);
        for (unsigned int i = 0; i < case_sectors.size(); i++) {
  deallog << "From z: " << case_sectors[i].z_0</pre>
366
367
                  << "(m: " << case_sectors[i].get_m(0.0)
368
                  << " v: " << case_sectors[i].get_v(0.0) << ")" << std::endl;</pre>
369
          370
371
                   << " v: " << case_sectors[i].get_v(1.0) << ")" << std::endl;</pre>
372
373
374
      } else {
375
        case_sectors.reserve(sectors);
        double m_0 = GlobalParams.M_W_Delta / 2.0;
double m_1 = -GlobalParams.M_W_Delta / 2.0;
376
377
        if (sectors == 1) {
378
          Sector<2> temp12(true, true, -GlobalParams.M_R_ZLength / 2.0,
379
380
                            GlobalParams.M_R_ZLength / 2.0);
381
          case_sectors.push_back(temp12);
382
          case_sectors[0].set_properties_force(
383
              GlobalParams.M_W_Delta / 2.0, -GlobalParams.M_W_Delta / 2.0,
384
              GlobalParams.M_C_Dim1In, GlobalParams.M_C_Dim1Out, 0, 0);
385
        } else {
386
          double length = Sector Length();
          Sector<2> temp(true, false, -GlobalParams.M_R_ZLength / (2.0),
387
                          -GlobalParams.M_R_ZLength / 2.0 + length);
388
389
          case_sectors.push_back(temp);
390
          for (int i = 1; i < sectors; i++) {</pre>
            391
392
393
                             -GlobalParams.M_R_ZLength / (2.0) + length * (i + 1.0));
394
            case_sectors.push_back(temp2);
395
396
          double length_rel = 1.0 / ((double) (sectors));
397
398
          case_sectors[0].set_properties_force(
399
              m_0, InterpolationPolynomialZeroDerivative(length_rel, m_0, m_1), 0,
              InterpolationPolynomialDerivative(length_rel, m_0, m_1, 0, 0));
```

```
401
          for (int i = 1; i < sectors; i++) {</pre>
           double z_l = i * length_rel;
double z_r = (i + 1) * length_rel;
403
404
             case_sectors[i].set_properties_force(
                 405
                 InterpolationPolynomialZeroDerivative(z_r, m_0, m_1), InterpolationPolynomialDerivative(z_1, m_0, m_1, 0, 0),
406
407
408
                 InterpolationPolynomialDerivative(z_r, m_0, m_1, 0, 0));
409
410
411 }
412 }
```

4.13.2.3 evaluate_for_z()

Since the Wavegudie itself may be circular or rectangular now, the evaluation routines should be moved to a point in the code where this information is included in the code.

Since I dont want to create derived classes from waveguide (which I should do eventually) I will for now include this functionality into the space transformation which is shape-sensitive. The waveguide only offers the evaluation at a point. The quadrature-rule has to be imposed by the space transformation.

Implements SpaceTransformation.

Definition at line 261 of file InhomogenousTransformationRectangular.cpp.

4.13.2.4 get_dof()

This is a getter for the values of degrees of freedom.

A getter-setter interface was introduced since the values are estimated automatically during the optimization and non-physical systems should be excluded from the domain of possible cases.

Parameters

dof The index of the degree of freedom to be retrieved from the structure of the modelled waveguide.

Returns

This function returns the value of the requested degree of freedom. Should this dof not exist, 0 will be returnd.

Implements SpaceTransformation.

Definition at line 267 of file Inhomogenous Transformation Rectangular.cpp.

 $References\ Inhomogenous Transformation Circular:: case_sectors,\ Inhomogenous Transformation Circular:: NDofs(), and Inhomogenous Transformation Circular:: sectors.$

```
2.67
                                                                            {
      if (dof < (int)NDofs() && dof >= 0) {
268
       int sector = floor(dof / 2);
if (sector == sectors) {
269
270
          return case_sectors[sector - 1].dofs_r[dof % 2];
271
272
      } else {
273
          return case_sectors[sector].dofs_1[dof % 2];
274
275
     } else {
      std::cout << "Critical: DOF-index out of bounds in "
277
                     "InhomogenousTransformationRectangular::get_dof!"
278
                  << std::endl;
279
        return 0.0;
280
281 }
```

4.13.2.5 get_free_dof()

```
double Inhomogenous
TransformationRectangular::get_free_dof ( int\ dof\ )\ const\ \ [virtual]
```

This is a getter for the values of degrees of freedom.

A getter-setter interface was introduced since the values are estimated automatically during the optimization and non-physical systems should be excluded from the domain of possible cases.

Parameters

dof The index of the degree of freedom to be retrieved from the structure of the modelled waveguide.

Returns

This function returns the value of the requested degree of freedom. Should this dof not exist, 0 will be returnd.

Implements SpaceTransformation.

Definition at line 283 of file Inhomogenous Transformation Rectangular.cpp.

 $References\ Inhomogenous Transformation Circular:: case_sectors,\ Inhomogenous Transformation Circular:: NDofs(), and Inhomogenous Transformation Circular:: sectors.$

```
283
284 int dof = in_dof + 2;
285 if (dof < (int)NDofs() - 2 && dof >= 0) {
286 int sector = floor(dof / 2);
```

```
if (sector == sectors) {
         return case_sectors[sector - 1].dofs_r[dof % 2];
289
       } else {
290
         return case_sectors[sector].dofs_1[dof % 2];
291
     } else {
292
293
      std::cout << "Critical: DOF-index out of bounds in "
294
                    "InhomogenousTransformationRectangular::get_free_dof!"
295
                 << std::endl;
296
       return 0.0;
297 }
298 }
```

4.13.2.6 get_Q1()

```
double InhomogenousTransformationRectangular::get_Q1 ( double z ) const [virtual]
```

This member calculates the value of Q1 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q1 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implements SpaceTransformation.

Definition at line 430 of file Inhomogenous Transformation Rectangular.cpp.

```
430 {
431 std::pair<int, double> two = Z_to_Sector_and_local_z(z_in);
432 return case_sectors[two.first].getQ1(two.second);
433 }
```

4.13.2.7 get_Q2()

```
double InhomogenousTransformationRectangular::get_Q2 ( double z ) const [virtual]
```

This member calculates the value of Q2 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q2 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implements SpaceTransformation.

Definition at line 435 of file Inhomogenous Transformation Rectangular.cpp.

References Inhomogenous Transformation Circular::case_sectors, and Space Transformation:: Z_{to} Sector_and_ \leftarrow local z().

```
435 {
436 std::pair<int, double> two = Z_to_Sector_and_local_z(z_in);
437 return case_sectors[two.first].getQ2(two.second);
438 }
```

4.13.2.8 get_Q3()

```
double InhomogenousTransformationRectangular::get_Q3 ( double z ) const [virtual]
```

This member calculates the value of Q3 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q3 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implements SpaceTransformation.

Definition at line 440 of file Inhomogenous Transformation Rectangular.cpp.

References Inhomogenous Transformation Circular::case_sectors, and Space Transformation:: Z_{to} Sector_and_ \leftarrow local_z().

```
440
441 std::pair<int, double> two = Z_to_Sector_and_local_z(z_in);
442 return case_sectors[two.first].getQ3(two.second);
443 }
```

4.13.2.9 IsDofFree()

Since Dofs() also returns restrained degrees of freedom, this function can be applied to determine if a degree of freedom is indeed free or restrained.

"restrained" means that for example the DOF represents the radius at one of the connectors (input or output) and therefore we forbid the optimization scheme to vary this value.

Implements SpaceTransformation.

Definition at line 459 of file Inhomogenous Transformation Rectangular.cpp.

 $References\ Inhomogenous\ Transformation\ Circular:: NDofs().$

```
459 {
460 return index > 1 && index < (int) NDofs() - 1;
461 }
```

4.13.2.10 NDofs()

```
unsigned\ int\ Inhomogenous Transformation Rectangular:: {\tt NDofs}\ (\ )\ const\ \ [virtual]
```

This function returns the total number of DOFs including restrained ones.

This is the lenght of the array returned by Dofs().

Implements SpaceTransformation.

Definition at line 467 of file InhomogenousTransformationRectangular.cpp.

 $References \ Inhomogenous Transformation Circular :: case_sectors, \ Inhomogenous Transformation Circular :: sectors, \ and \ Space Transformation :: Z_to_Sector_and_local_z().$

```
467
468 return sectors * 2 + 2;
469 }
```

4.13.2.11 PML_in_X()

```
bool InhomogenousTransformationRectangular::PML_in_X (  Point < 3 > \& position \ ) \ const \ [virtual]
```

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the x-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

position	Stores the position in which to test for presence of a PML-Material.
----------	--

Implements SpaceTransformation.

Definition at line 55 of file InhomogenousTransformationRectangular.cpp.

4.13.2.12 PML_in_Y()

```
bool InhomogenousTransformationRectangular::PML_in_Y ( Point< 3 > & position ) const [virtual]
```

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the y-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

position Stores the position in which to test for presence of a PML-Ma
--

Implements SpaceTransformation.

Definition at line 59 of file InhomogenousTransformationRectangular.cpp.

```
59
60   return p(1) < YMinus || p(1) > YPlus;
61 }
```

4.13.2.13 PML_in_Z()

```
bool InhomogenousTransformationRectangular::PML_in_Z ( Point< 3 > & position ) const [virtual]
```

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the z-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

position	Stores the position in which to test for presence of a PML-Material.
----------	--

Implements SpaceTransformation.

Definition at line 63 of file InhomogenousTransformationRectangular.cpp.

```
63
64 return p(2) < ZMinus || p(2) > ZPlus;
65 }
```

4.13.2.14 PML_X_Distance()

```
double InhomogenousTransformationRectangular::PML_X_Distance ( Point < 3 > \& \ position \ ) \ const \ \ [virtual]
```

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

position Stores the position from which to calculate the distance to the PML-surface.

Implements SpaceTransformation.

Definition at line 73 of file InhomogenousTransformationRectangular.cpp.

4.13.2.15 PML_Y_Distance()

```
double InhomogenousTransformationRectangular::PML_Y_Distance ( Point < ~3~>~\&~position~)~const~[virtual]
```

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

position Stores the position from which to calculate the distance to the PML-surface.

Implements SpaceTransformation.

Definition at line 82 of file Inhomogenous Transformation Rectangular.cpp.

4.13.2.16 PML_Z_Distance()

```
double InhomogenousTransformationRectangular::PML_Z_Distance ( Point < \ 3 \ > \ \& \ position \ ) \ const \ \ [virtual]
```

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

position Stores the position from which to calculate the distance to the PML-surface.

Implements SpaceTransformation.

Definition at line 91 of file InhomogenousTransformationRectangular.cpp.

References Inhomogenous Transformation Circular:: PML_in_X(), Inhomogenous Transformation Circular:: PML $_{\rm in}$ _Y(), Inhomogenous Transformation Circular:: PML_in_Z(), Inhomogenous Transformation Circular:: PML_X $_{\leftarrow}$ Distance(), Inhomogenous Transformation Circular:: PML_Y_Distance(), Inhomogenous Transformation Circular:: P $_{\leftarrow}$ ML_Z_Distance(), and Inhomogenous Transformation Circular:: Preconditioner_PML_Z_Distance().

4.13.2.17 Preconditioner_PML_in_Z()

```
bool InhomogenousTransformationRectangular::Preconditioner_PML_in_Z ( Point< 3 > & p, unsigned int block) const
```

Similar to the PML in Z only this function is used to generate the artificial PML used in the Preconditioner.

These Layers are not only situated at the surface of the computational domain but also inside it at the interfaces of Sectors.

4.13.2.18 set_dof()

This function sets the value of the dof provided to the given value.

It is important to consider, that some dofs are non-writable (i.e. the values of the degrees of freedom on the boundary, like the radius of the input-connector cannot be changed).

Parameters

dof	The index of the parameter to be changed.
value	The value, the dof should be set to.

Implements SpaceTransformation.

Definition at line 300 of file Inhomogenous Transformation Rectangular.cpp.

References InhomogenousTransformationCircular::case_sectors, InhomogenousTransformationCircular::NDofs(), and InhomogenousTransformationCircular::sectors.

```
300
301
      if (dof < (int) NDofs() && dof >= 0) {
        int sector = floor(dof / 2);
if (sector == sectors) {
302
303
        case_sectors[sector - 1].dofs_r[dof % 2] = in_val;
} else if (sector == 0) {
304
305
          case_sectors[0].dofs_1[dof % 2] = in_val;
306
307
        } else {
308
          case_sectors[sector].dofs_l[dof % 2] = in_val;
309
          case_sectors[sector - 1].dofs_r[dof % 2] = in_val;
310
      } else {
311
        std::cout << "Critical: DOF-index out of bounds in "</pre>
312
313
                       "InhomogenousTransformationRectangular::set_dof!"
314
                    << std::endl;
316 }
```

4.13.2.19 set_free_dof()

This function sets the value of the dof provided to the given value.

It is important to consider, that some dofs are non-writable (i.e. the values of the degrees of freedom on the boundary, like the radius of the input-connector cannot be changed).

Parameters

dof	The index of the parameter to be changed.
value	The value, the dof should be set to.

Implements SpaceTransformation.

Definition at line 318 of file InhomogenousTransformationRectangular.cpp.

 $References\ Inhomogenous Transformation Circular:: case_sectors,\ Inhomogenous Transformation Circular:: NDofs(), and Inhomogenous Transformation Circular:: sectors.$

```
319
320 int dof = in_dof + 2;
```

```
if (dof < (int)NDofs() - 2 && dof >= 0) {
      int sector = floor(dof / 2);
       if (sector == sectors) {
323
324
         case_sectors[sector - 1].dofs_r[dof % 2] = in_val;
      } else if (sector == 0) {
325
326
         case_sectors[0].dofs_1[dof % 2] = in_val;
327
      } else {
328
         case_sectors[sector].dofs_1[dof % 2] = in_val;
        case_sectors[sector - 1].dofs_r[dof % 2] = in_val;
329
330
     } else {
331
       std::cout << "Critical: DOF-index out of bounds in "
"InhomogenousTransformationRectangular::set_free_dof!"
332
333
334
                  << std::endl;
335
336 }
```

4.13.3 Member Data Documentation

4.13.3.1 case_sectors

```
std::vector<Sector<2> > InhomogenousTransformationRectangular::case_sectors
```

This member contains all the Sectors who, as a sum, form the complete Waveguide.

These Sectors are a partition of the simulated domain.

Definition at line 139 of file Inhomogenous Transformation Rectangular.h.

4.13.3.2 epsilon_K

```
const double InhomogenousTransformationRectangular::epsilon_K
```

The material-property ϵ_r has a different value inside and outside of the waveguides core.

This variable stores its value inside the core.

Definition at line 146 of file Inhomogenous Transformation Rectangular.h.

4.13.3.3 epsilon_M

```
const double InhomogenousTransformationRectangular::epsilon_M
```

The material-property ϵ_r has a different value inside and outside of the waveguides core.

This variable stores its value outside the core.

Definition at line 152 of file Inhomogenous Transformation Rectangular.h.

4.13.3.4 sectors

const int InhomogenousTransformationRectangular::sectors

Since the computational domain is split into subdomains (called sectors), it is important to keep track of the amount of subdomains.

This member stores the number of Sectors the computational domain has been split into.

Definition at line 158 of file Inhomogenous Transformation Rectangular.h.

The documentation for this class was generated from the following files:

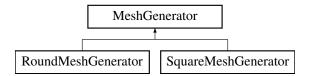
- · Code/SpaceTransformations/InhomogenousTransformationRectangular.h
- Code/SpaceTransformations/InhomogenousTransformationRectangular.cpp

4.14 MeshGenerator Class Reference

This is an interface for all the mesh generators in the project describing its role and functionality.

```
#include <MeshGenerator.h>
```

Inheritance diagram for MeshGenerator:



Public Member Functions

MeshGenerator (SpaceTransformation &in_ct)

Since objects of this type mainly depend on the measures and the selected shape, the constructor only requires a space transformation (which determines, which points are to be considered inside the waveguide etc.)

- virtual void refine global (parallel::distributed::Triangulation < 3 > *in tria, unsigned int times)=0
 - This function is intended to execute a global refinement of the mesh.
- virtual void refine_internal (parallel::distributed::Triangulation< 3 > *in_tria, unsigned int times)=0

This function is intended to execute an internal refinement of the mesh.

virtual void refine_proximity (parallel::distributed::Triangulation < 3 > *in_tria, unsigned int times, double factor)=0

This function is intended to execute a refinement inside and near the waveguide boundary.

virtual bool math_coordinate_in_waveguide (Point< 3 > position) const =0

This function checks if the given coordinate is inside the waveguide or not.

virtual bool phys_coordinate_in_waveguide (Point< 3 > position) const =0

This function checks if the given coordinate is inside the waveguide or not.

• virtual void prepare_triangulation (parallel::distributed::Triangulation $< 3 > *in_tria) = 0$

This function takes a triangulation object and prepares it for the further computations.

Public Attributes

- parallel::distributed::Triangulation < 3 >::active_cell_iterator cell
- parallel::distributed::Triangulation < 3 >::active_cell_iterator endc
- SpaceTransformation * ct
- · unsigned int Layers
- Point < 3 > origin
- Point < 3 > p1
- Point < 3 > p2
- std cxx11::array< Tensor< 1, 3 >, 3 > edges
- std::vector< unsigned int > subs
- double z min
- double z_max

4.14.1 Detailed Description

This is an interface for all the mesh generators in the project describing its role and functionality.

Since different shapes of waveguides (in the xz-plane) are interesting in application settings, we wish to introduce a mechanism to model this fact. Therefore all functionality related to the shape of the waveguide are encapsulated of specific objects which do all the heavy lifting. The problem si the fact that a rectangular geometry has more dofs then a square or circular one (radius versus width and height). This has implications on the space transformation and the optimization scheme and earlier versions were running the risk of getting too flawed by implementing loads of different case models over and over again. This structure leads to a higher readability of the code and reduces its error-proneness.

Author

Pascal Kraft

Date

28.11.2016

Definition at line 32 of file MeshGenerator.h.

4.14.2 Constructor & Destructor Documentation

4.14.2.1 MeshGenerator()

```
\label{lem:meshGenerator} \mbox{MeshGenerator::MeshGenerator (} $$ \mbox{SpaceTransformation \& } in\_ct \mbox{)}
```

Since objects of this type mainly depend on the measures and the selected shape, the constructor only requires a space transformation (which determines, which points are to be considered inside the waveguide etc.)

Parameters

in⊷	a Space Transformation which whill be stored internally for later use.
_ct	

4.14.3 Member Function Documentation

4.14.3.1 math_coordinate_in_waveguide()

This function checks if the given coordinate is inside the waveguide or not.

The naming convention of physical and mathematical system find application. In this version, the waveguide has been transformed and the check for a tubal waveguide for example only checks if the radius of a given vector is below the average of input and output radius. position This value gives us the location to check for.

Implemented in SquareMeshGenerator, and RoundMeshGenerator.

Referenced by Waveguide::estimate solution(), and RoundMeshGenerator::refine internal().

4.14.3.2 phys_coordinate_in_waveguide()

This function checks if the given coordinate is inside the waveguide or not.

The naming convention of physical and mathematical system find application. In this version, the waveguide is bent. If we are using a space transformation f then this function is equal to math_coordinate_in_waveguide(f(x,y,z)). position This value gives us the location to check for.

Implemented in SquareMeshGenerator, and RoundMeshGenerator.

4.14.3.3 prepare_triangulation()

```
virtual void MeshGenerator::prepare_triangulation ( parallel::distributed::Triangulation < 3 > * in\_tria ) [pure virtual]
```

This function takes a triangulation object and prepares it for the further computations.

It is intended to encapsulate all related work and is explicitely not const.

Parameters

in_tria	The triangulation that is supposed to be prepared. All further information is derived from the
	parameter file and not given by parameters.

Implemented in RoundMeshGenerator, and SquareMeshGenerator.

Referenced by Waveguide::estimate_solution().

4.14.3.4 refine_global()

```
virtual void MeshGenerator::refine_global ( parallel::distributed::Triangulation < 3 > * in\_tria, \\ unsigned int times ) [pure virtual]
```

This function is intended to execute a global refinement of the mesh.

This means that every cell will be refined in every direction (effectively multiplying the number of DOFs by 8). This version is the most expensive refinement possible and should be used with caution.

Parameters

times Number of refinement steps to be performed (gives us a multiplication of the number of degrees of freedom by 8^{times} .

Implemented in SquareMeshGenerator, and RoundMeshGenerator.

4.14.3.5 refine_internal()

This function is intended to execute an internal refinement of the mesh.

This means that every cell inside the waveguide will be refined in every direction. This method is rather cheap and only refines where the field is strong, however, the mesh outside the waveguide should not be too coarse to reduce numerical errors.

Parameters

times Number of refinement steps to be performed.

Implemented in SquareMeshGenerator, and RoundMeshGenerator.

4.14.3.6 refine_proximity()

This function is intended to execute a refinement inside and near the waveguide boundary.

Parameters

times Number of refinement steps to be performed.

Implemented in SquareMeshGenerator, and RoundMeshGenerator.

The documentation for this class was generated from the following files:

- · Code/MeshGenerators/MeshGenerator.h
- Code/MeshGenerators/MeshGenerator.cpp

4.15 ModeManager Class Reference

Public Member Functions

- void prepare_mode_in ()
- void prepare_mode_out ()
- int number_modes_in ()
- int number_modes_out ()
- double get_input_component (int, dealii::Point< 3, double >, int)
- double **get_output_component** (int, dealii::Point< 3, double >, int)
- · void load ()

4.15.1 Detailed Description

Definition at line 13 of file ModeManager.h.

The documentation for this class was generated from the following files:

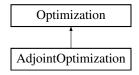
- · Code/Helpers/ModeManager.h
- Code/Helpers/ModeManager.cpp

4.16 Optimization Class Reference

This class is an abstract interface to describe the general workings of an optimization scheme.

```
#include <Optimization.h>
```

Inheritance diagram for Optimization:



Public Member Functions

• virtual void run ()=0

This function is the core implementation of an optimization algorithm.

Public Attributes

- const int type = -1
- · ConditionalOStream pout
- const int dofs = 1
- const int **freedofs** = 0
- SpaceTransformation * st
- MeshGenerator * mg

4.16.1 Detailed Description

This class is an abstract interface to describe the general workings of an optimization scheme.

It is used to compute optimization steps and controls the DOFs of the ShapeTransformation.

In general there are two kinds of Optimization Schemes derived from this class. On the one hand there are finite-difference kind schemes which are based on the idea of varying the value of one shape parameter slightly, resolving the problem (which is now slightly varied compaired to the original one) and hence computing the entry of the shape gradient. Repeating this pattern for any un-restrained dof we can compute the complete gradient. The other version is based on an adjoint model where we solve the forward problem and its dual and can compute the shape gradient for all DOFs from these two results.

Author

Pascal Kraft

Date

28.11.2016

Definition at line 35 of file Optimization.h.

4.16.2 Member Function Documentation

```
4.16.2.1 run()
```

```
virtual void Optimization::run ( ) [pure virtual]
```

This function is the core implementation of an optimization algorithm.

Currently it is very fundamental in its technical prowess which can be improved upon in later versions. Essentially, it calculates the signal quality for a configurations and for small steps in every one of the dofs. After that, the optimization-step is estimated based on difference-quotients. Following this step, a large step is computed based upon the approximation of the gradient of the signal-quality functional and the iteration starts anew. If a decrease in quality is detected, the optimization-step is undone and the step-width is reduced. This function controls both the Waveguide- and the Waveguide-structure object.

Implemented in AdjointOptimization.

The documentation for this class was generated from the following files:

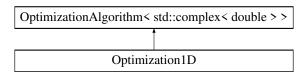
- · Code/OptimizationStrategies/Optimization.h
- · Code/OptimizationStrategies/Optimization.cpp

4.17 Optimization1D Class Reference

This class implements the computation of an optimization step by doing 1D optimization based on an adjoint scheme.

#include <Optimization1D.h>

Inheritance diagram for Optimization1D:



Public Member Functions

• bool perform_small_step_next (int small_steps_before)

The optimization is mainly split into two kinds of steps: Full and small steps.

double get_small_step_step_width (int small_steps_before)

For the optimization scheme to know, which step size is appropriate, this function was included.

bool perform big step next (int small steps before)

This functions returns true, if enough steps were performed to compute the next state to compute a full solution on.

std::vector< double > get_big_step_configuration ()

This function computes the states that should be computed next.

Additional Inherited Members

4.17.1 Detailed Description

This class implements the computation of an optimization step by doing 1D optimization based on an adjoint scheme.

Objects of the Type OptimizationAlgorithm are used by the class OptimizationStrategy to compute the next viable configuration based on former results. Its is encapsulated in it's own class to offer comparison and easy changing between differenct schemes.

Author

Pascal Kraft

Date

9.1.2017

Definition at line 16 of file Optimization1D.h.

4.17.2 Member Function Documentation

4.17.2.1 get_big_step_configuration()

```
std::vector< double > Optimization1D::get_big_step_configuration ( ) [virtual]
```

This function computes the states that should be computed next.

If the next step will be a small step the update can be done by simply updating all dofs with a step width (or only one depending on the pattern) so this function is only used when a big step will be computed next and therefore all dofs could change differently.

Returns

This is a vector of degrees of freedom which can be used by the Optimization Strategy to update the Space Transformation.

Implements OptimizationAlgorithm< std::complex< double >>.

Definition at line 53 of file Optimization1D.cpp.

```
53
     std::vector<double> ret;
55
     if (residuals.size() == 0 && states.size() == 0) {
56
       return ret;
    int small step count = states.size();
58
    int big_step_count = residuals.size();
59
60
     if (big_step_count == 0 ||
         (small_step_count != STEPS_PER_DOFS * big_step_count)) {
63
      std::cout << "Warning in Optimization1D::get_big_step_configuration()"</pre>
64
                << std::endl;
6.5
      std::complex<double> residual = residuals[big_step_count - 1];
66
      double state_red = std::abs(residual);
       unsigned int ndofs = states[small_step_count - 1].size();
69
       ret.resize(ndofs);
       for (unsigned int i = 0; i < ndofs; i++) {</pre>
70
71
        double max = 0:
        int index = -1;
72
        for (unsigned int j = 0; j < STEPS_PER_DOFS; j++) {</pre>
74
          double magn = std::abs(
75
               residual + states[small_step_count - STEPS_PER_DOFS + j][i]);
76
           if (magn > max && magn > state_red) {
77
            max = magn;
             index = j;
78
79
           }
        if (index != -1) {
81
82
           ret[i] = steps_widths[index];
83
        } else {
           ret[i] = 0.0;
84
85
         }
      }
88
     return ret;
89 1
```

4.17.2.2 get_small_step_step_width()

For the optimization scheme to know, which step size is appropriate, this function was included.

Parameters

small steps before	similar to perform_small_step_next this is the number of small steps before the current one.

Returns

double this is how much the values of the degrees of freedom should be adapted.

Implements OptimizationAlgorithm< std::complex< double >>.

Definition at line 35 of file Optimization1D.cpp.

4.17.2.3 perform_big_step_next()

This functions returns true, if enough steps were performed to compute the next state to compute a full solution on.

Parameters

small_steps_before	number of small steps performed before this call.
--------------------	---

Returns

true, if the next computation should be a big step - otherwise false.

Implements OptimizationAlgorithm< std::complex< double >>.

Definition at line 45 of file Optimization1D.cpp.

4.17.2.4 perform_small_step_next()

The optimization is mainly split into two kinds of steps: Full and small steps.

For FD based schemes, a small step is a computation of finite differences for all degrees of freedom which entails a lot of computation. Small here refers to the norm of the step width - not necessarily to the amount of computation required. In general this function is supposed to gather information about the target functional around the current state.

Parameters

small_steps_before	this number tells the scheme how many small steps were performed before the current
	request.

Returns

this is true, if the Optimization Scheme requires more small steps before a big step can be performed.

Implements OptimizationAlgorithm< std::complex< double >>.

Definition at line 23 of file Optimization1D.cpp.

The documentation for this class was generated from the following files:

- · Code/OptimizationAlgorithm/Optimization1D.h
- · Code/OptimizationAlgorithm/Optimization1D.cpp

4.18 OptimizationAlgorithm < datatype > Class Template Reference

This class is an interface for Optimization algorithms such as CG or steepest descent.

```
#include <OptimizationAlgorithm.h>
```

Public Member Functions

virtual void pass_result_small_step (std::vector< datatype > vec)

A function to pass a vector of values, computed by performing a single or multiple steps with short step-width.

virtual void pass result big step (datatype input)

Similar to pass_result_small_step but for the results of big steps.

virtual bool perform small step next (int small steps before)=0

The optimization is mainly split into two kinds of steps: Full and small steps.

virtual double get small step step width (int small steps before)=0

For the optimization scheme to know, which step size is appropriate, this function was included.

• virtual bool perform big step next (int small steps before)=0

This functions returns true, if enough steps were performed to compute the next state to compute a full solution on.

virtual std::vector< double > get_big_step_configuration ()=0

This function computes the states that should be computed next.

void WriteStepsOut (std::ofstream &)

Public Attributes

- std::vector< std::vector< datatype >> states
- std::vector< datatype > residuals

4.18.1 Detailed Description

```
template < typename datatype > class OptimizationAlgorithm < datatype >
```

This class is an interface for Optimization algorithms such as CG or steepest descent.

The derived classes take residuals and gradients, store them in a history and compute the next configuration based on the data. This functionality is encapsulated like this to enable easy exchange and comparison of convergence rates. Later on the interface will be extended to make use of output generators during runtime or at the end of the program to directly generate convergence plots. This class will also be extended to allow for restrained optimization which will become necessary at some point.

Author

Pascal Kraft

Date

29.11.2016

Definition at line 22 of file OptimizationAlgorithm.h.

4.18.2 Member Function Documentation

4.18.2.1 get_big_step_configuration()

```
template<typename datatype>
virtual std::vector<double> OptimizationAlgorithm< datatype >::get_big_step_configuration ( )
[pure virtual]
```

This function computes the states that should be computed next.

If the next step will be a small step the update can be done by simply updating all dofs with a step width (or only one depending on the pattern) so this function is only used when a big step will be computed next and therefore all dofs could change differently.

Returns

This is a vector of degrees of freedom which can be used by the Optimization Strategy to update the Space Transformation.

Implemented in OptimizationCG, OptimizationSteepestDescent, and Optimization1D.

4.18.2.2 get_small_step_step_width()

For the optimization scheme to know, which step size is appropriate, this function was included.

Parameters

small_st	eps_before	similar to perform_sma	l_step	_next this is the number of small steps before the current one	€.
----------	------------	------------------------	--------	--	----

Returns

double this is how much the values of the degrees of freedom should be adapted.

 $Implemented\ in\ Optimization CG,\ Optimization Steepest Descent,\ and\ Optimization 1D.$

4.18.2.3 pass_result_big_step()

Similar to pass result small step but for the results of big steps.

Since for a big step we always only perform the solution of one forward problem we also only get one change of the target functional. Therefore in this case we only pass a value, not a vector of the like.

Parameters

input

This is the value describing how much the target functional has changed upon performing the step last computed by this optimization algorithm.

Reimplemented in OptimizationCG.

Definition at line 44 of file OptimizationAlgorithm.cpp.

```
44
45  deallog.push("Big Step Result passed");
46  deallog << "Result:" << in_change << std::endl;
47  deallog.pop();
48  residuals.push_back(in_change);
49 }</pre>
```

4.18.2.4 pass_result_small_step()

A function to pass a vector of values, computed by performing a single or multiple steps with short step-width.

"small" in the name references the fact, that the step width is small. In gerneral this is done whenever an accurat approximation of a gradient is saught based on linearization. This computation (especially in finite difference based approaches) can be much more costly than a big step. In a big step, one forward problem has to be solved. A small step computation based on finite differences requires NDofs forward problems to be solved. This function has the purpose of passing the result of such computations to the optimization algorithm which will store it and use it to compute optimization steps in the future.

Parameters

vec

This parameter is a vector of changes of the target functional based on a change in the individual component. The components belonging to restrained degrees of freedom are set to zero.

Reimplemented in OptimizationCG.

Definition at line 13 of file OptimizationAlgorithm.cpp.

```
14
     deallog.push("Small Step Result");
15
     bool complex = std::is_same<datatype, std::complex<double>>::value;
16
18
       std::vector<double> values;
19
       values.resize(2 * in_step_result.size());
       for (unsigned int i = 0; i < in_step_result.size(); i++) {
  values[2 * i] = ((std::complex<double>)in_step_result[i]).real();
20
21
          values[2 * i + 1] = ((std::complex<double>)in_step_result[i]).imag();
23
       dealii::Utilities::MPI::sum(values, MPI_COMM_WORLD, values);
25
       for (unsigned int i = 0; i < in\_step\_result.size(); i++) {
          ((std::complex<double>)in_step_result[i]).real(values[2 * i]);
2.6
          ((std::complex < double >) in\_step\_result[i]).imag(values[2 * i + 1]);\\
28
     } else {
```

```
30
      }
32
      for (unsigned int i = 0; i < in_step_result.size(); i++) {</pre>
        deallog << in_step_result[i];
if (i != in_step_result.size() - 1) {
  deallog << " , ";</pre>
33
34
35
36
37
38
     deallog << std::endl;
39
     deallog.pop();
     states.push_back(in_step_result);
40
41 }
```

4.18.2.5 perform_big_step_next()

This functions returns true, if enough steps were performed to compute the next state to compute a full solution on.

Parameters

small_steps_before number of small steps performed before

Returns

true, if the next computation should be a big step - otherwise false.

Implemented in OptimizationCG, OptimizationSteepestDescent, and Optimization1D.

4.18.2.6 perform_small_step_next()

The optimization is mainly split into two kinds of steps: Full and small steps.

For FD based schemes, a small step is a computation of finite differences for all degrees of freedom which entails a lot of computation. Small here refers to the norm of the step width - not necessarily to the amount of computation required. In general this function is supposed to gather information about the target functional around the current state.

Parameters

small_steps_before	this number tells the scheme how many small steps were performed before the current		
	request.		

Returns

this is true, if the Optimization Scheme requires more small steps before a big step can be performed.

Implemented in OptimizationCG, OptimizationSteepestDescent, and Optimization1D.

The documentation for this class was generated from the following files:

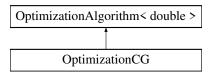
- · Code/OptimizationAlgorithm/OptimizationAlgorithm.h
- · Code/OptimizationAlgorithm/OptimizationAlgorithm.cpp

4.19 OptimizationCG Class Reference

This class implements the computation of an optimization step via a CG-method.

```
#include <OptimizationCG.h>
```

Inheritance diagram for OptimizationCG:



Public Member Functions

virtual void pass_result_small_step (std::vector< double >)

A function to pass a vector of values, computed by performing a single or multiple steps with short step-width.

virtual void pass_result_big_step (double)

Similar to pass result small step but for the results of big steps.

virtual bool perform_small_step_next (int small_steps_before)

The optimization is mainly split into two kinds of steps: Full and small steps.

virtual double get_small_step_step_width (int small_steps_before)

For the optimization scheme to know, which step size is appropriate, this function was included.

virtual bool perform_big_step_next (int small_steps_before)

This functions returns true, if enough steps were performed to compute the next state to compute a full solution on.

virtual std::vector< double > get_big_step_configuration ()

This function computes the states that should be computed next.

Additional Inherited Members

4.19.1 Detailed Description

This class implements the computation of an optimization step via a CG-method.

Objects of the Type OptimizationAlgorithm are used by the class OptimizationStrategy to compute the next viable configuration based on former results. Its is encapsulated in it's own class to offer comparison and easy changing between differenct schemes.

Author

Pascal Kraft

Date

29.11.2016

Definition at line 17 of file OptimizationCG.h.

4.19.2 Member Function Documentation

4.19.2.1 get_big_step_configuration()

```
std::vector< double > OptimizationCG::get_big_step_configuration ( ) [virtual]
```

This function computes the states that should be computed next.

If the next step will be a small step the update can be done by simply updating all dofs with a step width (or only one depending on the pattern) so this function is only used when a big step will be computed next and therefore all dofs could change differently.

Returns

This is a vector of degrees of freedom which can be used by the Optimization Strategy to update the Space Transformation.

Implements OptimizationAlgorithm < double >.

Definition at line 39 of file OptimizationCG.cpp.

```
39 {
40 std::vector<double> ret;
41 // TODO: implement this function as core functionality of CG-based stepping
42 // scheme.
43 return ret;
44 }
```

4.19.2.2 get_small_step_step_width()

For the optimization scheme to know, which step size is appropriate, this function was included.

Parameters

small_steps_before | similar to perform_small_step_next this is the number of small steps before the current one.

Returns

double this is how much the values of the degrees of freedom should be adapted.

Implements OptimizationAlgorithm < double >.

Definition at line 27 of file OptimizationCG.cpp.

```
27 {
28  // TODO: implement this function as core functionality of CG-based stepping
29  // scheme.
30  return 0.0;
31 }
```

4.19.2.3 pass_result_big_step()

Similar to pass_result_small_step but for the results of big steps.

Since for a big step we always only perform the solution of one forward problem we also only get one change of the target functional. Therefore in this case we only pass a value, not a vector of the like.

Parameters

input

This is the value describing how much the target functional has changed upon performing the step last computed by this optimization algorithm.

Reimplemented from OptimizationAlgorithm< double >.

Definition at line 15 of file OptimizationCG.cpp.

```
15 {
16  // TODO: implement this function as core functionality of CG-based stepping
17  // scheme.
18  return;
19 }
```

4.19.2.4 pass_result_small_step()

A function to pass a vector of values, computed by performing a single or multiple steps with short step-width.

"small" in the name references the fact, that the step width is small. In gerneral this is done whenever an accurat approximation of a gradient is saught based on linearization. This computation (especially in finite difference based approaches) can be much more costly than a big step. In a big step, one forward problem has to be solved. A small step computation based on finite differences requires NDofs forward problems to be solved. This function has the purpose of passing the result of such computations to the optimization algorithm which will store it and use it to compute optimization steps in the future.

Parameters

vec

This parameter is a vector of changes of the target functional based on a change in the individual component. The components belonging to restrained degrees of freedom are set to zero.

Reimplemented from OptimizationAlgorithm < double >.

Definition at line 10 of file OptimizationCG.cpp.

```
10 {
11 // TODO: This implementation is still missing - uncertain and unimportant.
12 return;
13 }
```

4.19.2.5 perform_big_step_next()

This functions returns true, if enough steps were performed to compute the next state to compute a full solution on.

Parameters

f small steps performed I	small_steps_before number
---------------------------	---------------------------

Returns

true, if the next computation should be a big step - otherwise false.

Implements OptimizationAlgorithm < double >.

Definition at line 33 of file OptimizationCG.cpp.

```
33 {
34    // TODO: implement this function as core functionality of CG-based stepping
35    // scheme.
36    return false;
37 }
```

4.19.2.6 perform_small_step_next()

The optimization is mainly split into two kinds of steps: Full and small steps.

For FD based schemes, a small step is a computation of finite differences for all degrees of freedom which entails a lot of computation. Small here refers to the norm of the step width - not necessarily to the amount of computation required. In general this function is supposed to gather information about the target functional around the current state.

Parameters

small_steps_before	this number tells the scheme how many small steps were performed before the cu	
	request.	

Returns

this is true, if the Optimization Scheme requires more small steps before a big step can be performed.

Implements OptimizationAlgorithm< double >.

Definition at line 21 of file OptimizationCG.cpp.

```
21 {
22  // TODO: implement this function as core functionality of CG-based stepping
23  // scheme.
24  return false;
25 }
```

The documentation for this class was generated from the following files:

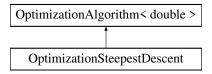
- · Code/OptimizationAlgorithm/OptimizationCG.h
- · Code/OptimizationAlgorithm/OptimizationCG.cpp

4.20 OptimizationSteepestDescent Class Reference

This class implements the computation of an optimization step via a Steepest-Descent-method.

```
#include <OptimizationSteepestDescent.h>
```

Inheritance diagram for OptimizationSteepestDescent:



Public Member Functions

• bool perform_small_step_next (int small_steps_before)

The optimization is mainly split into two kinds of steps: Full and small steps.

double get_small_step_step_width (int small_steps_before)

For the optimization scheme to know, which step size is appropriate, this function was included.

bool perform_big_step_next (int small_steps_before)

This functions returns true, if enough steps were performed to compute the next state to compute a full solution on.

std::vector< double > get_big_step_configuration ()

This function computes the states that should be computed next.

Additional Inherited Members

4.20.1 Detailed Description

This class implements the computation of an optimization step via a Steepest-Descent-method.

Objects of the Type OptimizationAlgorithm are used by the class OptimizationStrategy to compute the next viable configuration based on former results. Its is encapsulated in it's own class to offer comparison and easy changing between different schemes.

Author

Pascal Kraft

Date

29.11.2016

Definition at line 16 of file OptimizationSteepestDescent.h.

4.20.2 Member Function Documentation

4.20.2.1 get_big_step_configuration()

```
std::vector< double > OptimizationSteepestDescent::get_big_step_configuration ( ) [virtual]
```

This function computes the states that should be computed next.

If the next step will be a small step the update can be done by simply updating all dofs with a step width (or only one depending on the pattern) so this function is only used when a big step will be computed next and therefore all dofs could change differently.

Returns

This is a vector of degrees of freedom which can be used by the Optimization Strategy to update the Space Transformation.

Implements OptimizationAlgorithm < double >.

Definition at line 24 of file OptimizationSteepestDescent.cpp.

```
24
25    std::vector<double> ret;
26    if (residuals.size() == 0 && states.size() == 0) {
27        return ret;
28    }
29    int idx = states.size() - 1;
30    ret.resize(states[0].size());
31    for (unsigned int i = 0; i < states[0].size(); i++) {
32        ret[i] = -0.0001 * states[idx][i];
33    }
34    return ret;
35 }</pre>
```

4.20.2.2 get_small_step_step_width()

For the optimization scheme to know, which step size is appropriate, this function was included.

Parameters

small steps before	similar to perform_small_step_next this is the number of small steps before the current one.

Returns

double this is how much the values of the degrees of freedom should be adapted.

Implements OptimizationAlgorithm < double >.

Definition at line 16 of file OptimizationSteepestDescent.cpp.

```
16
17   return GlobalParams.StepWidth;
18 }
```

4.20.2.3 perform_big_step_next()

```
bool OptimizationSteepestDescent::perform_big_step_next ( int \ \mathit{small\_steps\_before} \ ) \quad [virtual]
```

This functions returns true, if enough steps were performed to compute the next state to compute a full solution on.

Parameters

	small_steps_before	number of small steps performed before this call.
--	--------------------	---

Returns

true, if the next computation should be a big step - otherwise false.

Implements OptimizationAlgorithm < double >.

Definition at line 10 of file OptimizationSteepestDescent.cpp.

Referenced by perform_small_step_next().

```
10
11  int full_steps = residuals.size();
12  int small_steps = states.size();
13  return (full_steps <= small_steps);
14 }</pre>
```

4.20.2.4 perform_small_step_next()

```
bool OptimizationSteepestDescent::perform_small_step_next ( int \ small\_steps\_before \ ) \quad [virtual]
```

The optimization is mainly split into two kinds of steps: Full and small steps.

For FD based schemes, a small step is a computation of finite differences for all degrees of freedom which entails a lot of computation. Small here refers to the norm of the step width - not necessarily to the amount of computation required. In general this function is supposed to gather information about the target functional around the current state.

Parameters

small_steps_before	this number tells the scheme how many small steps were performed before the current
	request.

Returns

this is true, if the Optimization Scheme requires more small steps before a big step can be performed.

Implements OptimizationAlgorithm < double >.

Definition at line 20 of file OptimizationSteepestDescent.cpp.

References perform_big_step_next().

```
20
21  return !perform_big_step_next(0);
22 }
```

The documentation for this class was generated from the following files:

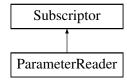
- · Code/OptimizationAlgorithm/OptimizationSteepestDescent.h
- Code/OptimizationAlgorithm/OptimizationSteepestDescent.cpp

4.21 ParameterReader Class Reference

This class is used to gather all the information from the input file and store it in a static object available to all processes.

```
#include <ParameterReader.h>
```

Inheritance diagram for ParameterReader:



Public Member Functions

• ParameterReader (ParameterHandler &prmhandler)

Deal Offers the ParameterHandler object wich contains all of the parsing-functionality.

void read_parameters (const std::string inputfile)

This member calls the read_input_from_xml()-function of the contained ParameterHandler and this replaces the default values with the values in the input file.

void declare_parameters ()

In this function, we add all values descriptions to the parameter-handler.

4.21.1 Detailed Description

This class is used to gather all the information from the input file and store it in a static object available to all processes.

The ParameterReader is a very useful tool. It uses a deal-function to read a xml-file and parse the contents to specific variables. These variables have default values used in their declaration. The members of this class do two things:

- 1. declare the variables. This includes setting a data-type for them and a default value should none be provided in the input file. Furthermore there can be restrictions like maximum or minimum values etc.
- 2. call an external function to parse an input-file.

After creating an object of this type and calling both declare() and read(), this object contains all the information from the input file and can be used in the code without dealing with persistence.

Author

Pascal Kraft

Date

23.11.2015

Definition at line 29 of file ParameterReader.h.

4.21.2 Constructor & Destructor Documentation

4.21.2.1 ParameterReader()

Deal Offers the ParameterHandler object wich contains all of the parsing-functionality.

An object of that type is included in this one. This constructor simply uses a copy-constructor to initialize it.

Definition at line 8 of file ParameterReader.cpp.

```
9 : prm(prmhandler) {}
```

4.21.3 Member Function Documentation

4.21.3.1 declare_parameters()

```
void ParameterReader::declare_parameters ( )
```

In this function, we add all values descriptions to the parameter-handler.

This includes

- 1. a default value,
- 2. a data-type,
- 3. possible restrictions (greater than zero etc.),
- 4. a description, which is displayed in deals ParameterGUI-tool,
- 5. a hierarchical structure to order the variables.

Deals Parameter-GUI can be installed at build-time of the library and offers a great and easy way to edit the input file. It displays appropriate input-methods depending on the type, so, for example, in case of a selection from three different values (i.e. the name of a solver that has to either be GMRES, MINRES or UMFPACK) it displays a dropdown containing all the options.

Definition at line 11 of file ParameterReader.cpp.

Referenced by read parameters().

```
12
     prm.enter_subsection("Output");
     prm.enter_subsection("Optimization");
13
     prm.enter_subsection("Gnuplot");
14
15
     prm.declare entry(
           "Optimization History Live", "false", Patterns::Bool(),
           "Currently not implemented. This will open an X-window at runtime and "
18
          "show the current shape to allow for full tracking of the current
19
          "procedure while it runs (to be able to abort as early as possible.");
20
     prm.declare_entry(
           "Optimization History Shapes", "true", Patterns::Bool(),
          "If this value is set to 'true', after every step a plot and a data file "
          "of the current shape will be generated. The plot shows single (tubular)
    "or multiple (rectangular) crossections of the current waveguide shape.");

prm.declare_entry("Optimization History", "true", Patterns::Bool(),

"If this value is set to 'true', a plot and data file will "

"be generated logging the values of the signal quality "
24
2.5
26
27
                           "after every step of the current optimization scheme.");
29
     prm.leave_subsection();
30
     prm.enter_subsection("VTK");
     prm.enter_subsection("TransformationWeights");
31
     prm.declare_entrv(
32
           "TransformationWeightsAll", "false", Patterns::Bool(),
33
          "If this is enabled, a .vtk file is generated in every step logging the "
34
          "norm of the transformation tensor as 3D data.");
     prm.declare_entry(
          "TransformationWeightsFirst", "false", Patterns::Bool(),
"If this is enabled, a .vtk file is generated in the first step logging "
37
38
           "the norm of the transformation tensor as 3D data.");
39
    prm.declare_entry(
          "TransformationWeightsLast", "false", Patterns::Bool(),
"If this is enabled, a .vtk file is generated in the last step logging "
          "the norm of the transformation tensor as 3D data.");
43
44
     prm.leave_subsection();
45
     prm.enter subsection("Solution");
     prm.declare_entry("SolutionAll", "false", Patterns::Bool(),
46
                           "If this is enabled, a .vtk file is generated in every "
```

```
"step logging the solution as 3D data.");
     prm.declare_entry("SolutionFirst", "true", Patterns::Bool(),
49
50
                        "If this is enabled, a .vtk file is generated in the first "
     "step logging the solution as 3D data.");
prm.declare_entry("SolutionLast", "true", Patterns::Bool(),

"If this is enabled, a .vtk file is generated in the last "
51
52
53
                        "step logging the solution as 3D data.");
55
     prm.leave_subsection();
     prm.leave_subsection();
56
57
     prm.leave subsection();
58
     prm.enter_subsection("Convergence");
     prm.enter_subsection("DataFiles");
59
     prm.declare_entry("ConvergenceFirst", "false", Patterns::Bool(),
60
                        "This causes the code to generate a datafile with the data "
62
                        "of the system matrix solution process of the first step.");
     6.3
64
                        "of the system matrix solution process of the last step.");
65
     prm.declare_entry("ConvergenceAll", "false", Patterns::Bool(),
66
                        "This causes the code to generate a datafile with the data "
                        "of the system matrix solution process of all steps.");
68
69
     prm.leave_subsection();
70
     prm.enter_subsection("Plots");
     prm.declare_entry("ConvergenceFirst", "false", Patterns::Bool(),
71
72
                        "This causes the code to generate a plot of the data of "
                        "the system matrix solution process of the first step.");
73
     prm.declare_entry("ConvergenceLast", "false", Patterns::Bool(),
74
75
                        "This causes the code to generate a plot of the data of " \,
     "the system matrix solution process of the last step.");
prm.declare_entry("ConvergenceAll", "false", Patterns::Bool(),
76
77
                        "This causes the code to generate a plot of the data of "
78
                        "the system matrix solution process of all steps.");
80
     prm.leave_subsection();
     prm.leave_subsection();
81
     prm.enter_subsection("General");
prm.declare_entry("SummaryFile", "true", Patterns::Bool(),
82
83
                        "This generates an output of the simulation (mathematical "
84
                        "terms. Convergence rates, residuals, parameters etc.)");
85
     prm.declare_entry("LogFile", "true", Patterns::Bool(),
                        "This generates a general log (Code steps, warnings, "
87
                        "errors, diagnostics)");
88
89
     prm.leave subsection();
     prm.leave_subsection();
90
     prm.enter_subsection("Measures");
     prm.enter_subsection("PredefinedCases");
     prm.declare_entry("ComputeCase", "false", Patterns::Bool(),
93
94
                        "Do you want to compute a predefined case?");
     9.5
96
97
     prm.leave subsection();
     prm.enter_subsection("Connectors");
prm.declare_entry("Shape", "Circle", Patterns::Selection("Circle|Rectangle"),
98
99
100
                         "Describes the shape of the input connector.");
101
      prm.declare_entry(
           "Dimension1 In", "2.0", Patterns::Double(0),
102
          "First dimension of the input connector. For a circular waveguide this "
103
          "is the radius. For a rectangular waveguide this is the width.");
104
105
      prm.declare entrv(
          "Dimension2 In", "2.0", Patterns::Double(0),
106
107
          "Second dimension of the input connector. For a circular waveguide this "
108
          "has no meaning. For a rectangular waveguide this is the height.");
109
      prm.declare_entry(
110
           "Dimension1 Out", "2.0", Patterns::Double(0),
          "First dimension of the output connector. For a circular waveguide this "
111
112
          "is the radius. For a rectangular waveguide this is the width.");
113
      prm.declare_entry(
          "Dimension2 Out", "2.0", Patterns::Double(0),
114
          "Second dimension of the output connector. For a circular waveguide this "
115
116
          "has no meaning. For a rectangular waveguide this is the height.");
117
      prm.leave_subsection();
118
      prm.enter_subsection("Region");
119
      prm.declare_entry(
          "XLength", "10.0", Patterns::Double(0),
"Length of the system in x-Direction (Connectors lie in the XY-plane and "
120
121
          "the offset lies in the y-direction. Measured in micrometres");
122
123
      prm.declare_entry(
          "YLength", "10.0", Patterns::Double(0),
124
125
          "Length of the system in y-Direction (Connectors lie in the XY-plane and " \,
126
          "the offset lies in the y-direction. Measured in micrometres");
127
      prm.declare entry(
           "ZLength", "6.0", Patterns::Double(0),
128
          "Length of the system in z-Direction (Connectors lie in the XY-plane and "
129
          "the offset lies in the y-direction. Measured in micrometres");
130
131
      prm.leave_subsection();
132
      prm.enter_subsection("Waveguide");
      prm.declare_entry(
    "Delta", "1.0", Patterns::Double(0),
133
134
```

```
135
           "Offset between the two connectors measured in micrometres.");
      prm.declare_entry(
    "epsilon in", "2.21", Patterns::Double(0),
136
137
           "Material-Property of the optical fiber (optical thickness).");
138
      prm.declare_entry(
    "epsilon out", "2.2", Patterns::Double(0),
139
140
           "Material-Property of environment of the fiber (optical thickness).");
141
      prm.declare_entry("Lambda", "5.6328", Patterns::Double(0),
142
      143
144
145
146
      prm.leave subsection();
      prm.enter_subsection("Boundary Conditions");
147
      prm.declare_entry("Type", "PML", Patterns::Selection("PML|HSIE"),
148
149
                          "The way the output-connector is modeled. HSIE uses the "
150
                          "Hardy-space infinite element for setting boundary " \,
      151
152
153
154
                          "for better wave coupling");
155
      prm.declare_entry(
           "ZPlus", "1", Patterns::Double(0),
"Thickness of the PML area on the side of the output connector.");
156
157
158
      prm.declare_entry(
           "XMinus", "1.0", Patterns::Double(0),
159
           "Thickness of the PML on the negative X-axis. Measured in micrometers");
160
161
      prm.declare_entry(
162
           "XPlus", "1.0", Patterns::Double(0),
163
           "Thickness of the PML on the positive X-axis. Measured in micrometers");
164
      prm.declare_entry(
    "YMinus", "1.0", Patterns::Double(0),
165
           "Thickness of the PML on the negative Y-axis. Measured in micrometers");
166
167
      prm.declare_entry(
168
           "YPlus", "1.0", Patterns::Double(0),
      169
170
171
172
173
                          "PML Tuning Parameter");
174
      prm.declare_entry("KappaZMax", "10.0", Patterns::Double(0),
      "PML Tuning Parameter");
prm.declare_entry("SigmaXMax", "10.0", Patterns::Double(0),
175
176
      "PML Tuning Parameter");
prm.declare_entry("SigmaYMax", "10.0", Patterns::Double(0),
177
178
      179
180
181
182
      prm.declare_entry(
           "DampeningExponentM", "3", Patterns::Integer(3),
183
           "Dampening Exponent M for the intensety of dampening in the PML region.");
184
185
      prm.leave_subsection();
186
      prm.leave_subsection();
187
      prm.enter_subsection("Schema");
      prm.declare_entry(
    "Homogeneity", "false", Patterns::Bool(),
188
189
           "If this is enabled, a space transformation is used which is equal the " identity on the PML-region for the dampening along the x and y axis.");
190
191
      prm.declare_entry("Optimization Schema", "Adjoint",
192
193
                          Patterns::Selection("Adjoint|FD"),
194
                          "If this is set to adjoint, the shape gradient will be " \,
                          "computed by means of an adjoint based method. If it is "
195
      "set to FD, finite differences are use.");
prm.declare_entry("Optimization Steps", "10", Patterns::Integer(1),
196
197
                          "Number of Optimization steps to be performed.");
198
199
      prm.declare_entry(
200
           "Stepping Method", "Steepest",
          Patterns::Selection("Steepest|CG|LineSearch"),
201
202
           "Method of step computation. Steepest uses steepest descent. CG uses a
203
           "conjugate gradient method to compute the next step. Line Search only
204
           "works based on an adjoint optimization setting, where searches can be "
205
           "performed cheaply.");
206
      // prm.declare_entry("Step Width", "Adjoint",
      // Patterns::Selection("Adjoint|Experimental"), "This parameter descibes the // scheme used to compute the next step width. This can be adjoint (if an
207
208
209
      // adjoint schema is used, which causees the computation of multiple shape
      // hradient with differing step widths in the parameters. This would be too
210
211
      // costly for FD and ist therefore not available in that mode. An experimental
212
       // approach can be used which tries to use information from the gradient and a
213
      // seperate step width control to compute the step. ");
      prm.leave_subsection();
214
215
      prm.enter subsection("Solver");
216
      prm.declare_entry(
           "Solver", "GMRES", Patterns::Selection("GMRES|UMFPACK|MINRES"),
217
      "Which Solver to use for the solution of the system matrix");

prm.declare_entry("GMRESSteps", "30", Patterns::Integer(1),

"Steps until restart of Krylow subspace generation");

prm.declare_entry("Preconditioner", "Sweeping",
218
219
220
221
```

```
222
                     Patterns::Selection(
                        "Sweeping|FastSweeping|HSIESweeping|HSIEFastSweeping"),
223
     "Which preconditioner to use");
prm.declare_entry("PreconditionerDampening", "0.0", Patterns::Double(0),
224
225
226
                     "Dampening for the preconditioner to acclelerate
    "convergence. Typically 0 (off) or 1.0");
prm.declare_entry("Steps", "30", Patterns::Integer(1),
227
228
                     "Number of Steps the Solver is supposed to do.");
229
230
     prm.declare_entry("Precision", "le-6", Patterns::Double(0),
231
                     "Minimal error value, the solver is supposed to accept as "
                     "correct solution.");
232
233
     prm.leave subsection();
234
     prm.enter_subsection("Constants");
235
     prm.declare_entry(
236
        "AllOne", "true", Patterns::Bool(),
    237
238
239
                     "measured in micrometers.");
240
    prm.declare_entry("MuZero", "1.257e-12", Patterns::Double(0),
241
                     "Physical constant Mu zero. The standard value is measured "
242
    243
2.44
2.45
246
     prm.leave_subsection();
247
     prm.enter_subsection("Refinement");
     prm.declare_entry("Global", "1", Patterns::Integer(0),
248
                     "Global refinement-steps.");
249
     250
251
252
                     "Waveguide-boundary and inside).");
    253
254
255
     prm.leave_subsection();
256 }
```

The documentation for this class was generated from the following files:

- · Code/Helpers/ParameterReader.h
- · Code/Helpers/ParameterReader.cpp

4.22 Parameters Class Reference

This structure contains all information contained in the input file and some values that can simply be computed from it.

```
#include <Parameters.h>
```

Public Attributes

- bool O_O_G_HistoryLive
- · bool O_O_G_HistoryShapes
- bool O_O_G_History
- bool O_O_V_T_TransformationWeightsAll
- bool O O V T TransformationWeightsFirst
- bool O_O_V_T_TransformationWeightsLast
- bool O_O_V_S_SolutionAll
- bool O_O_V_S_SolutionFirst
- bool O_O_V_S_SolutionLast
- bool O C D ConvergenceAll
- bool O_C_D_ConvergenceFirst
- bool O_C_D_ConvergenceLast
- bool O_C_P_ConvergenceAll

- bool O_C_P_ConvergenceFirst
- bool O_C_P_ConvergenceLast
- bool O_G_Summary
- bool O_G_Log
- ConnectorType M C Shape
- double M_C_Dim1In
- · double M C Dim2In
- double M_C_Dim1Out
- double M_C_Dim2Out
- · double M R XLength
- double M_R_YLength
- · double M R ZLength
- · double M_W_Delta
- · double M W epsilonin
- double M_W_epsilonout
- · int M W Sectors
- · double M W Lambda
- BoundaryConditionType M_BC_Type
- double M_BC_Zminus
- double M_BC_Zplus
- double M_BC_XMinus
- double M_BC_XPlus
- · double M BC YMinus
- double M_BC_YPlus
- double M BC KappaXMax
- double M_BC_KappaZMax
- double M_BC_KappaYMax
- double M_BC_SigmaXMax
- double M_BC_SigmaZMax
- double M_BC_SigmaYMax
- double M_BC_DampeningExponent
- bool Sc Homogeneity
- · OptimizationSchema Sc_Schema
- · int Sc_OptimizationSteps
- SteppingMethod Sc_SteppingMethod
- SolverOptions So_Solver
- PreconditionerOptions So_Preconditioner
- · double So PreconditionerDampening
- int So_ElementOrder
- · int So RestartSteps
- · int So TotalSteps
- · double So_Precision
- · bool C_AllOne
- double **C_Mu**
- double C_Epsilon
- · double C Pi
- · double C c
- double C_f0
- double C_k0
- · double C_omega
- int R Global
- · int R_Local
- int R_Interior
- · double LayerThickness
- · double SectorThickness

- · unsigned int MPI_Rank
- MPI_Comm MPIC_World
- · bool PMLLayer
- · double LayersPerSector
- int NumberProcesses
- bool **Head** = false
- · double SystemLength
- double Maximum_Z
- · double Minimum_Z
- · double Phys V
- · double Phys SpotRadius
- · double StepWidth
- bool M_PC_Use
- int M_PC_Case
- ShapeDescription sd

4.22.1 Detailed Description

This structure contains all information contained in the input file and some values that can simply be computed from it.

In the application, static Variable of this type makes the input parameters available globally.

Author

: Pascal Kraft

Date

: 28.11.2016

Definition at line 77 of file Parameters.h.

The documentation for this class was generated from the following file:

· Code/Helpers/Parameters.h

4.23 PointVal Class Reference

Public Member Functions

- PointVal (double, double, double, double, double, double)
- void set (double, double, double, double, double, double)
- · void rescale (double)

Public Attributes

- std::complex < double > Ex
- std::complex< double > Ey
- std::complex < double > Ez

4.23.1 Detailed Description

Definition at line 6 of file PointVal.h.

The documentation for this class was generated from the following files:

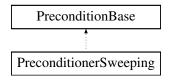
- · Code/Helpers/PointVal.h
- · Code/Helpers/PointVal.cpp

4.24 PreconditionerSweeping Class Reference

This class implements the DeallI preconditioner interface and offers a sweeping preconditioning mechanism.

#include <PreconditionerSweeping.h>

Inheritance diagram for PreconditionerSweeping:



Public Member Functions

• PreconditionerSweeping (MPI_Comm in_mpi_comm, int in_own, int in_others, int in_above, int bandwidth, dealii::IndexSet locally_owned, dealii::IndexSet *in_fixed_dofs, int rank, bool fast)

This constructor is the only one that should be used at this time.

void Hinv (const dealii::Vector< double > &src, dealii::Vector< double > &dst) const

For the application of the preconditioner we require the application of the inverse of H.

void LowerProduct (const dealii::Vector< double > &src. dealii::Vector< double > &dst) const

Cases in which we require multiplications with $A(E_{i+1}, E_i)$, are where this function is used.

void UpperProduct (const dealii::Vector < double > &src, dealii::Vector < double > &dst) const

Cases in which we require multiplications with $A(E_i, E_{i+1})$, are where this function is used.

virtual void vmult (dealii::TrilinosWrappers::MPI::BlockVector &dst, const dealii::TrilinosWrappers::MPI::←
 BlockVector &src) const

In order to be called by the iterative solver, this function has to be overloaded.

- virtual void vmult_slow (dealii::TrilinosWrappers::MPI::BlockVector &dst, const dealii::TrilinosWrappers::
 MPI::BlockVector &src) const
- void Prepare (dealii::TrilinosWrappers::MPI::BlockVector &src)
- void init (dealii::SolverControl in_sc, dealii::TrilinosWrappers::SparseMatrix *, dealii::TrilinosWrappers::
 SparseMatrix *)

Public Attributes

- dealii::TrilinosWrappers::SparseMatrix * matrix
- dealii::SparseMatrix< double > * prec matrix upper
- dealii::SparseMatrix< double > * prec_matrix_lower

4.24.1 Detailed Description

This class implements the DealII preconditioner interface and offers a sweeping preconditioning mechanism.

Details can be found in the paper A sweeping preconditioner for time-harmonic Maxwell's equations with finite elements. The general idea is as follows: Let Ω be the computational domain (internally) truncated by an absorbing boundary condition. This domain can be split into layers along a direction (in our case z and triangulated. We therefore have a triangulation spread across multiple processes. We chose the splitting such, that the degrees of freedom are ordered process-wise. Let K be the number of Layers and T_i $i \in \{1, \ldots, K\}$ the parts of the triangulation. For a PML function

$$\sigma_i(\xi) = \begin{cases} \theta \left(\frac{-1 + (i-1)l - \xi}{l} * \right)^2 & \xi \in [-1 + (i-2)l, -1 + (i-1)l] \\ 0, & \xi \in [-1 + *(i-1)l, 1 - l] \\ \Theta \left(\frac{\xi - 1 + l}{l} \right)^2, & \xi \in *[1 - l, 1] \end{cases}$$

we now regard the problem

$$\nabla \times *\tilde{\mu}_{r,i}^{-1} \nabla \times \boldsymbol{E} - *\kappa^2 \tilde{\epsilon}_{r,i} \boldsymbol{E} = 0$$
 in $* \operatorname{int}(T_{i-1} \cup T_i)$

where

Described in words: We put a PML into the neighboring block of the block we want to precondition and setup the system matrix for this smaller problem. This matrix we can then invert and name the Operator H_i^{-1} . We then define the operator

$$S(\mathbf{v}) = P_{0,n_i} H_i^{-1}(\mathbf{v} *, \mathbf{0}))$$

where P_{0,n_i} describes the extraction of the first n_i components. For the one block which has no neighbor the inverse of the block of the system matrix can be used. The inversion does not have to be performed numerically - a decomposition (performed by UMFPACK or MUMPS) is sufficient.

Date

28.11.2016

Author

Pascal Kraft

Definition at line 59 of file PreconditionerSweeping.h.

4.24.2 Constructor & Destructor Documentation

4.24.2.1 PreconditionerSweeping()

This constructor is the only one that should be used at this time.

Parameters

in_own	This is the number of degrees of freedom that the current process has to deal with (owned).
in_others	This is the number of degrees of freedom that the process below has. Every process has to deal with one other process. The other neighbor only contacts it for a multiplication with its own matrix block - in this case, no objects of unknown size are concerned. However: for the one process that does require more contact needs a vector tp be initialized. This vectors size is this int.
bandwidth	The number of dofs per line on average is required for the construction of matrices.
locally_owned	The degrees of freedom associated with the current process. Required for vector and matrix construction.
dampening_parameter	If set to zero, no dampening is used. Otherwise, dampening according to (3.10) in the sweeping preconditioner paper is used. Thi solves the equation $\nabla\times\tilde{\mu}^{-1}\nabla\times\boldsymbol{E}-(\kappa+i\alpha)^2\tilde{\epsilon}\boldsymbol{E}=0$

Definition at line 27 of file PreconditionerSweeping.cpp.

```
32
33
      locally_owned_dofs = in_locally_owned_dofs;
      own = in_own;
35
      others = in_others;
      IndexSet elements(own + others);
36
     elements.add_range(0, own + others);
indices = new int[in_locally_owned_dofs.n_elements()];
37
38
     sweepable = in_locally_owned_dofs.n_elements();
for (unsigned int i = 0; i < sweepable; i++) {
  indices[i] = in_locally_owned_dofs.nth_index_in_set(i);</pre>
40
41
42
43
     fixed_dofs = in_fixed_dofs;
      rank = in_rank;
44
45 bandwidth = in_bandwidth;
46 mpi_comm = in_mpi_comm;
47
     above = in_above;
48
     prec_matrix_lower = 0;
49
     prec_matrix_upper = 0;
     matrix = 0;
fast = in_fast;
50
```

4.24.3 Member Function Documentation

4.24.3.1 Hinv()

For the application of the preconditioner we require the application of the inverse of H.

This is implemented in this function. (The mathematical usage is included in lines 2, 6 and 13 and indirectly in every use of the Operator S.

Parameters

src	This is the vector to be multiplied by H_i^{-1} .
dst	This is the vector to store the result in.

Definition at line 213 of file PreconditionerSweeping.cpp.

```
214
215  dealii::Vector<double> inputb(own + others);
216  for (int i = 0; i < own; i++) {
217    inputb[i] = src(i);
218  }
219
220  solver->solve(inputb);
221
222  for (int i = 0; i < own; i++) {
223    dst[i] = inputb[i];
224  }
225 }</pre>
```

4.24.3.2 LowerProduct()

Cases in which we require multiplications with $A(E_{i+1}, E_i)$, are where this function is used.

See algorithm lines 2 and 4.

Parameters

src	This is the vector to be multiplied by $A(E_{i+1}, E_i)$.
dst	This is the vector to store the result in.

Definition at line 312 of file PreconditionerSweeping.cpp.

4.24.3.3 UpperProduct()

Cases in which we require multiplications with $A(E_i, E_{i+1})$, are where this function is used.

See algorithm lines 11 and 13.

Parameters

src	This is the vector to be multiplied by $A(E_i, E_{i+1})$.
dst	This is the vector to store the result in.

Definition at line 303 of file PreconditionerSweeping.cpp.

```
304
305    if ((int)rank + 1 == GlobalParams.NumberProcesses) {
306       std::cout << "ERROR!" << std::endl;
307    }
308
309    prec_matrix_upper->vmult(dst, src);
310 }
```

4.24.3.4 vmult()

In order to be called by the iterative solver, this function has to be overloaded.

It gets called from GMRES and is the core function which contains the implementation. For a description of the interface, see the implementation in the base class.

Parameters

dst	The vector to store the result in.
src	The vector to be multiplied by the approximate inverse.

Definition at line 62 of file PreconditionerSweeping.cpp.

```
64
65   if (fast) {
66     this->vmult_fast(dst, src);
67   } else {
68     this->vmult_slow(dst, src);
69   }
70 }
```

4.24.3.5 vmult_fast()

fast version starting here. if (rank == 0) { MPI_Send(&input[0], own, MPI_DOUBLE, rank + 1, 0, mpi_comm); } else { MPI_Recv(& recv_buffer_above[0], above, MPI_DOUBLE, rank-1, 0, mpi_comm, MPI_STATUS_IGNORE); if(rank < GlobalParams.NumberProcesses-1) MPI_Send(&input[0], own, MPI_DOUBLE, rank + 1, 0, mpi_comm); }

if(rank > 0) { LowerProduct(recv_buffer_above, temp_own); if(rank == GlobalParams.NumberProcesses-1) { solver->solve(temp_own); input -= temp_own; } else { Hinv(temp_own, temp_own_2); input -= temp_own_2; } }

for(int i = 0; i < own; i++){ if(! fixed_dofs->is_element(indices[i])){ dst[indices[i]] = input[i]; } }

Definition at line 72 of file PreconditionerSweeping.cpp.

```
74
75
     dealii::Vector<double> recv_buffer_above(above);
76
     dealii::Vector<double> recv_buffer_below(others);
77
     dealii:: Vector < double > temp_own (own);
     dealii::Vector<double> temp_own_2(own);
78
     dealii::Vector<double> input(own);
for (unsigned int i = 0; i < sweepable; i++) {</pre>
79
       input[i] = src[indices[i]];
81
82
83
     if (rank == GlobalParams.NumberProcesses - 1) {
84
85
       solver->solve(input);
     } else {
       if
          (rank > 0) {
88
         Hinv(input, temp_own);
89
90
     if
         (rank == GlobalParams.NumberProcesses - 1) {
91
       MPI_Send(&input[0], own, MPI_DOUBLE, rank - 1, 0, mpi_comm);
92
94
       MPI_Recv(&recv_buffer_below[0], others, MPI_DOUBLE, rank + 1, 0, mpi_comm,
95
                MPI_STATUS_IGNORE);
       if (rank > 0)
96
         MPI_Send(&temp_own[0], own, MPI_DOUBLE, rank - 1, 0, mpi_comm);
97
98
99
100
      if (rank < GlobalParams.NumberProcesses - 1) {</pre>
101
        UpperProduct(recv_buffer_below, temp_own);
102
        input -= temp_own;
103
104
105
      if (rank < GlobalParams.NumberProcesses - 1) {</pre>
        for (int i = 0; i < own; i++) {
106
107
          temp_own[i] = input[i];
108
        Hinv(temp_own, input);
109
110
111
112
113
       * fast version starting here.
114
       if ( rank == 0) {
          MPI_Send(&input[0], own, MPI_DOUBLE, rank + 1, 0, mpi_comm);
115
116
        } else {
117
          MPI_Recv(& recv_buffer_above[0], above, MPI_DOUBLE, rank-1, 0, mpi_comm,
       MPI_STATUS_IGNORE); if(rank < GlobalParams.NumberProcesses-1)</pre>
118
119
       MPI_Send(&input[0], own, MPI_DOUBLE, rank + 1, 0, mpi_comm);
120
121
122
        if(rank > 0) {
123
           LowerProduct(recv_buffer_above, temp_own);
           if(rank == GlobalParams.NumberProcesses-1) {
124
             solver->solve(temp_own);
125
126
             input -= temp_own;
           } else {
127
128
            Hinv(temp_own, temp_own_2);
129
             input -= temp_own_2;
130
131
132
        for(int i = 0; i < own; i++ ) {
  if(! fixed_dofs->is_element(indices[i])) {
133
134
            dst[indices[i]] = input[i];
135
136
137
138
         **/
      if (rank == 0) {
139
        MPI_Send(&input[0], own, MPI_DOUBLE, rank + 1, 0, mpi_comm);
140
141
142
        MPI_Recv(&recv_buffer_above[0], above, MPI_DOUBLE, rank - 1, 0, mpi_comm,
143
                  MPI_STATUS_IGNORE);
144
         LowerProduct(recv_buffer_above, temp_own);
145
        Hinv(temp_own, temp_own_2);
        input -= temp_own_2;
if ((int)rank + 1 < GlobalParams.NumberProcesses) {</pre>
146
147
148
          MPI_Send(&input[0], own, MPI_DOUBLE, rank + 1, 0, mpi_comm);
149
```

The documentation for this class was generated from the following files:

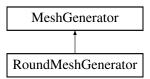
- · Code/Core/PreconditionerSweeping.h
- Code/Core/PreconditionerSweeping.cpp

4.25 RoundMeshGenerator Class Reference

This class generates meshes, that are used to discretize a rectangular Waveguide.

```
#include <RoundMeshGenerator.h>
```

Inheritance diagram for RoundMeshGenerator:



Public Member Functions

- RoundMeshGenerator (SpaceTransformation *in_ct)
- void refine_global (parallel::distributed::Triangulation < 3 > *in_tria, unsigned int times)

This function is intended to execute a global refinement of the mesh.

void refine_internal (parallel::distributed::Triangulation < 3 > *in_tria, unsigned int times)

This function is intended to execute an internal refinement of the mesh.

• void refine proximity (parallel::distributed::Triangulation < 3 > *in tria, unsigned int times, double factor)

This function is intended to execute a refinement inside and near the waveguide boundary.

bool math_coordinate_in_waveguide (Point< 3 > position) const

This function checks if the given coordinate is inside the waveguide or not.

bool phys_coordinate_in_waveguide (Point< 3 > position) const

This function checks if the given coordinate is inside the waveguide or not.

void set_boundary_ids (parallel::distributed::Triangulation < 3 > &tria) const

This function is a helper during distributed mesh generation.

void prepare_triangulation (parallel::distributed::Triangulation < 3 > *in_tria)

This function takes a triangulation object and prepares it for the further computations.

Additional Inherited Members

4.25.1 Detailed Description

This class generates meshes, that are used to discretize a rectangular Waveguide.

It is derived from MeshGenerator.

This Generator creates a mesh around a cylindrical waveguide. It should be used in conjunction with a Space Transformation, which uses a circular shape of the waveguide and an appropriate distribution of the DOFs.

Author

Pascal Kraft

Date

28.11.2016

Definition at line 21 of file RoundMeshGenerator.h.

4.25.2 Member Function Documentation

4.25.2.1 math_coordinate_in_waveguide()

This function checks if the given coordinate is inside the waveguide or not.

The naming convention of physical and mathematical system find application. In this version, the waveguide has been transformed and the check for a tubal waveguide for example only checks if the radius of a given vector is below the average of input and output radius. position This value gives us the location to check for.

Implements MeshGenerator.

Definition at line 243 of file RoundMeshGenerator.cpp.

Referenced by SquareMeshGenerator::refine_internal().

```
244 {
245 return Distance2D(in_position) <
246 (GlobalParams.M_C_DimlIn + GlobalParams.M_C_DimlOut) / 2.0;
247 }
```

4.25.2.2 phys_coordinate_in_waveguide()

This function checks if the given coordinate is inside the waveguide or not.

The naming convention of physical and mathematical system find application. In this version, the waveguide is bent. If we are using a space transformation f then this function is equal to math_coordinate_in_waveguide(f(x,y,z)). position This value gives us the location to check for.

Implements MeshGenerator.

Definition at line 249 of file RoundMeshGenerator.cpp.

References SpaceTransformation::get m(), and SpaceTransformation::get r().

```
250
251    Point<3, double> temp = in_position;
252    temp[1] -= ct->get_m(in_position[2]);
253    double r = ct->get_r(in_position[2]);
254    return (abs(temp[0]) < r && abs(temp[1]) < r);
255 }</pre>
```

4.25.2.3 prepare_triangulation()

```
void RoundMeshGenerator::prepare_triangulation ( parallel::distributed::Triangulation < 3 > * in\_tria ) [virtual]
```

This function takes a triangulation object and prepares it for the further computations.

It is intended to encapsulate all related work and is explicitely not const.

Parameters

in_tria The triangulation that is supposed to be prepared. All further information is derived from the parameter file and not given by parameters.

mesh info(*in tria, "Output"+std::to string(GlobalParams.MPI Rank)+".vtk");

Implements MeshGenerator.

Definition at line 107 of file RoundMeshGenerator.cpp.

References set_boundary_ids().

```
108 {
109 deallog.push("RoundMeshGenerator:prepare_triangulation");
110 deallog << "Starting Mesh preparation" << std::endl;
111
112 const std_cxx11::array<Tensor<1, 3>, 3> edges2(edges);
113
114 GridGenerator::subdivided_parallelepiped<3, 3>(*in_tria, origin, edges2, subs, false);
```

```
116
      in_tria->repartition();
117
118
119
     in_tria->signals.post_refinement.connect(
         120
121
122
123
      in_tria->refine_global(3);
124
125
      in_tria->set_all_manifold_ids(0);
126
127
      GridTools::transform(&Triangulation Stretch to circle, *in tria);
128
129
      unsigned int man = 1;
130
131
      in_tria->set_manifold(man, round_description);
132
133
      in tria->set all manifold ids(0);
134
      cell = in_tria->begin_active();
135
      endc = in_tria->end();
136
137
      for (; cell != endc; ++cell) {
       if (Distance2D(cell->center()) < 0.25) {</pre>
138
         cell->set_all_manifold_ids(1);
139
140
         cell->set_manifold_id(1);
141
142
143
144
      in_tria->set_manifold(man, round_description);
145
146
      in tria->set all manifold ids(0);
147
      cell = in_tria->begin_active();
148
      endc = in_tria->end();
      for (; cell != endc; ++cell) {
149
       if (Distance2D(cell->center()) < 0.25) {</pre>
150
151
         cell->set_all_manifold_ids(1);
         cell->set_manifold_id(1);
152
153
154
155
156
      in_tria->set_manifold(man, round_description);
157
      parallel::distributed::Triangulation<3>::active_cell_iterator
         cell = in tria->begin active(),
158
         endc = in_tria->end();
159
160
161
     double len = 2.0 / Layers;
162
163
      cell = in_tria->begin_active();
164
      for (; cell != endc; ++cell) {
165
       int temp = (int)std::floor((cell->center(true, false)[2] + 1.0) / len);
        if (temp >= (int)Layers || temp < 0)</pre>
166
         167
168
169
                    << std::endl;
170
171
172
      GridTools::transform(&Triangulation_Stretch_X, *in_tria);
173
      GridTools::transform(&Triangulation_Stretch_Y, *in_tria);
174
      GridTools::transform(&Triangulation_Stretch_Computational_Radius, *in_tria);
175
      if (GlobalParams.R_Global > 0) {
176
177
       in_tria->refine_global(GlobalParams.R_Global);
     }
178
179
180
      double MaxDistFromBoundary =
181
          ({\tt GlobalParams.M\_C\_DimlOut + GlobalParams.M\_C\_DimlIn}) \  \  \, * \  \, 1.4 \  \, / \  \, 2.0;\\
182
      for (int i = 0; i < GlobalParams.R_Local; i++) {</pre>
       cell = in_tria->begin_active();
183
        for (; cell != endc; ++cell) {
184
185
         if (std::abs(Distance2D(cell->center(true, false)) -
186
                       (GlobalParams.M_C_Dim1In + GlobalParams.M_C_Dim1Out) / 2.0) <
187
             MaxDistFromBoundary) {
188
            cell->set_refine_flag();
189
190
191
        in_tria->execute_coarsening_and_refinement();
192
        MaxDistFromBoundary
193
           (MaxDistFromBoundary +
194
             ((GlobalParams.M_C_Dim1Out + GlobalParams.M_C_Dim1In) / 2.0)) /
            2.0:
195
196
197
198
      for (int i = 0; i < GlobalParams.R_Interior; i++) {</pre>
199
        cell = in_tria->begin_active();
        for (; cell != endc; ++cell) {
  if (Distance2D(cell->center(true, false)) <</pre>
200
2.01
202
              (GlobalParams.M_C_Dim1In + GlobalParams.M_C_Dim1Out) / 2.0) {
```

```
203
            cell->set_refine_flag();
204
205
206
        in_tria->execute_coarsening_and_refinement();
207
208
      // mesh_info(triangulation, solutionpath + "/grid" +
209
      // static_cast<std::ostringstream*>( &(std::ostringstream() <<
// GlobalParams.MPI_Rank) )->str() + ".vtk");
210
211
212
213
      GridTools::transform(&Triangulation_Stretch_Z, *in_tria);
214
215
      GridTools::transform(&Triangulation_Shift_Z, *in_tria);
216
217
      z_{min} = 10000000.0;
      z_max = -10000000.0;
cell = in_tria->begin_active();
218
219
220
      endc = in_tria->end();
221
222
      for (; cell != endc; ++cell)
223
       if (cell->is_locally_owned()) {
224
          for (int face = 0; face < 6; face++) {</pre>
225
            z_min = std::min(z_min, cell->face(face)->center()[2]);
            z_max = std::max(z_max, cell->face(face)->center()[2]);
226
227
          }
228
      }
229
230
231
      cell = in_tria->begin_active();
232
      endc = in_tria->end();
233
234
      /// mesh_info(*in_tria,
235
      /// "Output"+std::to_string(GlobalParams.MPI_Rank)+".vtk");
236
237
      set_boundary_ids(*in_tria);
238
      deallog << "Done" << std::endl;
239
240
     deallog.pop();
241 }
```

4.25.2.4 refine_global()

This function is intended to execute a global refinement of the mesh.

This means that every cell will be refined in every direction (effectively multiplying the number of DOFs by 8). This version is the most expensive refinement possible and should be used with caution.

Parameters

times Number of refinement steps to be performed (gives us a multiplication of the number of degrees of freedom by 8^{times} .

Implements MeshGenerator.

Definition at line 257 of file RoundMeshGenerator.cpp.

```
258
259 in_tria->refine_global(times);
260 }
```

4.25.2.5 refine_internal()

This function is intended to execute an internal refinement of the mesh.

This means that every cell inside the waveguide will be refined in every direction. This method is rather cheap and only refines where the field is strong, however, the mesh outside the waveguide should not be too coarse to reduce numerical errors.

Parameters

times

Number of refinement steps to be performed.

Implements MeshGenerator.

Definition at line 278 of file RoundMeshGenerator.cpp.

References MeshGenerator::math_coordinate_in_waveguide().

4.25.2.6 refine_proximity()

This function is intended to execute a refinement inside and near the waveguide boundary.

Parameters

times Number of refinement steps to be performed.

Implements MeshGenerator.

Definition at line 262 of file RoundMeshGenerator.cpp.

```
264 {
```

```
265
      for (unsigned int t = 0; t < times; t++) {</pre>
        double R = (GlobalParams.M_C_DimlOut + GlobalParams.M_C_DimlIn) *
267
                     (1.0 + factor) / 2.0;
       cell = in_tria->begin_active();
268
        for (; cell != endc; ++cell) {
  if (Distance2D(cell->center(true, false)) < R) {</pre>
269
270
271
            cell->set_refine_flag();
272
273
274
         in_tria->execute_coarsening_and_refinement();
      }
275
276 }
```

The documentation for this class was generated from the following files:

- · Code/MeshGenerators/RoundMeshGenerator.h
- · Code/MeshGenerators/RoundMeshGenerator.cpp

4.26 Sector < Dofs_Per_Sector > Class Template Reference

Sectors are used, to split the computational domain into chunks, whose degrees of freedom are likely coupled.

```
#include <Sector.h>
```

Public Member Functions

Sector (bool in left, bool in right, double in z 0, double in z 1)

Constructor of the Sector class, that takes all important properties as an input property.

• Tensor< 2, 3, double > TransformationTensorInternal (double in_x, double in_y, double in_z) const

This method gets called from the WaveguideStructure object used in the simulation.

• void set_properties (double, double, double, double)

This function is used during the optimization-operation to update the properties of the space-transformation.

- void set properties (double, double, double, double, double, double)
- void set_properties_force (double, double, double, double)

This function is the same as set_properties with the difference of being able to change the values of the input- and output boundary.

- void set_properties_force (double, double, double, double, double, double)
- double getQ1 (double) const

The values of Q1, Q2 and Q3 are needed to compute the solution in real coordinates from the one in trnsformed coordinates.

double getQ2 (double) const

The values of Q1, Q2 and Q3 are needed to compute the solution in real coordinates from the one in transformed coordinates.

• double getQ3 (double) const

The values of Q1, Q2 and Q3 are needed to compute the solution in real coordinates from the one in transformed coordinates.

unsigned int getLowestDof () const

This function returns the number of the lowest degree of freedom associated with this Sector.

• unsigned int getNDofs () const

This function returns the number of dofs which are part of this sector.

· unsigned int getNInternalBoundaryDofs () const

In order to set appropriate boundary conditions it makes sense to determine, which degrees are associated with an edge which is part of an interface to another sector.

unsigned int getNActiveCells () const

This function can be used to query the number of cells in a Sector / subdomain.

void setLowestDof (unsigned int)

Setter for the value that the getter should return.

void setNDofs (unsigned int)

Setter for the value that the getter should return.

void setNInternalBoundaryDofs (unsigned int)

Setter for the value that the getter should return.

· void setNActiveCells (unsigned int)

Setter for the value that the getter should return.

• double get_dof (unsigned int i, double z) const

This function returns the value of a specified dof at a given internal position.

double get_r (double z) const

Get an interpolation of the radius for a coordinate z.

• double get v (double z) const

Get an interpolation of the tilt for a coordinate z.

double get_m (double z) const

Get an interpolation of the shift for a coordinate z.

Public Attributes

· const bool left

This value describes, if this Sector is at the left (small z) end of the computational domain.

· const bool right

This value describes, if this Sector is at the right (large z) end of the computational domain.

· const bool boundary

This value is true, if either left or right are true.

- const double z_0
- const double z_1

The objects created from this class are supposed to hand back the material properties which include the space-transformation Tensors.

- · unsigned int LowestDof
- · unsigned int NDofs
- · unsigned int NInternalBoundaryDofs
- · unsigned int NActiveCells
- double * dofs_I
- double * dofs_r
- · unsigned int * derivative
- bool * zero_derivative

4.26.1 Detailed Description

```
template < unsigned int Dofs_Per_Sector > class Sector < Dofs_Per_Sector >
```

Sectors are used, to split the computational domain into chunks, whose degrees of freedom are likely coupled.

The interfaces between Sectors lie in the xy-plane and they are ordered by their z-value.

Author

Pascal Kraft

Date

17.12.2015

Definition at line 19 of file Sector.h.

4.26.2 Constructor & Destructor Documentation

4.26.2.1 Sector()

Constructor of the Sector class, that takes all important properties as an input property.

Parameters

in_left	stores if the sector is at the left end. It is used to initialize the according variable.
in_right	stores if the sector is at the right end. It is used to initialize the according variable.
in_z⊷ _0	stores the z-coordinate of the left surface-plain. It is used to initialize the according variable.
in_z⊷ _1	stores the z-coordinate of the right surface-plain. It is used to initialize the according variable.

Definition at line 20 of file Sector.cpp.

```
22
        : left(in_left),
2.3
           right(in_right),
          boundary(in_left && in_right),
24
25
          z_0(in_z_0),
26
           z_1(in_z_1) {
    dofs_1 = new double[Dofs_Per_Sector];
dofs_r = new double[Dofs_Per_Sector];
27
    derivative = new unsigned int[Dofs_Per_Sector];
zero_derivative = new bool[Dofs_Per_Sector];
29
30
     if (Dofs_Per_Sector == 3) {
  zero_derivative[0] = true;
31
        zero_derivative[1] = false;
34
        zero_derivative[2] = true;
        derivative[0] = 0;
derivative[1] = 2;
35
36
        derivative[2] = 0;
37
38
     if (Dofs_Per_Sector == 2) {
40
        zero_derivative[0] = false;
41
        zero_derivative[1] = true;
42
        derivative[0] = 1;
       derivative[1] = 0;
43
44
45
46
    for (unsigned int i = 0; i < Dofs_Per_Sector; i++) {</pre>
       dofs_l[i] = 0;
dofs_r[i] = 0;
47
48
49
     NInternalBoundaryDofs = 0;
50
     LowestDof = 0;
     NActiveCells = 0;
     NDofs = Dofs_Per_Sector;
54 1
```

4.26.3 Member Function Documentation

4.26.3.1 get_dof()

```
template<unsigned int Dofs_Per_Sector> double Sector< Dofs_Per_Sector >::get_dof ( unsigned int i, double z) const
```

This function returns the value of a specified dof at a given internal position.

Parameters

- *i* index of the dof. This class has a template argument specifying the number of dofs per sector. This argument has to be less or equal.
- z this is a relative value for interpolation with $z \in [0,1]$. If z=0 the values for the lower end of the sector are returned. If z=1 the values for the upper end of the sector are returned. In between the values are interpolated according to the rules for the specific dof.

Definition at line 158 of file Sector.cpp.

```
158
      if (i > 0 && i < NDofs) {</pre>
160
        if (z < 0.0) z = 0.0;
161
        if (z > 1.0) z = 1.0;
162
       if (zero_derivative[i]) {
         return InterpolationPolynomialZeroDerivative(z, dofs_l[i], dofs_r[i]);
163
       } else {
164
         return InterpolationPolynomial(z, dofs_l[i], dofs_r[i],
165
166
                                          dofs_l[derivative[i]],
167
                                          dofs_r[derivative[i]]);
168
169
     } else {
170
       std::cout << "There seems to be an error in Sector::get_dof. i > 0 && i < "
171
                     "dofs_per_sector false."
172
                  << std::endl;
173
        return 0;
174 }
175 }
```

4.26.3.2 get_m()

Get an interpolation of the shift for a coordinate z.

Parameters

```
\mbox{\it double} \quad \mbox{\it z is the } z \in [0,1] \mbox{ coordinate for the interpolation}.
```

Definition at line 190 of file Sector.cpp.

```
190
191 if (z < 0.0) z = 0.0;
192 if (z > 1.0) z = 1.0;
```

4.26.3.3 get_r()

```
\label{lem:lemplate} $$ \ensuremath{\sf template}$ \ensuremath{\sf unsigned}$ int Dofs_Per_Sector>$ $$ \ensuremath{\sf double}$ $$ \ensuremath{\sf Sector}$ > ::get_r ($$ \ensuremath{\sf double}$ $z$ ) const $$
```

Get an interpolation of the radius for a coordinate z.

Parameters

Definition at line 178 of file Sector.cpp.

4.26.3.4 get_v()

```
template<unsigned int Dofs_Per_Sector> double Sector< Dofs_Per_Sector >::get_v ( double z ) const
```

Get an interpolation of the tilt for a coordinate z.

Parameters

Definition at line 203 of file Sector.cpp.

```
203
204 if (z < 0.0) z = 0.0;
```

```
205    if (z > 1.0) z = 1.0;
206    if (Dofs_Per_Sector == 2) {
207        return InterpolationPolynomialZeroDerivative(z, dofs_l[1], dofs_r[1]);
208    } else {
209        return InterpolationPolynomialZeroDerivative(z, dofs_l[2], dofs_r[2]);
210    }
211 }
```

4.26.3.5 getLowestDof()

```
template<unsigned int Dofs_Per_Sector>
unsigned int Sector< Dofs_Per_Sector >::getLowestDof ( ) const
```

This function returns the number of the lowest degree of freedom associated with this Sector.

Keep in mind, that the degrees of freedom associated with edges on the lower (small z) interface are not included since this functionality is supposed to help in the block-structure generation and those dofs are part of the neighboring block.

Definition at line 420 of file Sector.cpp.

```
420 {
421 return LowestDof;
422 }
```

4.26.3.6 getNActiveCells()

```
template<unsigned int Dofs_Per_Sector>
unsigned int Sector< Dofs_Per_Sector >::getNActiveCells ( ) const
```

This function can be used to query the number of cells in a Sector / subdomain.

In this case there are no problems with interface-dofs. Every cell belongs to exactly one sector (the problem arises from the fact, that one edge can (and most of the time will) belong to more then one cell).

Definition at line 435 of file Sector.cpp.

```
435 {
436 return NActiveCells;
437 }
```

4.26.3.7 getNDofs()

```
template<unsigned int Dofs_Per_Sector>
unsigned int Sector< Dofs_Per_Sector >::getNDofs ( ) const
```

This function returns the number of dofs which are part of this sector.

The same remarks as for getLowestDof() apply.

Definition at line 425 of file Sector.cpp.

```
425 {
426     return NDofs;
427 }
```

4.26.3.8 getNInternalBoundaryDofs()

```
template<unsigned int Dofs_Per_Sector>
unsigned int Sector< Dofs_Per_Sector >::getNInternalBoundaryDofs ( ) const
```

In order to set appropriate boundary conditions it makes sense to determine, which degrees are associated with an edge which is part of an interface to another sector.

Due to the reordering of dofs this is especially easy since the dofs on the interface are those in the interval

```
[LowestDof + NDofs - NInternalBoundaryDofs, LowestDof + NDofs]
```

Definition at line 430 of file Sector.cpp.

```
430 {
431 return NInternalBoundaryDofs;
432 }
```

4.26.3.9 getQ1()

```
template<unsigned int Dofs_Per_Sector> double Sector< Dofs_Per_Sector >::getQ1 ( double z ) const
```

The values of Q1, Q2 and Q3 are needed to compute the solution in real coordinates from the one in trnsformed coordinates

This function returnes Q1 for a given position and the current transformation.

Definition at line 214 of file Sector.cpp.

```
214
215 return 1 / (dofs_1[0] + z * z * z * (2 * dofs_1[0] - 2 * dofs_r[0]) - 216
217 }

(dofs_1[0] + z * z * z * (2 * dofs_1[0] - 2 * dofs_r[0]));
```

4.26.3.10 getQ2()

```
template<unsigned int Dofs_Per_Sector> double Sector< Dofs_Per_Sector >::getQ2 ( double z ) const
```

The values of Q1, Q2 and Q3 are needed to compute the solution in real coordinates from the one in transformed coordinates.

This function returnes Q2 for a given position and the current transformation.

Definition at line 220 of file Sector.cpp.

4.26.3.11 getQ3()

The values of Q1, Q2 and Q3 are needed to compute the solution in real coordinates from the one in transformed coordinates.

This function returnes Q3 for a given position and the current transformation.

Definition at line 226 of file Sector.cpp.

```
226 {
227 return 0.0;
228 }
```

4.26.3.12 set_properties()

This function is used during the optimization-operation to update the properties of the space-transformation.

However, to ensure, that the boundary-conditions remain intact, this function cannot edit the left defrees of freedom if left is true and it cannot edit the right degrees of freedom if right is true

Definition at line 127 of file Sector.cpp.

Referenced by Sector< 3 >::Sector(), and Sector< 3 >::set_properties().

```
127
128 std::cout << "The code does not work for this number of dofs per Sector."
129 << std::endl;
130 return;
131 }
```

4.26.3.13 setLowestDof()

Setter for the value that the getter should return.

Called after Dof-reordering.

Definition at line 440 of file Sector.cpp.

```
440
441 LowestDof = in_lowestdof;
442 }
```

4.26.3.14 setNActiveCells()

```
template<unsigned int Dofs_Per_Sector> void Sector< Dofs_Per_Sector >::setNActiveCells ( unsigned int in\_nactivecells)
```

Setter for the value that the getter should return.

Called after Dof-reordering.

Definition at line 456 of file Sector.cpp.

```
456
457 NActiveCells = in_nactivecells;
458 }
```

4.26.3.15 setNDofs()

```
template<unsigned int Dofs_Per_Sector>
void Sector< Dofs_Per_Sector >::setNDofs (
          unsigned int in_ndofs)
```

Setter for the value that the getter should return.

Called after Dof-reordering.

Definition at line 445 of file Sector.cpp.

```
445 {
446 NDofs = in_ndofs;
447 }
```

4.26.3.16 setNInternalBoundaryDofs()

Setter for the value that the getter should return.

Called after Dof-reordering.

Definition at line 450 of file Sector.cpp.

```
451 {
452 NInternalBoundaryDofs = in_ninternalboundarydofs;
453 }
```

4.26.3.17 TransformationTensorInternal()

This method gets called from the WaveguideStructure object used in the simulation.

This is where the Waveguide object gets the material Tensors to build the system-matrix. This method returns a complex-values Matrix containing the system-tensors μ^{-1} and ϵ .

Parameters

in⊷	x-coordinate of the point, for which the Tensor should be calculated.
_X	
in⊷	y-coordinate of the point, for which the Tensor should be calculated.
_y	
in⊷	z-coordinate of the point, for which the Tensor should be calculated.
_z	

Definition at line 411 of file Sector.cpp.

Referenced by Sector< 3 >::getQ3().

```
412 {
413 Tensor<2, 3, double> ret;
414 std::cout << "The code does not work for you Sector specification."
415 << Dimension << std::endl;
416 return ret;
417 }
```

4.26.4 Member Data Documentation

4.26.4.1 z_1

```
template<unsigned int Dofs_Per_Sector>
const double Sector< Dofs_Per_Sector >::z_1
```

The objects created from this class are supposed to hand back the material properties which include the space-transformation Tensors.

For this to be possible, the Sector has to be able to transform from global coordinates to coordinates that are scaled inside the Sector. For this purpose, the z_0 and z_1 variables store the z-coordinate of both, the left and right surface.

Definition at line 60 of file Sector.h.

The documentation for this class was generated from the following files:

- · Code/Core/Sector.h
- · Code/Core/Sector.cpp

4.27 ShapeDescription Class Reference

Public Member Functions

void SetByString (std::string)

Public Attributes

- · int Sectors
- std::vector< double > m
- std::vector < double > v
- std::vector < double > z

4.27.1 Detailed Description

Definition at line 14 of file ShapeDescription.h.

The documentation for this class was generated from the following files:

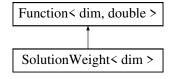
- · Code/Helpers/ShapeDescription.h
- · Code/Helpers/ShapeDescription.cpp

4.28 SolutionWeight < dim > Class Template Reference

This function has internal usage to execute a function only on the interior of the Waveguide.

```
#include <SolutionWeight.h>
```

Inheritance diagram for SolutionWeight < dim >:



Public Member Functions

· SolutionWeight ()

The whole class contains no specific data.

virtual double value (const Point < dim > &p, const unsigned int component) const

This function returns 1, if the given component is inside the Waveguide and 0 otherwise.

virtual void vector value (const Point< dim > &p, Vector< double > &value) const

This function gets called by the framework and calls value(const Point<dim> &p, const unsigned int component) for all components and stores the results in value.

4.28.1 Detailed Description

```
template<int dim> class SolutionWeight< dim>
```

This function has internal usage to execute a function only on the interior of the Waveguide.

SolutionWeight is a class, that has been derived from the class Function and which can be used to generate handles to functions, that return specific values. The pattern of passing object built from classes derived from Function is a commonly used one in Deal.II. This function offers a weight for locations inside the waveguide. In order to integrate or calculate the L2-norm inside the Waveguide, this is needed. The value of the function to be used is multiplied with this weighing-function which returns 1 for any point inside the Waveguide and 0 outside of it. Mathematically, this function can be represented by

$$f: \mathbb{R}^{dim} o \{1,0\}, \ oldsymbol{x} \mapsto egin{cases} 1 & ext{for } oldsymbol{x} \in \Omega_W \ 0 & ext{else} \end{cases}$$

, where Ω_W is the set of all points contained in the Waveguide.

Definition at line 40 of file SolutionWeight.h.

4.28.2 Constructor & Destructor Documentation

4.28.2.1 SolutionWeight()

```
template<int dim>
SolutionWeight< dim >::SolutionWeight ( )
```

The whole class contains no specific data.

The only information it needs stem from the Parameters object parsed from the input file. This object gets initialized inside this constructor.

Definition at line 29 of file SolutionWeight.cpp.

```
29 : Function<dim>(6) {}
```

4.28.3 Member Function Documentation

4.28.3.1 value()

This function returns 1, if the given component is inside the Waveguide and 0 otherwise.

Since this method is intended also for vector-valued functions, this method also has to account for a component of the result which for scalar functions is 0.

Parameters

р	This is the location in which the test should be executed.
component	Determines which component is to be evaluated. In this case that information does not have any
	further meaning.

Definition at line 8 of file SolutionWeight.cpp.

4.28.3.2 vector_value()

This function gets called by the framework and calls value(const Point<dim> &p, const unsigned int component) for all components and stores the results in value.

Parameters

р	The location is given here and gets passed along to the individual value-calls.
value	This is a vector which returns the results in place. It is a reference that is edited in value(const
	Point <dim> &p, const unsigned int component).</dim>

Definition at line 22 of file SolutionWeight.cpp.

The documentation for this class was generated from the following files:

- · Code/Core/SolutionWeight.h
- · Code/Core/SolutionWeight.cpp

4.29 SpaceTransformation Class Reference

The SpaceTransformation class encapsulates the coordinate transformation used in the simulation.

```
#include <SpaceTransformation.h>
```

Inheritance diagram for SpaceTransformation:



Public Member Functions

- SpaceTransformation (int, int)
- virtual Point< 3 > math_to_phys (Point< 3 > coord) const =0
- virtual Point< 3 > phys_to_math (Point< 3 > coord) const =0
- bool is_identity (Point< 3 > coord) const
- virtual Tensor < 2, 3, std::complex < double > > get_Tensor (Point < 3 > &coordinate) const =0
- virtual Tensor< 2, 3, std::complex< double >> **get_Preconditioner_Tensor** (Point< 3 > &coordinate, int block) const =0
- virtual Tensor < 2, 3, double > get_Space_Transformation_Tensor (Point < 3 > &coordinate) const =0
- virtual Tensor< 2, 3, double > get_Space_Transformation_Tensor_Homogenized (Point< 3 > &coordinate) const =0
- virtual Tensor < 2, 3, std::complex < double >> **Apply_PML_To_Tensor** (Point < 3 > &coordinate, Tensor < 2, 3, double > Tensor input) const =0
- virtual Tensor< 2, 3, std::complex< double > > Apply_PML_To_Tensor_For_Preconditioner (Point< 3 > &coordinate, Tensor< 2, 3, double > Tensor_input, int block) const =0
- virtual Tensor< 2, 3, std::complex< double >> get_Tensor_for_step (Point< 3 > &coordinate, unsigned int dof, double step_width)
- virtual bool PML_in_X (Point< 3 > &position) const =0

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the x-axis.

virtual bool PML_in_Y (Point< 3 > &position) const =0

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the y-axis.

virtual bool PML_in_Z (Point< 3 > &position) const =0

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the z-axis.

virtual double Preconditioner_PML_Z_Distance (Point < 3 > &p, unsigned int block) const =0

This function fulfills the same purpose as those with similar names but it is supposed to be used together with Preconditioner_PML_in_Z instead of the versions without "Preconditioner".

virtual double PML X Distance (Point < 3 > &position) const =0

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

virtual double PML Y Distance (Point < 3 > &position) const =0

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

virtual double PML Z Distance (Point < 3 > &position) const =0

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

virtual void estimate and initialize ()=0

At the beginning (before the first solution of a system) only the boundary conditions for the shape of the waveguide are known.

virtual double get_Q1 (double z) const =0

This member calculates the value of Q1 for a provided z-coordinate.

virtual double get_Q2 (double z) const =0

This member calculates the value of Q2 for a provided *z*-coordinate.

• virtual double get_Q3 (double z) const =0

This member calculates the value of Q3 for a provided z-coordinate.

• virtual double get_dof (int dof) const =0

This is a getter for the values of degrees of freedom.

virtual void set_dof (int dof, double value)=0

This function sets the value of the dof provided to the given value.

- virtual std::pair< double, double > dof_support (unsigned int index) const
- bool point_in_dof_support (Point< 3 > location, unsigned int dof_index) const
- virtual double get_free_dof (int dof) const =0

This is a getter for the values of degrees of freedom.

virtual void set_free_dof (int dof, double value)=0

This function sets the value of the dof provided to the given value.

- std::pair< int, double > Z_to_Sector_and_local_z (double in_z) const

Using this method unifies the usage of coordinates.

double Sector_Length () const

Returns the length of one sector.

• virtual double get_r (double in_z) const =0

Returns the radius for a system-coordinate;.

virtual double get_m (double in_z) const =0

 ${\it Returns\ the\ shift\ for\ a\ system-coordinate;}.$

virtual double get_v (double in_z) const =0

Returns the tilt for a system-coordinate;.

int Z_to_Layer (double) const

This Method writes a comprehensive description of the current structure to the console.

virtual Vector< double > Dofs () const =0

Other objects can use this function to retrieve an array of the current values of the degrees of freedom of the functional we are optimizing.

virtual unsigned int NFreeDofs () const =0

This function returns the number of unrestrained degrees of freedom of the current optimization run.

virtual unsigned int NDofs () const =0

This function returns the total number of DOFs including restrained ones.

• virtual bool IsDofFree (int) const =0

Since Dofs() also returns restrained degrees of freedom, this function can be applied to determine if a degree of freedom is indeed free or restrained.

• virtual void Print () const =0

Console output of the current Waveguide Structure.

virtual std::complex< double > evaluate_for_z (double, Waveguide *)=0

Since the Wavegudie itself may be circular or rectangular now, the evaluation routines should be moved to a point in the code where this information is included in the code.

- std::complex< double > evaluate_for_z_with_sum (double, double, Waveguide *)
- std::complex< double > gauss_product_2D_sphere (double z, int n, double R, double Xc, double Yc, Waveguide *in_w)

Public Attributes

- bool homogenized = false
- · const unsigned int dofs_per_layer
- · const unsigned int boundary dofs in
- const unsigned int boundary_dofs_out
- · const double epsilon_K

The material-property ϵ_r has a different value inside and outside of the waveguides core.

· const double epsilon_M

The material-property ϵ_r has a different value inside and outside of the waveguides core.

· const int sectors

Since the computational domain is split into subdomains (called sectors), it is important to keep track of the amount of subdomains.

· const double deltaY

This value is initialized with the value Delta from the input-file.

Vector< double > InitialDofs

This vector of values saves the initial configuration.

· double InitialQuality

This vector of values saves the initial configuration.

const int rank

4.29.1 Detailed Description

The SpaceTransformation class encapsulates the coordinate transformation used in the simulation.

Two important decisions have to be made in the computation: Which shape should be used for the waveguide? This can either be rectangular or tubular. Should the coordinate-transformation always be equal to identity in any domain where PML is applied? (yes or no). However, the space transformation is the only information required to compute the Tensor g which is a 3x3 matrix whilch (multiplied by the material value of the untransformed coordinate either inside or outside the waveguide) gives us the value of ϵ and μ . From this class we derive several different classes which then specify the interface specified in this class.

Author

Pascal Kraft

Date

17.12.2015

Definition at line 29 of file SpaceTransformation.h.

4.29.2 Member Function Documentation

4.29.2.1 Dofs()

```
virtual Vector<double> SpaceTransformation::Dofs ( ) const [pure virtual]
```

Other objects can use this function to retrieve an array of the current values of the degrees of freedom of the functional we are optimizing.

This also includes restrained degrees of freedom and other functions can be used to determine this property. This has to be done because in different cases the number of restrained degrees of freedom can vary and we want no logic about this in other functions.

Implemented in DualProblemTransformationWrapper, InhomogenousTransformationCircular, Homogenous ← TransformationCircular, HomogenousTransformationRectangular, and InhomogenousTransformationRectangular.

Referenced by DualProblemTransformationWrapper::Dofs().

4.29.2.2 estimate_and_initialize()

```
virtual void SpaceTransformation::estimate_and_initialize ( ) [pure virtual]
```

At the beginning (before the first solution of a system) only the boundary conditions for the shape of the waveguide are known.

Therefore the values for the degrees of freedom need to be estimated. This function sets all variables to appropriate values and estimates an appropriate shape based on averages and a polynomial interpolation of the boundary conditions on the shape.

Implemented in DualProblemTransformationWrapper, HomogenousTransformationCircular, Homogenous ← TransformationRectangular, InhomogenousTransformationCircular, and InhomogenousTransformationRectangular.

Referenced by DualProblemTransformationWrapper::estimate and initialize().

4.29.2.3 evaluate for z()

Since the Wavegudie itself may be circular or rectangular now, the evaluation routines should be moved to a point in the code where this information is included in the code.

Since I dont want to create derived classes from waveguide (which I should do eventually) I will for now include this functionality into the space transformation which is shape-sensitive. The waveguide only offers the evaluation at a point. The quadrature-rule has to be imposed by the space transformation.

Implemented in DualProblemTransformationWrapper, InhomogenousTransformationCircular, Homogenous ← TransformationCircular, HomogenousTransformationRectangular, and InhomogenousTransformationRectangular.

Referenced by DualProblemTransformationWrapper::evaluate_for_z().

4.29.2.4 get_dof()

This is a getter for the values of degrees of freedom.

A getter-setter interface was introduced since the values are estimated automatically during the optimization and non-physical systems should be excluded from the domain of possible cases.

Parameters

dof The index of the degree of freedom to be retrieved from the structure of the modelled waveguide.

Returns

This function returns the value of the requested degree of freedom. Should this dof not exist, 0 will be returned.

Implemented in DualProblemTransformationWrapper, HomogenousTransformationCircular, Homogenous TransformationRectangular, InhomogenousTransformationCircular, and InhomogenousTransformationRectangular.

Referenced by DualProblemTransformationWrapper::get dof(), and Z to Layer().

4.29.2.5 get_free_dof()

This is a getter for the values of degrees of freedom.

A getter-setter interface was introduced since the values are estimated automatically during the optimization and non-physical systems should be excluded from the domain of possible cases.

Parameters

dof The index of the degree of freedom to be retrieved from the structure of the modelled waveguide.

Returns

This function returns the value of the requested degree of freedom. Should this dof not exist, 0 will be returnd.

Implemented in DualProblemTransformationWrapper, HomogenousTransformationCircular, Homogenous TransformationRectangular, InhomogenousTransformationCircular, and InhomogenousTransformationRectangular.

Referenced by DualProblemTransformationWrapper::get_free_dof().

4.29.2.6 get_Q1()

```
virtual double SpaceTransformation::get_Q1 ( double z ) const [pure virtual]
```

This member calculates the value of Q1 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q1 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implemented in DualProblemTransformationWrapper, HomogenousTransformationCircular, Homogenous TransformationRectangular, InhomogenousTransformationCircular, and InhomogenousTransformationRectangular.

Referenced by DualProblemTransformationWrapper::get_Q1().

```
4.29.2.7 get_Q2()
```

```
virtual double SpaceTransformation::get_Q2 ( double z ) const [pure virtual]
```

This member calculates the value of Q2 for a provided *z*-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q2 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

Implemented in DualProblemTransformationWrapper, HomogenousTransformationCircular, Homogenous TransformationRectangular, InhomogenousTransformationCircular, and InhomogenousTransformationRectangular.

Referenced by DualProblemTransformationWrapper::get_Q2().

```
4.29.2.8 get_Q3()
```

```
virtual double SpaceTransformation::get_Q3 ( double z ) const [pure virtual]
```

This member calculates the value of Q3 for a provided z-coordinate.

This value is used in the transformation of the solution-vector in transformed coordinates (solution of the system-matrix) to real coordinates (physical field).

Parameters

z The value of Q3 is independent of x and y. Therefore only a z-coordinate is provided in a call to the function.

 $\label{thm:local_problem} \begin{tabular}{ll} Implemented in Dual Problem Transformation Wrapper, Homogenous Transformation Circular, Homogenous Transformation Circular, and Inhomogenous Transformation Rectangular. \\ \begin{tabular}{ll} Inhomogenous Transformation Circular, and Inhomogenous Transformation Rectangular. \\ \begin{tabular}{ll} Inhomogenous Transformation Circular, and Inhomogenous Transformation Rectangular. \\ \begin{tabular}{ll} Inhomogenous Transformation Circular, and Inhomogenous Circular, and Inho$

Referenced by DualProblemTransformationWrapper::get Q3().

4.29.2.9 IsDofFree()

Since Dofs() also returns restrained degrees of freedom, this function can be applied to determine if a degree of freedom is indeed free or restrained.

"restrained" means that for example the DOF represents the radius at one of the connectors (input or output) and therefore we forbid the optimization scheme to vary this value.

Implemented in DualProblemTransformationWrapper, InhomogenousTransformationCircular, HomogenousCransformationRectangular, and InhomogenousTransformationRectangular.

Referenced by DualProblemTransformationWrapper::lsDofFree(), and Waveguide::run().

4.29.2.10 NDofs()

```
virtual unsigned int SpaceTransformation::NDofs ( ) const [pure virtual]
```

This function returns the total number of DOFs including restrained ones.

This is the lenght of the array returned by Dofs().

Implemented in DualProblemTransformationWrapper, InhomogenousTransformationCircular, Homogenous ← TransformationCircular, HomogenousTransformationRectangular, and InhomogenousTransformationRectangular.

Referenced by DualProblemTransformationWrapper::NDofs(), and Waveguide::run().

4.29.2.11 PML_in_X()

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the x-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

position	Stores the position in which to test for presence of a PML-Material.

Implemented in DualProblemTransformationWrapper, HomogenousTransformationCircular, HomogenousCransformationRectangular, InhomogenousTransformationCircular, and InhomogenousTransformationRectangular.

 $Referenced\ by\ Dual Problem Transformation Wrapper:: PML_in_X().$

4.29.2.12 PML_in_Y()

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the y-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

position	Stores the position in which to test for presence of a PML-Material.
----------	--

Implemented in DualProblemTransformationWrapper, HomogenousTransformationCircular, Homogenous TransformationRectangular, InhomogenousTransformationCircular, and InhomogenousTransformationRectangular.

Referenced by DualProblemTransformationWrapper::PML_in_Y().

4.29.2.13 PML_in_Z()

This function is used to determine, if a system-coordinate belongs to a PML-region for the PML that limits the computational domain along the z-axis.

Since there are 3 blocks of PML-type material, there are 3 functions.

Parameters

Stores the position in which to test for presence of	of a PML-Material.
--	--------------------

Implemented in DualProblemTransformationWrapper, HomogenousTransformationCircular, Homogenous TransformationRectangular, InhomogenousTransformationCircular, and InhomogenousTransformationRectangular.

Referenced by DualProblemTransformationWrapper::PML_in_Z().

4.29.2.14 PML_X_Distance()

```
virtual double SpaceTransformation::PML_X_Distance ( Point < 3 \, > \, \& \, position \, ) \, const \, \, [pure \, virtual]
```

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

position	Stores the position from which to calculate the distance to the PML-surface.
----------	--

Implemented in DualProblemTransformationWrapper, HomogenousTransformationCircular, Homogenous TransformationRectangular, InhomogenousTransformationCircular, and InhomogenousTransformationRectangular.

Referenced by DualProblemTransformationWrapper::PML_X_Distance().

4.29.2.15 PML_Y_Distance()

```
virtual double SpaceTransformation::PML_Y_Distance ( Point < 3 > \& position \ ) \ const \ [pure virtual]
```

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

|--|

Implemented in DualProblemTransformationWrapper, HomogenousTransformationCircular, Homogenous ← TransformationRectangular, InhomogenousTransformationCircular, and InhomogenousTransformationRectangular.

Referenced by DualProblemTransformationWrapper::PML Y Distance().

4.29.2.16 PML_Z_Distance()

```
virtual double SpaceTransformation::PML_Z_Distance ( Point < 3 \, > \, \& \, position \, ) \, const \, \, [pure \, virtual]
```

This function calculates for a given point, its distance to a PML-boundary limiting the computational domain.

This function is used merely to make code more readable. There is a function for every one of the dimensions since the normal vectors of PML-regions in this implementation are the coordinate-axis. This value is set to zero outside the PML and positive inside both PML-domains (only one for the z-direction).

Parameters

position Stores the position from which to calculate the distance to the PML-surface.	position	Stores the position from which to calculate the distance to the PML-surface.
---	----------	--

 $Implemented \quad in \quad Dual Problem Transformation Wrapper, \quad Homogenous Transformation Circular, \quad Homogenous Transformation Circular, \quad and \quad Inhomogenous Transformation Rectangular.$

Referenced by DualProblemTransformationWrapper::PML_Z_Distance().

4.29.2.17 set_dof()

This function sets the value of the dof provided to the given value.

It is important to consider, that some dofs are non-writable (i.e. the values of the degrees of freedom on the boundary, like the radius of the input-connector cannot be changed).

Parameters

dof	The index of the parameter to be changed.
value	The value, the dof should be set to.

Implemented in DualProblemTransformationWrapper, HomogenousTransformationCircular, Homogenous TransformationRectangular, InhomogenousTransformationCircular, and InhomogenousTransformationRectangular.

Referenced by DualProblemTransformationWrapper::set_dof(), and Z_to_Layer().

4.29.2.18 set_free_dof()

This function sets the value of the dof provided to the given value.

It is important to consider, that some dofs are non-writable (i.e. the values of the degrees of freedom on the boundary, like the radius of the input-connector cannot be changed).

Parameters

dof	The index of the parameter to be changed.
value	The value, the dof should be set to.

Implemented in DualProblemTransformationWrapper, HomogenousTransformationCircular, Homogenous TransformationRectangular, InhomogenousTransformationCircular, and InhomogenousTransformationRectangular.

Referenced by DualProblemTransformationWrapper::set_free_dof().

4.29.2.19 Z_to_Sector_and_local_z()

```
std::pair< int, double > SpaceTransformation::Z_{to}Sector_and_local_z ( double in_z ) const
```

Using this method unifies the usage of coordinates.

This function takes a global z coordinate (in the computational domain) and returns both a Sector-Index and an internal z coordinate indicating which sector this coordinate belongs to and how far along in the sector it is located.

Parameters

```
|| double || in_z global system z coordinate for the transformation.
```

Definition at line 13 of file SpaceTransformation.cpp.

References deltaY, epsilon_K, epsilon_M, InitialQuality, and sectors.

Referenced by InhomogenousTransformationRectangular::get_m(), HomogenousTransformationRectangular::get \leftarrow ::get_m(), InhomogenousTransformationRectangular::get_ \leftarrow _Q1(), HomogenousTransformationRectangular::get_Q1(), InhomogenousTransformationCircular::get_Q1(), InhomogenousTransformationRectangular::get_Q2(), HomogenousTransformationRectangular::get_Q2(), InhomogenousTransformationRectangular::get_Q2(), HomogenousTransformationRectangular::get_Q3(), HomogenousTransformationCircular::get_Q3(), InhomogenousTransformationCircular::get_Q3(), InhomogenousTransformationCircular::get_Q3(), InhomogenousTransformationCircular::get_Q3(), InhomogenousTransformationRectangular::get_V(), InhomogenousTransformationRectangular::get_V(), InhomogenousTransformationRectangular::NDofs(), InhomogenousCircular::PML_Z_Distance(), and DualProblemTransformationWrapper::Z to Sector and local z().

```
std::pair<int, double> ret;
15
     ret.first = 0;
     ret.second = 0.0:
17
18
    if (in_z <= -GlobalParams.M_R_ZLength / 2.0) {</pre>
       ret.first = 0;
19
      ret.second = 0.0;
            if (abs(in_z) < GlobalParams.M_R_ZLength / 2.0) {</pre>
      ret.first = floor((in_z + GlobalParams.M_R_ZLength / 2.0) /
23
                         (GlobalParams.SectorThickness));
      ret.second = (in_z + GlobalParams.M_R_ZLength / 2.0
2.4
2.5
                     (ret.first * GlobalParams.SectorThickness)) /
                     (GlobalParams.SectorThickness);
26
    } else if (in_z >= GlobalParams.M_R_ZLength / 2.0) {
28
       ret.first = sectors - 1;
29
       ret.second = 1.0;
30
31
     return ret;
```

4.29.3 Member Data Documentation

4.29.3.1 epsilon_K

```
const double SpaceTransformation::epsilon_K
```

The material-property ϵ_r has a different value inside and outside of the waveguides core.

This variable stores its value inside the core.

Definition at line 143 of file SpaceTransformation.h.

Referenced by Z to Sector and local z().

4.29.3.2 epsilon_M

```
const double SpaceTransformation::epsilon_M
```

The material-property ϵ_r has a different value inside and outside of the waveguides core.

This variable stores its value outside the core.

Definition at line 149 of file SpaceTransformation.h.

Referenced by Z_to_Sector_and_local_z().

4.29.3.3 sectors

```
const int SpaceTransformation::sectors
```

Since the computational domain is split into subdomains (called sectors), it is important to keep track of the amount of subdomains.

This member stores the number of Sectors the computational domain has been split into.

Definition at line 155 of file SpaceTransformation.h.

Referenced by Z_to_Sector_and_local_z().

The documentation for this class was generated from the following files:

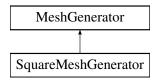
- · Code/SpaceTransformations/SpaceTransformation.h
- Code/SpaceTransformations/SpaceTransformation.cpp

4.30 SquareMeshGenerator Class Reference

This class generates meshes, that are used to discretize a rectangular Waveguide.

```
#include <SquareMeshGenerator.h>
```

Inheritance diagram for SquareMeshGenerator:



Public Member Functions

- SquareMeshGenerator (SpaceTransformation *st)
- void refine global (parallel::distributed::Triangulation < 3 > *in tria, unsigned int times)

This function is intended to execute a global refinement of the mesh.

void refine_internal (parallel::distributed::Triangulation < 3 > *in_tria, unsigned int times)

This function is intended to execute an internal refinement of the mesh.

void refine_proximity (parallel::distributed::Triangulation < 3 > *in_tria, unsigned int times, double factor)

This function is intended to execute a refinement inside and near the waveguide boundary.

• bool math_coordinate_in_waveguide (Point< 3 > position) const

This function checks if the given coordinate is inside the waveguide or not.

bool phys_coordinate_in_waveguide (Point< 3 > position) const

This function checks if the given coordinate is inside the waveguide or not.

void prepare_triangulation (parallel::distributed::Triangulation < 3 > *in_tria)

This function takes a triangulation object and prepares it for the further computations.

• void **set_boundary_ids** (parallel::distributed::Triangulation< 3 > &tria) const

Public Attributes

- parallel::distributed::Triangulation< 3 >::active_cell_iterator cell
- parallel::distributed::Triangulation < 3 >::active cell iterator endc

4.30.1 Detailed Description

This class generates meshes, that are used to discretize a rectangular Waveguide.

It is derived from MeshGenerator.

The original intention of this project was to model tubular (or cylindrical) waveguides. The motivation behind this thought was the fact, that for this case the modes are known analytically. In applications however modes can be computed numerically and other shapes are easier to fabricate. For example square or rectangular waveguides can be printed in 3D on the scales we currently compute while tubular waveguides on that scale are not yet feasible.

Author

Pascal Kraft

Date

28.11.2016

Definition at line 24 of file SquareMeshGenerator.h.

4.30.2 Member Function Documentation

4.30.2.1 math_coordinate_in_waveguide()

This function checks if the given coordinate is inside the waveguide or not.

The naming convention of physical and mathematical system find application. In this version, the waveguide has been transformed and the check for a tubal waveguide for example only checks if the radius of a given vector is below the average of input and output radius. position This value gives us the location to check for.

Implements MeshGenerator.

Definition at line 191 of file SquareMeshGenerator.cpp.

```
192
193 return std::abs(in_position[0]) <
194 (GlobalParams.M_C_DimlIn + GlobalParams.M_C_DimlOut) / 2.0 &&
195 std::abs(in_position[1]) <
196 (GlobalParams.M_C_Dim2In + GlobalParams.M_C_Dim2Out) / 2.0;
197 }
```

4.30.2.2 phys_coordinate_in_waveguide()

This function checks if the given coordinate is inside the waveguide or not.

The naming convention of physical and mathematical system find application. In this version, the waveguide is bent. If we are using a space transformation f then this function is equal to math_coordinate_in_waveguide(f(x,y,z)). position This value gives us the location to check for.

Implements MeshGenerator.

Definition at line 199 of file SquareMeshGenerator.cpp.

References SpaceTransformation::get_m(), and SpaceTransformation::get_r().

```
200
201
      std::cout
      << "NOT IMPLEMENTED: SquareMeshGenerator::phys_coordinate_in_waveguide"</pre>
202
          << std::endl;
203
     Point<3, double> temp = in position;
204
     temp[1] -= ct->get_m(in_position[2]);
     double r = ct->get_r(in_position[2]);
207
     return (abs(temp[0]) < r && abs(temp[1]) < r);</pre>
208
     return false;
209 }
```

4.30.2.3 prepare_triangulation()

This function takes a triangulation object and prepares it for the further computations.

It is intended to encapsulate all related work and is explicitely not const.

Parameters

in tria

The triangulation that is supposed to be prepared. All further information is derived from the parameter file and not given by parameters.

Implements MeshGenerator.

Definition at line 93 of file SquareMeshGenerator.cpp.

References RoundMeshGenerator::set boundary ids().

```
94
     deallog.push("SquareMeshGenerator:prepare_triangulation");
deallog << "Starting Mesh preparation" << std::endl;</pre>
95
96
     const std_cxx11::array<Tensor<1, 3>, 3> edges2(edges);
100
      GridGenerator::subdivided_parallelepiped<3, 3>(*in_tria, origin, edges2, subs,
101
102
103
      in_tria->repartition();
104
105
      in_tria->signals.post_refinement.connect(
106
          std_cxx11::bind(&SquareMeshGenerator::set_boundary_ids,
107
                           std_cxx11::cref(*this), std_cxx11::ref(*in_tria)));
108
109
      in tria->refine global(3);
110
      GridTools::transform(&Triangulation_Stretch_Computational_Rectangle,
112
                             *in_tria);
113
      parallel::distributed::Triangulation<3>::active_cell_iterator
114
115
          cell = in_tria->begin_active(),
116
          endc = in_tria->end();
117
119
     double len = 2.0 / Layers;
120
      cell = in_tria->begin_active();
121
122
      for (; cell != endc; ++cell) {
123
        int temp = (int)std::floor((cell->center()[2] + 1.0) / len);
124
        if (temp >= (int)Layers || temp < 0)</pre>
          125
126
127
                     << std::endl;
128
     }
129
      if (GlobalParams.R_Global > 0) {
130
131
       in_tria->refine_global(GlobalParams.R_Global);
132
133
134
      double MaxDistX =
135
          (GlobalParams.M_C_DimlOut + GlobalParams.M_C_DimlIn) * 1.4 / 2.0;
136
      double MaxDistY =
          (GlobalParams.M_C_Dim2Out + GlobalParams.M_C_Dim2In) * 1.4 / 2.0;
138
      for (int i = 0; i < GlobalParams.R_Local; i++) {</pre>
139
        cell = in_tria->begin_active();
140
        for (; cell != endc; ++cell) {
         if (std::abs(cell->center()[0]) < MaxDistX &&</pre>
141
142
              std::abs(cell->center()[1]) < MaxDistY) {</pre>
143
            cell->set_refine_flag();
144
          }
145
        in_tria->execute_coarsening_and_refinement();
146
        MaxDistX = (GlobalParams.M_C_DimlOut + GlobalParams.M_C_DimlIn) * 1.4 / 2.0;
MaxDistY = (GlobalParams.M_C_Dim2Out + GlobalParams.M_C_Dim2In) * 1.4 / 2.0;
147
148
149
150
151
      for (int i = 0; i < GlobalParams.R_Interior; i++) {</pre>
        cell = in_tria->begin_active();
152
153
        for (; cell != endc; ++cell) {
154
          if (std::abs(cell->center()[0]) <</pre>
155
                   (GlobalParams.M_C_Dim1In + GlobalParams.M_C_Dim1Out) / 2.0 &&
156
               std::abs(cell->center()[1]) <</pre>
157
                   (GlobalParams.M_C_Dim2In + GlobalParams.M_C_Dim2Out) / 2.0) {
158
            cell->set_refine_flag();
159
          }
160
        in_tria->execute_coarsening_and_refinement();
161
```

```
162
       }
163
164
       GridTools::transform(&Triangulation_Stretch_Z, *in_tria);
165
166
       GridTools::transform(&Triangulation_Shift_Z, *in_tria);
167
       z_{min} = 10000000.0;
168
169
       z_{max} = -10000000.0;
170
       cell = in_tria->begin_active();
171
       endc = in_tria->end();
172
       for (; cell != endc; ++cell) {
173
        if (cell->is_locally_owned()) {
   for (int face = 0; face < 6; face++) {</pre>
174
175
              z_min = std::min(z_min, cell->face(face)->center()[2]);
z_max = std::max(z_max, cell->face(face)->center()[2]);
176
177
178
            }
         }
179
180
181
       cell = in_tria->begin_active();
endc = in_tria->end();
182
183
184
       set_boundary_ids(*in_tria);
185
186
187
      deallog << "Done" << std::endl;
188
      deallog.pop();
189 }
```

4.30.2.4 refine global()

This function is intended to execute a global refinement of the mesh.

This means that every cell will be refined in every direction (effectively multiplying the number of DOFs by 8). This version is the most expensive refinement possible and should be used with caution.

Parameters

times

Number of refinement steps to be performed (gives us a multiplication of the number of degrees of freedom by 8^{times} .

Implements MeshGenerator.

Definition at line 211 of file SquareMeshGenerator.cpp.

```
212
213 in_tria->refine_global(times);
214 }
```

4.30.2.5 refine_internal()

```
void SquareMeshGenerator::refine_internal ( parallel::distributed::Triangulation<~3~>*~in\_tria, unsigned~int~times~)~[virtual]
```

This function is intended to execute an internal refinement of the mesh.

This means that every cell inside the waveguide will be refined in every direction. This method is rather cheap and only refines where the field is strong, however, the mesh outside the waveguide should not be too coarse to reduce numerical errors.

Parameters

times Number of refinement steps to be performed.

Implements MeshGenerator.

Definition at line 234 of file SquareMeshGenerator.cpp.

References RoundMeshGenerator::math coordinate in waveguide().

```
for (unsigned int i = 0; i < times; i++) {
    cell = in_tria->begin_active();
    for (; cell != endc; ++cell) {
        if (math_coordinate_in_waveguide(cell->center())) {
            cell->set_refine_flag();
        }
        in_tria->execute_coarsening_and_refinement();
    }
}
```

4.30.2.6 refine_proximity()

This function is intended to execute a refinement inside and near the waveguide boundary.

Parameters

times Number of refinement steps to be performed.

Implements MeshGenerator.

Definition at line 216 of file SquareMeshGenerator.cpp.

```
218
       double X = (GlobalParams.M_C_Dim1Out + GlobalParams.M_C_Dim1In) *
219
       (1.0 + factor) / 2.0;
double Y = (GlobalParams.M_C_Dim2Out + GlobalParams.M_C_Dim2In) *
220
221
       (1.0 + factor) / 2.0;
for (unsigned int i = 0; i < times; i++) {
222
223
224
         cell = in_tria->begin_active();
         for (; cell != endc; ++cell) {
   if (std::abs(cell->center()[0]) < X && std::abs(cell->center()[1]) < Y) {</pre>
225
226
227
              cell->set_refine_flag();
228
         }
```

The documentation for this class was generated from the following files:

- · Code/MeshGenerators/SquareMeshGenerator.h
- Code/MeshGenerators/SquareMeshGenerator.cpp

4.31 tagGSPHERE Struct Reference

Public Attributes

- int **n**
- double * r
- double * t
- double * q
- double * A
- double B

4.31.1 Detailed Description

Definition at line 23796 of file QuadratureFormulaCircle.cpp.

The documentation for this struct was generated from the following file:

• Code/Helpers/QuadratureFormulaCircle.cpp

4.32 Waveguide Class Reference

This class encapsulates all important mechanism for solving a FEM problem.

```
#include <Waveguide.h>
```

Public Member Functions

Waveguide (MPI_Comm in_mpi_comm, MeshGenerator *in_mg, SpaceTransformation *in_st)

This is the constructor that should be used to initialize objects of this type.

• void run ()

This method as well as the rerun() method, are used by the optimization-algorithm to use and reuse the Waveguideobject.

void assemble part ()

The assemble_part function is a part of the assemble_system() functionality.

• std::complex< double > evaluate for Position (double x, double y, double z)

To compute the output quality of the signal and it's transmition along the waveguid-axis, this function performs a comparison of the fundamental mode of a waveguide and the actual situation.

• double evaluate_for_z (double)

To compute the output quality of the signal and it's transmition along the waveguid-axis, this function performs a comparison of the fundamental mode of a waveguide and the actual situation.

· void evaluate ()

This function has the purpose of filling the qualities array in every process with the appropriate Values from the other ones.

· void store ()

The storage has the following purpose: Regarding the optimization-process there are two kinds of runs.

• void estimate solution ()

This function is currently not in use.

- std::vector< std::complex< double >> assemble_adjoint_local_contribution (double stepwidth)
- void switch_to_primal (SpaceTransformation *primal_st)
- void switch_to_dual (SpaceTransformation *dual_st)
- Point< 3, double > transform_coordinate (const Point< 3, double >)

Public Attributes

- double * qualities
- MeshGenerator * mg

4.32.1 Detailed Description

This class encapsulates all important mechanism for solving a FEM problem.

In earlier versions this also included space transformation and computation of materials. Now it only includes FEM essentials and solving the system matrix.

Upon initialization it requires structural information about the waveguide that will be simulated. The object then continues to initialize the FEM-framework. After allocating space for all objects, the assemblation-process of the system-matrix begins. Following this step, the user-selected preconditioner and solver are used to solve the system and generate outputs. This class is the core piece of the implementation.

Author

Pascal Kraft

Date

03.07.2016

Definition at line 102 of file Waveguide.h.

4.32.2 Constructor & Destructor Documentation

4.32.2.1 Waveguide()

This is the constructor that should be used to initialize objects of this type.

Parameters

param	This is a reference to a parsed form of the input-file.
structure	This parameter gives a reference to the structure of the real Waveguide. This is necessary since during matrix-assembly it is required to call a function which generates the transformation tensor
	which is purely structure-dependent.

Definition at line 44 of file Waveguide.cpp.

```
: fe(FE_Nedelec<3>(GlobalParams.So_ElementOrder), 2),
46
          triangulation(in_mpi_comm,
48
                         parallel::distributed::Triangulation<3>::MeshSmoothing(
49
                              parallel::distributed::Triangulation<3>::none),
50
                          parallel::distributed::Triangulation<</pre>
51
                              3>::Settings::no_automatic_repartitioning),
          even(Utilities::MPI::this_mpi_process(in_mpi_comm) % 2 == 0),
52
53
          rank(Utilities::MPI::this_mpi_process(in_mpi_comm)),
54
          real(0),
55
          imag(3),
56
          57
         true, true),
dof_handler(triangulation),
58
          run_number(0),
60
          condition_file_counter(0),
          eigenvalue_file_counter(0),
62
          Layers (GlobalParams.NumberProcesses),
63
          Dofs_Below_Subdomain(Layers),
          Block_Sizes(Layers),
64
          is_stored(false),
65
          Sectors (GlobalParams.M_W_Sectors),
         minimum_local_z(2.0 * GlobalParams.M_R_ZLength),
maximum_local_z(-2.0 * GlobalParams.M_R_ZLength),
pout(std::cout, rank == 0),
timer(in_mpi_comm, pout, TimerOutput::OutputFrequency::summary,
67
68
69
70
                 TimerOutput::wall_times),
71
          es(GlobalParams.M_C_Shape == ConnectorType::Rectangle) {
72
     mg = in_mg;
st = in_st;
73
74
     mpi_comm = in_mpi_comm;
solution = NULL;
7.5
76
     is_stored = false;
78
     solver_control.log_frequency(10);
79
     const int number = Layers - 1;
80
     qualities = new double[number];
     execute_recomputation = false;
mkdir((solutionpath + "/" + "primal").c_str(), ACCESSPERMS);
81
82
     mkdir((solutionpath + "/" + "dual").c_str(), ACCESSPERMS);
83
```

4.32.3 Member Function Documentation

4.32.3.1 assemble_part()

```
void Waveguide::assemble_part ( )
```

The assemble part function is a part of the assemble system() functionality.

It builds a part of the system-matrix. assemble_system() creates the global system matrix. After splitting the degrees of freedom into several blocks, this method takes one block (identified by the integer passed as an argument) and calculates all matrix-entries that reference it.

Date

25.10.2018

Author

Pascal Kraft

4.32.3.2 estimate_solution()

```
void Waveguide::estimate_solution ( )
```

This function is currently not in use.

It is supposed to create a useful input-vector for the first step of the iteration. However currently this is not used, since current cases simply use a zero-vector for the first step and previous solutions in the subsequent steps.

Definition at line 112 of file Waveguide.cpp.

References MeshGenerator::math_coordinate_in_waveguide(), MeshGenerator::prepare_triangulation(), and ExactSolution::vector value().

```
113
     MPI_Barrier(mpi_comm);
114
     deallog.push("estimate_solution");
     deallog << "Starting solution estimation..." << std::endl;
115
     DoFHandler<3>::active_cell_iterator cell, endc;
117
     deallog << "Lambda: " << GlobalParams.M_W_Lambda << std::endl;</pre>
      unsigned int min_dof = locally_owned_dofs.nth_index_in_set(0);
119
      unsigned int max_dof =
120
          {\tt locally\_owned\_dofs.nth\_index\_in\_set(locally\_owned\_dofs.n\_elements() - 1);}
      cell = dof_handler.begin_active(), endc = dof_handler.end();
121
      for (; cell != endc; ++cell) {
122
123
          (cell->is_locally_owned()) {
124
          for (unsigned int i = 0; i < GeometryInfo<3>::faces_per_cell; i++) {
125
           std::vector<types::global_dof_index> local_dof_indices(
126
                fe.dofs_per_line);
            for (unsigned int j = 0; j < GeometryInfo<3>::lines_per_face; j++) {
127
              ((cell->face(i))->line(j))->get_dof_indices(local_dof_indices);
128
129
              Tensor<1, 3, double> ptemp =
130
                  ((cell->face(i))->line(j))->center(true, false);
131
              if (std::abs(ptemp[2] - GlobalParams.Minimum_Z) > 0.0001) {
132
                Point<3, double> p(ptemp[0], ptemp[1], ptemp[2]);
               Tensor<1, 3, double> dtemp = ((cell->face(i))->line(j))->vertex(0) -
    ((cell->face(i))->line(j))->vertex(1);
133
134
135
                dtemp = dtemp / dtemp.norm();
136
                Point<3, double> direction(dtemp[0], dtemp[1], dtemp[2]);
137
                Vector<double> val(6);
138
                es.vector_value(p, val);
               139
140
                double b = direction(0) * val(3) + direction(1) * val(4) +
141
142
                           direction(2) * val(5);
```

```
143
                  if (local_dof_indices[0] >= min_dof &&
                       local_dof_indices[0] < max_dof) {</pre>
144
145
                     EstimatedSolution[local_dof_indices[0]] = a;
146
147
                  if (local_dof_indices[1] >= min_dof &&
    local_dof_indices[1] < max_dof) {</pre>
148
149
                     EstimatedSolution[local_dof_indices[1]] = b;
150
151
152
           }
153
154
155
156
      MPI_Barrier(mpi_comm);
157
      EstimatedSolution.compress(VectorOperation::insert);
158
      deallog << "Done." << std::endl;</pre>
159
      deallog.pop();
160 }
```

4.32.3.3 evaluate()

```
void Waveguide::evaluate ( )
```

This function has the purpose of filling the qualities array in every process with the appropriate Values from the other ones.

Now it will become necessary to build an optimization-scheme ontop, which can handle this information on process one and then distribute a new shape to the others. The function will use the Waveguide-Property execute_rebuild to signal a need for recomputation.

4.32.3.4 evaluate_for_Position()

```
\label{eq:std:complex} $$ \text{double } > \text{Waveguide::evaluate\_for\_Position (} $$ double $x$, $$ double $y$, $$ double $z$ )
```

To compute the output quality of the signal and it's transmition along the waveguid-axis, this function performs a comparison of the fundamental mode of a waveguide and the actual situation.

For this purpose we integrate the product of the two functions over a cross-section of the waveguide in transformed coordinates. To perform this action we need to use numeric integration so the integral is decomposed into a sum over local evaluations. For this to be possible this function can be handed x,y and z coordinates and returns the according value.

Parameters

X	gives the x-coordinate.
У	gives the y-coordinate.
Z	gives the z-coordinate.

Definition at line 88 of file Waveguide.cpp.

References ExactSolution::vector_value().

Referenced by Inhomogenous Transformation Circular:: PML_Z_Distance(), Homogenous Transformation Circular:: \leftarrow PML_Z_Distance(), and Space Transformation:: Z_to_Layer().

```
dealii::Point<3, double> position(x, y, z);
     Vector<double> result(6);
91
92
    Vector<double> mode(6);
9.3
    if (primal) {
       VectorTools::point_value(dof_handler, primal_with_relevant, position,
94
95
                                result);
97
       VectorTools::point_value(dof_handler, primal_solution, position, result);
98
    position[2] = GlobalParams.Minimum_Z;
99
100
     this->es.vector_value(position, mode);
101
102
      std::complex<double> c1(result(0), result(3));
103
      std::complex<double> c2(result(1), result(4));
104
      std::complex<double> c3(result(2), result(5));
      std::complex<double> m1(mode(0), mode(3));
105
     std::complex<double> m2 (mode(1), mode(4));
106
     std::complex<double> m3(mode(2), mode(5));
107
108
109
     return m1 * c1 + m2 * c2 + m3 * c3;
110 }
```

4.32.3.5 evaluate_for_z()

To compute the output quality of the signal and it's transmition along the waveguid-axis, this function performs a comparison of the fundamental mode of a waveguide and the actual situation.

For this purpose we integrate the product of the two functions over a cross-section of the waveguide in transformed coordinates. To perform this action we need to use numeric integration so the integral is decomposed into a sum over local evaluations. For this to be possible this function can be handed x,y and z coordinates and returns the according value.

Parameters

X	gives the x-coordinate.
У	gives the y-coordinate.
Z	gives the z-coordinate.

4.32.3.6 run()

```
void Waveguide::run ( )
```

This method as well as the rerun() method, are used by the optimization-algorithm to use and reuse the Waveguideobject.

Since the system-matrix consumes a lot of memory it makes sense to reuse it, rather then creating a new one for every optimization step. All properties of position[2]the object have to be created properly for this function to work.

Definition at line 1630 of file Waveguide.cpp.

References SpaceTransformation::IsDofFree(), and SpaceTransformation::NDofs().

```
1630
1631
       deallog.push("Waveguide_" + path_prefix + "_run");
1632
       if (run_number == 0) {
  deallog << "Setting up the mesh..." << std::endl;</pre>
1633
1634
         timer.enter_subsection("Setup Mesh");
1635
1636
         make_grid();
1637
         timer.leave_subsection();
1638
1639
         Compute Dof Numbers();
1640
         deallog << "Setting up FEM..." << std::endl;
1641
         timer.enter_subsection("Setup FEM");
1642
1643
         setup_system();
1644
         timer.leave_subsection();
1645
         timer.enter_subsection("Reset");
1646
1647
         timer.leave_subsection();
1648
1649
1650
         Prepare_Boundary_Constraints();
1651
1652
         timer.enter_subsection("Reset");
1653
         reinit all();
1654
         timer.leave_subsection();
1655
1656
1657
       deallog.push("Assembly");
       deallog << "Assembling the system..." << std::endl;
1658
       timer.enter_subsection("Assemble");
1659
1660
       assemble system():
1661
       timer.leave_subsection();
1662
       deallog.pop();
1663
       deallog.push("Solving");
deallog << "Solving the system..." << std::endl;</pre>
1664
1665
       timer.enter_subsection("Solve");
1666
1667
       solve();
1668
       timer.leave_subsection();
1669
       deallog.pop();
1670
       timer.enter_subsection("Evaluate");
1671
1672
       timer.leave subsection();
1673
1674
       timer.print_summary();
1675
1676
       deallog << "Writing outputs..." << std::endl;</pre>
1677
       timer.reset();
1678
1679
       output results (false);
1680
1681
       deallog.pop();
1682
       run_number++;
1683 }
```

4.32.3.7 store()

```
void Wavequide::store ( )
```

The storage has the following purpose: Regarding the optimization-process there are two kinds of runs.

The first one, taking place with no knowledge of appropriate starting values for the degrees of freedom, and the following steps, in which the prior results can be used to estimate appropriate starting values for iterative solvers as well as the preconditioner. This function switches the behaviour in the following way: Once it is called, it stores the current solution in a run-independent variable, making it available for later runs. Also it sets a flag, indicating, that prior solutions are now available for usage in the solution process.

Definition at line 1457 of file Waveguide.cpp.

```
1457 {
1458 reinit_storage();
1459 // storage.reinit(dof_handler.n_dofs());
1460 if (primal) {
1461 storage = primal_solution;
1462 } else {
1463 storage = dual_solution;
1464 }
1465 is_stored = true;
1466 }
```

The documentation for this class was generated from the following files:

- Code/Core/Waveguide.h
- Code/Core/Waveguide.cpp

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