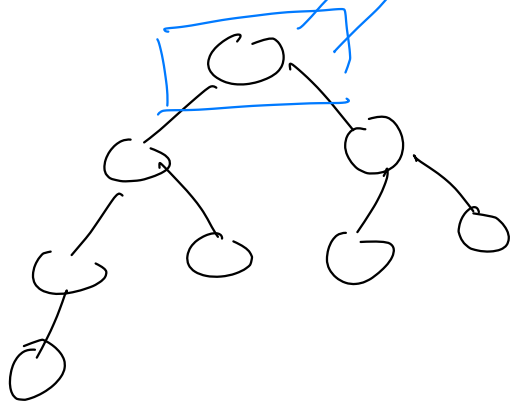


Heap $\begin{cases} \text{Min Heap} \\ \text{Max Heap} \end{cases}$



Heap Property

Parent data $>$
MAX (child's data)

Largest
Value always at top.

Hash Table

→ Store data = Linear Hierarchy

→ Search & Sort

```
graph TD; A[Search & Sort] --> B["O(n)"]; A --> C["O(log n)"]
```

Problem: Stream of numbers between 1 to N .
Stream ends when we get a 0.
When we get a number from stream,
tell if it is duplicate.

Ex: 5 9 1 8 5 3 2 7 2 8 1 ...
Dup Dup Dup

BST \rightarrow insert $O(\log n)$
 \rightarrow search $O(\log n)$

linked \rightarrow insert $O(1)$
 list \rightarrow search $O(n)$

BitMap \rightarrow insert $O(1)$
~~XXXX~~ \rightarrow search $O(1)$
 Direct Address Table

T } 1 bit
 F }
 integer \rightarrow 4 bytes
 $4 \times \frac{1}{8}$ bits
 $= 32 \text{ bits}$

1 ... N (100)										99 100	
1	2	3	4	5	6	7	8	9	...	F	F
F	F	F	F	F	F	F	F	F	...	F	F

map [elem]
 12084 = 8 bits

N = integer
 $= 2^{31}$
 $= 2^{31} \text{ bytes}$
 $\frac{4GB}{8} \approx 4GB$

$N = 100$

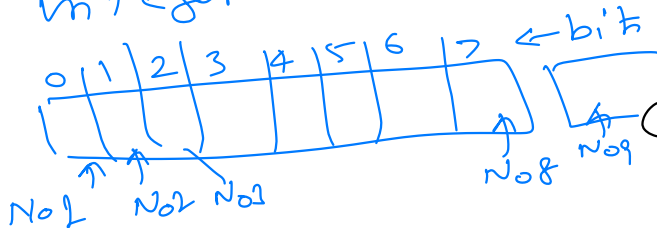
`bool map [100];`
100 bytes

1 byte

`T/F` 2 options \Rightarrow 1 bit
100 values \Rightarrow 100 bits

\Downarrow
 $100/8$ bytes.

integer map [4];



$\frac{100}{32}$ bytes = 3.125 bytes
(4 x 8 bits)
 \Downarrow
integer

≈ 4 bytes

1 ... 100
 \Downarrow
0 ... 99

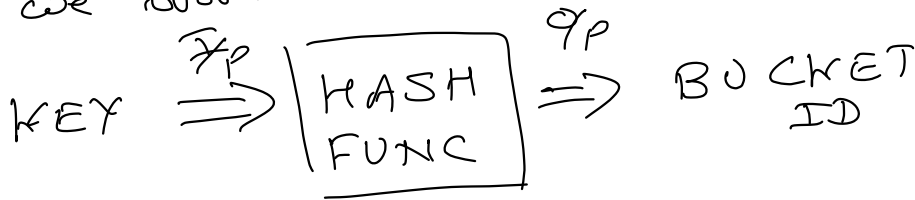
Hash Table

↳ is a group of BUCKETS

↓
that store elements

Hash Function : Maps a key to a unique bucket.

What we store in hash table \Rightarrow KEY



int hashTable [10];

int hashFn (int Key) {
return Key % 10; // MOD N
}

Size of
hash
Table

Time
 $O(1)$

Add (elem) \Rightarrow hashFn (elem)

1. bucket id = hashFn (elem)

2. hashTable [bucket id] = elem

23 \rightarrow HF \rightarrow 3

99 \rightarrow HF \rightarrow 9

Add (23)
Add (99)

H.T Size = 10

0	
1	
2	
3	23
4	
5	
6	
7	
8	
9	99

hash Table

Bucket Size = 1

Size of Hash Table = Number of Buckets in H.T.

Search (elem)

1. bucketid = hashFn(elem)

2. if (hashTable [bucketid] == elem)

return true

3. return false.

Time = $O(1)$

Add(13)

13 \rightarrow HF \rightarrow 3

Bucket 3 already
stores a elem (23)
and it is not 13.

How to solve collision
 \rightarrow Use a better hash function.
 \rightarrow Handle collision

23 \rightarrow HF \rightarrow 3
13 \rightarrow MOD N

COLLISION

When hash function
maps more than one
key to a bucket id.

Hash Function

$$\underline{1} \text{ MOD } N$$

$$\text{Key} = \underline{\underline{93367}}$$

$$N = 100$$

$$\text{bucket id} = 93367 \text{ MOD } 100 = 67$$

2. Folding. \Rightarrow Divide Key into multiple parts & combine (fold) them together.

$$\text{Key} = \underline{9} \underline{33} \underline{67}$$

Combine them \rightarrow

09
33
67
+
109

Break Key into multiple parts

$$\underline{9} \underline{67} \underline{33}$$

$$\text{MOD } N = 9$$

$$96733 \text{ MOD } 100 = 33$$

$$5767 \text{ MOD } 100 = 67$$

$$\begin{array}{r} 5767 \\ \downarrow \\ 57 \\ + 67 \\ \hline 124 \\ \text{MOD } N = 24 \end{array}$$

3. Mid Square : Square the key & Pick digits from middle of square.

$$93367 = 8717396689$$

⇓

$$5767 = 33258289 \text{ bucket id } 39$$

⇓

bucket id 58

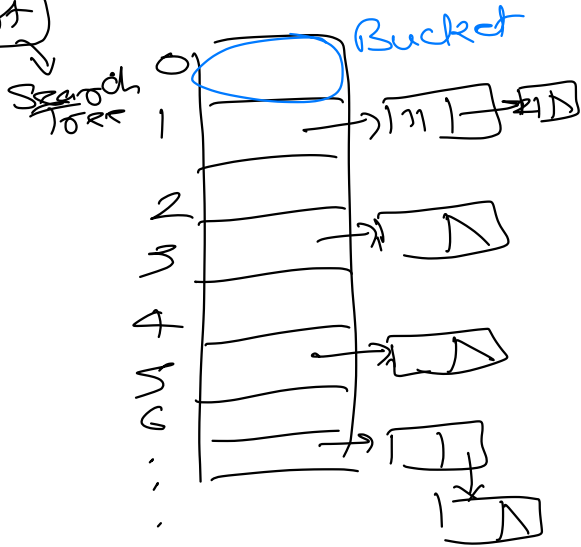
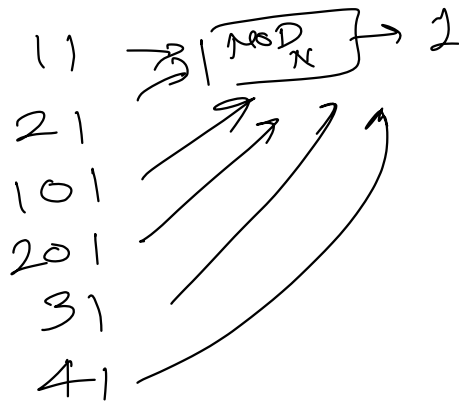
$$96733 = 9357273289$$

⇓

bucket id = 27

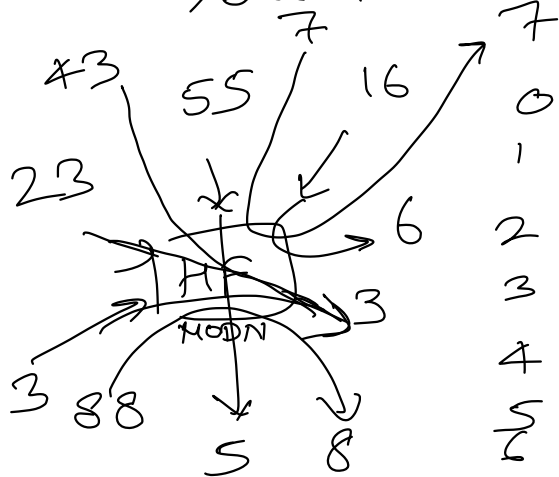
Handling Collision

1. Chaining : Bucket is implemented as a Linked list



2. Open Addressing

- ↳ Linear Probing.
- ↳ Quadratic Probing.



↳ Double Hashing

N elements to be stored in H.T.

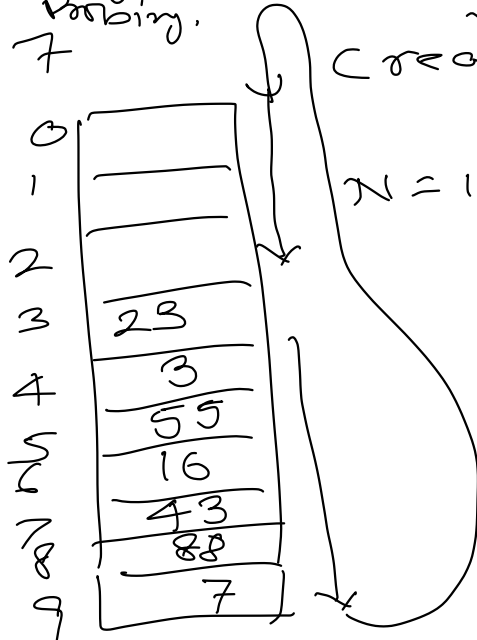
||

Create a H.T. of N Buckets

$N = 10$

quad
eq.

$$n^2 + n$$



Symbol Table

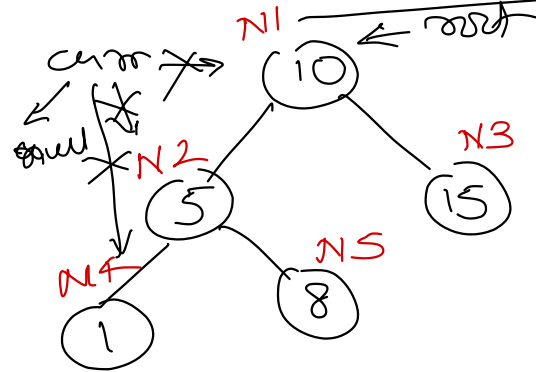
H.T. of Keywords.

Chaining \Rightarrow we try to keep bucket size as small as possible.

Bucket size = R
 $R \ll n \rightarrow$ Size of H.T.

$$O(\log R)$$

Inorder Traversal



N3
N5
N4
N2
N1

Impl Stack

curr →	N4
	null
N1	N2
N3	N5
null	null
N3	N5
null	null

- inorder (node)
1. if (node is null)
STOP
 2. inorder (node->left)
 3. Process node
 4. inorder (node->right)

N4	node
N2	node
N1	node

$BST_{\text{tree}} < \text{int} >$ $a = \text{new}$
 $BST < \text{int} > \text{ } (?) ;$

