# assignment1 SHUHENG XU 190186546

## April 19, 2020

# 1 [COM4513-6513] Assignment 1: Text Classification with Logistic Regression

#### 1.0.1 Instructor: Nikos Aletras

The goal of this assignment is to develop and test two text classification systems:

- Task 1: sentiment analysis, in particular to predict the sentiment of movie review, i.e. positive or negative (binary classification).
- Task 2: topic classification, to predict whether a news article is about International issues, Sports or Business (multiclass classification).

For that purpose, you will implement:

- Text processing methods for extracting Bag-Of-Word features, using (1) unigrams, bigrams and trigrams to obtain vector representations of documents. Two vector weighting schemes should be tested: (1) raw frequencies (3 marks; 1 for each ngram type); (2) tf.idf (1 marks).
- Binary Logistic Regression classifiers that will be able to accurately classify movie reviews trained with (1) BOW-count (raw frequencies); and (2) BOW-tfidf (tf.idf weighted) for Task 1.
- Multiclass Logistic Regression classifiers that will be able to accurately classify news articles trained with (1) BOW-count (raw frequencies); and (2) BOW-tfidf (tf.idf weighted) for Task 2.
- The Stochastic Gradient Descent (SGD) algorithm to estimate the parameters of your Logistic Regression models. Your SGD algorithm should:
  - Minimise the Binary Cross-entropy loss function for Task 1 (3 marks)
  - Minimise the Categorical Cross-entropy loss function for Task 2 (3 marks)
  - Use L2 regularisation (both tasks) (1 mark)
  - Perform multiple passes (epochs) over the training data (1 mark)
  - Randomise the order of training data after each pass (1 mark)
  - Stop training if the difference between the current and previous validation loss is smaller than a threshold (1 mark)
  - After each epoch print the training and development loss (1 mark)
- Discuss how did you choose hyperparameters (e.g. learning rate and regularisation strength)? (2 marks; 0.5 for each model in each task).
- After training the LR models, plot the learning process (i.e. training and validation loss in each epoch) using a line plot (1 mark; 0.5 for both BOW-count and BOW-tfidf LR models in each task) and discuss if your model overfits/underfits/is about right.

• Model interpretability by showing the most important features for each class (i.e. most positive/negative weights). Give the top 10 for each class and comment on whether they make sense (if they don't you might have a bug!). If we were to apply the classifier we've learned into a different domain such laptop reviews or restaurant reviews, do you think these features would generalise well? Can you propose what features the classifier could pick up as important in the new domain? (2 marks; 0.5 for BOW-count and BOW-tfidf LR models respectively in each task)

#### 1.0.2 Data - Task 1

The data you will use for Task 1 are taken from here: http://www.cs.cornell.edu/people/pabo/movie-review-data/ and you can find it in the ./data\_sentiment folder in CSV format:

- data\_sentiment/train.csv: contains 1,400 reviews, 700 positive (label: 1) and 700 negative (label: 0) to be used for training.
- data\_sentiment/dev.csv: contains 200 reviews, 100 positive and 100 negative to be used for hyperparameter selection and monitoring the training process.
- data\_sentiment/test.csv: contains 400 reviews, 200 positive and 200 negative to be used for testing.

#### 1.0.3 Data - Task 2

The data you will use for Task 2 is a subset of the AG News Corpus and you can find it in the ./data\_topic folder in CSV format:

- data\_topic/train.csv: contains 2,400 news articles, 800 for each class to be used for training.
- data\_topic/dev.csv: contains 150 news articles, 50 for each class to be used for hyperparameter selection and monitoring the training process.
- data\_topic/test.csv: contains 900 news articles, 300 for each class to be used for testing.

#### 1.0.4 Submission Instructions

You should submit a Jupyter Notebook file (assignment1.ipynb) and an exported PDF version (you can do it from Jupyter: File->Download as->PDF via Latex).

You are advised to follow the code structure given in this notebook by completing all given functions. You can also write any auxilliary/helper functions (and arguments for the functions) that you might need but note that you can provide a full solution without any such functions. Similarly, you can just use only the packages imported below but you are free to use any functionality from the Python Standard Library, NumPy, SciPy and Pandas. You are not allowed to use any third-party library such as Scikit-learn (apart from metric functions already provided), NLTK, Spacy, Keras etc..

Please make sure to comment your code. You should also mention if you've used Windows (not recommended) to write and test your code. There is no single correct answer on what your accuracy should be, but correct implementations usually achieve F1-scores around 80% or higher. The quality of the analysis of the results is as important as the accuracy itself.

This assignment will be marked out of 20. It is worth 20% of your final grade in the module.

The deadline for this assignment is **23:59** on Fri, **20** Mar **2020** and it needs to be submitted via MOLE. Standard departmental penalties for lateness will be applied. We use a range of strategies to detect unfair means, including Turnitin which helps detect plagiarism, so make sure you do not plagiarise.

## 1.1 Load Raw texts and labels into arrays

First, you need to load the training, development and test sets from their corresponding CSV files (tip: you can use Pandas dataframes).

```
[2]: # Load dataset

data_tr = pd.read_csv("./data_sentiment/train.csv", header=None,

→names=["text","label"])

data_te = pd.read_csv("./data_sentiment/test.csv", header=None,

→names=["text","label"])

data_dev = pd.read_csv("./data_sentiment/dev.csv", header=None,

→names=["text","label"])
```

If you use Pandas you can see a sample of the data.

```
[3]: data_tr.head()

[3]: text label

O note: some may consider portions of the follo... 1

1 note: some may consider portions of the follo... 1

2 every once in a while you see a film that is s... 1

3 when i was growing up in 1970s, boys in my sc... 1

4 the muppet movie is the first, and the best m... 1
```

The next step is to put the raw texts into Python lists and their corresponding labels into NumPy arrays:

```
[4]: # transform test to list, and label to numpy arrays
def transform(df):
    return list(df['text']), df['label'].to_numpy().reshape(-1,1)

X_tr_raw, Y_tr = transform(data_tr)
X_te_raw, Y_te = transform(data_te)
X_dev_raw, Y_dev = transform(data_dev)
```

## 2 Bag-of-Words Representation

To train and test Logisite Regression models, you first need to obtain vector representations for all documents given a vocabulary of features (unigrams, bigrams, trigrams).

## 2.1 Text Pre-Processing Pipeline

To obtain a vocabulary of features, you should: - tokenise all texts into a list of unigrams (tip: using a regular expression) - remove stop words (using the one provided or one of your preference) - compute bigrams, trigrams given the remaining unigrams - remove ngrams appearing in less than K documents - use the remaining to create a vocabulary of unigrams, bigrams and trigrams (you can keep top N if you encounter memory issues).

#### 2.1.1 N-gram extraction from a document

You first need to implement the extract\_ngrams function. It takes as input: - x\_raw: a string corresponding to the raw text of a document - ngram\_range: a tuple of two integers denoting the type of ngrams you want to extract, e.g. (1,2) denotes extracting unigrams and bigrams. - token\_pattern: a string to be used within a regular expression to extract all tokens. Note that data is already tokenised so you could opt for a simple white space tokenisation. - stop\_words: a list of stop words - vocab: a given vocabulary. It should be used to extract specific features.

and returns:

• a list of all extracted features.

See the examples below to see how this function should work.

```
[6]: def extract_ngrams(x_raw, ngram_range=(1,3),__
      →token_pattern=r'\b[A-Za-z][A-Za-z]+\b', stop_words=[], vocab=set()):
         """N-gram extraction from a document.
         Args:
             x_raw: a string corresponding to the raw text of a document
             ngram\_range: a tuple of two integers denoting the type of ngrams you\sqcup
      \hookrightarrow want
                  to extract, e.g. (1,2) denotes extracting unigrams and bigrams.
              token\_pattern: a string to be used within a regular expression to_{\sqcup}
      \rightarrow extract
                  all tokens. Note that data is already tokenised so you could opt for
                  a simple white space tokenisation.
             stop_words: a list of stop words
             vocab: a given vocabulary. It should be used to extract specific_
      \hookrightarrow features.
         Returns:
             A list of terms to the corresponding N-gram. Each part fits one N-gram,
             except 1-gramrow. For example:
             ['great', 'movie', 'watch',
              ('great', 'movie'),('movie', 'watch'),
              ('great', 'movie', 'watch')]
         11 11 11
         def finder(s,n):
             if n \le 0 or n > len(s):
                  raise Exception('n is out of range')
             if n == 1:
                 return s
             else:
                  return map(lambda i: tuple(s[i:i+n]),range(len(s)-n+1))
         # Find all words by condition
         pattern = re.compile(token_pattern)
         term_eligible = [term.lower() for term in pattern.findall(x_raw) if term.
      →lower() not in stop_words]
         # Find combinations of different N-grams
         x = [term for n in range(ngram_range[0],ngram_range[1]+1) for term in_u
      →finder(term_eligible,n)]
         if not vocab:
             return x
```

[8]: ['great', ('great', 'movie')]

Note that it is OK to represent n-grams using lists instead of tuples: e.g. ['great', ['great', 'movie']]

#### 2.1.2 Create a vocabulary of n-grams

Then the <code>get\_vocab</code> function will be used to (1) create a vocabulary of ngrams; (2) count the document frequencies of ngrams; (3) their raw frequency. It takes as input: - X\_raw: a list of strings each corresponding to the raw text of a document - ngram\_range: a tuple of two integers denoting the type of ngrams you want to extract, e.g. (1,2) denotes extracting unigrams and bigrams. - token\_pattern: a string to be used within a regular expression to extract all tokens. Note that data is already tokenised so you could opt for a simple white space tokenisation. - stop\_words: a list of stop words - vocab: a given vocabulary. It should be used to extract specific features. - min\_df: keep ngrams with a minimum document frequency. - keep\_topN: keep top-N more frequent ngrams.

and returns:

- vocab: a set of the n-grams that will be used as features.
- df: a Counter (or dict) that contains ngrams as keys and their corresponding document frequency as values.
- ngram\_counts: counts of each ngram in vocab

Hint: it should make use of the extract\_ngrams function.

```
[9]: def get_vocab(X_raw, ngram_range=(1,3), token_pattern=r'\b[A-Za-z][A-Za-z]+\b', □ → min_df=0, keep_topN=0, stop_words=[]):
```

```
'''1. create a vocabulary of ngrams
       2. count the document frequencies of ngrams
       3. their raw frequency
   Arqs:
        X_raw: a list of strings each corresponding to the raw text of a_{\sqcup}
\rightarrow document
        ngram\_range: a tuple of two integers denoting the type of ngrams\ you_{\sqcup}
\hookrightarrow want
             to extract, e.g. (1,2) denotes extracting unigrams and bigrams.
        token\_pattern: a string to be used within a regular expression to_{\sqcup}
\rightarrow extract
             all tokens. Note that data is already tokenised so you could opt for
             a simple white space tokenisation.
        stop_words: a list of stop words
        min_df: keep ngrams with a minimum document frequency.
        keep_topN: keep top-N more frequent ngrams.
   Returns:
        vocab: a set of the n-grams that will be used as features.
        \mathit{df} \colon \mathit{a} \ \mathit{Counter} \ (\mathit{or} \ \mathit{dict}) \ \mathit{that} \ \mathit{contains} \ \mathit{ngrams} \ \mathit{as} \ \mathit{keys} \ \mathit{and} \ \mathit{their}_\sqcup
\hookrightarrow corresponding
             document frequency as values.
        ngram_counts: counts of each ngram in vocab
    IIII
   bag_of_ngrams = list()
   df = Counter()
   for line in X_raw:
        ngrams =
→extract_ngrams(line,ngram_range=(1,3),token_pattern=token_pattern,stop_words=stop_words)
        bag of ngrams += ngrams
        df.update(set(ngrams))
   df = Counter({k:v for k,v in df.items() if v >=min_df})
   ngram_counts = Counter(bag_of_ngrams)
   vocab = [items[0] for items in ngram_counts.most_common() if items[0] in df.
→keys()][:keep_topN]
   return vocab, df, ngram_counts
```

Now you should use get\_vocab to create your vocabulary and get document and raw frequencies of n-grams:

```
[10]: vocab, df, ngram_counts = get_vocab(X_tr_raw, ngram_range=(1,3), 

⇒keep_topN=5000, stop_words=stop_words)
```

```
print(len(vocab))
print()
print(list(vocab)[:100])
print()
print(df.most_common()[:10])
```

5000

```
['film', 'but', 'one', 'movie', 'not', 'all', 'there', 'like', 'so', 'out',
'about', 'more', 'up', 'when', 'their', 'some', 'just', 'if', 'into', 'him',
'even', 'only', 'no', 'than', 'time', 'good', 'most', 'story', 'would', 'much',
'character', 'also', 'get', 'two', 'well', 'characters', 'other', 'very',
'first', 'see', 'after', 'because', 'way', 'make', 'off', 'plot', 'while',
'had', 'any', 'too', 'little', 'life', 'films', 'does', 'where', 'people',
'then', 'how', 'me', 'really', 'man', 'scene', 'my', 'never', 'bad', 'being',
'over', 'best', 'don', 'scenes', 'doesn', 'many', 'new', 'know', 'director',
'here', 'action', 'such', 'great', 'through', 'movies', 're', 'love', 'another',
'made', 'go', 'big', 'end', 'seems', 'something', 'still', 'back', 'world',
'us', 'work', 'now', 'down', 'before', 'makes', 'however']

[('but', 1334), ('one', 1247), ('film', 1231), ('not', 1170), ('all', 1117),
('movie', 1095), ('out', 1080), ('so', 1047), ('there', 1046), ('like', 1043)]
```

Then, you need to create vocabulary id -> word and id -> word dictionaries for reference:

Now you should be able to extract n-grams for each text in the training, development and test sets:

## 2.2 Vectorise documents

Next, write a function vectoriser to obtain Bag-of-ngram representations for a list of documents. The function should take as input: - X\_ngram: a list of texts (documents), where each text is represented as list of n-grams in the vocab - vocab: a set of n-grams to be used for representing the documents

and return: -  $X_{\text{vec}}$ : an array with dimensionality Nx|vocab| where N is the number of documents and |vocab| is the size of the vocabulary. Each element of the array should represent the frequency of a given n-gram in a document.

```
[13]: def vectorise(X_ngram, vocab):
           '''1. select the features of vocab from X_ngram.
              2. convert X_ngram into matrix
          Args:
               X_ngram(list\ of\ list): a list of texts (documents)
       \rightarrow features (Bag-of-ngram)
               vocab(list): a set of selected features(n-grams)
          Returns:
               X vec: an array shapes (#document, #vocab), where document is a single \Box
       \hookrightarrow line
                   in dataset.
           111
          X vec = np.zeros([len(X ngram),len(vocab)])
          for docs index in range(len(X ngram)):
               temp = Counter(X_ngram[docs_index])
               for feature_index in range(len(vocab)):
                   X_vec[docs_index,feature_index] = temp.get(vocab[feature_index],0)
          return X_vec
```

Finally, use **vectorise** to obtain document vectors for each document in the train, development and test set. You should extract both count and tf.idf vectors respectively:

```
Count vectors
[14]: X_tr_count = vectorise(X_tr_ngram, vocab_tr)
    X_te_count = vectorise(X_te_ngram, vocab_tr)
    X_dev_count = vectorise(X_dev_ngram, vocab_tr)

[15]: X_tr_count.shape
[16]: X_tr_count[:2,:50]
```

```
[16]: array([[20., 6., 8., 0., 4., 1., 1., 0., 3., 1., 1., 1.,
            0., 6., 1., 2., 1., 2., 0., 3.,
                                             4., 1., 1., 0.,
            4., 2., 3., 1.,
                            3., 0., 0., 1.,
                                             0., 4., 0.,
                                                         0.,
            1., 0., 0., 0.,
                            0., 1., 0., 3.,
                                             2., 1.,
                                                     0.],
                            2., 4., 2., 3.,
                                             3., 2., 2., 3.,
          [6., 2., 5., 0.,
            0., 0., 2., 0.,
                            2., 2., 5., 0., 0., 1., 3., 2.,
            2., 2., 1., 1., 5., 1., 1., 1., 0., 0., 1., 0.,
            1., 0., 1., 2., 1., 0., 2., 3., 0., 1.,
                                                    0.11)
```

**TF.IDF vectors** First compute idfs an array containing inverted document frequencies (Note: its elements should correspond to your vocab)

Then transform your count vectors to tf.idf vectors:

```
[18]: X_tr_tfidf = X_tr_count*idfs_tr
X_te_tfidf = X_te_count*idfs_te
X_dev_tfidf = X_dev_count*idfs_dev
[19]: X_tr_tfidf[1,:50]
```

```
[19]: array([0.3352199 , 0.04194441, 0.25130791, 0. , 0.15588435, 0.39229945, 0.2531927 , 0.38353118, 0.37854406, 0.22540856, 0.28361332, 0.38728409, 0.55011146, 0. , 0. , 0.32320144, 0. , 0.34692489, 0.36468042, 1.24525516, 0. , 0. , 0.21927133, 0.55839959, 0.40923321, 0.22967409, 0.43239695, 0.52266534, 0.25626631, 0.24195367, 1.37569611, 0.26818108, 0.26076682, 0.2699102 , 0. ,
```

```
0. , 0.25794854, 0. , 0. , 0.30664999, 
0. , 0.34472433, 0.59341724, 0.29609478, 0. , 
0.67313664, 0.94469503, 0. , 0.32395996, 0. ])
```

# 3 Binary Logistic Regression

After obtaining vector representations of the data, now you are ready to implement Binary Logistic Regression for classifying sentiment.

First, you need to implement the sigmoid function. It takes as input:

• z: a real number or an array of real numbers

and returns:

• sig: the sigmoid of z

```
[20]: def sigmoid(z):
           '''Calculate sigmod results
          In order to avoid data overflow, the corresponding data boundary is added.
          Since np.exp() is a np.float64 operation function, so we need to avoid
       \hookrightarrow overflow.
           It is easy to find out the boundary of `np.float64` by calling np.finfo(np.
          Usually, it should be written as np.minimum(np.exp(z), np.finfo(np.float64).
       \hookrightarrow max),
           but I prefer to written inside the exp function, since it somehow can be \Box
       \hookrightarrow faster.
          For the input of np.exp(), it should not be greater than 709.782 to ensure,
           output will not overflow.
          Returns:
               z: the same size of z.
          \# z = 1 / (1 + np.minimum(np.exp(z), np.finfo(np.float64).max))
          z = 1 / (1 + np.exp(np.minimum(-z,709.782)))
          return z
```

```
[21]: print(sigmoid(0))
print(sigmoid(np.array([-5., 1.2])))
```

## 0.5 [0.00669285 0.76852478]

Then, implement the predict\_proba function to obtain prediction probabilities. It takes as input:

- X: an array of inputs, i.e. documents represented by bag-of-ngram vectors  $(N \times |vocab|)$
- weights: a 1-D array of the model's weights (1, |vocab|)

#### and returns:

• preds\_proba: the prediction probabilities of X given the weights

```
[22]: def predict_proba(X, weights):
    # Get the output by mutipling x * w.T
    preds_proba = X.dot(weights.T)

# Verify the size of the data
    assert preds_proba.shape == (X.shape[0],1)

return sigmoid(preds_proba)
```

Then, implement the predict\_class function to obtain the most probable class for each vector in an array of input vectors. It takes as input:

- X: an array of documents represented by bag-of-ngram vectors  $(N \times |vocab|)$
- weights: a 1-D array of the model's weights (1, |vocab|)

#### and returns:

• preds\_class: the predicted class for each x in X given the weights

```
[23]: def predict_class(X, weights):
    '''1. Calculate the probability
    2. Classify according to probability

Args:
    preds_proba: Probability of each data, the same
        size of input data.(X.shape[0])

Returns:
    preds_class: The classification corresponding
        to the input data, the size is consistent
        with the amount of input data.(X.shape[0])

'''

preds_proba = predict_proba(X, weights)
    preds_class = np.where(preds_proba>=0.5,1,0)

# Verify the size of the data
```

```
assert preds_class.shape == (X.shape[0],1)
return preds_class
```

To learn the weights from data, we need to minimise the binary cross-entropy loss. Implement binary\_loss that takes as input:

- X: input vectors
- Y: labels
- weights: model weights
- alpha: regularisation strength

#### and return:

• 1: the loss score

```
[24]: def binary loss(X, Y, weights, alpha=0.00001):
          '''1. Calculate the probability
             2. Calculate the Euclidean distance between label and probability
             3. Calculate the average distance
          Here I use 'esp' to represent the smallest data unit of the data type.
          The main function of `esp` is to ensure the rationality of arithmetic
          operations. For example, in the division operation, add 'esp' to the
          denominator to ensure that the denominator is not 0, and it does not
          affect the data result. This is the habit I developed when I wrote Matlab
          in my undergraduate period. `esp` is more common in Matlab.
          Arqs:
              eps: the minimum value in the current data type. Used to ensure
                  that the input of the log function is greater than O.
              preds_proba: Probability of each data, the same
                  size of input data.(X.shape[0])
          Returns:
              1: Used to save losses and calculate the average at the end
          111
          eps = np.finfo(np.float64).eps
          preds_proba = predict_proba(X, weights)
          1 = -1*(Y*np.log10(preds_proba+eps) + (1-Y)*np.log10(1-preds_proba+eps)) + ___
       →alpha*np.multiply(weights, weights)
          1 = np.mean(1)
          # Verify the size of the data
          assert 1.shape == (1,1) or type(1) == np.float64
          return 1
```

```
[25]: def gradient(X, y, weights, alpha=0.00001):
    '''Only calculate the gradient of the corresponding position

Args:
    m: the total number of the dataset sample.
    h: an numpy array of prediction corresponding to the
        dataset points. Shape (#dataset,1)

Returns:
    dw: the corresponding gradient. Shape the same with
        weight.

'''

m = len(X)
h = predict_proba(X, weights)
dw = np.dot((h - y).T,X) + 2*alpha*weights
# Verify the size of the data
assert dw.shape == weights.shape
return dw/m
```

Now, you can implement Stochastic Gradient Descent to learn the weights of your sentiment classifier. The SGD function takes as input:

- X\_tr: array of training data (vectors)
- Y\_tr: labels of X\_tr
- X\_dev: array of development (i.e. validation) data (vectors)
- Y\_dev: labels of X\_dev
- 1r: learning rate
- alpha: regularisation strength
- epochs: number of full passes over the training data
- tolerance: stop training if the difference between the current and previous validation loss is smaller than a threshold
- print\_progress: flag for printing the training progress (train/validation loss)

#### and returns:

- weights: the weights learned
- training\_loss\_history: an array with the average losses of the whole training set after each epoch
- validation\_loss\_history: an array with the average losses of the whole development set after each epoch

```
validation_loss_history = []
   # Stage 1: Init weights
   weights = np.zeros((1,X_tr.shape[1]))
   # Stage 2: Init stochastic index
   idx_list = np.array(range(X_tr.shape[0]))
   # Stage 3: Training
   for epoch in range(epochs):
       loss tr = 0
       np.random.shuffle(idx_list) # disorder dataset
       for i in idx_list:
           X_{tr_i}, Y_{tr_i} = X_{tr_i}].reshape(1,-1),Y_{tr_i}].reshape(1,-1) # qet_{l}
\rightarrowa single data pair
           dw = gradient(X_tr_i, Y_tr_i, weights, alpha) # gradient
           weights -= lr*dw # update
           loss_tr += binary_loss(X_tr_i, Y_tr_i, weights, alpha) # add loss
       # calculate loss
       loss_dev = binary_loss(X_dev, Y_dev, weights, alpha)
       loss_tr /= len(idx_list)
       # Add to history
       training_loss_history.append(loss_tr)
       validation_loss_history.append(loss_dev)
       # print function
       if print_progress == True:
           print("Epoch: %d| Training loss: %f| Validation loss: __
→%f"%(epoch,loss_tr,loss_dev))
       # check tolerance to break
       if epoch >1 and_
→(validation_loss_history[-2]-validation_loss_history[-1]) <= tolerance:
           break
   return weights, training_loss_history, validation_loss_history
```

## 3.1 Train and Evaluate Logistic Regression with Count vectors

First train the model using SGD:

```
Y_dev=Y_dev,
lr=0.0001,
alpha=0.001,
epochs=100)
```

```
Epoch: 0 | Training loss: 0.281198 | Validation loss: 0.280390
Epoch: 1 | Training loss: 0.258984 | Validation loss: 0.267200
Epoch: 2 | Training loss: 0.242545 | Validation loss: 0.256740
Epoch: 3 | Training loss: 0.229901 | Validation loss: 0.248940
Epoch: 4 | Training loss: 0.218922 | Validation loss: 0.242651
Epoch: 5 | Training loss: 0.210565 | Validation loss: 0.237559
Epoch: 6 | Training loss: 0.202685 | Validation loss: 0.232486
Epoch: 7 | Training loss: 0.195936 | Validation loss: 0.229208
Epoch: 8 | Training loss: 0.189990 | Validation loss: 0.224886
Epoch: 9 | Training loss: 0.184416 | Validation loss: 0.222042
Epoch: 10 | Training loss: 0.179316 | Validation loss: 0.219922
Epoch: 11 | Training loss: 0.174928 | Validation loss: 0.216306
Epoch: 12 | Training loss: 0.170694 | Validation loss: 0.213822
Epoch: 13 | Training loss: 0.166703 | Validation loss: 0.211881
Epoch: 14 | Training loss: 0.163014 | Validation loss: 0.209455
Epoch: 15 | Training loss: 0.159598 | Validation loss: 0.207629
Epoch: 16 | Training loss: 0.156189 | Validation loss: 0.205890
Epoch: 17 | Training loss: 0.153474 | Validation loss: 0.204341
Epoch: 18 | Training loss: 0.150632 | Validation loss: 0.202479
Epoch: 19 | Training loss: 0.147939 | Validation loss: 0.201133
Epoch: 20 | Training loss: 0.145376 | Validation loss: 0.199716
Epoch: 21 | Training loss: 0.142932 | Validation loss: 0.198529
Epoch: 22 | Training loss: 0.140548 | Validation loss: 0.197355
Epoch: 23 | Training loss: 0.138346 | Validation loss: 0.196000
Epoch: 24 | Training loss: 0.136033 | Validation loss: 0.195695
Epoch: 25 | Training loss: 0.134227 | Validation loss: 0.193908
Epoch: 26 | Training loss: 0.132114 | Validation loss: 0.192935
Epoch: 27 | Training loss: 0.130310 | Validation loss: 0.191987
Epoch: 28 | Training loss: 0.128483 | Validation loss: 0.191048
Epoch: 29 | Training loss: 0.126455 | Validation loss: 0.190900
Epoch: 30 | Training loss: 0.125059 | Validation loss: 0.189396
Epoch: 31 | Training loss: 0.123383 | Validation loss: 0.188613
Epoch: 32 | Training loss: 0.121719 | Validation loss: 0.188297
Epoch: 33 | Training loss: 0.120255 | Validation loss: 0.187205
Epoch: 34 | Training loss: 0.118783 | Validation loss: 0.186540
Epoch: 35 | Training loss: 0.117360 | Validation loss: 0.185867
Epoch: 36 | Training loss: 0.115978 | Validation loss: 0.185224
Epoch: 37 | Training loss: 0.114585 | Validation loss: 0.184636
Epoch: 38 | Training loss: 0.113304 | Validation loss: 0.184078
Epoch: 39 | Training loss: 0.112001 | Validation loss: 0.183510
Epoch: 40 | Training loss: 0.110790 | Validation loss: 0.182968
Epoch: 41 | Training loss: 0.109556 | Validation loss: 0.182445
```

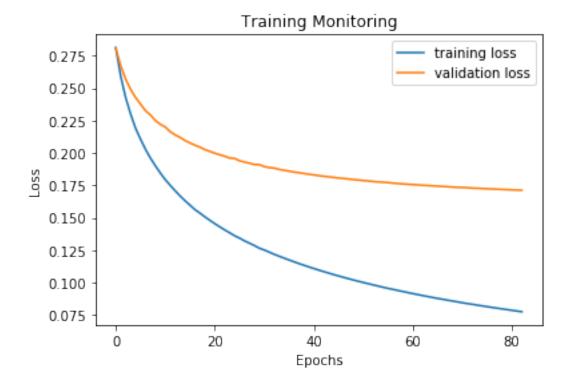
```
Epoch: 42 | Training loss: 0.108398 | Validation loss: 0.181960
Epoch: 43 | Training loss: 0.107248 | Validation loss: 0.181496
Epoch: 44 | Training loss: 0.106090 | Validation loss: 0.181031
Epoch: 45 | Training loss: 0.105063 | Validation loss: 0.180584
Epoch: 46 | Training loss: 0.103959 | Validation loss: 0.180237
Epoch: 47 | Training loss: 0.102945 | Validation loss: 0.179825
Epoch: 48 | Training loss: 0.101922 | Validation loss: 0.179404
Epoch: 49 | Training loss: 0.100949 | Validation loss: 0.179044
Epoch: 50 | Training loss: 0.099997 | Validation loss: 0.178630
Epoch: 51 | Training loss: 0.099058 | Validation loss: 0.178292
Epoch: 52 | Training loss: 0.098120 | Validation loss: 0.177929
Epoch: 53 | Training loss: 0.097208 | Validation loss: 0.177572
Epoch: 54 | Training loss: 0.096327 | Validation loss: 0.177324
Epoch: 55 | Training loss: 0.095451 | Validation loss: 0.177059
Epoch: 56 | Training loss: 0.094682 | Validation loss: 0.176641
Epoch: 57 | Training loss: 0.093828 | Validation loss: 0.176345
Epoch: 58 | Training loss: 0.093032 | Validation loss: 0.176051
Epoch: 59 | Training loss: 0.092221 | Validation loss: 0.175765
Epoch: 60 | Training loss: 0.091432 | Validation loss: 0.175528
Epoch: 61 | Training loss: 0.090661 | Validation loss: 0.175256
Epoch: 62 | Training loss: 0.089896 | Validation loss: 0.175012
Epoch: 63 | Training loss: 0.089182 | Validation loss: 0.174785
Epoch: 64 | Training loss: 0.088416 | Validation loss: 0.174578
Epoch: 65 | Training loss: 0.087736 | Validation loss: 0.174342
Epoch: 66 | Training loss: 0.087064 | Validation loss: 0.174092
Epoch: 67 | Training loss: 0.086364 | Validation loss: 0.173871
Epoch: 68 | Training loss: 0.085735 | Validation loss: 0.173618
Epoch: 69 | Training loss: 0.085073 | Validation loss: 0.173407
Epoch: 70 | Training loss: 0.084381 | Validation loss: 0.173288
Epoch: 71 | Training loss: 0.083721 | Validation loss: 0.173147
Epoch: 72 | Training loss: 0.083203 | Validation loss: 0.172822
Epoch: 73 | Training loss: 0.082528 | Validation loss: 0.172679
Epoch: 74 | Training loss: 0.081920 | Validation loss: 0.172473
Epoch: 75 | Training loss: 0.081358 | Validation loss: 0.172270
Epoch: 76 | Training loss: 0.080778 | Validation loss: 0.172105
Epoch: 77 | Training loss: 0.080182 | Validation loss: 0.171957
Epoch: 78 | Training loss: 0.079640 | Validation loss: 0.171783
Epoch: 79 | Training loss: 0.079087 | Validation loss: 0.171620
Epoch: 80 | Training loss: 0.078536 | Validation loss: 0.171466
Epoch: 81 | Training loss: 0.078002 | Validation loss: 0.171317
Epoch: 82 | Training loss: 0.077440 | Validation loss: 0.171229
```

Now plot the training and validation history per epoch. Does your model underfit, overfit or is it about right? Explain why.

```
[28]: %matplotlib inline
fig = plt.figure()
plt.plot(range(len(loss_tr_count)),loss_tr_count,label='training loss')
```

```
plt.plot(range(len(dev_loss_count)),dev_loss_count,label='validation loss')
plt.xlabel('Epochs')
plt.ylabel('Loss')
plt.title('Training Monitoring')

plt.legend()
plt.show()
```



Conclusion: Overfitting \* Discuss Overfitting: The loss on the validation set is twice the loss on the training set, which indicates that the model overfits the training set. \* Discuss Underfitting: Both the loss on the validation set and the loss on the training set are kept at very small values. Thus there is no underfit.

Compute accuracy, precision, recall and F1-scores:

```
[29]: # Get test output from the model
preds_te_count = predict_class(X_te_count,w_count)

print('Accuracy:', accuracy_score(Y_te,preds_te_count))
print('Precision:', precision_score(Y_te,preds_te_count))
print('Recall:', recall_score(Y_te,preds_te_count))
print('F1-Score:', f1_score(Y_te,preds_te_count))
```

Accuracy: 0.835

Precision: 0.831683168316

Recall: 0.84

'movies'l

F1-Score: 0.835820895522388

Finally, print the top-10 words for the negative and positive class respectively.

```
[30]: # Stort the index by weight parameters
    sorted_index = w_count.copy().flatten().argsort()
    top_neg_ngram = [vocab[i] for i in sorted_index[:10]]
    print("Top-10 negative words:")
    print(top_neg_ngram)

Top-10 negative words:
    ['bad', 'only', 'unfortunately', 'worst', 'script', 'why', 'boring', 'plot',
    'any', 'nothing']

[31]: # Stort the index by weight parameters
    top_pos_ngram = [vocab[i] for i in sorted_index[-10:][::-1]]
    print("Top-10 positive words:")
    print(top_pos_ngram)

Top-10 positive words:
    ['great', 'well', 'seen', 'fun', 'also', 'many', 'life', 'both', 'world',
```

If we were to apply the classifier we've learned into a different domain such laptop reviews or restaurant reviews, do you think these features would generalise well? Can you propose what features the classifier could pick up as important in the new domain?

Conclusion: No, although it works, it may not work well.. \* Data distribution: Although the model can be used in other domain, the learned parameters are not. The data in the training set should be independent and identically distributed. However, after switching domains, the data may never appear in the training set, which means that the data set in this field is distributed in the training set as 0. This can lead to poor performance. \* Vocabulary Corpus: New words appearing in different domain can also lead to poor performance.

According to the existing training models and parameters, the classifier can only extract as important features the same as the training set. Extracting new features can be obtained by retraining the classifier. However, there are many words that have positive or negative emotional color. These words are especially important for classifiers even in different domain. For example, 'great' itself means positive, 'bad' itself means negative

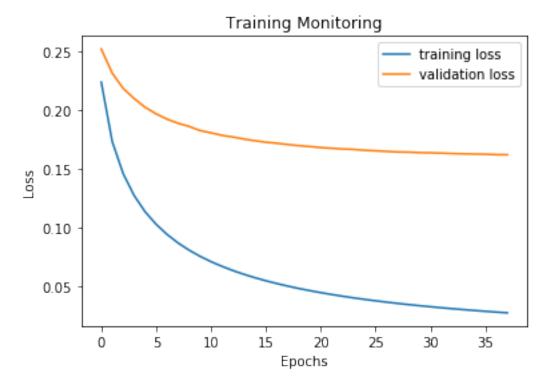
## 3.2 Train and Evaluate Logistic Regression with TF.IDF vectors

Follow the same steps as above (i.e. evaluating count n-gram representations).

```
lr=0.0006,
alpha=0.0001,
epochs=50)
```

```
Epoch: 0| Training loss: 0.224120| Validation loss: 0.252379
Epoch: 1 | Training loss: 0.173527 | Validation loss: 0.231832
Epoch: 2 | Training loss: 0.146122 | Validation loss: 0.218790
Epoch: 3 | Training loss: 0.127485 | Validation loss: 0.210185
Epoch: 4 | Training loss: 0.113679 | Validation loss: 0.202728
Epoch: 5 | Training loss: 0.103069 | Validation loss: 0.197134
Epoch: 6 | Training loss: 0.094403 | Validation loss: 0.192620
Epoch: 7 | Training loss: 0.087173 | Validation loss: 0.189145
Epoch: 8 | Training loss: 0.081058 | Validation loss: 0.186442
Epoch: 9 | Training loss: 0.075826 | Validation loss: 0.182934
Epoch: 10 | Training loss: 0.071235 | Validation loss: 0.180977
Epoch: 11 | Training loss: 0.067270 | Validation loss: 0.178854
Epoch: 12 | Training loss: 0.063653 | Validation loss: 0.177424
Epoch: 13 | Training loss: 0.060475 | Validation loss: 0.175679
Epoch: 14 | Training loss: 0.057581 | Validation loss: 0.174263
Epoch: 15 | Training loss: 0.054981 | Validation loss: 0.172982
Epoch: 16 | Training loss: 0.052593 | Validation loss: 0.172125
Epoch: 17 | Training loss: 0.050424 | Validation loss: 0.171028
Epoch: 18 | Training loss: 0.048402 | Validation loss: 0.170069
Epoch: 19 | Training loss: 0.046570 | Validation loss: 0.169303
Epoch: 20 | Training loss: 0.044854 | Validation loss: 0.168428
Epoch: 21 | Training loss: 0.043269 | Validation loss: 0.167827
Epoch: 22 | Training loss: 0.041794 | Validation loss: 0.167227
Epoch: 23 | Training loss: 0.040390 | Validation loss: 0.166867
Epoch: 24 | Training loss: 0.039114 | Validation loss: 0.166081
Epoch: 25 | Training loss: 0.037906 | Validation loss: 0.165673
Epoch: 26 | Training loss: 0.036772 | Validation loss: 0.165164
Epoch: 27 | Training loss: 0.035698 | Validation loss: 0.164713
Epoch: 28 | Training loss: 0.034687 | Validation loss: 0.164539
Epoch: 29 | Training loss: 0.033736 | Validation loss: 0.164133
Epoch: 30 | Training loss: 0.032833 | Validation loss: 0.163937
Epoch: 31 | Training loss: 0.031974 | Validation loss: 0.163667
Epoch: 32 | Training loss: 0.031172 | Validation loss: 0.163343
Epoch: 33 | Training loss: 0.030399 | Validation loss: 0.163104
Epoch: 34 | Training loss: 0.029662 | Validation loss: 0.162953
Epoch: 35 | Training loss: 0.028957 | Validation loss: 0.162770
Epoch: 36 | Training loss: 0.028295 | Validation loss: 0.162397
Epoch: 37 | Training loss: 0.027656 | Validation loss: 0.162318
```

Now plot the training and validation history per epoch. Does your model underfit, overfit or is it about right? Explain why.



Conclusion: Overfitting \* Discuss Overfitting: The loss on the validation set is 8 times larger than the loss on the training set, which indicates that the model overfits the training set. \* Discuss Underfitting: Both the loss on the validation set and the loss on the training set are kept at very small values. Thus there is no underfit.

Compute accuracy, precision, recall and F1-scores:

```
[34]: # Evaluate on test dataset
preds_te = predict_class(X_te_tfidf,w_tfidf)
print('Accuracy:', accuracy_score(Y_te,preds_te))
```

```
print('Precision:', precision_score(Y_te,preds_te))
print('Recall:', recall_score(Y_te,preds_te))
print('F1-Score:', f1_score(Y_te,preds_te))
```

Accuracy: 0.855 Precision: 0.855 Recall: 0.855 F1-Score: 0.855

print(top\_pos\_ngram)

Print top-10 most positive and negative words:

```
[35]: # Stort the index by weight parameters
    sorted_index = w_tfidf.copy().flatten().argsort()
    top_neg_ngram = [vocab[i] for i in sorted_index[:10]]
    print("Top-10 negative words:")
    print(top_neg_ngram)

Top-10 negative words:
    ['bad', 'worst', 'boring', 'supposed', 'unfortunately', 'script', 'nothing',
    'why', 'waste', 'plot']

[36]: # Stort the index by weight parameters
    top_pos_ngram = [vocab[i] for i in sorted_index[-10:][::-1]]
    print("Top-10 positive words:")
```

```
Top-10 positive words:
['great', 'fun', 'hilarious', 'terrific', 'memorable', 'perfectly', 'overall', 'truman', 'definitely', 'seen']
```

3.2.1 Discuss how did you choose model hyperparameters (e.g. learning rate and regularisation strength)? What is the relation between training epochs and learning rate? How the regularisation strength affects performance?

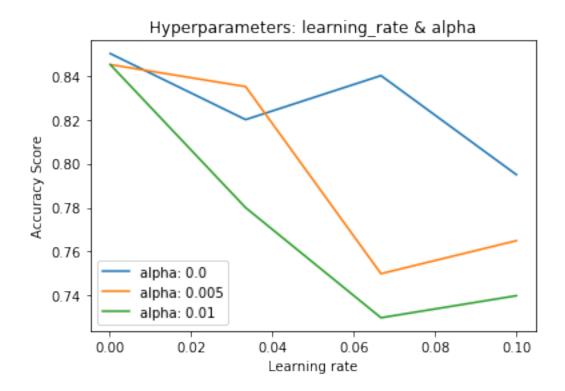
## 1. Choose Model Hyperparameters:

To choose hyperparameters, like learning rate and regularisation strength alpha, thay can be found by drawing a line chart. Basically, use grid search to find the optimal hyperparameters. This method is simple but time-consuming. Ideally, cross-validation should be used to screen the optimal hyperparameters, but because the training and validation sets have been divided, cross-validation is not very convenient. (Code of grid search is given below)

**note:** The following hyperparameter optimization has limitations. Only a fixed training set and verification set are used. Ideally, it should be divided into multiple groups and cross-validation should be used. Specifically, Leave-One-Out Cross-Validation (LOOCV) is used when drawing.

```
[37]: # Run a training on a set of hyperparameters
def get_score(lr,alpha):
    w_tfidf, trl, devl = SGD(X_tr_tfidf, Y_tr,
```

```
X_dev=X_dev_tfidf,
                         Y_dev=Y_dev,
                         lr=lr,
                         alpha=alpha,
                         epochs=100,
                         print_progress=False)
    preds_dev = predict_class(X_dev_tfidf,w_tfidf)
    return accuracy_score(Y_dev,preds_dev)
# Initial hyperparameters
fig = plt.figure()
lrs_num = 4
alphas_num = 3
lrs = np.linspace(0.0001,0.1,lrs_num)
alphas = np.linspace(0.,0.01,alphas_num)
# Run trainings on different sets of hyperparameters
for i in range(alphas_num):
    alpha = alphas[i]
    tmp = list()
    for j in range(lrs_num):
        lr = lrs[j]
        score = get_score(lr, alpha)
        tmp.append(score)
    plt.plot(lrs,tmp,label='alpha: {}'.format(alpha))
plt.xlabel('Learning rate')
plt.ylabel('Accuracy Score')
plt.title('Hyperparameters: learning_rate & alpha')
plt.legend()
plt.show()
```



As shown in the figure above, the X axis represents the learning rate, and the Y axis refers to the accuracy rate. And different colored polylines indicate different regularisation strength.

When the learning rate is increased, the model will not fully converge, and it will continue to oscillate around the lowest point. The performance of the model will also decrease. As shown in the above figure, after the three polylines increase the learning rate, the accuracy of the model will be different decline.

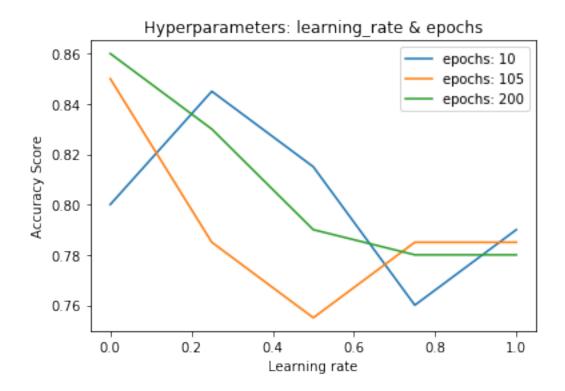
However, as the learning rate continues to increase again, the performance of the model will increase, mainly because there are other local minimum points in the direction of the gradient, and the model will converge to other local minimum values. (Think of the existence of many low-lying areas in the valley—the local minimum points, although the optimal solution is the global minimum point).

#### 2. Relationship between training epochs and learning rate:

In simple terms, the smaller the learning rate, the more epochs are needed. But there are some special cases. **Epoch:** If there are too few epochs, there may be insufficient training, resulting in underfitting. If there are too many epochs, the loss may have already converged, and the extra epochs are too wasteful of time. **Learning rate:** Too large a learning rate will not only cause data overflow, but also cause the loss function to fail to converge. Too small a learning rate will consume training time. At the same time, the convex optimization problem should also be considered, otherwise, the loss function may fall into a local minimum. It can also be observed from the line chart below.

```
[38]: # Run a training on a set of hyperparameters
def get_score(lr,epoch):
```

```
w_tfidf, trl, devl = SGD(X_tr_tfidf, Y_tr,
                         X_dev=X_dev_tfidf,
                         Y_dev=Y_dev,
                         lr=lr,
                         alpha=0.0001,
                         epochs=epoch,
                         print_progress=False)
   preds_dev = predict_class(X_dev_tfidf,w_tfidf)
   return accuracy_score(Y_dev,preds_dev)
# Initial hyperparameters
fig = plt.figure()
lrs_num = 5
epochs_num = 3
lrs = np.linspace(0.0001,1,lrs_num)
epochs = np.linspace(10,200,epochs_num,dtype=int)
# Run trainings on different sets of hyperparameters
for i in range(epochs_num):
   epoch = epochs[i]
   tmp = list()
   for j in range(lrs_num):
       lr = lrs[j]
       score = get_score(lr,epoch)
       tmp.append(score)
   plt.plot(lrs,tmp,label='epochs: {}'.format(epoch))
plt.xlabel('Learning rate')
plt.ylabel('Accuracy Score')
plt.title('Hyperparameters: learning_rate & epochs')
plt.legend()
plt.show()
```



Observing the above figure, when the epochs is not enough which refers to underfitting, such as the start of the blue polyline, increasing the learning rate can greatly help the model to converge, thereby improving the model performance (accuracy). Increasing the learning rate may not converge to the lowest point, as shown by the green and orange lines in the figure. However, when it is increased again, it may converge to the new local minimum point, just like the orange and blue lines whose accuracy started to increase again with the learning rate around 0.7.

## 3. Regularisation Strength:

Regularization prevents the classifier from overfitting by limiting the number of parameters. The regularization intensity refers to the size of the penalty. The higher the regularization intensity, the more limited the number of parameters. However, when the regularization intensity is too high, the loss function may not converge.

## 3.3 Full Results

Add here your results:

LR	Precision	Recall	F1-Score
BOW-count	0.831	0.840	0.835 $0.855$
BOW-tfidf	0.855	0.855	

# 4 Multi-class Logistic Regression

Now you need to train a Multiclass Logistic Regression (MLR) Classifier by extending the Binary model you developed above. You will use the MLR model to perform topic classification on the AG news dataset consisting of three classes:

- Class 1: World
- Class 2: Sports
- Class 3: Business

You need to follow the same process as in Task 1 for data processing and feature extraction by reusing the functions you wrote.

```
[39]: # Load dateset
      data_tr = pd.read_csv("./data_topic/train.csv", header=None,_
       →names=['label','text'])
      data te = pd.read csv("./data topic/test.csv", header=None,
       →names=['label','text'])
      data_dev = pd.read_csv("./data_topic/dev.csv", header=None,_
       →names=['label','text'])
[40]: data_tr.head()
「40]:
         label
             1 Reuters - Venezuelans turned out early\and in ...
             1 Reuters - South Korean police used water canno...
      1
             1 Reuters - Thousands of Palestinian\prisoners i...
             1 AFP - Sporadic gunfire and shelling took place...
             1 AP - Dozens of Rwandan soldiers flew into Suda...
[41]: X_tr_raw, Y_tr = transform(data_tr)
      X_te_raw, Y_te = transform(data_te)
      X_dev_raw, Y_dev = transform(data_dev)
[42]: |vocab, df, ngram_counts = get_vocab(X_tr_raw, ngram_range=(1,3),__

→keep_topN=5000, stop_words=stop_words)
      print(len(vocab))
      print()
      print(list(vocab)[:100])
      print()
      print(df.most_common()[:10])
```

5000

```
['reuters', 'said', 'tuesday', 'new', 'wednesday', 'after', 'athens', 'ap', 'monday', 'first', 'their', 'us', 'olympic', 'york', ('new', 'york'), 'two', 'over', 'but', 'oil', 'inc', 'more', 'prices', 'year', 'company', 'world', 'gt', 'lt', 'than', 'aug', 'about', 'had', 'one', 'united', 'out', 'sunday',
```

```
'against', 'up', 'quot', 'into', 'fullquote', 'second', 'last', 'stocks',
     'team', 'president', 'gold', 'percent', 'iraq', 'three', 'when', 'greece',
     'night', ('york', 'reuters'), ('new', 'york', 'reuters'), 'time', 'not', 'no',
     'games', 'yesterday', 'home', 'olympics', 'washington', 'states', 'off',
     ('united', 'states'), 'google', ('oil', 'prices'), 'day', 'public', 'billion',
     'record', ('athens', 'reuters'), 'week', 'win', 'all', 'men', 'government',
     'won', ('said', 'tuesday'), 'najaf', 'american', 'years', 'officials', 'today',
     'city', 'would', 'shares', 'offering', 'people', 'final', 'medal', 'minister',
     'afp', 'corp', 'sales', 'million', 'back', 'four', 'investor', 'com']
     [('reuters', 631), ('said', 432), ('tuesday', 413), ('wednesday', 344), ('new',
     325), ('after', 295), ('ap', 275), ('athens', 245), ('monday', 221), ('first',
     210)]
[43]: vocab tr, df_tr, ngram_counts_tr = get_vocab(X_tr_raw, ngram_range=(1,3),__
      vocab_dev, df_dev, ngram_counts_dev = get_vocab(X_dev_raw, ngram_range=(1,3),_
      →keep_topN=5000, stop_words=stop_words)
     vocab_te, df_te, ngram_counts_te = get_vocab(X_te_raw, ngram_range=(1,3),_
      ⇒keep_topN=5000, stop_words=stop_words)
     X_tr_ngram = [extract_ngrams(line,ngram_range=(1,3),stop_words=stop_words) for__
      →line in X tr raw]
     X te_ngram = [extract_ngrams(line,ngram_range=(1,3),stop_words=stop_words) for_
      →line in X_te_raw]
     X dev ngram = [extract ngrams(line,ngram range=(1,3),stop words=stop words) for___
      →line in X dev raw]
     X_tr_count = vectorise(X_tr_ngram, vocab_tr)
     X_te_count = vectorise(X_te_ngram, vocab_tr)
     X_dev_count = vectorise(X_dev_ngram, vocab_tr)
```

Now you need to change SGD to support multiclass datasets. First you need to develop a softmax function. It takes as input:

• z: array of real numbers

and returns:

• smax: the softmax of z

```
[44]: def softmax(z):

'''Calculate softmax results

In order to avoid data overflow, the corresponding data boundary is added.

Since np.exp() is a `np.float64` operation function, so we need to avoid

→overflow.
```

Then modify predict\_proba and predict\_class functions for the multiclass case:

```
[45]: def predict_proba(X, weights):
    preds_proba = X.dot(weights.T)
    assert preds_proba.shape == (X.shape[0],weights.shape[0])
    return softmax(preds_proba)
```

```
[46]: def predict_class(X, weights):
    preds_class = np.argmax(predict_proba(X, weights),axis=1)+1
    assert preds_class.shape == (X.shape[0],)
    return preds_class
```

Toy example and expected functionality of the functions above:

```
[47]: X = np.array([[0.1,0.2],[0.2,0.1],[0.1,-0.2]])
w = np.array([[2,-5],[-5,2]])
```

```
[48]: predict_proba(X, w)
```

```
[48]: array([[0.33181223, 0.66818777], [0.66818777, 0.33181223], [0.89090318, 0.10909682]])
```

```
[49]: predict_class(X, w)
[49]: array([2, 1, 1])
     Now you need to compute the categorical cross entropy loss (extending the binary loss to support
     multiple classes).
[50]: def categorical_loss(X, Y, weights, num_classes=5, alpha=0.00001):
          '''1. Calculate the probability
             2. Calculate the Euclidean distance between label and probability
             3. Calculate the average distance
          Here I use `esp` to represent the smallest data unit of the data type.
          The main function of `esp` is to ensure the rationality of arithmetic
          operations. For example, in the division operation, add 'esp' to the
          denominator to ensure that the denominator is not 0, and it does not
          affect the data result. This is the habit I developed when I wrote Matlab
          in my undergraduate period. `esp` is more common in Matlab.
          Args:
              eps: the minimum value in the current data type. Used to ensure
                   that the input of the log function is greater than O.
              preds proba: Probability of each data, the same
                  size of input data.(X.shape[0])
          Returns:
              1: Used to save losses and calculate the average at the end
          assert Y.shape[0] == X.shape[0]
          eps = np.finfo(np.float64).eps
          preds_proba = predict_proba(X, weights)
          Y = np.eye(weights.shape[0], weights.shape[0])[Y-1].reshape(X.
       \rightarrow shape [0], weights.shape [0])
          11 = -np.sum(Y*np.log10(preds proba+eps),1)
          12 = alpha*np.sum(np.multiply(weights, weights))
          l=np.mean(11)+12/X.shape[0]
          return 1
[51]: def gradient(X, Y, weights, alpha=0.00001):
          '''Only calculate the gradient of the corresponding position
```

m: the total number of the dataset sample.

Args:

```
h: an numpy array of prediction corresponding to the
dataset points. Shape (#dataset,1)

Returns:
dw: the corresponding gradient. Shape the same with
weight.

"""

m = len(X)
Y_c = Y.copy()
Y = np.eye(weights.shape[0], weights.shape[0])[Y-1].reshape(X.
→shape[0], weights.shape[0])
h = predict_proba(X, weights)
dw = -np.dot(np.sum(Y-Y*h,axis=1),X) + 2*alpha*weights[(Y_c-1).item()]

return dw/m
```

Finally you need to modify SGD to support the categorical cross entropy loss:

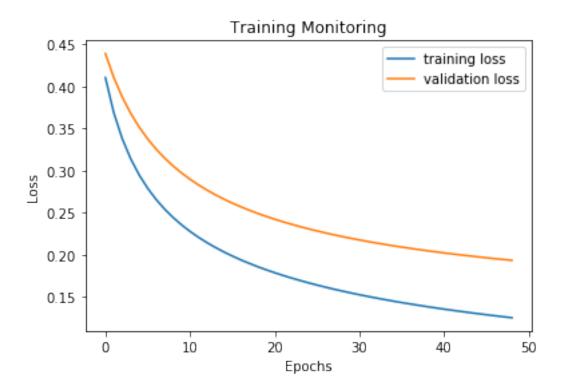
```
[52]: def SGD(X_tr, Y_tr, X_dev=[], Y_dev=[], num_classes=5, lr=0.01, alpha=0.00001,__
       →epochs=5, tolerance=0.001, print_progress=True):
          cur loss tr = 1.
          cur_loss_dev = 1.
          training loss history = []
          validation_loss_history = []
          # Stage 1: Init weights
          weights = np.zeros((num_classes, X_tr.shape[1]))
          # Stage 2: Init stochastic value
          idx_list = np.array(range(X_tr.shape[0]))
          # Stage 3: Training
          for epoch in range(epochs):
              np.random.shuffle(idx_list) # disorder dataset
              for i in idx_list:
                  X_{tr_i}, Y_{tr_i} = X_{tr_i}.reshape(1,-1), Y_{tr_i}.reshape(1,-1) # get_i
       \rightarrowa single data pair
                  dw = gradient(X_tr_i, Y_tr_i, weights, alpha) # gradient
                  weights[(Y_tr_i-1).item()] -= lr*dw # update
              loss_dev = categorical_loss(X dev, Y_dev, weights, num_classes, alpha)
              loss_tr = categorical_loss(X_tr, Y_tr, weights, num_classes, alpha)
              # Add history
              training_loss_history.append(loss_tr)
              validation_loss_history.append(loss_dev)
```

Now you are ready to train and evaluate you MLR following the same steps as in Task 1 for both Count and thidf features:

```
Epoch: 0 | Training loss: 0.410661 | Validation loss: 0.439247
Epoch: 1 | Training loss: 0.368637 | Validation loss: 0.410634
Epoch: 2 | Training loss: 0.337847 | Validation loss: 0.387376
Epoch: 3 | Training loss: 0.313983 | Validation loss: 0.368050
Epoch: 4 | Training loss: 0.294851 | Validation loss: 0.351723
Epoch: 5 | Training loss: 0.279054 | Validation loss: 0.337735
Epoch: 6 | Training loss: 0.265740 | Validation loss: 0.325617
Epoch: 7 | Training loss: 0.254328 | Validation loss: 0.315016
Epoch: 8 | Training loss: 0.244400 | Validation loss: 0.305661
Epoch: 9 | Training loss: 0.235646 | Validation loss: 0.297329
Epoch: 10 | Training loss: 0.227854 | Validation loss: 0.289844
Epoch: 11 | Training loss: 0.220857 | Validation loss: 0.283103
Epoch: 12 | Training loss: 0.214522 | Validation loss: 0.276969
Epoch: 13 | Training loss: 0.208742 | Validation loss: 0.271358
Epoch: 14 | Training loss: 0.203437 | Validation loss: 0.266208
Epoch: 15 | Training loss: 0.198552 | Validation loss: 0.261471
Epoch: 16 | Training loss: 0.194028 | Validation loss: 0.257085
Epoch: 17 | Training loss: 0.189822 | Validation loss: 0.253016
Epoch: 18 | Training loss: 0.185897 | Validation loss: 0.249232
Epoch: 19 | Training loss: 0.182211 | Validation loss: 0.245674
Epoch: 20 | Training loss: 0.178755 | Validation loss: 0.242354
Epoch: 21 | Training loss: 0.175495 | Validation loss: 0.239230
Epoch: 22 | Training loss: 0.172410 | Validation loss: 0.236284
Epoch: 23 | Training loss: 0.169492 | Validation loss: 0.233508
Epoch: 24 | Training loss: 0.166720 | Validation loss: 0.230878
Epoch: 25 | Training loss: 0.164091 | Validation loss: 0.228403
```

```
Epoch: 26 | Training loss: 0.161585 | Validation loss: 0.226052
Epoch: 27 | Training loss: 0.159193 | Validation loss: 0.223813
Epoch: 28 | Training loss: 0.156909 | Validation loss: 0.221685
Epoch: 29 | Training loss: 0.154721 | Validation loss: 0.219655
Epoch: 30 | Training loss: 0.152625 | Validation loss: 0.217726
Epoch: 31 | Training loss: 0.150611 | Validation loss: 0.215872
Epoch: 32 | Training loss: 0.148680 | Validation loss: 0.214112
Epoch: 33 | Training loss: 0.146817 | Validation loss: 0.212414
Epoch: 34 | Training loss: 0.145027 | Validation loss: 0.210791
Epoch: 35 | Training loss: 0.143300 | Validation loss: 0.209239
Epoch: 36 | Training loss: 0.141633 | Validation loss: 0.207742
Epoch: 37 | Training loss: 0.140026 | Validation loss: 0.206313
Epoch: 38 | Training loss: 0.138469 | Validation loss: 0.204927
Epoch: 39 | Training loss: 0.136965 | Validation loss: 0.203602
Epoch: 40 | Training loss: 0.135509 | Validation loss: 0.202320
Epoch: 41 | Training loss: 0.134096 | Validation loss: 0.201081
Epoch: 42 | Training loss: 0.132730 | Validation loss: 0.199895
Epoch: 43 | Training loss: 0.131402 | Validation loss: 0.198746
Epoch: 44 | Training loss: 0.130109 | Validation loss: 0.197624
Epoch: 45 | Training loss: 0.128856 | Validation loss: 0.196546
Epoch: 46 Training loss: 0.127639 Validation loss: 0.195505
Epoch: 47 | Training loss: 0.126453 | Validation loss: 0.194496
Epoch: 48 | Training loss: 0.125298 | Validation loss: 0.193514
```

Plot training and validation process and explain if your model overfit, underfit or is about right:



Compute accuracy, precision, recall and F1-scores:

```
[55]: # Evaluate on test dataset
preds_te = predict_class(X_te_count,w_count)

print('Accuracy:', accuracy_score(Y_te,preds_te))
print('Precision:', precision_score(Y_te,preds_te,average='macro'))
print('Recall:', recall_score(Y_te,preds_te,average='macro'))
print('F1-Score:', f1_score(Y_te,preds_te,average='macro'))
```

Accuracy: 0.84666666666667 Precision: 0.8508050575599119 Recall: 0.846666666666667 F1-Score: 0.8459211261526534

Print the top-10 words for each class respectively.

```
[56]: # Stort the index by weight parameters
sorted_index = w_count.copy().argsort()[:,-10:][:,::-1]
for class_i in range(len(sorted_index)):
    print("Class {}:".format(class_i+1))
    top_neg_ngram = [vocab[i] for i in sorted_index[class_i]]
    print(top_neg_ngram,'\n')
```

Class 1:

```
['said', 'tuesday', 'reuters', 'new', 'ap', 'after', 'monday', 'wednesday',
'athens', 'their']

Class 2:
['athens', 'ap', 'reuters', 'tuesday', 'olympic', 'after', 'first', 'team',
'new', 'wednesday']

Class 3:
['reuters', 'said', 'new', 'tuesday', 'oil', 'company', 'after', 'wednesday',
'prices', 'us']
```

4.0.1 Discuss how did you choose model hyperparameters (e.g. learning rate and regularisation strength)? What is the relation between training epochs and learning rate? How the regularisation strength affects performance?

## 1. Choose Model Hyperparameters:

To choose hyperparameters, like learning rate and regularisation strength alpha, thay can be found by drawing a line chart. Basically, use grid search to find the optimal hyperparameters. This method is simple but time-consuming. Ideally, cross-validation should be used to screen the optimal hyperparameters, but because the training and validation sets have been divided, cross-validation is not very convenient. (Code of grid search is given below)

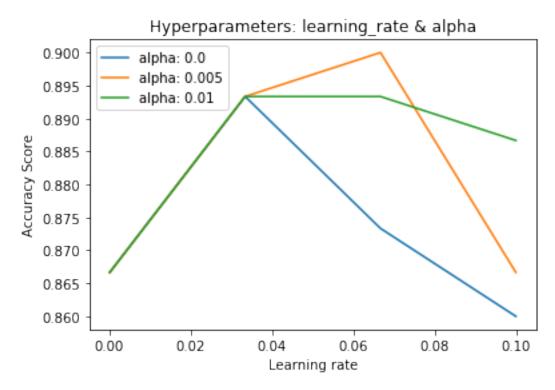
**note:** The following hyperparameter optimization has limitations. Only a fixed training set and verification set are used. Ideally, it should be divided into multiple groups and cross-validation should be used. Specifically, Leave-One-Out Cross-Validation (LOOCV) is used when drawing.

```
[57]: # Run a training on a set of hyperparameters
      def get_score(lr,alpha):
          w, trl, devl = SGD(X_tr_count, Y_tr,
                               X_dev=X_dev_count,
                               Y_dev=Y_dev,
                               num_classes=3,
                               lr=lr.
                               alpha=alpha,
                               epochs=200,
                               print_progress=False)
          preds dev = predict class(X dev count,w)
          return accuracy_score(Y_dev,preds_dev)
      # Initial hyperparameters
      fig = plt.figure()
      lrs_num = 4
      alphas_num = 3
      lrs = np.linspace(0.0001,0.1,lrs_num)
      alphas = np.linspace(0.,0.01,alphas_num)
```

```
# Run trainings on different sets of hyperparameters
for i in range(alphas_num):
    alpha = alphas[i]
    tmp = list()
    for j in range(lrs_num):
        lr = lrs[j]
        score = get_score(lr, alpha)
        tmp.append(score)
    plt.plot(lrs,tmp,label='alpha: {}'.format(alpha))

plt.xlabel('Learning rate')
plt.ylabel('Accuracy Score')
plt.title('Hyperparameters: learning_rate & alpha')

plt.legend()
plt.show()
```



As can be seen from the above figure, appropriately increasing the learning rate can make the model converge better and the model effect is better. After the three polylines increase the learning rate, they all reach their peak accuracy rates.

However, when the learning rate is increased again, the effectiveness of the model is reduced. This is mainly because the excessive learning rate will cause the value of the loss function to continuously oscillate around the local minimum point and fail to converge to a lower point.

As for the regularisation strength, there is little difference before the model has converged to the lowest point. When the learning rate reaches about 0.03, the effect of regularization begins to appear. Compared with the binary classification problem, the regularization effect is more obvious in the case of multiple classifications. For example, in the figure above, when the learning rate is around 0.07, the accuracy of the orange and green polylines is higher than that of the blue polylines, where the regularization coefficient of the blue polylines is 0. In addition, the model corresponding to the orange line performs better than the model corresponding to the green line. This shows that the regularization coefficient needs to be appropriate. If it is too large or too small, it will reduce the generalization ability of the model.

## 2. Relationship between training epochs and learning rate:

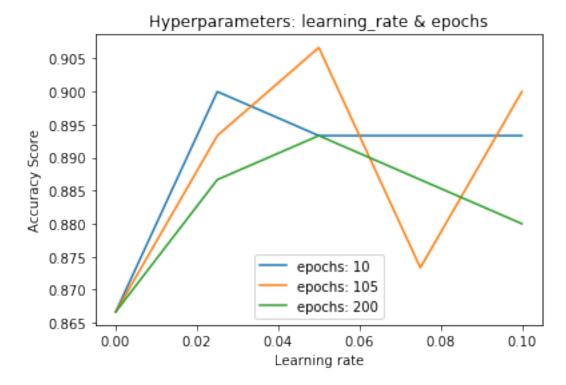
In simple terms, the smaller the learning rate, the more epochs are needed. But there are some special cases. **Epoch:** If there are too few epochs, there may be insufficient training, resulting in underfitting. If there are too many epochs, the loss may have already converged, and the extra epochs are too wasteful of time. **Learning rate:** Too large a learning rate will not only cause data overflow, but also cause the loss function to fail to converge. Too small a learning rate will consume training time. At the same time, the convex optimization problem should also be considered, otherwise, the loss function may fall into a local minimum. It can also be observed from the line chart below.

```
[58]: # Run a training on a set of hyperparameters
      def get_score(lr,epoch):
          w, trl, devl = SGD(X_tr_count, Y_tr,
                               X_dev=X_dev_count,
                                Y dev=Y dev,
                                num classes=3,
                                lr=lr,
                                alpha=0.005,
                                epochs=epoch,
                                print_progress=False)
          preds_dev = predict_class(X_dev_count,w)
          return accuracy_score(Y_dev,preds_dev)
      # Initial hyperparameters
      fig = plt.figure()
      lrs num = 5
      epochs num = 3
      lrs = np.linspace(0.0001, 0.1, lrs num)
      epochs = np.linspace(10,200,epochs_num,dtype=int)
      # Run trainings on different sets of hyperparameters
      for i in range(epochs_num):
          epoch = epochs[i]
          tmp = list()
          for j in range(lrs_num):
              lr = lrs[j]
              score = get_score(lr,epoch)
              tmp.append(score)
```

```
plt.plot(lrs,tmp,label='epochs: {}'.format(epoch))

plt.xlabel('Learning rate')
plt.ylabel('Accuracy Score')
plt.title('Hyperparameters: learning_rate & epochs')

plt.legend()
plt.show()
```



Observing the above figure, when the epochs is not enough which refers to underfitting, such as the start of all three polylines, increasing the learning rate can greatly help the model to converge, thereby improving the model performance (accuracy). Increasing the learning rate may not converge to the lowest point, as shown by all three lines in the figure. After continuing to increase the learning rate, the performance of all the models corresponding to the line has decreased to varying degrees. However, when it is increased again, it may converge to the new local minimum point, just like the orange line whose accuracy started to increase again with the learning rate around 0.1 and reach the performance peak again.

## 3. Regularisation Strength:

Regularization prevents the classifier from overfitting by limiting the number of parameters. The regularization intensity refers to the size of the penalty. The higher the regularization intensity, the more limited the number of parameters. However, when the regularization intensity is too high, the loss function may not converge.

#### 4.0.2 Now evaluate BOW-tfidf...

```
[59]: idfs_tr = get_idfs(vocab_tr,df_tr,len(X_tr_raw))
      idfs_te = get_idfs(vocab_tr,df_te,len(X_te_raw))
      idfs_dev = get_idfs(vocab_tr,df_dev,len(X_dev_raw))
[60]: X_tr_tfidf = X_tr_count*idfs_tr
      X_te_tfidf = X_te_count*idfs_te
      X_dev_tfidf = X_dev_count*idfs_dev
[61]: w_count, loss_tr_count, dev_loss_count = SGD(X_tr_tfidf, Y_tr,
                                                    X_dev=X_dev_tfidf,
                                                    Y_dev=Y_dev,
                                                    num_classes=3,
                                                    lr=0.0001,
                                                     alpha=0.001,
                                                     epochs=200)
     Epoch: 0| Training loss: 0.455029| Validation loss: 0.466185
     Epoch: 1 | Training loss: 0.436180 | Validation loss: 0.456380
     Epoch: 2 | Training loss: 0.419637 | Validation loss: 0.447402
     Epoch: 3 | Training loss: 0.404834 | Validation loss: 0.439071
     Epoch: 4 | Training loss: 0.391402 | Validation loss: 0.431271
     Epoch: 5 | Training loss: 0.379117 | Validation loss: 0.423931
     Epoch: 6 | Training loss: 0.367810 | Validation loss: 0.416998
     Epoch: 7 | Training loss: 0.357359 | Validation loss: 0.410435
     Epoch: 8 | Training loss: 0.347663 | Validation loss: 0.404208
     Epoch: 9 | Training loss: 0.338640 | Validation loss: 0.398290
     Epoch: 10 | Training loss: 0.330215 | Validation loss: 0.392653
     Epoch: 11 | Training loss: 0.322334 | Validation loss: 0.387282
     Epoch: 12 | Training loss: 0.314941 | Validation loss: 0.382153
     Epoch: 13 | Training loss: 0.307993 | Validation loss: 0.377252
     Epoch: 14 | Training loss: 0.301448 | Validation loss: 0.372562
     Epoch: 15 | Training loss: 0.295273 | Validation loss: 0.368071
     Epoch: 16 | Training loss: 0.289435 | Validation loss: 0.363763
     Epoch: 17 | Training loss: 0.283906 | Validation loss: 0.359629
     Epoch: 18 | Training loss: 0.278661 | Validation loss: 0.355658
     Epoch: 19 | Training loss: 0.273678 | Validation loss: 0.351838
     Epoch: 20 | Training loss: 0.268937 | Validation loss: 0.348161
     Epoch: 21 | Training loss: 0.264421 | Validation loss: 0.344621
     Epoch: 22 | Training loss: 0.260113 | Validation loss: 0.341207
     Epoch: 23 | Training loss: 0.255996 | Validation loss: 0.337914
     Epoch: 24 | Training loss: 0.252060 | Validation loss: 0.334735
     Epoch: 25 | Training loss: 0.248290 | Validation loss: 0.331663
     Epoch: 26 | Training loss: 0.244677 | Validation loss: 0.328693
     Epoch: 27 | Training loss: 0.241209 | Validation loss: 0.325819
     Epoch: 28 | Training loss: 0.237878 | Validation loss: 0.323038
```

```
Epoch: 29 | Training loss: 0.234674 | Validation loss: 0.320343
Epoch: 30 | Training loss: 0.231592 | Validation loss: 0.317730
Epoch: 31 | Training loss: 0.228622 | Validation loss: 0.315197
Epoch: 32 | Training loss: 0.225759 | Validation loss: 0.312739
Epoch: 33 | Training loss: 0.222996 | Validation loss: 0.310353
Epoch: 34 | Training loss: 0.220327 | Validation loss: 0.308034
Epoch: 35 | Training loss: 0.217748 | Validation loss: 0.305781
Epoch: 36 | Training loss: 0.215255 | Validation loss: 0.303590
Epoch: 37 | Training loss: 0.212840 | Validation loss: 0.301458
Epoch: 38 | Training loss: 0.210502 | Validation loss: 0.299383
Epoch: 39 | Training loss: 0.208236 | Validation loss: 0.297363
Epoch: 40 | Training loss: 0.206039 | Validation loss: 0.295395
Epoch: 41 | Training loss: 0.203906 | Validation loss: 0.293476
Epoch: 42 | Training loss: 0.201836 | Validation loss: 0.291606
Epoch: 43 | Training loss: 0.199825 | Validation loss: 0.289783
Epoch: 44 | Training loss: 0.197869 | Validation loss: 0.288003
Epoch: 45 | Training loss: 0.195968 | Validation loss: 0.286266
Epoch: 46 | Training loss: 0.194119 | Validation loss: 0.284569
Epoch: 47 | Training loss: 0.192318 | Validation loss: 0.282912
Epoch: 48 | Training loss: 0.190564 | Validation loss: 0.281293
Epoch: 49 | Training loss: 0.188856 | Validation loss: 0.279711
Epoch: 50 | Training loss: 0.187190 | Validation loss: 0.278164
Epoch: 51 | Training loss: 0.185566 | Validation loss: 0.276652
Epoch: 52 | Training loss: 0.183981 | Validation loss: 0.275172
Epoch: 53 | Training loss: 0.182434 | Validation loss: 0.273723
Epoch: 54 | Training loss: 0.180924 | Validation loss: 0.272306
Epoch: 55 | Training loss: 0.179449 | Validation loss: 0.270917
Epoch: 56 | Training loss: 0.178007 | Validation loss: 0.269557
Epoch: 57 | Training loss: 0.176598 | Validation loss: 0.268225
Epoch: 58 | Training loss: 0.175220 | Validation loss: 0.266919
Epoch: 59 | Training loss: 0.173873 | Validation loss: 0.265639
Epoch: 60 | Training loss: 0.172554 | Validation loss: 0.264384
Epoch: 61 | Training loss: 0.171264 | Validation loss: 0.263154
Epoch: 62 | Training loss: 0.170000 | Validation loss: 0.261947
Epoch: 63 | Training loss: 0.168763 | Validation loss: 0.260762
Epoch: 64 | Training loss: 0.167550 | Validation loss: 0.259600
Epoch: 65 | Training loss: 0.166362 | Validation loss: 0.258459
Epoch: 66 | Training loss: 0.165198 | Validation loss: 0.257339
Epoch: 67 | Training loss: 0.164056 | Validation loss: 0.256239
Epoch: 68 | Training loss: 0.162936 | Validation loss: 0.255158
Epoch: 69 | Training loss: 0.161838 | Validation loss: 0.254097
Epoch: 70 | Training loss: 0.160760 | Validation loss: 0.253054
Epoch: 71 | Training loss: 0.159702 | Validation loss: 0.252029
Epoch: 72 | Training loss: 0.158664 | Validation loss: 0.251021
Epoch: 73 | Training loss: 0.157644 | Validation loss: 0.250030
```

```
[62]: # Evaluate on test dataset
      preds_te = predict_class(X_te_tfidf,w_count).reshape(-1,1)
      print('Accuracy:', accuracy_score(Y_te,preds_te))
      print('Precision:', precision_score(Y_te,preds_te,average='macro'))
      print('Recall:', recall_score(Y_te,preds_te,average='macro'))
      print('F1-Score:', f1_score(Y_te,preds_te,average='macro'))
     Accuracy: 0.885555555555555
     Precision: 0.8872497496851856
     Recall: 0.8855555555555555
     F1-Score: 0.884978503362328
[63]: # Stort the index by weight parameters
      sorted_index = w_count.copy().argsort()[:,-10:][:,::-1]
      for class_i in range(len(sorted_index)):
          print("Class {}:".format(class_i+1))
          top_neg_ngram = [vocab[i] for i in sorted_index[class_i]]
          print(top_neg_ngram, '\n')
     Class 1:
     ['said', 'tuesday', 'afp', 'ap', 'monday', 'president', 'reuters', 'after',
     'their', 'people']
     Class 2:
     ['athens', 'olympic', 'ap', 'team', 'first', 'games', 'olympics', 'quot',
     'night', 'two']
     Class 3:
     ['company', 'oil', 'new', 'reuters', 'said', 'prices', 'inc', 'us', 'tuesday',
     'billion'
```

## 4.1 Full Results

Add here your results:

LR	Precision	Recall	F1-Score
BOW-count	0.850	0.846	0.845
BOW-tfidf	0.887	0.885	0.884