- [1] Building Abstractions with functions
- 1.1 Getting Started
- Computer fundamentals:

representing information

specifying logic to process it

designing abstractions that manage the complexity of that topic

- Recommended textbook: Structure and Interpretation of Computer Programs (SICP)
- 1.1.1 Programming in Python
- 1.1.2 Installing Python 3
- 1.1.3 Interactive Sessions
- In an interactive Python session, you type some Python code after the ">>>". The Python interpreter reads and executes what you type, carrying out your various commands.
- To start an interactive session, type "python3" at a terminal prompt.
- Interactive controls: each session keeps a history of what you have typed. To access that history, press [Ctrl-p] (previous) or [Ctrl-n] (next). You can exit a session with [Ctrl-d], which discards the history. Up and down arrows also cycle through history on some systems.
- 1.1.4 First Example
- Statements & Expressions: Python code consists of expressions and statements. Broadly, computer programs consist of instructions to either computer some value or carry out some actions.

 Statements typically describe actions. Expressions typically describe computations.
- Functions: functions encapsulates logic that manipulates data.
- Objects: an object seamlessly bundles together data and the logic that manipulates that data, in a way that manages the complexity of both.
- Interpreters: evaluating compound expressions requires a precise procedure that interprets code in a predictable way. A program that implements such a procedure, evaluating compound expressions, is called an interpreter. When compared with other computer programs, interpreters for programming languages are unique in their generality.
- 1.1.5 Errors
- Computers are rigid: even the smallest spelling and formatting changes can cause unexpected output and errors. Learning to interpret errors and diagnose the cause of unexpected errors is called debugging.
- Some guiding principles of debugging are:

Test incrementally

Isolate errors: trace the error to the smallest fragment of code you can before correcting it. Check your assumptions

Consult others

1.2 Elements of Programming

- Programs serve to communicate ideas among members for a programming community. Thus,
 programs must be written for people to read, and only incidentally for machines to execute.
- When we describe a language, we should pay particular attention to the means that the language provide for combining simple ideas to from more complex ideas. Each powerful language has three such mechanisms:

primitive expressions and statements: represent the simplest building blocks

means of combination: by which compound elements are built from simpler ones means of abstraction: by which compound elements can be named and manipulated as units

1.2.1 Expressions

- primitive expressions like numbers in base 10: 42
- compound expressions like numbers combined with mathematical operators: -1 -1

1.2.2 Call Expressions

- The most important kind of compound expression is a call expression, which applies a function to
- A call expression can have subexpressions.
- The order of the arguments in a call function matters.
- Function notation has three principle advantages over the mathematical convention of infix notation

functions may take an arbitrary number of arguments

function notation extends in a straightforward way to nested expressions

mathematical notations has a great variety of forms, while this complexity can be unified via the notation of call expressions

1.2.3 Importing Library Functions

• Python defines a very large number of functions, including the operator functions mentioned in the preceding section, but does not make all of their names available by default. Instead, it organizes the functions and other quantities that it knows into modules,, which together comprise the Python library. To use these elements, one imports them. Below are examples:

>>> from math import sqrt

>>> from operator import add, mul

1.2.4 Names and the Environment

- A critical aspect of a programming language it the means it provides for using names to refer to computational objects. If a value as been given a name, we say that the name binds to the value.
- In Python, we can establish new bindings using the assignment statement, like

```
>>> radius = 10
```

>>> radius

10

Here "=" is called the assignment operator. <mark>Assignment is our simplest means of abstraction</mark>.

- The possibility of binding names to values and later retrieving those values by names means that the interpreter must maintain some sort of memory that keeps track of the names, values and bindings. This memory is called an environment.
- Names can also be bound to functions, like

```
>>> f = max
>>> f
```

<built-in function max>

>>> f(1, 2, 3, 4)

 In Python, names are called variable names or variables, because they can be bound to different values in the course of executing a program. When a name is bound to a new value through assignment, it is no longer bound to any previous value. One can even bind built-in names to new values, like max.

We can assign multiple values to multiple names in a single statement, like
 area, circumference = pi * radius * radius, 2 * pi * radius
 note that after assignment, even if we change the value of radius, area will not change

(because in nature, variables are bound to values, not expressions)

- 1.2.5 Evaluating Nested Expressions
- To evaluate a call expression, Python will do the following: evaluate the operator and operand subexpressions

apply the function that is the value of the operator subexpression to the arguments that are the values of the operand subexpressions

- Note that the evaluation procedure is recursive in nature. If we draw each expression that we evaluate, we can visualize the hierarchical structure of this process. This illustrations is called an expression tree. In computer science, trees conventionally grow from the top down. The objects at each point in a tree are called nodes, here they are expressions paired with values.
- 1.2.6 The Non-Pure Print Function
- Pure functions: have some input (arguments) and return some output (the result of applying them). Pure functions have the property that applying them has no effects beyond returning a value. Moreover, a pure function must always return the same value when passed in same arguments.
- Non-pure function: can generate side effects, which make some changes to the state of the
 interpreter or computer. A common side effect is to generate additional output beyond the return
 value, using the print function. The value that print returns is always None (a special Python
 value that represents nothing)
- Below is a special case:

>>>print(print(1), print(2))

1

2

None, None

#Note that None evaluates to nothing, and will not be displayed by the interpreter as a value, like >>> None

1.3 Defining New Functions

- 3 elements which make Python and other programming languages so powerful:

 Numbers and arithmetic operations are primitive built-in data values and functions

 Nested function application provides a means of combining operations

 Binding names to values provides a limited means of abstraction
- Function definition is a much more powerful abstraction technique by which a name can be bound to compound operation, which can then be referred to as a unit.
- How to define a function:

def <name> (<formal parameters>):

return <return expression>

The return expression is not evaluated right away; it is stored as part of the newly defined function and evaluated only when the function is eventually applied.

 We can use the defined function as a building block in defining other function. Actually, userdefined functions are used in exactly the same way as built-in functions

1.3.1 Environments

- An environment in which an expression is evaluated consists of a sequence of frames, depicted as
 boxes. Each frame contains bindings, each of which associates a name with its corresponding
 value.
- global frame
- The name of a function can be repeated twice, once in the frame and again as part of the function itself. The name appearing in the function is called the intrinsic name. The name in a frame is a bound name. There is a difference between the two: different names may refer to the same function, but that function itself has only one intrinsic name. The name bound to a function in a frame is the one used during evaluation. The intrinsic name of a function does not play a role
- Function signature: a description of the formal parameters of a function, like max(...). Note that the "..." here means max can take an arbitrary number of arguments.
- 1.3.2 Calling User-Defined Functions
- Applying a user-defined function introduces a second local frame, which is only accessible to that function. To apply a user-defined function to some arguments:

Bind the arguments to the names of the function's formal parameters in a new local frame. Execute the body of the function in the environment that starts with the frame

Note that the first step: bound names, is very tricky! As we have mentioned before, binding is only between values and variable names. So here what we are really doing, is not changing names for the parameters, but evaluating their values and assigning these values to new names! [see HW1 Q5]

- Name evaluation: a name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.
- 1.3.3 Example: Calling a User-Defined Function
- 1.3.4 Local Names
- One detail of a function's implementation that should not affect the function's behavior is the implementer's choice of names for the function's formal parameters. The simplest function of it is that the parameter names of a function must remain local to the body of the function.
- 1.3.5 Choosing Names
- Important principles in choosing function and parameter names:

Function names are lowercase, with words separated by underscores. Descriptive names are encouraged.

Function names typically evoke operations applied to arguments by the interpreter, or the name of the quantity that results.

Parameter names are lowercase, with words separated by underscores. Single-word names are preferred.

Parameter names should evoke the role of the parameter in the function, not just the kind of argument that is allowed.

Single letter parameter names are acceptable when their role is obvious, but avoid 1, 0 or 1 to avoid confusion with numerals.

- 1.3.6 Functions as Abstractions
- To master the use of a functional abstraction, it is often useful to consider 3 core attributes: the domain of a function is the set of arguments it can take the range of a function is the set of values it can return

the intent of a function is the relationship it computes between inputs and output (as well as any side effects it might generate)

1.3.7 Operators

distinguish among / (normal division, which results to a floating point, or truediv in operator), //
 (rounds the result to an integer, or floordiv in operator), and % (mod)

1.4 Designing Functions

The qualities of good functions:
 each function should have exactly one job
 don't repeat yourself (DRY principle)
 functions should be defined generally

1.4.1 Documentation

- A function definition will often include documentation describing the function, called a docstring, which must be indented along with the function body. Docstrings are conventionally triple quoted. The first line describes the job of the function in one line. The following lines can describe arguments and clarify the behavior of the function.
- When you call [help] with the name of a function as an argument, you see its docstring (type [q]
 to exit), like
 - >>> help(pressure)
- Comments in Python can be attached to the end of a line following the "#" symbol

1.4.2 Default Argument Values

>>> def pressure(v, t, n = 6):

• In Python, we can provide default values for the arguments of a function. When calling that function, arguments with default values are optional. If they are not provided, then the default value is bound to the formal parameter name instead. Below is an example:

```
>>> pressure (1, 273.25) # pass in 2 parameters 2269
>>> pressure (1, 273.15, 6)
2269
```

1.5 Control

• Control statements are statements that control the flow of a program's execution based on the results of logical comparisons.

1.5.1 Statements

- So far, we have seen 3 statements already: def, assignment, and return.
- Rather than being evaluated, statements are executed. Each statement describes some change to the interpreter state, and executing a statement applies that change.

1.5.2 Compound Statements

• In general, Python code is a sequence of statements. A simple statement is a single line that doesn't end in a colon. A compound statement is so-called because it's composed of other statements. Compound statements typically span multiple lines and start with a one-line header ending in colon, which identifies the type of statement. Together, a header and an indented suite of statements is called a clause. A compound statement consists of one or more clauses.

, <h< td=""><td>neader>:</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td>•</td><td></td><td></td><td></td><td></td></h<>	neader>:									•				
	<statement></statement>				0								0	
	<statement></statement>													
< S	eparating header>:													
	<statement></statement>													
	<statement></statement>													
· We	can catalog the sta	temer	ntş w	e hav	e lear	nt:								
E>	opressions, return s	tatem	ent,	and a	ssignm	nent s	taten	nents	are si	mple	stater	nents.		
	def statement is a													
	can understand mul													ne first
	ement. If that stat													
	ence of statements				i edii e	دا ،دن		IIICII	proce	eu .10	CACCO		e 1,es1	oi me
					+			•						
	efining Functions I													C::11:
	never a user-define													
	ecuted in a local e													
	function. A return													
	first return statem				and t	he va	lue of	f the i	returr	expr	ession	is, th	e retu	urned
value	of the function be	eing a	pplied	d	0								0	
	conditional Stateme													
A cor	nditional statement	in Py	thon	consi	sts of	a ser	ries of	head	ers ar	nd sui	ts: a r	require	ed "if	" clause
an or	otional sequence of	"elif"	clau	ises, d	and, fin	nally o	an opt	ional	"else"	claus	e:		0	
>>	> if <expression>:</expression>													
	<suite></suite>													
>>	> elif <expression>:</expression>													0
	<suite></suite>													
· >>	> else:													
	<suite></suite>		•	•	•	•	•				•	•	•	•
• The	computational proc	ess of	exec	utina	a con	dition	al cla	use fo	ollows			•	٠	•
	valuate th header's				u ,0011		iai joio		J.1.0.1.10		•			•
	it is a true value,				ta Th	on cl	in all	subse	auan:	Folau	sas in	the c	onditi	ional
		evecc	116 11	ie sui	16. 111	le11, 31	vip aii	SUDSE	equen	ı cıau	3E3 III	IIIe C	Jonain	Origi
statem		, ha h-			, ma-1-	·	ond:L:	المالم صد	Lanks	ana !	h a al -		n t c t	
	expressions inside t													
	n value matter to c													
Pyth	on includes several	false	value	es, inc	cluding	0, N	one, "	", [], (and th	e boo	lean v	alue !	False.	All

• Python has two boolean values: True and False.

other numbers are true values.

- Python has three boolean operators: and, or, and not, the first two of which has the so-called short-circuit evaluation behavior.
- 1. [not] returns the opposite truth value of the following expression (so not will always return either True of False).
- 2. [and] evaluates expressions in order and stops evaluating (short-circuits) once it reaches the first false value, and then returns it. If all values evaluate to a true value, the last value is

0	returnea.													
3.	[or] short-circuits at	the first	true	value	and	retur	ns it.	If all	value	s eva	luate	to a	false	value,
	the last value is retu	ırned.												
>>>	not None					0								
Tru	ue,													
>>>	-1 and 0 and 1													
0						0								0
>>>	False or 999 or 1/0													
99	9													
1.5	5.5 Iteration													
. /	A while clause structu	re is like:												
	>>> while <expression< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></expression<>													
	<suite></suite>													•
1.5	5.6 Testing													•
	Testing a function is tl	he act of	verif	vina t	hat t	he fu	unction	n's bel	havior	mate	hes e	xpect	ations	. A
	test is a mechanism fo													
	of another function th													
	returned value is then													
	meant to be general, t													
	Tests also serve as do													
	values are suitable.			,		•							ş g	.,
	assert: when the expr	ession bei	na as	serte	d eva	luate:	s to a	true	· value.	exec	utina	an as	sert	•
	statement has no effe													•
	execution.					,, u.								0
•	>>> assert f(8) == 1	3				•	•			•		•	•	•
•	>>> def f_test():					•	•	•		•			•	•
•	assert f(2) ==	1			•	0	•	•		•		•	•	0
	assert f(3) ==					•	•	•		•	•		•	
٠	assert f(50) ==				•	0	•	•	•	•	•	•	•	0
• [Python provides a conv		ethod	for n	lacin	n simi	ole te	sts dir	· ·ectly	in th	e doce	trina	of a	0
	function. THE first line													•
	followed by a blank lin													0
	addition, the docstring													n the
	nteraction can be veri												i, ilie	11, 1116
•	>>> def f(n):	rieu via į	ne uo	cresi	illoud	AIE. D	elow i	3 411 6	zamp	ie oi	usage	•	•	0
	""" Return the	sum of t	ha fi	rct n	oloma	onts		•	•	•	•	•		•
	, Kejuili ille	sain or i	ne n	131 11	eteine	șiiis.	0			•			•	0
	>>> f(2)					0		•	•	•				0
							•			•		•	•	
•	55				•	6	•	•		•			0	0
	>>> f(10)				•	0		•						•
	458				•					•	•			
•					•	•	•	•		•				0
	>>> from doctest im	port testi	mod											

```
>>> testmod()
          TestResults(failed = 0, attempted = 2)

    When writing Python in files, rather than directly into the interpreter, tests are typically

  written in the same file or a neighboring file with the suffix "_test.py". Then all doctests can be
  run by starting Python with the doctest command line option: [python3 -m doctest (-v)
  <python_file>]
• A test that applies a single function is called a unit test.
1. To prevent the ok autograder from interpreting print statements as output: print with 'DEBUG:'
   at the front of the outputted line
2. To open n interactive terminal to investigate a failing test for question sum_digits in assignment
   lab01: [python3 ok -q sum_digits -i]
3. To look at an environment diagram to investigate a failing test for question sum_digits in
   assignment lab01: [python3 ok -q sum_digits —trace]
1.6 Higher-Order Functions

    We need to construct functions that can accept other functions as arguments, or return

  functions as values. Functions that manipulate functions are called higher-order functions.
1.6.1 Functions as Arguments
Below is an example:
     >>> def summation(n, term):
          ... ...
    >>> def identity(x):
     >>> def sum_naturals(x, identity):
1.6.2 Functions as General Methods

    With higher-order functions, we begin to see a more powerful kind of abstraction: some functions

  express general methods of computation, independent of the particular functions they call.

    We learnt about two related big ideas in computer science:

    Naming and functions allow us to abstract away a vast amount of complexity.

2. It is only by virtue of the fact that we have an extremely general evaluation procedure for the
   Python language that small components can be composed into complex processes.
• 1.6.3 Defining Functions III: Nested Definitions
• There are two negative consequences of passing functions as arguments:
1. The global frame becomes cluttered with names of small functions, which must all be unique.
2. We are constrained by particular function signatures
-> Nested function definitions address both of these problems, but require us to enrich our
environment model.
Below is an example:
     >>> def sqrt(a):
         def sqrt_update(x):
               return average(x, a/x)
         def sqrt_close(x):
```

```
return approx_eq(x * x, a)
          return improve(sqrt_update, sqrt_close)
     Note that we now place function definitions inside the body of other definitions.
• Like local assignment, local def statements only affect the local frame. These functions are only
  in scope while sart is being evaluated. Locally defined functions also have access to the name
  bindings in the scope in which they are defined. This discipline of sharing names among nested
  definitions are called lexical scoping.
• We require two extensions to our environment model to enable lexical scoping:
1. Each user-defined function has a [parent environment where it was defined.
2. When a user-defined function is called, its local frame extends its parent environment.
• Functions values each have a new annotation that we will include in environment diagrams from
  now on: a parent. The parent of a function value is the first frame of the environment in which
  that function was defined. Functions without parent annotations were defined in the global
  environment. When a user-defined function is called, the frame created has the same parent as
  that function.
1.6.4 Functions as Returned Values

    Function composition: h(x) = f(q(x))

1.6.5 Example: Newton's Method
1.6.6 Currying
• Given a function f(x, y), we can define a function q such that q(x)(y) = f(x, y). Here, q is a higher-
  order function that takes in a single argument x and returns another function that takes in a
  single argument y. This transformation is called <mark>currying</mark>. Currying is useful when we require a
  function that takes in only a single argument (like the map function).
• Inverse Currying transformation:
1. given f, return g <-currying
>>> def curry(f):
     def g(x):
          def h(y):
               return f(x, y)
          return h
     return g
2. given g, return f <-uncurrying
>>> def uncurry(g):
     def f(x, y):
          return q(x)(y)
     return f
>>> uncurry(curry(f))
f
1.6.7 Lambda Expressions
• In Python, we can create function values on the fly using lambda expressions, which evaluate to
  unnamed functions. A lambda expression evaluates to a function that has a single return
  expression as its body. Assignment and control statements are not allowed. Below is an example:
```

>>> def compose(f, g):

return lambda x: f(g(x))

We can understand the s	tructure	of a la	ambda e	xpression	by co	nstruct	ing a	corres	ponding	g sent	ence:
lambda	x	: .	•	f(g(x))							
A function that take	s x, and	l return	ns f(g	g(x))							
• The result of a lambda	express	ion is c	alled a	lambda f	unction	. It has	no i	ntrinsic	name	, but	
otherwise it behaves li	ke any o	ther fu	nction.								
>>> s = lambda x; x* x											
>>> S											
<function <lambda=""> at 0x</function>	f3f490>										
>>> s(12)											
144											
>>> (lambda x: x*x)(12)											
.144											
• The main difference be	tween la	ımbda e	expressi	ons and c	lef sta	tements	is th	at, onl	y the	def	
statements give the fu	nction in	trinsiç	names.	All lamba	la expr	essions	share	the n	ame [G	reek	
letter(x)]											
• There is one key point	about la	mbda e	xpression	ons: they	cannot	recurs	ively	call th	emselv	es.	
>>> $h = lambda x: f(h(x))$	#wrong										
>>> h = (lambda g:lambda	x: f(g(x)) is)(h)	#corre	ect .							
1.6.8 Abstractions and Fi	rst-Class	Functi	ions								
• Programming languages	impose	restrict	tions on	the way	s in wh	ich com	puta	ional e	lemen	ts car	be
manipulated. Elements	with the	fewes	t reștric	ctions are	said t	o be ho	ive fi	rsț-cla	ss stat	us. S	ome
of the "rights and privi	ileges" of	f first-	class el	ements a	re:						
1 There were be becaut to	o namas										
1. They may be bound t	o mames.		0						0		0
2. They may be passed			function	ons.							
	as argum	ents to				•		0			0 0
2. They may be passed	as argum d as the	ents to results	of fund		0	0	•	•			0 0
 They may be passed They may be returned 	as argum d as the l in data	ents to results structu	of fund ures.	ctions.	be ma	nipulate	ed as	values.	They	are	0 0
 They may be passed They may be returned They may be included 	as argum d as the l in data n nature,	ents to results structu are fu	of fund ures, nctions	ctions. that can							nction
 They may be passed of They may be returned They may be included First-class functions, in 	as argum d as the l in data n nature,	ents to results structu are fu	of fund ures, nctions	ctions. that can							nction
 They may be passed They may be returned They may be included First-class functions, in opposite to higher-order 	as argum d as the l in data n nature, er functio	ents to results structu are fu	of fund ures, nctions	ctions. that can							nction
 2. They may be passed of 3. They may be returned 4. They may be included First-class functions, in opposite to higher-order as a return value 	as argum d as the I in data n nature, er functions	ents to results structu are fu ons, whi	of fund ures, nctions ich take	ctions. that can function	ns as an	rgumen:	t yalu	es, or	return	a fur	nction
 2. They may be passed of 3. They may be returned 4. They may be included • First-class functions, in opposite to higher-order as a return value 1.6.9 Function Decorators 	as argum d as the l in data n nature, er functions s l syntax	ents to results structu are fui ons, whi	of fundares. nctions ich take	ctions. that can function	unction	rgumen is as pa	t yalu	es, or	return	a fur	nction
 They may be passed of They may be returned They may be included First-class functions, in opposite to higher-order as a return value 1.6.9 Function Decorators Python provides special 	as argum d as the l in data n nature, er functions s l syntax	ents to results structu are fui ons, whi	of fundares. nctions ich take	ctions. that can function	unction	rgumen is as pa	t yalu	es, or	return	a fur	nction
 They may be passed of They may be returned They may be included First-class functions, in opposite to higher-order as a return value 1.6.9 Function Decorators Python provides special statement, called a decorate 	as argum d as the l in data n nature, er functions s l syntax	ents to results structu are fui ons, whi	of fundares. nctions ich take	ctions. that can function	unction	rgumen is as pa	t yalu	es, or	return	a fur	nction
 They may be passed of the statement, called a despectation. They may be included to the first-class functions, in opposite to higher-order as a return value. Python provides special statement, called a despectation. 	as argum d as the l in data n nature, er function s l syntax ecorator	ents to results structu are fui ons, whi	of fundares. nctions ich take	ctions. that can function	unction	rgumen is as pa	t yalu	es, or	return	a fur	nction
 They may be passed of the statement, called a def wrapped(x): 	as argum d as the l in data n nature, er function s l syntax ecorator	ents to results structu are fui ons, whi	of fundares. nctions ich take	ctions. that can function	unction	rgumen is as pa	t yalu	es, or	return	a fur	nction
 They may be passed of the passe	as argum d as the l in data n nature, er function s l syntax ecorator	ents to results structu are fui ons, whi	of fundares. nctions ich take	ctions. that can function	unction	rgumen is as pa	t yalu	es, or	return	a fur	nction
 They may be passed of the passe	as argum d as the l in data n nature, er function s l syntax ecorator	ents to results structu are fui ons, whi	of fundares. nctions ich take	ctions. that can function	unction	rgumen is as pa	t yalu	es, or	return	a fur	action
 They may be passed of the passe	as argum d as the l in data n nature, er function s l syntax ecorator	ents to results structu are fui ons, whi	of fundares. nctions ich take	ctions. that can function	unction	rgumen is as pa	t yalu	es, or	return	a fur	nction
 They may be passed of the statement of the s	as argum d as the l in data n nature, er function s l syntax ecorator	ents to results structu are fui ons, whi	of fundares. nctions ich take	ctions. that can function	unction	rgumen is as pa	t yalu	es, or	return	a fur	nction
 They may be passed of the statement of the s	as argum d as the l in data n nature, er function s l syntax ecorator	ents to results structu are fui ons, whi	of fundares. nctions ich take	ctions. that can function	unction	rgumen is as pa	t yalu	es, or	return	a fur	nction
 They may be passed of the statement of the s	as argumd as the lin data n nature, er functions l syntax ecorator.	ents to results structu are fui ons, whi to appl Below	of fund ures. nctions ich take y highe is the n	ctions. that can function	unction	rgumen is as pa	t yalu	es, or	return	a fur	nction
 They may be passed of the statement of the s	as argumd as the lin data n nature, er functions l syntax ecorator.	ents to results structu are fui ons, whi to appl Below	of fund ures. nctions ich take y highe is the n	ctions. that can function	unction	rgumen is as pa	t yalu	es, or	return	a fur	action
 They may be passed of the statement of the s	as argumd as the lin data n nature, er functions l syntax ecorator.	ents to results structu are fui ons, whi to appl Below	of fund ures. nctions ich take y highe is the n	ctions. that can function	unction	rgumen is as pa	t yalu	es, or	return	a fur	nction

>>> def triple(x): return 3*x

>>> triple = trace(triple)

• The decorator symbol "@" may also be followed by a call expression. The expression following @ is evaluated first (just as the name trace was evaluated first), the def statement second, and finally the result of evaluating the decorator expression is applied to the newly defined function, and the result if bound to the name in the def statement.

1.7 Recursive Functions

- A function is called recursive if the body of the function calls the function itself.
- 1.7.1 The Anatomy of Recursive Functions
- A common pattern can be found in the body of many recursive functions. the body begins with a
 base case, a conditional statement that defines the behavior of the function for the inputs that
 are simplest to process. Some recursive functions will have multiple base cases. They are then
 followed by one or more recursive calls, which always have a certain character: they simplify the
 original problem incrementally.
- Treating a recursive call as a functional abstraction has been called a recursive leap of faith.

 We define a function in terms of itself, but simply trust that the simpler cases will work

 correctly when verifying the correctness of the function. Verifying the correctness of a recursive
 function is a form of proof by induction.

1.7.2 Mutual Recursion

- When a recursive procedure is divided among two functions that call each other, the functions are said to be mutually cursive.
- 1.7.3 Printing in Recursive Functions
- 1.7.4 Tree Recursions
- Another common pattern of computation is called tree recursion, in which a function calls itself more than once.
- A function with multiple recursive calls is said to be tree recursive, because each of call branches into multiple smaller calls, each of which branches into yet smaller calls, just as the branch of a tree become smaller but more numerous as they extend from the trunk.
- 1.7.5 Example: Partitions

[2] Building Abstract	ions w	ith Da	ta						•				0		
2.1 Introduction															
2.1.1 Native data Ty	pes														
• Every value in Pyt	họn hơ	as a cl	ass th	nat de	ețermi	ines w	hat t	ype o	fvalu	e it is	. The	built-	in [ty	pe]	
function allows us	to ins	pect t	he cla	ass of	any	value.									
>>> type(2)															
<class 'int'=""></class>															
• Native data types	have	the fol	lowin	g pro	pertie	s;									
1. There are expres	sions	that e	valua	te to	value	s of r	ative	types	, calle	ed lite	rals.				
2. There are built-i	n func	ctions o	and of	perat	ors to	mani	pulate	value	es of	native	type	s.			
• Python includes th	ree ni	umeric	types	s: int	(inted	jers),	float	(real	numbe	ers) an	nd con	nplex	(comp	lex	
numbers).															
• The difference bet	ween	int and	d floo	ıt is v	ery ir	nport	ant: in	t obj	ects r	epres	ent in	teger	exac	tly;	
float objects can i															
represented exact															
• There are also non		eric tyl	pes of	fdata	ı, sucl	n as t	he bo	ol clas	ss for	value	s Tru	e and	False.		
2.2 Data Abstraction	1		•	•	0	•	•	•					•	٠	0
• The general techni		f isola	ina t	he pa	rts of	a pr	oaram	that	deal	with h	ow d	ata ar	e	•	
represented from														•	•
methodology called														an.	•
maintain, and modi															
2.2.1 Example: Ratio		umbers													
2.2.2 Pairs															
• List:		•													
>>> pair = [10, 20]	•	•		•		•							٠	•	۰
>>> x, y = pair	•			•	•	•	•	•			•	•	•	•	
>>> X															
10													•		
>>> pair[0]															
10															
>>> from operator im	port c	etitem	1				•						•		
>>> getitem(pair, 0)		,			•	•	•	•			•	•		•	
10		•		•	٠	٠	•	•			•	•	0	٠	0
2.2.3 Abstraction Ba	rriers	•			•		•						٠		
• Function can be div			veral	laver	s of a	ıbstra	ction.	In e	ich la	ver. t	he fui	nction:	s enfa	rce ai	n
abstraction barrie															
level of abstractio															+
can use higher lev												- F	F 3		
2.2.4 The Properties			,					,55	,,,,,		•	٠	٠	٠	0

- 2.3 Sequences
- A sequence is an ordered collection of values. There are many different kinds of sequences, but they all share common behaviors:
- 1. A sequence has a finite length. An empty sequence has length 0.
- 2. A sequence has an element corresponding to any non-negative integer index less than its length, starting from 0 for the first element.

```
2.3.1 Lists
```

```
>>> digits = [1, 8, 2, 8]
>>> len(digits)
4
```

```
>>> [2, 7] + digits * 2
```

30

2.3.2 Sequence Iteration

- In many cases, we would like to iterate over the elements of a sequence and perform some computation for each element in turn. This pattern is so common that Python has an additional control statement to process sequential data: the for loop.
- A for statement consists of a single clause with the form:

for <name> in <expression>:

<suite>

And a for statement is executed by the following procedure:

- 1. Evaluate the header <expression>, which must yield an iterable value.
- 2. For each element value in that iterable value, in order:
 - 1. Bind <name> to that value in the current frame
 - 2. Execute the <suite>
- A common pattern in programs is to have a sequence of elements that are themselves sequences, but all of a fixed length. A for statement may include multiple names in its header to "unpack" each element sequence into its respective elements. Such pattern of binding multiple names to multiple values in a fixed-length sequence is called sequence unpacking.

```
>>> pairs = [[1, 2], [2, 2], [2, 3], [3, 4]]
```

>>> same = False

>>> for x, y in pairs:

same = True

>>> same

True

- A range is another built-in type of sequence in Python, which represents a range of integers. range takes in two integer arguments: the first number and one beyond the last number in the desired range. If only one argument is given, it is interpreted as one beyond the last value for a range that starts at 0.
- A common convention is to use a single underscore character for the name in the for header if the name is unused in the suite. This underscore is just another name in the environment as far

as the interpreter is concerned, but has a conventional meaning among programmers that indicates the name will not appear in any future expressions.

2.3.3 Sequence Processing

• Many sequence processing operations can be expressed by evaluating a fixed expressions for the sequence processing operations.

Many sequence processing operations can be expressed by evaluating a fixed expressions for each
element in a sequence and collecting the resulting values in a result sequence. In Python, a list
comprehension is an expression that performs such a computation.

```
>>> odds = [1, 3, 5, 7, 9]
>>> [x+1 for x in odds]
```

[2, 4, 6, 8, 10]

Notice the above for keyword is contained within square brackets, therefore, it is not part of a for statement, but instead part of a list comprehension. The subexpression x+1 is evaluated with x bound to each element of adds in turn, and the resulting value are collected into a list.

• List comprehension can also help to select a subset of values that satisfy some condition.

```
>>> [x for x in odds if 25 % x == 0]
```

[1, 5]

The general form of a list comprehension is

[<map expression> for <name> in <sequence expression> if <filter expression>]

To evaluate a list comprehension, Python evaluates the «sequence expression», which must return an iterable value. Then, for each element in order, the element value is bound to «name», the filter expression is evaluated, and if it yields a true value, the map expression is evaluated. The values of the map expression are collected into a list.

- A third common pattern in sequence processing is to aggregate all values in a sequence into a single value. The built-in functions sum, min, and max are all examples.
- The common patterns we have observed in sequence processing can be expressed using higherorder functions.
- 2.3.4 Sequence Abstraction
- A value can be tested for membership in a sequence. Python has two operators [in] and [not in] that evaluates to True or False depending on whether an element appears in a sequence.

>>> digits

[1, 8, 2, 8]

>>> 2 in digits

True

• Sequence contain smaller sequences within them. A slice of a sequence is any contiguous span of the original sequence, designated by a pair of integers. As with the range constructor, the first integer indicates the starting index of the slice and the second indicates one beyond the ending index. In Python, sequence slicing is expressed similarly to element selection, using square brackets. A colon separates the starting and ending indices. Any bound that is omitted is assumed to be an extreme value: O for the starting index, and the length of the sequence for the ending index.

```
>>> digits[0:2]
```

[1, 8]

>>> digits[1;]

[8, 2, 8]

2.3.5 Strings

- The native data type for text in Python is called a string, and corresponds to the constructor str.
- String literals can express arbitrary text, surrounded by either single or double quotation marks (If you use double quotes, then you can use single quotes inside of it. Otherwise you cannot.).
- The elements of a string are themselves strings that have only a single character. A character is
 any single letter of the alphabet, punctuation mark, or other symbol. Unlike many other
 programming languages, Python does not have a separate character type.
- Like lists, strings can also be combined via addition and multiplication.

>>> 'Berkeley' + ', CA'

'Berkeley, CA'

>>> 'Shabu' * 2

'Shabu Shabu'

• The membership operator [in] applies to strings, but has an entirely different behavior than when it is applied to sequences. It matches substrings rather than elements.

>>> 'here' in 'Where's she'

True

- Strings are not limited to a single line. Triple quotes delimit string literals that span multiple
 lines. '\n' is a single element that represents a new line, and is considered a single character for
 the purpose of length and element selection.
- A string can be created from any object in Python by calling the str constructor function with an
 object value as its argument

2.3.6 Trees

- Our ability to use lists as the elements of other lists provides a new means of combination in our
 programming language. The ability is called a closure property of a data type. In general, a
 method for combining data values has closure property if the result of combination can itself be
 combined using the same method. Closure is the key to power in any means of combination
 because it permits hierarchical structures.
- Nesting lists within lists can introduce complexity. The tree is a fundamental data abstraction that imposes regularity on how hierarchical values are structured and manipulated. A tree has a root label and a sequence of branches. Each branch of a tree is a tree. A tree with no branches is called a leaf. Any tree contained with a tree is called a sub-tree of that tree. The root of each sub-tree is called a node in that tree. A tree is well-formed only if it has a root label and all branches are also trees.

2.3.7 Linked Lists

- A common representation of a sequence constructed from nested pairs is called a linked list.
- Linked lists have recursive structure: the rest of a linked list or 'empty'.

2.4 Mutable Data

We need strategies to help us structure large systems to be modular, meaning that they divide
naturally into coherent parts that can be separately developed and maintained. One powerful
technique for creating modular programs is to incorporate data that may change state over time.
In this way, a single data object can represent something that evolves independently of the rest
of the program. Adding state to data is a central ingredient of a paradigm called object-oriented
programming.

2.4.1 The Object Metaphor

- Objects combine data values with behavior. Objects are both information and processes, bundled together to represent the properties, interactions, and behaviors of complex things.
- >>> from datetime import date

The name [date] is bound to a class. As we have seen, a class represents a kind of value. Individual dates are called instances of that class. Instances are constructed by calling the class on arguments that characterize the instance.

Objects have attributes, which are named values that are part of the object. in Python, like
many other programming languages, we use dot notation to designate an attribute of an object.
 expression>.

The <expression> evaluates to an object, and <name> is the name of an attribute for that object. These attributes are not available in the general environment.

- Objects also have methods, which are function-valued attributes. By implementation, methods are functions that compute their values from both their arguments and their object. The expression for attribute also applies to methods.
- All values in Python are objects.
- 2.4.2 Sequence Objects
- Instances of primitive built-in values such as numbers are immutable. The values themselves cannot change over the course of program execution. Lists on the other hand are mutable.
- Mutable objects are used to represent values that change over time. An object may have changing properties due to muting operations. Most changes are performed by invoking methods on list objects.
- Here are many list modification operations:
- >>> chinese = ['coin', 'string', 'myriad']
- >>> suits = chinese
- >>> suits.pop()

'myriad' #remove and return the final element

- >>> suits.remove('string') #remove the first element that equals the argument
- >>> suits.append('cup') #add an element to the end
- >>> suits.extend(['sword', 'club']) #add all elements of a sequence to the end
- >>> suits[2] = 'spade' #replace an element
- >>> suits[0:2] = ['heart', 'diamond'] #replace a slice
- >>> suits

['heart', 'diamond', 'spade', 'club']

Note all of these mutation operations change the value of the list; they do not create new list objects. Since the object bound to the name chinese has also changed, because it is the same list object that was bound to suits! This behavior is different from what we have learned from primitive data types. With mutable data, methods called on one name can affect another name at the same time.

• Lists can be copied using the [list] constructor function. Changes to one list do not affect another, unless they share structure.

>>> new = list(suits)

Note that we can use slicing to shallow copy lists, but actually the mechanism is: for lists or something that we must store in memory (not other prmitive data types like ints), we copied the references to them instead of the items themselves. Therefore, I can say that both elements [is]

the same thing, but modifying one element means changing that reference without change the item, and the other will not be affected. >>> suits.insert(2, 'Joker') #insert an element at index 2, shifting the rest Because two lists may have the same contents but in fact be different lists, we require a means to test whether two objects are the same. Python includes two comparison operators, called [is] and [is not], that test whether two expressions in fact evaluate to the identical object. Two objects are identical if they are equal in their current value, and any change to on will always be reflected in the other. Identity is a stronger condition than equality. >>> suits is ['heart, 'diamond', 'spade', 'club'] #check for identity >>> suits == ['heart, 'diamond', 'spade', 'club'] #check for equality • A list comprehension always creates a new list. • It is very dangerous to use a mutable data type as the default value for a function argument (list lists). It is because in the function definition of Python, all default values for function arguments are only computed once, instead of computing each time the function is called. Therefore, every time the function is called, its default value will be changed (since it is mutable). A tuple, an instance of the built-in tuple type, is an immutable sequence. Tuples are created using a tuple literal that separates element expressions by commas. Parentheses are optional but used commonly in practice. Any objects can be placed into tuples. >>> 1, 2 + 3 (1, 5)There are also empty and one-element tuples which has special syntax. >>> () 0 >>> tuple() >>> (10,) (10,)Here are some methods of tuples which are shared between it and lists: in & not in; mul and add; len; []; slice >>> code = (1, 1, 2, 2, 3, 4, 3, 4) >>> code.count(2) 2 >>> code.index(3) 4 But note that the methods for manipulating the contents of a list are not available for tuples, because they are immutable. It is possible to change the value of a mutable element contained within a tuple. >>> nested = (10, 20, [30, 40]) >>> nested[2].pop()

Note that you can change the elements inside of a mutable element, but you cannot change the

```
whole element itself, for it is part of the immutable tuple.
>>> lst = [1, 2, [0]]
>>> lst[2] = [1]
Tuples are often used implicitly in multiple assignment. An assignment of two values to two names
creates a two-element tuple and then unpacks it.
2.4.3 Dictionaries

    Dictionaries are Python's built-in data type for storing and manipulating correspondence

  relationships. A dictionary contains key-value pairs, where both the keys and values are objects.
  The purpose of a dictionary is to provide an abstraction for storing and retrieving values that are
  indexed not by consecutive integers, but by descriptive keys.
• Look up values:
>>> numerals = ['i': 1.0, 'v': 5, 'x':10]
>>> numerals['x']
10

    A dictionary can have at most one value for each key. Adding new key-value pairs and changing

  the existing value for a key can both be achieved with assignment statements:
>>> numerals['i'] = 1
>>> numerals['l'] = 50
Note that the newly added key-values pair is not added to the end of the dictionary, because
dictionaries are unordered collections of key-value pairs. When we print a dictionary, the keys are
values are rendered in some order, but as users of the language we cannot predict what the order
will be. The order may change when running a program multiple times.
• The methods keys, values and items all return iterable values.
• A list of key-value pairs can be converted into a dictionary by calling the [dict] constructor.
• Dictionaries have some restrictions:
1. A key of a dictionary cannot be or contain mutable value.
2. There can be at most one value for a given key.
According to the first restriction, tuples are often used as keys in dictionaries instead of lists. On
the other hand, a list not allowed be used as keys for dictionaries (unhashable list). Tuples can
contain anything, including lists; but those containing a list as an element cannot be used as keys.
• A useful method implemented by dictionaries is [get], which returns either the value for a key, if
  the key is present or a default value. The arguments to get are the key and the default value.
>>> numerals.get('a', 0)
0
>>> numerals.get(`v', 5)
• We can also remove one key-value pair using key
>>> numerals.pop('v')
5

    Dictionaries have a comprehension syntax analogous to those of lists. A key expression and a vaue

  expression are separated by a colon. Evaluating a dictionary comprehension creates a new
  dictionary object.
>>> [x: x * x fr x in range(3, 6)]
```

[3:9;4:16;5:25]

2.4.4 Local State

- Lists and dictionaries have local state: they are changing values that have some particular
 contents at any point in the execution of a program. The word "state" implies an evolving process
 in which that state may change.
- Functions can also have local state.
 nonlocal balance

The nonlocal statement declares that whenever we change the binding of the name balance, the binding is changed in the first frame in which balance is already bound. If balance has not previously been bound to a value, then the nonlocal statement will give an error.

- Ever since we first encountered nested def statements, we have observed that a locally defined function can look up names outside of its local frames. No nonlocal statement is required to access a non-local name. By contrast, only after a nonlocal statement can a function change the binding of names in these frames.
- Note that in our example, balance is bound to an immutable value (an integer). If we bound a temporary variable to a mutable value, like a list, we can refer to or modify the value of elements inside of it in the local frame, without defining non-local.
- 2.4.5 The Benefits of Non-Local Assignment
- Non-local assignment is an important step on our path to viewing a program as a collection of independent and autonomous objects, which interact with each other but each manage their own internal state. In particular, non-local assignment has given us the ability to maintain some state that is local to a function, but evolves over successive calls to that function.
- 2.4.6 The Cost of Non-Local Assignment
- When two names are both bound to a function, it does matter whether they are bound to the same function, or different instances of that function. By introducing non-pure functions that change the non-local environment, we have changed the nature of expressions. An expression that contains only pure function calls is referentially transparent: its value does not change if we substitute one of its subexpression with the value of that subexpression. Re-binding operations violate the conditions of referential transparency because they do more than return a value.
- 2.4.7 Implementing Lists and Dictionaries
- None is None, but [] is not [] (they are equal, but not identical).
- We design our mutable linked list function as a dispatch function, and its arguments are first a message, followed by additional arguments to parameterize that method. This message is a string naming what the function should do. Dispatch functions are effectively many functions in one: the message determines the behavior of the function, and the additional arguments are used in that behavior.
- The approach, which encapsulates the logic for all operations on a data value within one function that responds to different messages, is a discipline called message passing. A program that uses message passing defines dispatch functions, each of which may have local state, and organizes computation by passing "messages" as the first argument to those functions. The messages are strings that correspond to particular behaviors.
- 2.4.8 Dispatch Dictionaries
- 2.4.9 Propagating Constraints
- Declarative programming: in which a programmer declares the structure of a program to be

solved, but abstracts away the details of exactly how the solution to the problem is computed.

- Computer programs are traditionally organized as one-directional computations, which perform
 operations on pre-specified arguments to produce desired outputs. On the other hand, we often
 want to model systems in terms of relations among quantities. Such a model is not onedirectional.
- We can use a message passing system to coordinate constraints and connectors. Constraints are dictionaries that do not hold local states themselves. Their responses to messages are non-pure functions that change the connectors that they constrain. Connectors are dictionaries that hold a current value and respond to messages that manipulate that value. Constraints will not change the value of connectors directly, but will do so by sending messages, so that the connector can notify other constraints in response to the change. In this way, a connector represents a number, but also encapsulates connector behavior.

2.5 Object-Oriented Programming

2.5.1 Objects and Classes

- A class serves as a template for all objects whose type is that class. Every object is an instance of some particular class. The objects we have used so far all have built-in classes, but new user-defined classes can be created as well. A class definition specifies the attributes and methods shared among objects of that class.
- The act of creating a new object instance is known as instantiating the class. The syntax in Python for instantiating a class is identical to the syntax of calling a function.

>>> a = Account('Kirk')

- An attribute o an object is a name-value pair associated with the object, which is accessible via
 dot notation. The attribute specific to a particular object, as opposed to all objects of a class,
 are called instance attributes.
- Functions that operate on the object or perform object-specific computations are called methods. 2.5.2 Defining Classes
- User-defined classes are created by class statements, which consist of a single clause. A class statement defines the class name, then includes a suite of statement to define the attributes of the class.

class <name>:

<suite>

• An example:

class Account:

```
def __init__(self, account_holder): #constructor
    self.balance = 0
    self.holder = account_holder
```

The __init__ method has two formal parameters. The first one, self, is bound to the newly created object. The second one, is bound to the argument passed into the class when it is called to be instantiated.

• Each new object instance has its own attribute, the value of which is independent of other objects of the same class. To enforce this separation, every object that is an instance of a user-defined class has a unique identity. Object identity is compared using is and is not operators. As usual, binding an object to a new name using assignment does not create a new object.

```
>>> c = a
>>> c is a
New objects that have user-defined classes are only created when a class is instantiated with call
expression syntax.
2.5.3 Message Passing and Dot Expressions

    The built-in function [getattr] returns an attribute for an object by name.

>>> getattr (spock_account, 'balance')
10
(getattr and dot expressions look up a name in the same way)

    The built-in function [hasattr] checks whether an object has a named attribute.

>>> hasattr (spock_account, 'balance')
True
• The difference between functions and bound methods:
1. Functions, which we have been creating since the beginning of the course.
2. Bound methods, which couple together a function and the object on which that method will be
   invoked. (Object + Function = Bound Method)
>>> type(Account.deposit)
<class 'function'>
>>> type(spock_account.deposit)
<class 'method'>
The first is a standard two-argument function with parameters self and amount. The second is a
one-argument method, where the name self will be bound to the object when the method is called.
We can call deposit in two ways:
>>> Account.deposit(sa, 100) #the deposit function takes two arguments
>>> sa.deposit(100) #the deposit function take one argument
• Class names are conventionally written using the CapWords convention
2.5.4 Class Attributes

    Some attribute values are shared across all objects of a given class. Such attributes are

  associated with the class itself, rather than any individual instance of the class. Class attributes
  are created by assignment statements in the suite of a class statement, outside of any method
  definition (they may also be called class variables or static variables.)
class Account:
    interest = 0.02
    def __init__(self, account_holder): #constructor
         self.balance = 0
         self.holder = account_holder
A single assignment statement to a class attribute changes the value of the attribute for all
instances of the class. However, it is not vice versa.
>>> Account.interest = 0.04
>>> account.interest
0.04
>>> account.interest = 0.08
>>> Account.interest
```

0.04													
• Dot expression consists of	of an expre	ssion,	a dot	, and	a nam	e:							0
<expression>.<name></name></expression>									•				
To evaluate a dot expressi													0
1. evaluate the expression	on> to the	left of	f the	dot, w	hich y	yields	the o	bject	of th	e dot	expre	ssion	
2. <name> is matched aga</name>	inst the ins	tance	attri	butes	of the	e obj	eçt; if	an a	tţribu	te wit	h tha	t,	0
name exists, its value i	s returned												0
3. if <name> does not app</name>	ear among	instan	ce at	tribut	es, th	en <n< td=""><td>ame> i</td><td>is, look</td><td>ked up</td><td>in th</td><td>e clas</td><td>s,</td><td></td></n<>	ame> i	is, look	ked up	in th	e clas	s,	
which yields a class at	tribute valı	ue.											
4. that value is returned	unless it is	a fun	ction,	in wh	ich co	ise a	bound	meth	od is	returr	ned ins	itead.	0
Objects receive messages	via dot not	ation.											
tom_account.deposite(10)					0						0		0
[Dot expression]													
[Call expression]													
2.5.5 Inheritance													0
• Two classes may have sin	milar attrik	outes,	but o	ne rep	oresen	its a	specia	l case	of th	ne oth	er. B	iş a	
specialization of A. In O	OP termina	logy,	the g	eņeric	çlass	(A) v	vill sei	rve as	the b	oase c	lass o	f B.	
. The terms parent class of	and supercl	ass ar	e also	used	for t	he ba	se cla	ss, wh	nile ch	nild cla	ass is	also	0
used for the subclass.													
• A subclass inherits the a	ittributes c	fits	base o	class,	but m	ay ov	erride	certa	ain at	tribut	es, inc	luding	0
certain methods. With in	heritance,	we on	ly spe	cify v	vhat i	s diff	erent	betw	een th	ne sub	class	and	
the base class. Anything	that we le	eave u	nspec	ified i	n the	subcl	ass is	autor	natica	lly as	sumed	to	
behave just as it would	for the bas	e clas	s.								0		0
• is-a and has-a relationsh	nip .												
2.5.6 Using Inheritance													
• The implementation of B													
>>> class Account:													20000
>>> class CheckingAccount(Account):												No. of Contract of
• We can define the proce	dure to loc	k up	a nam	e in a	class	recu	rsively	<i>/</i> :					THE PARTY OF
1. If it names an attribut									•	•	•		
2. Otherwise, look up the											•	•	
• Attributes that have be								iects.					
>>> class CheckingAccount(4,0000	.,	.,	.,	J		•	٠	•	
withdraw_charge = 1						•				•	•	•	
interest = 0.01		•			•	•			•		•		0
def withdraw(self, am	ount).		•			•	•			•	•	•	
return Account.v		olf am	ount	امی ام	withd	Iraw	chara	ره	•	•	•		
2.5.7 Multiple Inheritance		it, um					cilai 9	د,	•	٠	•	•	
• Python supports the con-		ubclas			Lattri		from	· mul+i	nle h	150 04			
language feature called				si, i i i i i g	μιιιι	Dures	i i om	ijiutii	hie no	ise ca	ues, a	•	
이 경기 때 하는 사람이 보고 있는 것이 되었다. 그는 것은 것은 것이 없는 것이 없다.		neilla	iice.	0	0			•			0	0	0
>>> class SavingsAccount(A	ccount):										•		

>>> class specialAccount(CheckingAccount, SavingsAccount):

• For a diamond shape inheritance relationship, Python resolves names from left to right, then upwards. This is vital when it comes to find names for ambiguous references.

2.5.8 The Role of Objects

2.9 Recursive Objects

• Objects can have other objects as attribute values. When an object of some class has an attribute value of that same class, it is a recursive object.

2.9.1 Linked List Class

- A linked list is composed of a first element and the rest of the list. The rest of a linked list is itself a linked list a recursive definition. The empty list is a special kind of linked list that has no first element or rest. A linked list is a sequence: it has a finite length and supports element selection by index.
- The link class has the closure property. A link can contain a link as its first element.
- Recursive functions are particularly well-suited to manipulate linked lists.
- 2.9.2 Tree Class

2.9.3 Sets

• In sets, duplicate elements are removed upon construction. Sets are unordered collection.

```
>>> s = {3, 2, 1, 4, 4}
>>> s
```

{1, 2, 3, 4}

Common built-in functions for sets:

```
>>> 3 in s #membership tests
```

True

```
>>> len(s) #length computation
```

4

```
>>> s.union({1, 5}) #set union
```

{1, 2 3, 4, 5}

{3, 4}

• Sets are mutable, and can be changed one element at a time using add, remove, discard, and pop.

2.7 Object Abstraction

A central concept in object abstraction is a generic function, which is a function that can accept
values of multiple different types. We will consider three different techniques for implementing
generic functions: shared interfaces, type dispatching, and type coercion.

2.7.1 String Conversion

- To represent data effectively, an object should behave like the kind of data it is meant to represent, including producing a string representation of itself.
- Python stipulates that all objects should produce two different string representations: one that is human-interpretable text and one that is a Python-interpretable expression. The constructor function for strings, [str], returns a human-readable string. Where possible, the [repr] function returns a Python expression that evaluates to an equal object. The result of calling repr on the

value of an ex		what Py	thon pr	rints in	an in	terac	tive s	ession	. Ofte	eņtime	es str	and r	epr .
are the same	runctions.		•								•		0 0
>>> a .							•	•		•			
.1													
>>. print(repr(a))													
1 #the two exp													
• We would like													
different form													
function alway													
 By implementing 	ng this san	ne metho	d in use	r-defi	ned cl	asses,	we c	an ex	tend :	the ap	plicat	oility (of repr
to any class w	e create i	n the fut	ure, Th	is exai	nple t	nighlig	hts a	nothe	r bene	efit of	f dot e	expres	ssions
in general: the object types.	y provide	a mechar	nism for	exter	ding t	he do	main	of exi	sting	funct	ions to	oʻuem	
• These polymor	nhic funct	ions are	evamnla	s of a	more	gener	ral nr	inciple	· cer	tain f	unctio	ns sha	 uld
apply to multi													
attribute nam							s suci	ı a ıuı	iiç Holi	js 10	use a	Snare	eu .
		niereni (ieniinno	m in e	ıçn cı	uss.	•		•	•	•		
2.7.2 Special Me				. la d. la.						· .			
• In Python, cer													
For instance, 1													5
constructed. T						tically	whe	n prin	ting, d	ınd	_repr_	IS	
invoked in an i					es.	•							
• True and False													
• sequence oper													
• In Python, fun													
. attributes like	any other	r object.	Python	also a	llows	us to	defin	e obje	ects t	hat c	an be	"calle	d" like
functions by in	icluding a	call	. metho	d. Wit	n, this	meth	od, w	e can	define	e a cl	ass th	at be	haves
like a higher-c	order functions	tion.											
• Certain names	are specie	al becaus	e they	have b	uilt-ir	beho	vior.	These	name	es alw	ays st	tart a	nd end
with two unde	rscores.												
init> Met	hod invoke	d automa	tically	when a	an obj	ect is	cons	tructe	ęd.				
repr> Me	thod invok	ed to dis	play an	object	as a	Pytho	on ex	pressio	on.				
add> Met													
bool> Me	thod invok	ed to con	vert an	objec	t to t	rue or	Fals	e.					
float> Me									mber.				
Special methods											y are	applie	ed to
user-defined obj												711	
2.7.3 Multiple R		ions	•		•	•	•		•		•	•	
 Object attribution 			orm of r	messaa	e nase	sina a	llows	diffe	rent c	lata t	unes t	to res	pond
to the same m													
from different													
attribute nam								mileri	uce 13	u se	i or sr	iui eu	
								Five 4	ralat:	onchi-	·	o a a b	other.
• The requireme													viner,
is a new probl													
compute the o	ther repre	esentation	n whene	ver it	is nee	ded. H	ytho	n has	a sim	ple te	ature	tor	

computing attrib	butes o	n the fly	from z	ero-a	rgume	nt fun	ctions	s. The	@pro	perty	deco	rator	allows
functions to be	called	without c	all exp	ressio	n synt	ax (po	arenth	neses	follow	ing ar	expr	ression	1).
@property													
def magnitude(self	F): .												٠

• The interface approach to encoding multiple representations has appealing properties. The class for each representation can be developed separately; they must only agree on the names of the attributes they share, as well as many behavior conditions for those attributes. The interface is also additive: if another programmer wanted to add a third representation of complex numbers to the same program, they would have to create another class with the same attributes.

2.7.4 Generic Functions

- One way to implement cross-type operations is to select behavior based on the types of the arguments to a function or method. The idea of type dispatching is to write functions that inspect the type of arguments they receive.
- We use the type-tag attribute to distinguish types of arguments. One could directly use the built-in isinstance method as well, but tags simplify the implementation.
- Often the different data types are not completely independent, and there may be ways by which
 objects of one type may be viewed as being of another type. This process is called coercion. In
 general, we can implement this idea by designing coercion functions that transform an object of
 one type into an equivalent object of another type.
- Further advantages come from extending coercion. Some more sophisticated coercion schemes do not just try to coerce one type into another, but instead may try to coerce two different types each into a third common type. Another extension to coercion is iterative coercion, in which one data type is coerced into another via intermediate types. Chaining coercion in this way can reduce the total number of coercion functions that are required by a program.