

1 Assorted ADTs

A **list** is an ordered collection, or *sequence*.

```
1 List
2   add(element); // adds element to the end of the list
3   add(index, element); // adds element at the given index
4   get(index); // returns element at the given index
5   size(); // the number of elements in the list
```

A **set** is a (usually unordered) collection of unique elements.

```
1 Set
2   add(element); // adds element to the collection
3   contains(object); // checks if set contains object
4   size(); // number of elements in the set
5   remove(object); // removes specified object from set
```

A **map** is a collection of key-value mappings, like a dictionary in Python. Like a set, the keys in a map are unique.

```
1 Map
2   put(key, value); // adds key-value pair to the map
3   get(key); // returns value for the corresponding key
4   containsKey(key); // checks if map contains the specified key
5   keySet(); // returns set of all keys in map
```

Stacks and queues are two similar types of linear collections with special behavior.

A **stack** is a last-in, first-out ADT: elements are always added or removed from one end of the data structure. A **queue** is a first-in, first-out ADT. Both data types support three basic operations: **push(e)** which adds an element, **peek()** which returns the next element, and **poll()** which returns and removes the next element.

stack.pop() is correct;
stack.poll() is incorrect

Java defines an interface that combines both stacks and queues in the Deque. A **deque** (double ended queue, pronounced “deck”) is a linear collection that supports element insertion and removal at both ends.

```
1 Deque
2   addFirst(e); // adds e to front of deque
3   removeFirst(); // removes and returns front element of deque
4   getFirst(); // returns front element of deque
5   addLast(e); // adds e to end of deque
6   removeLast(); // removes and returns last element of deque
7   getLast(); // returns last element of deque
```

Generally-speaking, a priority queue is like a regular queue except each element has a priority associated with it which determines in what order elements are removed from the queue.

```

1 PriorityQueue
2   add(e); // adds element e to the priority queue
3   peek(); // looks at the highest priority element, but does not remove it from the PQ
4   poll(); // pops the highest priority element from the PQ

```

instead of push

2 Solving Problems with ADTs

2.1 For each problem, which of the ADTs given in the previous section might you use to solve each problem? Which ones will make for a better or more efficient implementation?

- (a) Given a news article, find the frequency of each word used in the article.

I will use a map. Firstly I will set up an empty map. When I read the article word by word, I will check whether the word has already existed in the map as a key. If not, I put it into the map combined with a value of 1; otherwise, I will just increment the value associated with the word by 1.

- (b) Given an unsorted array of integers, return the array sorted from least to greatest.

I will use a priority queue, with the exact value as the priority. Then when I do deque (poll), values will be returned in a increasing or decreasing order, which I will store in an array.

- (c) Implement the forward and back buttons for a web browser.

I will use two stacks, one for each button. Every time I click the forward button, the current web page is pushed into back stack, and popped from forward stack. Vice versa.

2.2 Java supports many built-in ADTs and data structures that implement these ADTs. But if we want something more complicated, we'll have to build it ourselves.

If you wish to use sorting as part of your design, assume that it will take $\Theta(N \log N)$ time where the length of the sequence is N .

- (a) Suppose we want an ADT called `BiDividerMap` that allows lookup in both directions: given a value, return its corresponding key, and vice versa. It should also support `numLessThan` which returns the number of mappings whose key is less than a given key.

```

1 BiDividerMap
2   put(k, V); // put a key, value pair
3   getByKey(K); // get the value corresponding to a key
4   getByValue(V); // get the key corresponding to a value
5   numLessThan(K); // return number of keys in map less than K

```

Describe how you could implement this ADT by using existing Java ADTs as building blocks. Come up with an idea that is correct first before trying to make it more efficient.

In addition to the `BiDividerMap`, I will also build another map whose key is BDM's value, and value is the corresponding key. For `numLessThan`, I will use the `KeySet` method and iteration.

- (b) Next, Suppose we would like to invent a new ADT called `MedianFinder` which is a collection of integers and supports finding the median of the collection.

```

1 MedianFinder
2   add(x); // adds x to the collection of numbers
3   median(); // returns the median from a collection of numbers

```

Describe how you could implement this ADT by using existing Java ADTs as building blocks. What's the most efficient implementation you can come up with?

I will use array and sorting algorithm. Returned the elements at the middle index when called.

- 2.3 Define a `Queue` class that implements the `push` and `poll` methods of a queue ADT using only a `Stack` class which implements the stack ADT.

Hint: Consider using two stacks.

```
import java.util.Stack;

> public class Queue<T> {
    4 usages
    private final Stack<T> stack1;
    4 usages
    private final Stack<T> stack2;

    1 usage
    public Queue() {
        stack1 = new Stack<>();
        stack2 = new Stack<>();
    }

    2 usages
    public void push(T item) {
        stack1.push(item);
    }

    2 usages
    public T poll() { // Take care of the return type!
        if (stack2.isEmpty()) {
            while (!stack1.isEmpty()) {
                stack2.push(stack1.pop());
            }
        }
        return stack2.pop(); // But there might still be no elements at all
    }
}
```