# ECON 3201 Econometrics for Economics and Finance

# Assignment 1

#### **Due Date**

September 18, 2025 at the start of class

#### **Directions**

Answer all questions. Submit both a PDF and Quarto file to the nexus assignment portal.

## 1. Git and GitHub

- (a) Create a GitHub repository called **econ\_3201** and connect it to RStudio.
- (b) Create a new R project in this newly created directory called **assignment\_1**. (Note, you do not have to click "Create git repository" as the directory is contained in a git enabled directory, i.e., **econ\_3201**).
- (c) Download the assignment PDF and Quarto file the **assignment** 1 folder.
- (d) Commit and push the changes to your econ\_3201 repository on GitHub.com.

# 2. LaTeX

LaTeX is useful for writing math equations and presents them in a neat and orderly way. To write in math mode, wrap your text in \$ for inline text use two \$s for display (i.e., centered on the page). Some very useful functions include:

• Fractions:\frac{}{}, e.g.  $\frac{1}{2}$  gives  $\frac{1}{2}$  and  $\frac{1}{2}$  gives:

 $\frac{1}{2}$ .

• Subscripts: \_ gives a subscript, e.g.  $x_1$  gives  $x_1$ . To include more than one term in the subscript, the items in the subscript must be enclosed by {}. E.g.  $x_1$ , 1} gives  $x_1$ , 1 (Note that  $x_1$ , 1\$ gives  $x_1$ , 1)

• Exponents:  $\hat{ }$ , e.g.  $x^2$  gives  $x^2$ .  $\hat{ }$  can also be used for superscripts in other math functions, including summations and integrals.

• Aligned: aligned neatly aligns multiple lines of an equation. Align is useful when writing multiple steps to solving an equation. To use it in Quarto, write \$\$\begin{aligned}...\end{aligned}. The & is used to mark the point where the lines should be aligned. Use \\ at the end of each line E.g. \$\$\begin{aligned}

\end{aligned}\$\$

gives

$$x = 3 + 5$$
$$= 8$$

• Summation: \sum gives the summation sign, i.e.  $\sum$ . To include subscripts, use \_ and to use superscripts use ^, e.g.  $\sum_{i=1}^n s$  gives  $\sum_{i=1}^n s$ , which reads as the sum of i equals 1 to n.

Integral: \int gives an integral, i.e. ∫. To place a lower limit use \_ and to place an upper limit, use ^, e.g. \$\int\_{a}^{b}\$\$ gives ∫<sub>a</sub><sup>b</sup>.
Greek letters: \$\alpha, \beta, \gamma, \Gamma, \delta, \Delta, \epsilon,

• Greek letters: \$\alpha, \beta, \gamma, \Gamma, \delta, \Delta, \epsilon, \varepsilon, \zeta, \sigma, \Sigma, \theta, \vartheta, \Theta, \iota, \kappa, \lambda, \Lambda, \mu\$ gives  $\alpha, \beta, \gamma, \Gamma, \delta, \Delta, \epsilon, \varepsilon, \zeta, \eta, \sigma, \Sigma, \theta, \vartheta, \Theta, \iota, \kappa, \lambda, \Lambda, \mu$ . (See https://www.overleaf.com/learn/latex/List\_of\_Greek\_letters\_and\_math\_symbols)

• Accents:  $\hat{Y}$ ,  $\hat{Y}$ , and  $\hat{Y}$ , and  $\hat{Y}$ , and  $\hat{Y}$ , and  $\hat{Y}$ , respectively.

• Text: To include text in your equation, i.e. non italicized text, use text, e.g. x=2 if y=1 gives x=2 if y=1.

Inequalities: Some mathematical expressions may be written as inequalities, rather than equations. For 'less than' and 'greater than', you can just use the symbol on your keyboard, i.e. < and >, respectively. For ≤, use \$\leq\$ and for ≥, use \$\geq\$. An important note is that after writing a command, put a space after the command before writing the next term, otherwise you may get an error. E.g. To write a ≤ b, write \$a\leq b\$, not \$a\leqb\$.

Re-write the following equations in LaTeX.

(a) 
$$E(Y) = y_1 p_1 + \dots + y_k p_k = \sum_{i=1}^k y_i p_i$$

(b) 
$$\sigma_Y = \mathrm{Var}(Y) = E\big[(Y-\mu_y)^2\big] = \sum_{i=1}^k (y_i - \mu_y)^2 p_i$$

(c) 
$$\hat{\beta} = \frac{\sum_{i=1}^{n} (y_i - \bar{y})(x_i - \bar{x})}{\sum_{i=1}^{n} (x_i - \bar{x})^2}$$

(d) 
$$P(a \le Y \le b) = \int_a^b f_Y(y) \, dy$$

(e) 
$$\hat{g}(x) = \frac{\frac{1}{nh} \sum_{i=1}^{n} y_i \, k(\frac{x_i - x}{h})}{\frac{1}{nh} \sum_{i=1}^{n} k(\frac{x_i - x}{h})}$$

# 3. R

## 3.1. Assignment

Note: When creating variables based on equation, separate each element in the equation with the appropriate arithmetic symbol. E.g., to compute x(y-2) in R, you would have to type x\*(y-2). x(y-2), with not arithmetic symbol between x and the left bracket would result in an error.

(a) In statistics, n is often used to denoted the sample size. Set the number of observations n = 1000.

#### n <-1000

(b) Generate two random variables,  $u_1 \sim U(0,1)$  and  $u_2 \sim U(0,1)$  with n/2 = 500 observations. That is, create two variables that follow a uniform distribution between 0 and 1 that each have 500 observations. In R, we can create random uniform variables using the runif(k,min,max) function, where k is number of observations, min is the minimum value, and max is the maximum value. The default values for min and max are 0 and 1, respectively. Type ?runif into your console to learn more.

```
u1 \leftarrow runif(n/2, min = 0, max = 1) # uniform random numbers between 0 and 1 u2 \leftarrow runif(n/2, min = 0, max = 1) # uniform random numbers between 0 and 1
```

(c) Generate two variables  $z_1$  and  $z_2$  that take on the following values:

$$z_1 = \sqrt{-2\ln(u_1)} \times \cos(2\pi u_2)$$

and

$$z_1 = \sqrt{-2\ln(u_1)} \times \sin(2\pi u_2).$$

In R,  $\sqrt{\ }$  is computed using sqrt(), ln is computed using log(), cos is computed using cos(), and sin is computed using sin().

```
z1 <- sqrt(-2 * log(u1)) * cos(2 * pi * u2)
z2 <- sqrt(-2 * log(u1)) * sin(2 * pi * u2)
```

(d) Generate a vector  $z = [z_1, z_2]$ 

```
z \leftarrow c(z1, z2)
```

(e) Generate two variables  $\mu$  (spelled mu) and  $\sigma$  (spelled sigma). Set  $\mu = 5$  and  $\sigma = 2$ .

```
mu <- 5
sigma <- 2
```

(f) Generate a variable  $x = \mu + \sigma \times z$ 

```
x <- mu + sigma * z
```

(g) Calculate the mean of x, using mean() and the standard deviation of x using sd().

```
mean(x)
```

[1] 5.040638

```
sd(x)
```

- [1] 2.056363
  - (h) Use the following code to plot a histogram of x with the normal distribution curve.

```
hist(x,
    freq = FALSE,
    ylab = "Density",
    xlab = "$x$")

curve(dnorm(x, mean = mu, sd = sigma),
    col = "red", lwd = 2, add = TRUE)
```

# Histogram of x

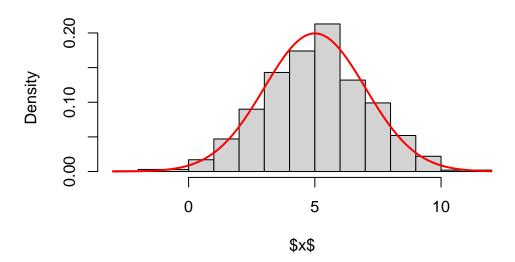


Figure 1: Histogram of x

# 3.2. Data frames and Indexing

A data frame in R is a table-like data structure used to store data in rows and columns, similar to a spreadsheet or a database table. It is one of the most commonly used structures for storing datasets in R.

Table 1 displays the total health expenditure by use of funds in Canada from 1975 to 2022. The data is stored in the data.frame called df.

Table 1: Total health expenditure by use of funds, in millions of current dollars, Canada, 1975 to 2022 (Source: CIHI National Health Expenditure Trends)

Year	Hospitals	Physicians	Other Services	Dental	Vision	Other Professionals
1,975	5,136.77	1,813.15	796.62	56.40	35.86	46.72
1,976	5,977.68	2,041.52	999.08	69.81	40.65	53.92
1,977	$6,\!372.73$	$2,\!252.12$	1,175.16	83.70	44.86	60.54
1,978	6,861.92	2,528.34	1,367.51	103.96	51.91	75.52
1,979	$7,\!487.62$	2,804.48	$1,\!581.37$	143.83	57.99	88.88
1,980	8,585.16	$3,\!235.98$	1,821.48	194.94	67.23	104.90
1,981	$10,\!127.35$	3,775.12	$2,\!146.66$	278.44	78.74	126.67
1,982	12,001.93	4,353.14	$2,\!531.36$	270.04	91.13	143.01
1,983	$13,\!174.55$	4,973.30	2,794.37	260.66	105.68	163.99
1,984	13,936.30	$5,\!444.58$	2,923.26	266.74	117.66	181.02
1,985	14,737.75	5,962.06	$3,\!066.46$	275.52	130.42	214.58
1,986	15,937.05	$6,\!597.89$	2,982.43	287.16	146.05	260.66
1,987	17,154.21	$7,\!266.23$	$3,\!132.08$	286.27	157.30	276.36
1,988	$18,\!497.17$	$7,\!862.51$	$3,\!468.29$	311.35	180.78	296.02
1,989	$20,\!268.98$	8,422.71	3,828.51	350.27	205.62	341.53
1,990	$20,\!528.15$	9,090.92	$5,\!100.45$	371.70	235.89	379.81
1,991	21,783.23	$10,\!014.44$	$5,\!868.30$	387.93	265.51	442.89
1,992	22,652.40	$10,\!249.61$	$6,\!253.82$	394.80	262.22	470.54
1,993	22,619.06	$10,\!306.29$	$6,\!190.38$	407.31	229.69	460.64
1,994	22,096.82	$10,\!533.27$	$6,\!266.36$	418.63	221.20	429.23
1,995	$21,\!849.46$	$10,\!506.52$	$6,\!498.12$	408.13	197.12	427.63
1,996	21,997.29	10,651.80	$6,\!591.26$	373.98	196.90	426.18
1,997	$22,\!307.52$	$11,\!103.52$	$6,\!834.19$	365.18	215.12	448.14
1,998	$23,\!530.41$	11,627.85	$7,\!172.47$	352.30	204.66	481.07
1,999	24,751.97	$12,\!255.39$	$7,\!578.69$	380.04	219.28	523.72
2,000	26,950.76	13,045.53	$8,\!170.94$	397.63	230.47	577.24
2,001	$28,\!606.54$	14,001.53	8,784.35	406.72	247.80	559.25
2,002	$30,\!683.55$	14,939.47	$9,\!308.19$	421.57	239.86	521.36
2,003	32,903.18	16,084.37	9,841.96	409.33	244.00	526.93
2,004	$35,\!269.82$	17,084.00	$10,\!629.24$	425.19	250.30	530.73
2,005	$37,\!112.35$	18,302.66	$11,\!064.58$	450.38	223.05	469.67
2,006	39,704.71	19,743.14	$11,\!593.52$	504.41	231.54	482.76
2,007	$42,\!376.77$	$21,\!308.72$	$12,\!192.52$	541.84	239.84	541.96
2,008	$45,\!362.04$	$23,\!370.83$	12,809.06	586.77	264.34	619.50
2,009	47,996.52	$25,\!249.61$	$13,\!578.95$	664.37	295.77	671.40
2,010	50,947.81	27,107.23	14,316.45	714.70	311.87	692.20
2,011	$52,\!126.35$	$28,\!813.05$	$15,\!324.80$	721.61	332.69	734.94

Table 1: Total health expenditure by use of funds, in millions of current dollars, Canada, 1975
to 2022 (Source: CIHI National Health Expenditure Trends)

						Other
Year	Hospitals	Physicians	Other Services	Dental	Vision	Professionals
2,012	53,299.96	29,801.63	15,923.80	759.13	353.62	782.67
2,013	54,954.28	31,202.28	$16,\!386.15$	762.36	358.08	730.08
2,014	56,123.22	$32,\!490.79$	16,966.03	782.00	389.71	685.88
2,015	$57,\!352.33$	33,886.08	18,313.73	821.42	430.46	1,179.18
2,016	$58,\!168.97$	$35,\!283.98$	18,809.91	875.86	461.42	$1,\!355.90$
2,017	$60,\!356.12$	$36,\!490.87$	$19,\!665.65$	918.62	484.33	1,491.51
2,018	$62,\!896.86$	$37,\!494.64$	$20,\!548.31$	961.17	517.89	1,614.12
2,019	$65,\!034.33$	38,914.04	$21,\!446.58$	1,018.36	557.19	1,729.01
2,020	$67,\!221.53$	$37,\!288.46$	$23,\!675.08$	896.76	513.22	1,711.94
2,021	$69,\!663.71$	$41,\!479.50$	25,678.66	922.86	559.07	1,906.92
2,022	73,778.17	$44,\!195.30$	28,095.86	991.82	584.06	2,047.50

(a) Determine if there are any missing values for the variable Hospitals.

#### is.na(df\$Hospitals)

- [1] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
- [13] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
- [25] FALSE FALSE
- [37] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
- (b) Add a variable called "Total Other Services" to the data frame df, where

Total Other Services = Dental + Vision + Other Professional.

To add a newly created variable to a data frame use the syntax dataframe\$varname <-expression.

#### df\$TotalOtherServices <- df\$Dental+df\$Vision+df\$"Other Professionals"</pre>

- (c) Are there any years for which Total Other Professionals
- (d) Another way to add a variable to a data frame is to simply create a new data frame and append the new variable to it. Note: we can use the same data frame name. I.e., df<-data.frame(df,newvarname = newvar). Add the variable "Prescription Drugs" to the df data frame using the append method, where presricption drugs is named "Prescribed.Drugs" in the cihi data.frame.

#### df <- data.frame(df, "Prescription.Drugs"= cihi\$Prescribed.Drugs)</pre>

(e) Using a single R command, determine the expenditure on hospitals in 1983.

```
df$Hospitals[df$Year==1983]
```

#### [1] 13174.55

48

(f) Using a singe R command, list the expenditures by year for 2012-2022.

```
df[df$Year>=2012 & df$Year<=2022,]</pre>
```

3623.38

```
Year Hospitals Physicians Other.Services
                                              Dental Vision Other.Professionals
38 2012
         53299.96
                    29801.63
                                    15923.80
                                              759.13 353.62
                                                                           782.67
39 2013
        54954.28
                    31202.28
                                              762.36 358.08
                                                                           730.08
                                    16386.15
40 2014
         56123.22
                    32490.79
                                    16966.03
                                              782.00 389.71
                                                                           685.88
41 2015
         57352.33
                    33886.08
                                    18313.73
                                              821.42 430.46
                                                                          1179.18
42 2016
         58168.97
                    35283.98
                                    18809.91
                                              875.86 461.42
                                                                          1355.90
43 2017
         60356.12
                    36490.87
                                    19665.65
                                              918.62 484.33
                                                                          1491.51
44 2018
                    37494.64
                                              961.17 517.89
         62896.86
                                    20548.31
                                                                          1614.12
45 2019
         65034.33
                    38914.04
                                    21446.58 1018.36 557.19
                                                                          1729.01
46 2020
         67221.53
                    37288.46
                                    23675.08
                                              896.76 513.22
                                                                          1711.94
47 2021
         69663.71
                    41479.50
                                              922.86 559.07
                                    25678.66
                                                                          1906.92
48 2022
         73778.17
                    44195.30
                                    28095.86
                                              991.82 584.06
                                                                          2047.50
   TotalOtherServices Prescription.Drugs
38
              1895.42
                                 12114.49
39
              1850.52
                                 12199.19
40
              1857.59
                                 12668.45
41
              2431.06
                                 13298.98
42
              2693.18
                                 13616.80
43
              2894.46
                                 13957.25
44
              3093.18
                                 14442.70
45
              3304.56
                                 14939.93
46
              3121.92
                                 15435.35
47
              3388.85
                                 16034.55
```

17094.52

#### 3.3 Other useful R commands.

Load the mpg dataset from the ggplot2 package using mpg <-ggplot2::mpg. (Be sure to install the gglot2 package before you start.)

```
library(ggplot2)
mpg <-ggplot2::mpg</pre>
```

(a) Subset the data to include only observations from 2008. Search ?subset in the console.Calculate the maximum and minimum miles per gallon in city limits (cty). Search ?min in the console.

```
mpg_2008 <- subset(mpg, year==2008)
max(mpg_2008$cty)</pre>
```

[1] 28

```
min(mpg_2008$cty)
```

[1] 9

(b) Estimate the average miles per gallon within city limits for cars produced in 2008 using the formula

$$\text{Average mpg} = \frac{\sum_{i=1}^{n} \text{cty}_i}{n}.$$

Recall that n is the number of observations. Search ?length in the console.

```
#Avg_mpg
sum(mpg_2008$cty)
```

[1] 1954

```
length(mpg_2008$cty)
```

[1] 117

```
sum(mpg_2008$cty)/length(mpg_2008$cty)
```

#### [1] 16.70085

(c) Estimate the average miles per gallon within city limits for cars produced in 2008 using the mean() function.

```
mean(mpg_2008$cty)
```

# [1] 16.70085

(d) Create a variable called compact, which takes a value of 1 if the vehichle is a compact and 0 otherwise. Search ?ifelse in the console.

```
mpg_2008$compact <- ifelse(mpg_2008$class == "compact", 1, 0)</pre>
```

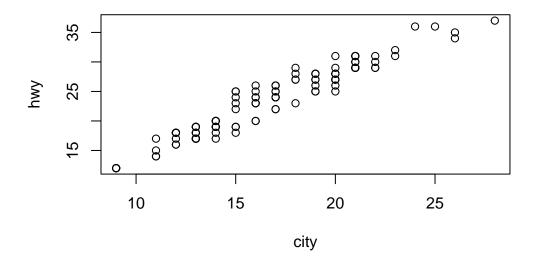
(e) Estimate the average miles per gallon within city limits for compact cars. (You may use whichever method you prefer).

```
mean(mpg_2008$cty[mpg_2008$compact == 1])
```

#### [1] 20.54545

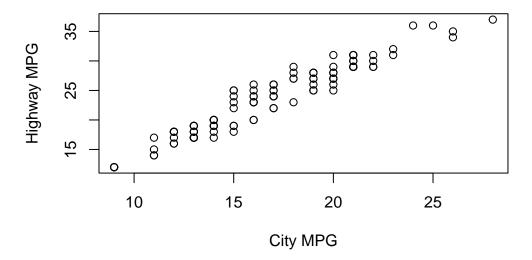
(f) Create a simple scatter plot with city mpg (cty) on the x-axis and highway mpg (hwy) on the y-axis. Search ?plot and choose "Generic X-Y Plotting".

```
city <- mpg_2008$cty
hwy <- mpg_2008$hwy
plot(x = city,
y = hwy)</pre>
```



(i) Change the x-axis label using the option `xlab = "City MPG"` and change the y-axis label

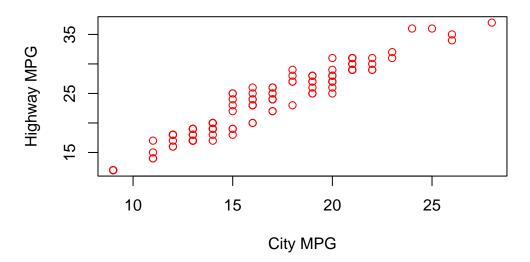
```
plot(city, hwy,
xlab = "City MPG",
ylab = "Highway MPG")
```



(ii) Add the caption "City Versus Highway Fuel Efficiency (MPG)"

```
plot(city, hwy,
xlab = "City MPG",
ylab = "Highway MPG",
main = "City Versus Highway Fuel Efficiency (MPG)",
col = "red")
```

# **City Versus Highway Fuel Efficiency (MPG)**



(iii) Cross reference the figure and add the text "Figure 1 shows the fuel efficiency for circular Figure 1 shows the Fuel efficiency for city driving versus highway driving