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Page No.

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## Parameter Estimation Assignment

1) normal distri.

given mean =  $\theta_1$

variance =  $\theta_2$

$$PDF = f(x) = \frac{1}{\sqrt{2\pi\sigma^2}} \cdot e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

$$L = \prod_{i=1}^n \frac{1}{\sqrt{2\pi\sigma^2}} \cdot e^{-\frac{(x_i-\mu)^2}{2\sigma^2}}$$

Take ln

$$\ln L = n \cdot \ln \left( \frac{1}{\sqrt{2\pi\sigma^2}} \right) + \ln \left( e^{-\frac{1}{2\sigma^2} \sum (x_i-\mu)^2} \right)$$

$$= n(\ln 1 - \ln(\sqrt{2\pi\sigma^2})) - \frac{1}{2\sigma^2} \sum (x_i-\mu)^2$$

$$= -n \ln(\sqrt{2\pi\sigma^2}) - \frac{1}{2\sigma^2} \sum (x_i-\mu)^2$$

For  $\mu$

$$\frac{\partial \ln L}{\partial \mu} = 0 \Rightarrow \frac{1}{2\sigma^2} \sum (x_i-\mu)(-1)$$

$$= \frac{1}{\sigma^2} E(x_i - \mu) = 0$$

$$\mu = \frac{E(x_i)}{n} = \bar{x} = \text{sample mean}$$

for  $\sigma^2$

$$\frac{\partial \ln(L)}{\partial \sigma^2} = 0$$

$$-\frac{n}{2} \times \frac{1}{2\pi\sigma^2} \times 2\pi + \frac{1}{2\sigma^4} E(x_i - \mu)^2 = 0$$

$$\left( \sigma^2 = \frac{\sum_{i=1}^n \frac{(x_i - \mu)^2}{n}}{n} \right)$$

$$2) \text{ Pdf} = {}^m C_{x_i} \theta^{x_i} (1-\theta)^{m-x_i}$$

$$L = \prod_{i=1}^n {}^m C_{x_i} \theta^{x_i} (1-\theta)^{m-x_i}$$

$$\ln(L) = \sum_{i=1}^n ( \ln({}^m C_{x_i}) + x_i \ln \theta + (m-x_i) \ln(1-\theta) )$$

$$\sum_{i=1}^n \left( \frac{x_i}{\theta} - \frac{(m-x_i)}{1-\theta} \right) = 0$$

$$\frac{\sum x_i}{\theta} = \frac{nm - \sum x_i}{1-\theta}$$

$$\theta = \frac{\sum x_i}{n.m.}$$