

103.

- This is answered very clearly on p. 137 of the text book (starting with "CAUTION!" at the bottom of the first column). See also Fig. 6-12.
- You would see a hole in an image of a star if the star were out of focus, though. But provided the telescope is in focus, all the rays of light come to a point, and the only effect of the obstruction is to dim the total light a bit.

104.

- The focal length is $20 \times 2.5\text{m} = 50\text{m}$.
- $s = f \theta$, where θ is in radians. Now, $1 \text{ arcmin} = 1/60 \text{ deg} \times 1 \text{ deg}/57.3 \text{ rad}$. So $\theta = 0.000291 \text{ rad}$.
- Therefore $s = 0.000291 \times 50\text{m} = 0.0145\text{m} = 1.45\text{cm}$

104a.

- The physical size of the moon ($\theta = 1/2 \text{ deg} = 0.0087 \text{ radians}$) is $s = f \cdot \theta = 0.0087 \cdot 50 \text{ mm} = 0.436 \text{ mm}$ (note that θ has to be in radians).
- So $0.436 \text{ mm} = 4.36 \times 10^{-4} \text{ m} = 436 \mu\text{m}$ (where μm means "micron" = 10^{-6} m). The total area of the image is then $\pi \cdot (436 \mu / 2)^2 = 1.49 \times 10^5 \mu\text{m}^2$.
- Now, 1 pixel of the detector is $15 \mu\text{m} \times 15 \mu\text{m} = 225 \mu\text{m}^2$. So there are $1.49 \times 10^5 / 225 = 664$ pixels in the image.

101.

- Angular size of Betelgeuse = $2 \times 1\text{AU} / 150\text{pc rad}$
= $2 \text{ AU} / (206265 \text{ AU/pc} \times 150 \text{ pc}) \text{ rad} = 6.46\text{E-}8 \text{ rad}$
[Note: 2AU, not 1 AU! need the diameter.]

$$\lambda = 550\text{nm: resolution angle is given by } \theta[\text{rad}] = \lambda/D;$$
$$D = \lambda/\theta = 5.50\text{e-}7 \text{ m} / 6.46\text{e-}8 = \underline{8.5 \text{ m}}$$

$$\lambda = 5\mu\text{m: } D = \lambda/\theta = 5.00\text{e-}6 \text{ m} / 6.46\text{e-}8 = \underline{77\text{m}}$$

102.

(a) Again, $\theta[\text{rad}] = \lambda/D = 5.5\text{e-}7\text{m} / 5\text{e-}3\text{m} = 1.1\text{e-}4 \text{ rad} = 23 \text{ arcsec}$

(b) See Appendix A-1 for Jupiter. $\theta = 143000\text{km} / (7.78\text{e}8\text{km})$
 $= 0.000183 \text{ rad} = 37.9 \text{ arcsec}$

See Appendix A-3 for moon: $\theta = 3476\text{km} / 384400 \text{ km} =$
 $= 0.00904 \text{ rad} = 1865 \text{ arcsec} (\sim 1/2 \text{ deg})$

So it's not too surprising that we can resolve the moon: the eye's resolution angle is much smaller than the moon's size. Jupiter is a bit more interesting. We should be able to see it as slightly resolved.

[You don't have to say this as part of your answer, but in fact we cannot resolve Jupiter or in fact anything under about 2 arcmin - the eye is limited by the rods and cones in the retina rather than the theoretical resolution limit of the pupil!]

105.

(a) Effective collecting area = $\pi D_{\text{prim}}^2/4 - \pi D_{\text{sec}}^2/4 = 1963\text{cm}^2 - 314\text{cm}^2$
= 1649cm^2

(b) Detection rat = $(10 \text{ phot s}^{-1} \text{ cm}^{-2} \text{ nm}^{-1}) \times 1649\text{cm}^2 \times 100\text{nm}$
 $\times 0.85 \times 0.85 \times 0.3 = 3.57\text{e}5 \text{ photons/sec}$