

Assignment 1

CSC 226

Theoretical Part

Question 1 (*Searching, lower bounds*). Argue convincingly: The problem of searching for the k^{th} smallest element when given a sequence of n pairwise comparable elements has the following lower bound: $\Omega(n)$

Question 2 (*Linear Selection*). If we would vary the pivot determination in the linear selection algorithm studied in class such that we break the given sequence S in short sequences of size 3 instead of size 5 and then continue the algorithm as described, the running time is not linear anymore. Why? When writing up your answer, argue convincingly!

Question 3 (*MST, graph properties*). In class, we studied the cycle and cut properties when determining minimum spanning trees for a given edge weighted graph. In both proofs we assumed that every edge in the given graph is of distinct weight.

- a) Argue correctness of the cycle property for the case that edges in the graph can be of identical weight.
- b) Argue correctness of the cut property for the case that edges in the graph can be of identical weight.

Question 4 (*MST algorithm*). Borůvka's algorithm assumes that all edges in the given graph are of distinct weight. Assume you are given a graph that does not satisfy this property but you are determined to apply Borůvka's algorithm to find a minimum spanning tree.

- a) What problem can the algorithm run into? Give an example of a graph where Borůvka's algorithm as presented in class may fail.
- b) Expand Borůvka's algorithm to overcome the difficulty. Describe your algorithm in pseudocode.