20 % 1) A 3 kg mass is connected to two identical springs on a frictionless horizontal surface. It oscillates horizontally with a period of 2s, and an amplitude of 4cm. At time t=0s, the mass is a distance of ½ its maximum displacement away from the equilibrium position, traveling to the left, and accelerating to the right. At this same time, one of the two springs breaks (thus changing the effective spring constant). Where is the mass at t=3s?

10 %

The initial position, velocity, and acceleration of an object moving in simple harmonic motion are x_i , v_i , and a_i ; the angular frequency of oscillation is ω . (a) Show that the position and velocity of the object for all time can be written as

$$x(t) = x_i \cos \omega t + \left(\frac{v_i}{\omega}\right) \sin \omega t$$

 $v(t) = -x_i \omega \sin \omega t + v_i \cos \omega t$

(b) If the amplitude of the motion is A, show that

$$v^2 - ax = v_i^2 - a_i x_i = \omega^2 A^2$$

10 %

3)

A 1.00-kg glider attached to a spring with a force constant of 25.0 N/m oscillates on a horizontal, frictionless air track. At t=0 the glider is released from rest at x=-3.00 cm. (That is, the spring is compressed by 3.00 cm.) Find (a) the period of its motion, (b) the maximum values of its speed and acceleration, and (c) the position, velocity, and acceleration as functions of time.

20 %

4)

A 65.0-kg bungee jumper steps off a bridge with a light bungee cord tied to herself and to the bridge (Figure P15.22). The unstretched length of the cord is 11.0 m. She reaches the bottom of her motion 36.0 m below the bridge before bouncing back. Her motion can be separated into an 11.0-m free fall and a 25.0-m section of simple harmonic oscillation. (a) For what time interval is she in free fall? (b) Use the principle of conservation of energy to find the spring constant of the bungee cord. (c) What is the location of the equilibrium point where the spring force balances the gravitational force acting on the jumper? Note that this point is taken as the origin in our mathematical description of simple harmonic oscillation. (d) What is the angular frequency of the oscillation? (e) What time interval is required for the cord to stretch by 25.0 m? (f) What is the total time interval for the entire 36.0-m drop?

20 %

5)

A pendulum of length L and mass M has a spring of force constant k connected to it at a distance k below its point of suspension (Fig. P15.59). Find the frequency of vibration of the system for small values of the amplitude (small θ). Assume the vertical suspension of length L is rigid, but ignore its mass.

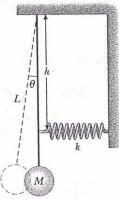


Figure P15.59

20 %

6)

A solid sphere (radius = R) rolls without slipping in a cylindrical trough (radius = 5R) as shown in Figure P15.56. Show that, for small displacements from equilibrium perpendicular to the length of the trough, the sphere executes simple harmonic motion with a period $T = 2\pi\sqrt{28R/5g}$.

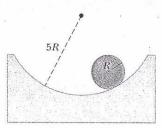


Figure P15.56