

UNIVERSITY OF VICTORIA

Department of Electrical and Computer Engineering
ELEC 360 – Control Systems I

Laboratory

Experiment no.: 3

Title: Position Control Using a DC Motor

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(should be within one week from the date of the experiment)

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Table of Contents

[1.0 Summary](#)

[2.0 Introduction](#)

[3.0 Answers to the Pre-laboratory Assignments](#)

[4.0 Experimental Results](#)

[Lab Section 4.2](#)

[Lab Section 4.3](#)

[Lab Section 4.4](#)

[Lab Section 4.5](#)

[5.0 Discussion](#)

[6.0 Conclusions](#)

1.0 Summary

The lab Position Control Using a DC Motor uses the QICii software to further examine the speed and position properties of a DC motor. With the tools available, the experimenters will gain an understanding of Proportional and Integral control as it applies to the position of the motor. They will also gain an understanding of the the design of controllers for specifications on the set-point response, and the tracking of triangular signals. With the results, the experimenters will be able to determine the steady state error using a PD controller.

2.0 Introduction

The objective of this lab project is to develop and understanding of Proportional and Integral controls that are applied to changes in position of a DC motor. In particular, the qualitative properties of proportional and derivative action in regards to settling and peak times to achieve a steady stable state when modifying the position of a DC motor.

3.0 Answers to the Pre-laboratory Assignments

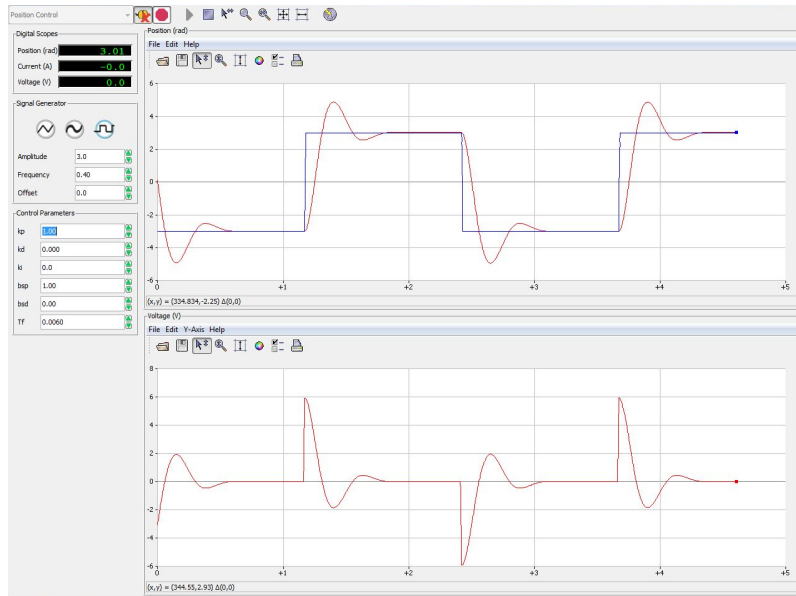
<i>Description</i>	<i>Symbol</i>	<i>Value</i>	<i>Units</i>
Open-loop steady-state gain t	k	19.9	rad/(V*s)
Open-loop time constant	T	0.0929	s
PI Controller Design			
Proportional Gain	k_p	1.62	V/rad
Derivative Gain	k_d	0.0366	V*s/rad
Set-Point Weight On Derivative Part	b_{sd}	0	
Desired Damping Ratio	ζ	0.5	
Desired Undamped Natural Frequency	ω_n	18.6	rad/s
Given Maximum Percentage Overshoot	PO	16.3	%
Given 2% Settling Time	T_s	0.43	s
Desired Peak Time	t_p	0.195	s
Steady-State Value of Position using PD	$\theta_{ss\ PD}$	r_0	rad
Tracking Triangular Signals			
Steady State Error using PD control	$e_{ss\ PD}$	1.72	rad

4.0 Experimental Results

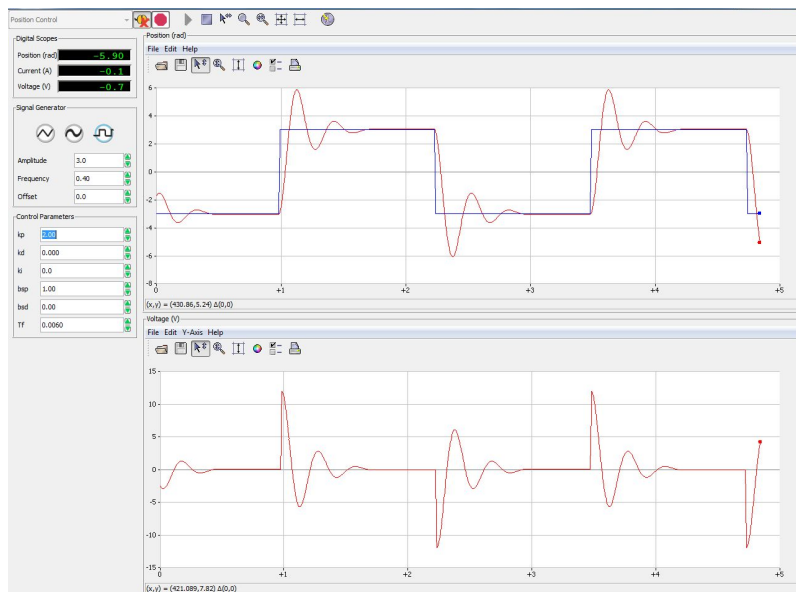
Lab Section 4.2

STEP2

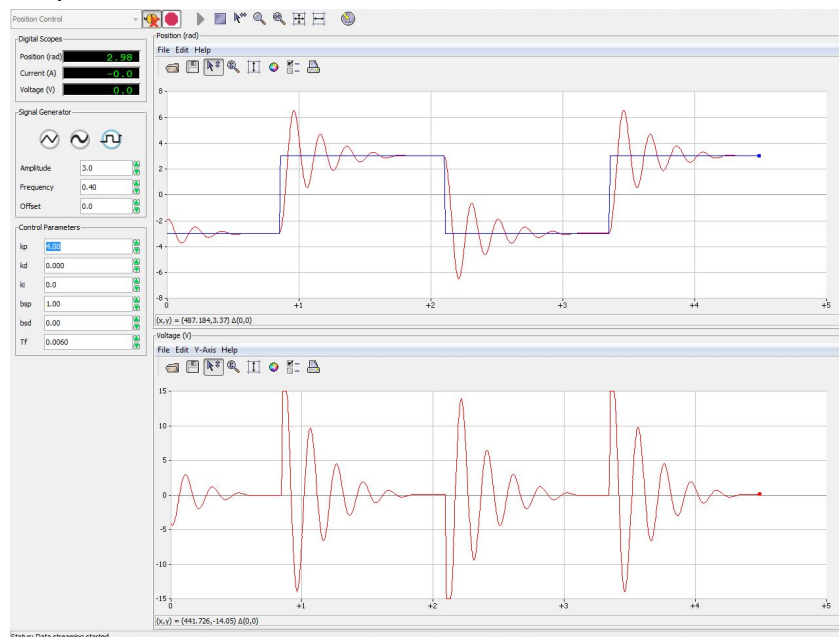
At $k_p = 1$:



At $k_p = 2$:



At $k_p = 4$:



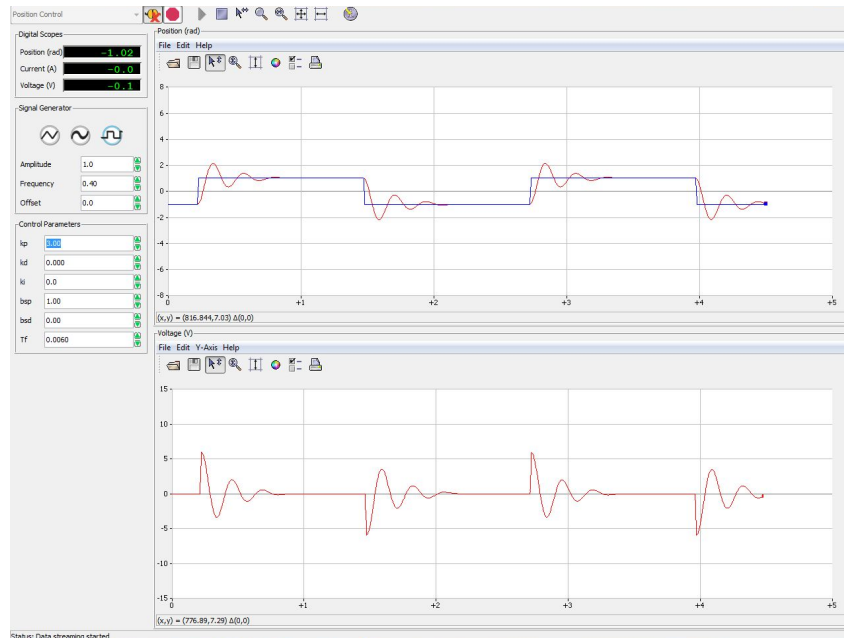
It can be seen that with increase in K_p value, the overshoot becomes higher and the oscillations stay longer.

STEP3

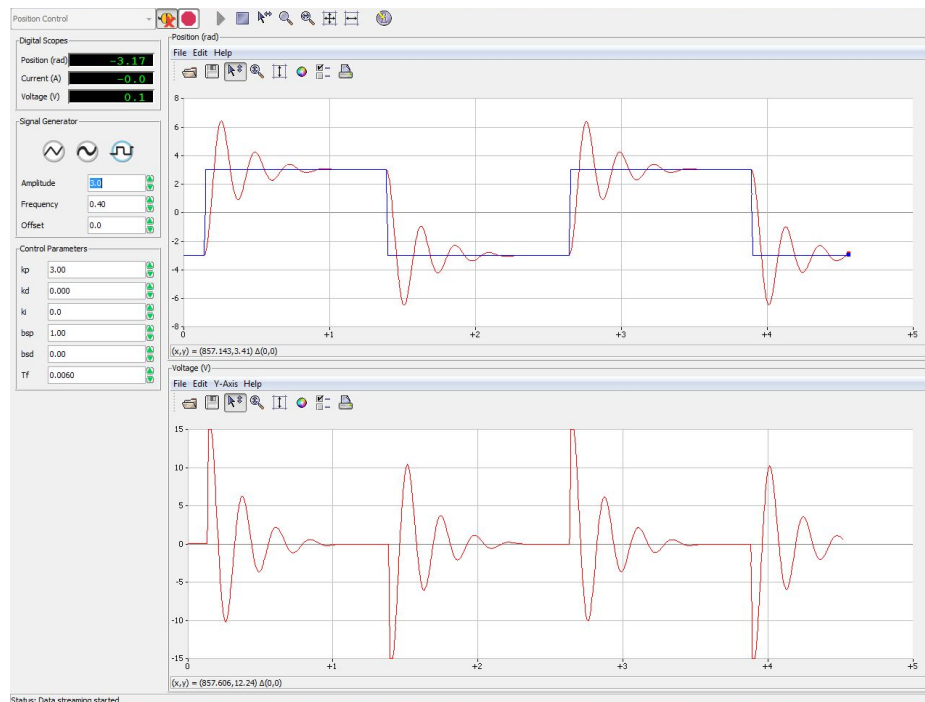
With increase in the k_p value, the overshoot becomes higher and and the oscillation stays longer.

STEP4

With amplitude= 1:



With amplitude = 3:

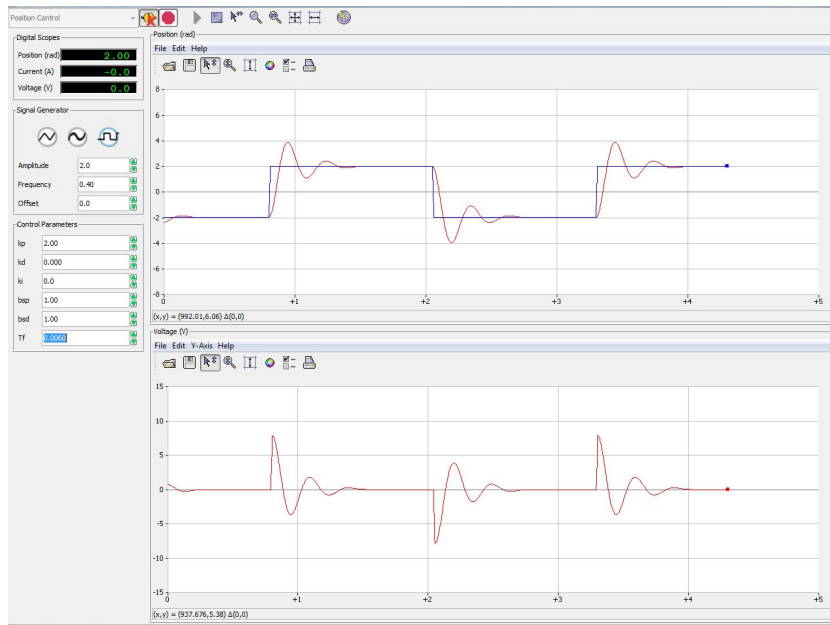


The peaks of the overshoots are higher with higher amplitude. The signal saturates at amplitude 15.

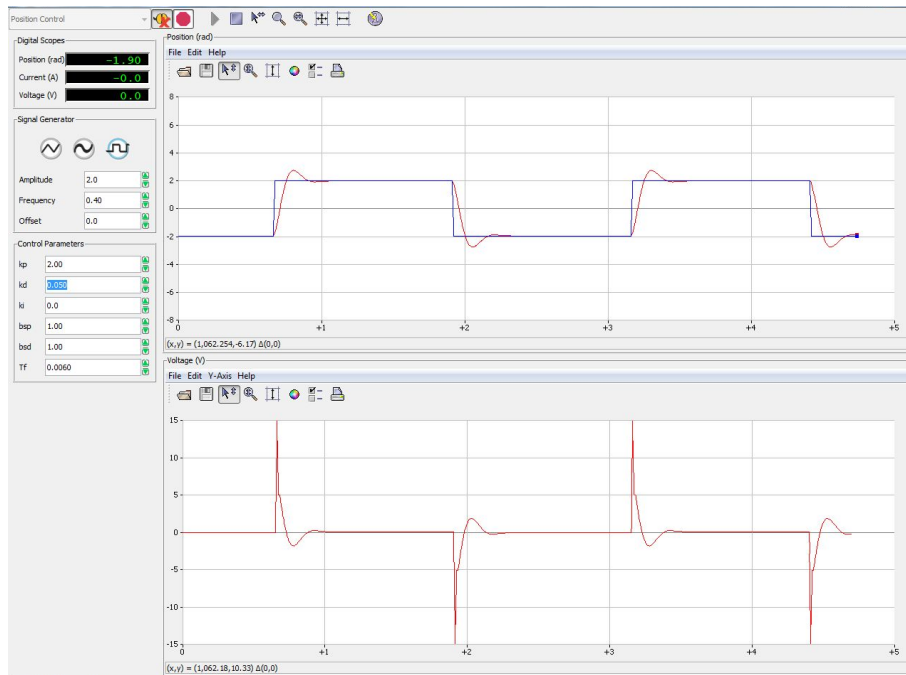
Lab Section 4.3

STEP2

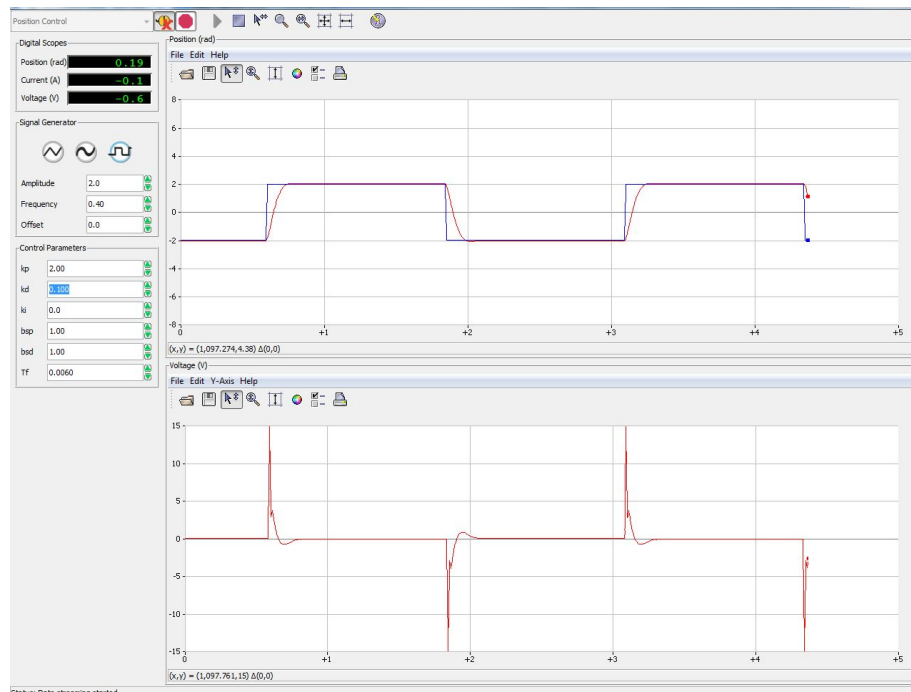
For $k_d = 0$:



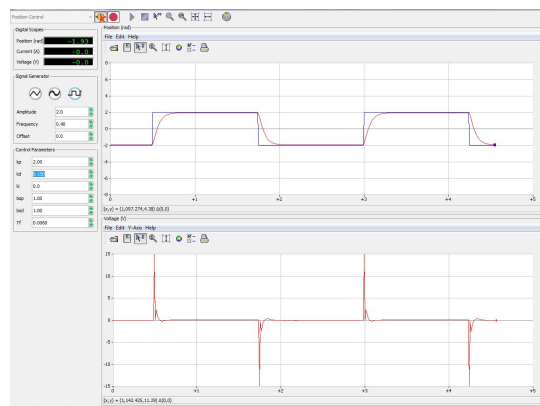
For $k_d = 0.05$:



For $k_d = 0.1$:

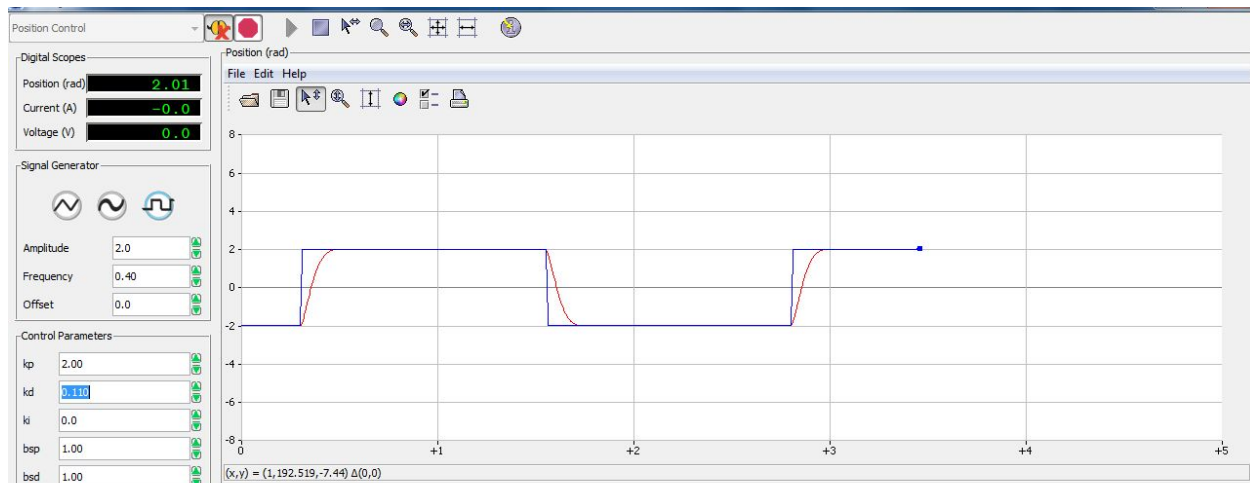


For $k_d = 0.15$:



Observation: The overshoot decreases with increase of k_d .

STEP3



The kd value is 0.11

Settling time:

Point 1 = 6.159

Point 2 = 6.324

Settle = $6.324 - 6.159 = 0.165$ seconds

Compare to Ts of 0.195, difference is 0.03

Lab Section 4.4

STEP2

Is PO < 18%?

Calculate overshoot:

Point1 = 4.43

Point2 = 6.11

Overshoot = $(6.03 - 4.43) / 9 = 0.177777778$

Overshoot is not greater than 18%

Calculate Ts

Point1 = 56.011

Point2 = 56.459

Settling time = $56.459 - 56.011 = 0.448$

Compare to Ts of 0.43, difference is 0.018

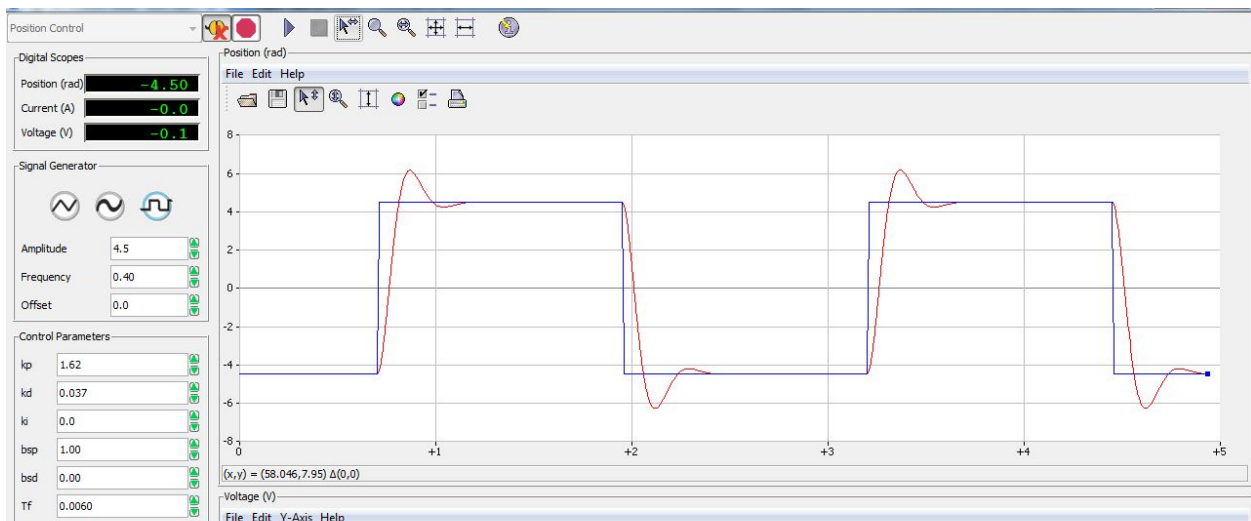
Calculate T_p

Point1 = 56.011

Point2 = 56.181

Peak time = $56.181 - 56.011 = 0.170$

Yes, the system's actual response meets the desired requirement. The measured settling time, T_s is within the 0.018s difference between the calculated value. The measured T_p is within 0.17s within the calculated value.



Lab Section 4.5

STEP2

Slope of r_0

rise/run

Rise:

Point1 = 15.8

Point2 = -9.9

Rise = $15.8 - -9.9 = 25.7$

Run:

Point1 = 118.459

Point2 = 117.651

Run = $118.459 - 117.651 = 0.808$

Slope = $25.7/0.808 = 31.806930693$

Compared to a given value of 32, the measured value is well within the range.

STEP3

Tracking error:

Point1 = 17.6

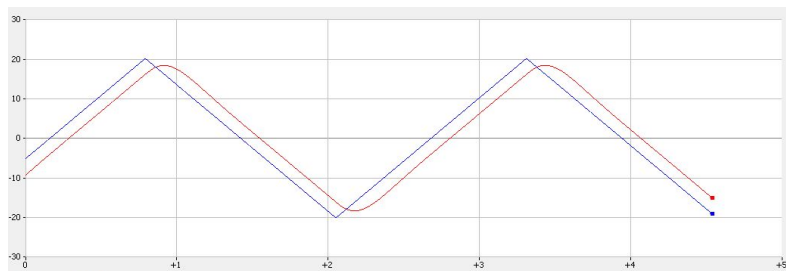
Point2 = 15.8

Error = $17.6 - 15.8 = 1.8$

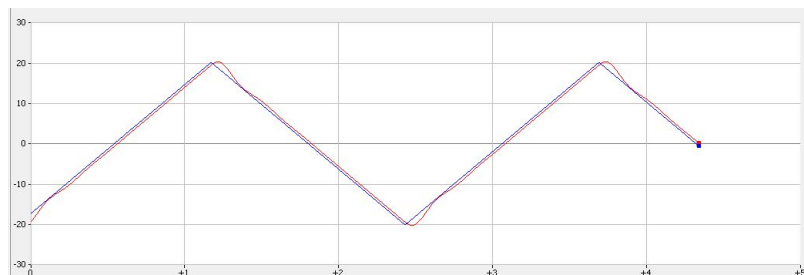
Compared to given value of 1.72, the measured value is higher, but well within the range.

STEP4

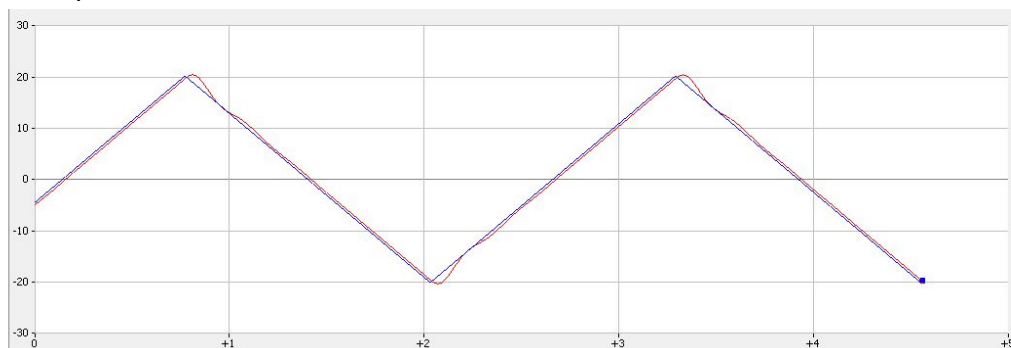
For $K_p = 0.62$:



For $K_p = 2.62$:



For $K_p = 3.12$:



As K_p increases, the tracking error decreases up to a point which it then becomes unstable.

5.0 Discussion

The proportional control, closed loop system for proportional controllers with different gains has been observed. The k_p values were set to 1, 2 and 4 V/rad consecutively. It has been observed that with increase in the K_p value, the overshoots in the system became higher and the oscillations after the overshoot stayed longer till it came back to a stable state again. The observations have been repeated again by changing the amplitude of the reference signal. It has been observed that the control signal saturates at 15V of reference signal amplitude.

The proportional derivative control section focused on exploring the combination of proportional and derivative control on the signals. The derivative gain has been incremented at a step of 0.05 V.s/rad to investigate the closed-loop system for PD controllers with different derivative gains. It has been observed that the overshoot decreases with the increase in the value of derivative gain, K_d . The lowest value of the derivative gain, K_d which gives a step response without overshoot has been found to be 0.11 V.s/rad. The settling time for this particular value is 0.165 seconds.

The PD controller design to given specifications included verification for PD controller design to given specifications. The experimental result has shown that the system's actual response meets the desired requirement. The measured settling time, T_s is within the 0.018s difference between the calculated value. The measured T_p is within 0.17s within the calculated value.

For tracking triangular signals, the measured slope is 31.8. Compared to the calculated value in the pre-lab section which is 32, the values are well within the ranges of each other. The tracking error is 1.8, and the calculated error is 1.72. The values are close to each other; Hence, the experiment has been a success.

6.0 Conclusions

The goal of this experiment was to attain a stable system with a steady error constant when the position of the DC motor was changed. It was found that by varying the K_p value of the system, the overshoot became higher and there were prolonged oscillations. The peaks of the K_p overshoot increased in height as the amplitude of the system increased. The signal was found to be saturated at an amplitude of 15. As the K_d increases, the overshoot of the system decreases. The measured settling time T_s and the measured T_p are well within acceptable values. For triangular signals, the tracking error decreased up to a point in which it becomes extremely unstable and the error increases dramatically.