## Homework 4–CSC 320 Summer 2015

Due in class, Tuesday July 21, at 11:20am

1. Prove that the language

 $L = \{\langle M \rangle \mid M \text{ when started on the blank tape, eventually writes a \$ somewhere on the tape} \}$  is undecidable. Use the undecidability of  $A_{TM}$  to do this.

2. Give a reduction from

$$HALT_{TM} = \{ \langle M, w \rangle \mid M \text{ is a TM which halts on } w \}$$

to

$$L = \{ \langle M, j \rangle \mid M \text{ halts on all inputs with less than } j \text{ 1's} \}.$$

Prove it's a reduction.

- 3. Show that  $\overline{E_{TM}}$  is recognizable by giving a high level description of a nondeterministic TM which recognizes it.
- 4. Show that  $\{\langle M_1, M_2 \rangle \mid L(M_1) \cap L(M_2) = \emptyset\}$  is not recognizable. Use  $E_{TM}$ .
- 5. Say a TM M is reversible if for every string w, M accepts w iff M accepts the reverse of w. (Recall that the reverse of  $w_1w_2...w_k$  is  $w_kw_{k-1}...w_1$ .) Prove that the language

$$T = \{ \langle M \rangle \mid M \text{ is a reversible TM} \}$$

is undecidable.