

Solution 4

1.

(a) Direct-mapped: 3-bit **Block** = \mathbf{A}_{5-3} , 1-bit **Word** = \mathbf{A}_2 ; miss rate = 6/10.

| Tag | Word 1 | Word 0 | |
|--------|--------|--------|---------|
| 001000 | [20C] | [208] | Block 0 |
| 000010 | [094] | [090] | Block 1 |
| 001001 | [25C] | [258] | Block 2 |
| | | | Block 3 |
| | | | Block 4 |
| | | | Block 5 |
| | | | Block 6 |
| | | | Block 7 |

(b) 2-way set-associative: 2-bit **Set** = \mathbf{A}_{4-3} , 1-bit **Word** = \mathbf{A}_2 ; miss rate = 5/10.

| Tag | Word 1 | Word 0 | |
|---------|--------|--------|-------|
| | | | Set 0 |
| | | | Set 0 |
| 0010000 | [20C] | [208] | Set 1 |
| | | | Set 1 |
| 0000100 | [094] | [090] | Set 2 |
| 0010010 | [254] | [250] | Set 2 |
| 0000100 | [09C] | [098] | Set 3 |
| 0010010 | [25C] | [258] | Set 3 |

(c) Fully associative: 1-bit **Word** = **A**₂; miss rate = 5/10.

| Tag | Word 1 | Word 0 |
|-----------|--------|--------|
| 000010011 | [09C] | [098] |
| 000010010 | [094] | [090] |
| 001001010 | [254] | [250] |
| 001000001 | [20C] | [208] |
| 001001011 | [25C] | [258] |
| | | |
| | | |
| | | |

2.

(a) Direct-mapped: 2-bit **Block** = **A**₆₋₅, 3-bit **Word** = **A**₄₋₂; miss rate = 5/10.

[illegible]

(b) 4-way set-associative: 1-bit **Set** = **A₅**, 3-bit **Word** = **A₄₋₂**; miss rate = 5/10.

| Tag | Word 7 | Word 6 | Word 5 | Word 4 | Word 3 | Word 2 | Word 1 | Word 0 | |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|-------|
| 001000 | [21C] | [218] | [214] | [210] | [20C] | [208] | [204] | [200] | Set 0 |
| 000010 | [09C] | [098] | [094] | [090] | [08C] | [088] | [084] | [080] | Set 0 |
| 001000 | [23C] | [238] | [234] | [230] | [22C] | [228] | [224] | [220] | Set 1 |
| | | | | | | | | | Set 1 |

(c) Fully associative: 3-bit **Word** = **A₄₋₂**; miss rate = 4/10.

| Tag | Word 7 | Word 6 | Word 5 | Word 4 | Word 3 | Word 2 | Word 1 | Word 0 |
|---------|--------|--------|--------|--------|--------|--------|--------|--------|
| 0000100 | [09C] | [098] | [094] | [090] | [08C] | [088] | [084] | [080] |
| 0010010 | [25C] | [258] | [254] | [250] | [24C] | [248] | [244] | [240] |
| 0010000 | [21C] | [218] | [214] | [210] | [20C] | [208] | [204] | [200] |
| 0010001 | [23C] | [238] | [234] | [230] | [22C] | [228] | [224] | [220] |

3.

$$T_{ave} = h_1 C_1 + (1-h_1)h_2 C_2 + (1-h_1)(1-h_2)M = 7.2\tau - 4.8h_2.$$

If $h_2 = 1$ (i.e., 100% hit rate), then $T_{ave} = 2.4\tau$ (minimum).

If $T_{ave} = 4\tau$, then $h_2 = 2/3$ (i.e., 67% hit rate).