

CSC 226 - Fall 2014

Pseudocode for a Union-Find Data Structure

The pseudocode listings below give the three core operations for a union-find structure with union-by-rank and path compression. The listings on the left use an object-based linked structure and the listings on the right use a flat array representation. For clarity, the arrays in the right-hand listings are treated as global variables. An actual implementation should avoid this and instead have the **parent** and **rank** arrays be accepted as arguments to each function. The array-based version requires that the maximum number of elements n be fixed in advance (since the arrays have a fixed size).

Note: The term ‘rank’ is not defined consistently between sources. Depending on the interpretation, it may refer to the number of items in a set or the height of the corresponding union-find tree. Both interpretations give the same running times in a union-find structure when used consistently. Formally, the term ‘rank’ refers to the size of a set. Pseudocode for both versions are given here.

The version below uses ‘rank’ to refer to set size.

```
1:
2:
3:
4: procedure MAKESET( $k$ )
5:   node  $\leftarrow$  new Node
6:   node.value  $\leftarrow k$ 
7:   node.rank  $\leftarrow 0$ 
8:   node.parent  $\leftarrow$  node
9:   return node
10: end procedure
11:
12: procedure FIND( $X$ )
13:   if  $X$ .parent =  $X$  then
14:     return  $X$ 
15:   else
16:      $X$ .parent  $\leftarrow$  FIND( $X$ .parent)
17:     return  $X$ .parent
18:   end if
19: end procedure
20:
21: procedure UNION( $X, Y$ )
22:    $X \leftarrow$  FIND( $X$ )
23:    $Y \leftarrow$  FIND( $Y$ )
24:   if  $X$ .rank >  $Y$ .rank then
25:      $Y$ .parent  $\leftarrow X$ 
26:      $X$ .rank  $\leftarrow X$ .rank +  $Y$ .rank
27:   else
28:      $X$ .parent  $\leftarrow Y$ 
29:      $Y$ .rank  $\leftarrow X$ .rank +  $Y$ .rank
30:   end if
31: end procedure
```

```
parent  $\leftarrow$  Array of  $n$  integers.
rank  $\leftarrow$  Array of  $n$  integers.

procedure MAKESET( $k$ )
  parent[ $k$ ]  $\leftarrow k$ 
  rank[ $k$ ]  $\leftarrow 0$ 
end procedure

procedure FIND( $x$ )
  if parent[ $x$ ] =  $x$  then
    return  $x$ 
  else
    parent[ $x$ ]  $\leftarrow$  FIND(parent[ $x$ ])
    return parent[ $x$ ]
  end if
end procedure

procedure UNION( $x, y$ )
   $x \leftarrow$  FIND( $x$ )
   $y \leftarrow$  FIND( $y$ )
  if rank[ $x$ ] > rank[ $y$ ] then
    parent[ $y$ ]  $\leftarrow x$ 
    rank[ $x$ ]  $\leftarrow$  rank[ $x$ ] + rank[ $y$ ]
  else
    parent[ $x$ ]  $\leftarrow y$ 
    rank[ $y$ ]  $\leftarrow$  rank[ $x$ ] + rank[ $y$ ]
  end if
end procedure
```

The version below uses ‘rank’ to refer to the height of the union-find tree.

<pre>1: 2: 3: 4: procedure MAKESET(k) 5: node \leftarrow new Node 6: node.value $\leftarrow k$ 7: node.rank $\leftarrow 0$ 8: node.parent \leftarrow node 9: return node 10: end procedure 11: 12: procedure FIND(X) 13: if X.parent = X then 14: return X 15: else 16: X.parent \leftarrow FIND(X.parent) 17: return X.parent 18: end if 19: end procedure 20: 21: procedure UNION(X, Y) 22: $X \leftarrow$ FIND(X) 23: $Y \leftarrow$ FIND(Y) 24: if X.rank > Y.rank then 25: Y.parent $\leftarrow X$ 26: else 27: X.parent $\leftarrow Y$ 28: Y.rank \leftarrow max(Y.rank, X.rank + 1) 29: end if 30: end procedure</pre>	<pre>parent \leftarrow Array of n integers. rank \leftarrow Array of n integers. procedure MAKESET(k) parent[k] $\leftarrow k$ rank[k] $\leftarrow 0$ end procedure procedure FIND(x) if parent[x] = x then return x else parent[x] \leftarrow FIND(parent[x]) return parent[x] end if end procedure procedure UNION(x, y) $x \leftarrow$ FIND(x) $y \leftarrow$ FIND(y) if rank[x] > rank[y] then parent[y] $\leftarrow x$ else parent[x] $\leftarrow y$ rank[y] \leftarrow max(rank[y], rank[x] + 1) end if end procedure</pre>
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