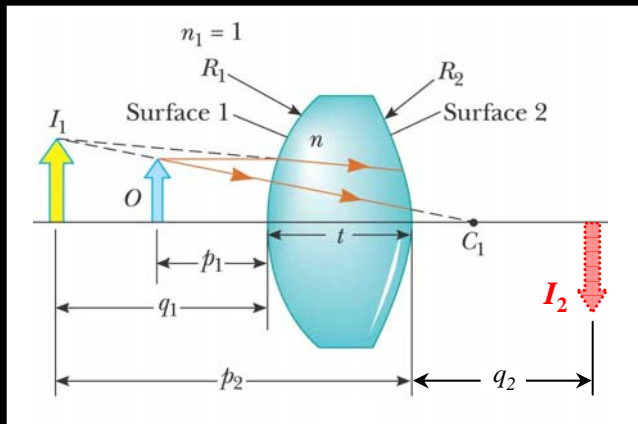


## 36.4 Thin lenses

- 2) A lens with *two spherical surfaces* with radii of curvature  $R_1$  and  $R_2$ .  
 → The image formed by one refracting surface serves as the object for the second surface.



$$\frac{n_1}{p} + \frac{n_2}{q} = \frac{(n_2 - n_1)}{R}$$

$$1/f = (n - 1) \left( 1/R_1 - 1/R_2 \right)$$

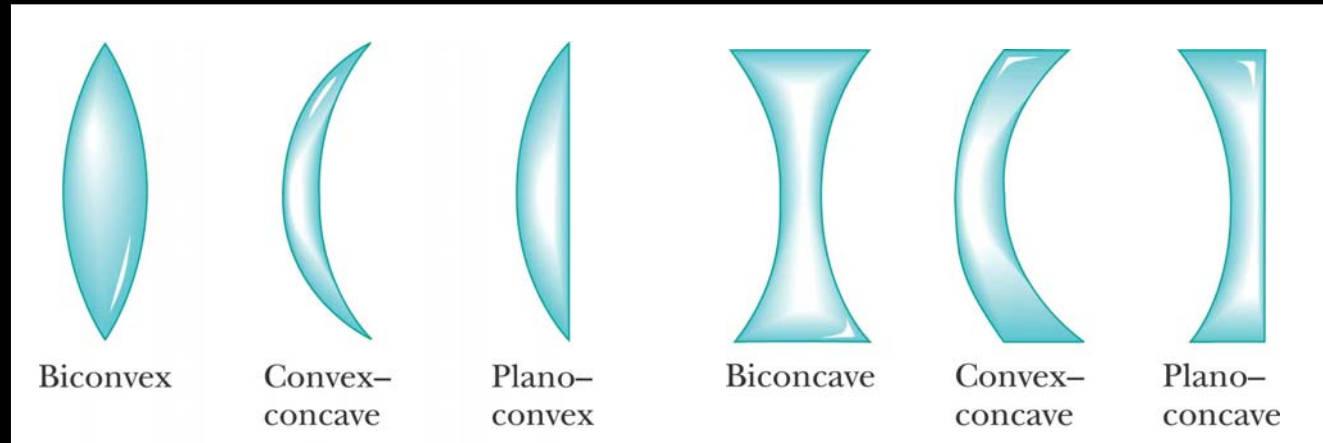
( Lens Makers' Equation )

$$1/p + 1/q = 1/f \quad \text{( Thin Lens Equation )}$$

- Sign conventions for thin lenses :

	p	q	$R_1$ & $R_2$	f
+	real object ( <i>front of lens</i> )	real image ( <i>back of lens</i> )	C is in back of lens	converging
-	virtual object ( <i>back of lens</i> )	virtual image ( <i>front of lens</i> )	C is in front of lens	diverging

### 3) Various lens shapes :



### 2) A lens with two spherical surfaces with radii of curvature $R_1$ and $R_2$ .

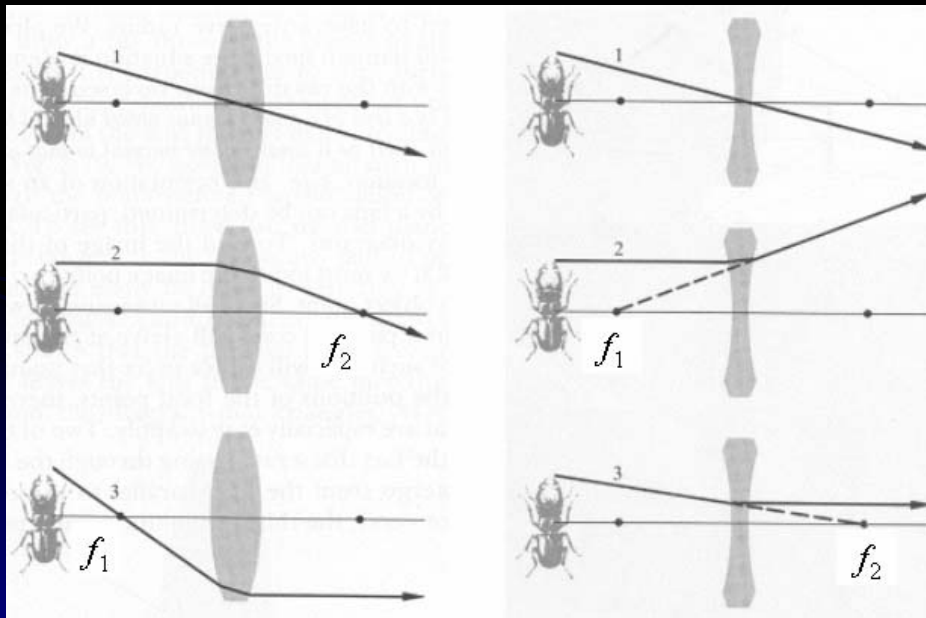
$$\frac{1}{f} = (n - 1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right) \quad (\text{Lens Makers' Equation})$$

$$\frac{1}{p} + \frac{1}{q} = \frac{1}{f} \quad (\text{Thin Lens Equation})$$

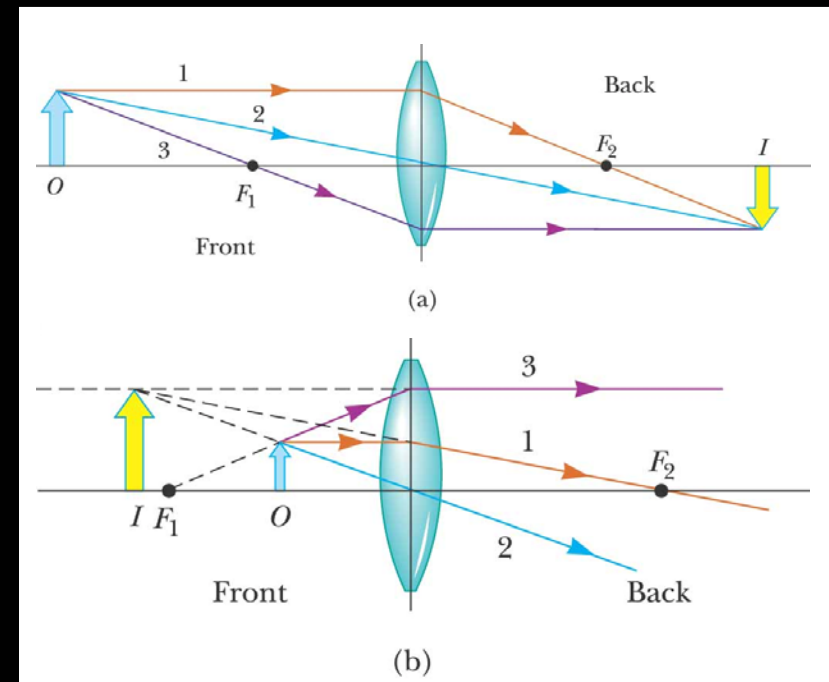
	p	q	$R_1$ & $R_2$	f
+	real object ( <i>front of lens</i> )	real image ( <i>back of lens</i> )	C is in back of lens	converging
-	virtual object ( <i>back of lens</i> )	virtual image ( <i>front of lens</i> )	C is in front of lens	diverging

#### 4) Ray diagrams by using principal rays for convex (and concave) lens.

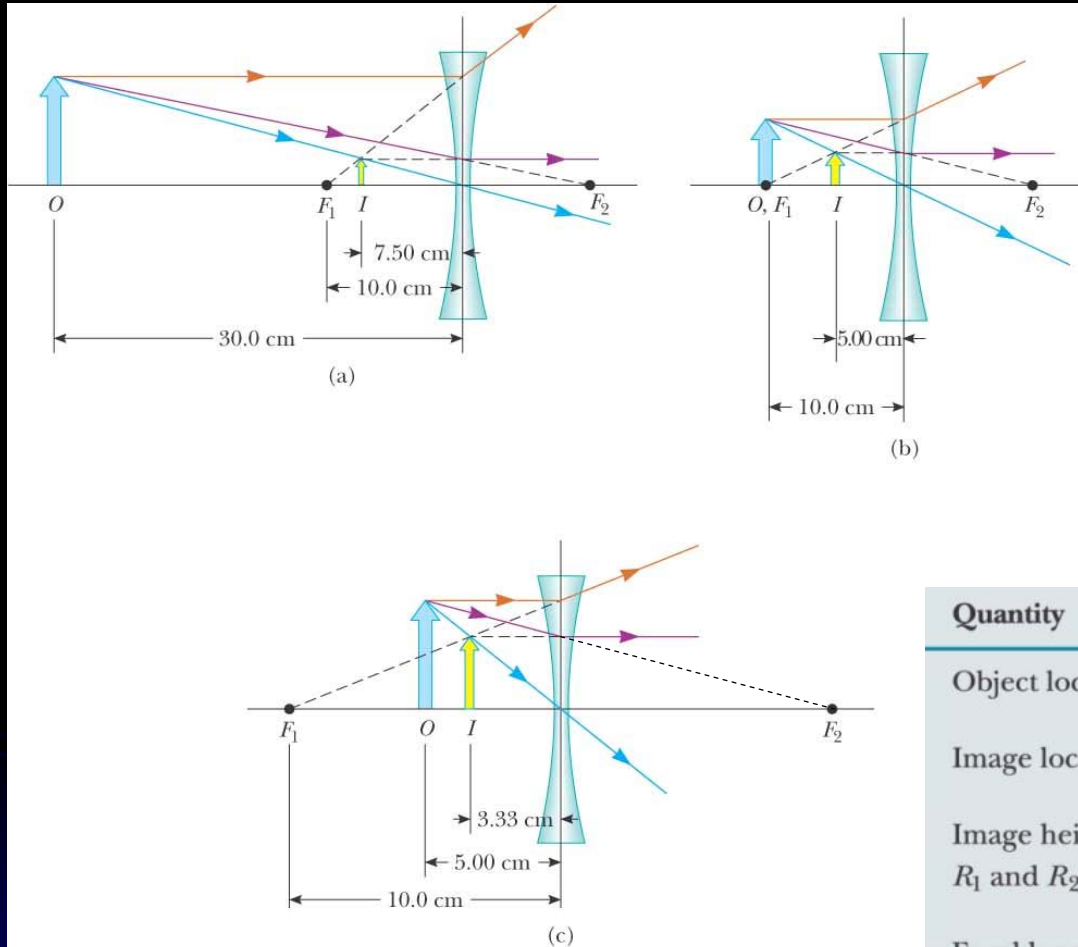
- (1) a ray passing through the center of the lens continues in a straight line.  
(cf. same for concave lens.)
- (2) a ray initially // to the principal axis passes through  $f_2$ .  
(cf. appears from  $f_1$  for concave lens.)
- (3) a ray passing through  $f_1$  continues // to the principal axis.  
(cf. drawn toward  $f_2$  continues // to the principal axis for concave lens.)



#### (A) Convex lens



## (B) Concave lens



Quantity	Positive When	Negative When
Object location ( $p$ )	Object is in front of lens (real object)	Object is in back of lens (virtual object)
Image location ( $q$ )	Image is in back of lens (real image)	Image is in front of lens (virtual image)
Image height ( $h'$ )	Image is upright	Image is inverted
$R_1$ and $R_2$	Center of curvature is in back of lens	Center of curvature is in front of lens
Focal length ( $f$ )	Converging lens	Diverging lens

(Example 36.10) Images formed by a diverging lens.

- (a) The object is farther from the lens than the focal point.
- (b) The object is at the focal point.
- (c) The object is closer to the lens than the focal point.

## 5) Combination of thin lenses :

- (1) The image formed by the 1<sup>st</sup> lens acts as a *real object* for the 2<sup>nd</sup> lens.
- (2) The image formed by the 1<sup>st</sup> lens acts as a *virtual object* for the 2<sup>nd</sup> lens.

$$1/p + 1/q = 1/f$$

( Thin Lens Equation )

	p	q	$R_1$ & $R_2$	f
+	real object ( <i>front of lens</i> )	real image ( <i>back of lens</i> )	C is in back of lens	converging
-	virtual object ( <i>back of lens</i> )	virtual image ( <i>front of lens</i> )	C is in front of lens	diverging