# **PyTimeVar**

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## **ONE**

## **PYTIMEVAR**

## 1.1 PyTimeVar package

## 1.1.1 Subpackages

## PyTimeVar.bhpfilter package

#### **Submodules**

## PyTimeVar.bhpfilter.bHP module

```
class PyTimeVar.bhpfilter.bHP.BoostedHP(vY, dLambda=1600, iMaxIter=100)
```

Bases: object

Class for performing the boosted HP filter

#### **Parameters**

- **vY** (*np.ndarray*) The dependent variable (response) array.
- **dLambda** (*float*) The smoothing parameter.
- **iMaxIter** (*int*) The maximum number of iterations for the boosting algorithm.

vΥ

The input time series data.

#### Type

array-like

#### dLambda

The smoothing parameter.

#### Type

float

#### **iMaxIter**

The maximum number of iterations for the boosting algorithm.

#### Type

int

#### results

A tuple containing the results of the Boosted HP filter.

```
Type
              tuple
dAlpha
     The significance level for the stopping criterion 'adf'.
          Type
              float
stop
     Stopping criterion ('adf', 'bic', 'aic', 'hq').
          Type
              string
results
     Contains the trends per iteration, the current residuals, the information criteria values, the number of iter-
     ations, and the estimated trend.
          Type
              tuple
fit()
     Fits the Boosted HP filter to the data.
summary()
     Prints a summary of the results.
plot()
     Plot true data against estimated trend.
fit(boost=True, stop='adf', dAlpha=0.05, verbose=False)
     Fits the Boosted HP filter to the data.
          Parameters
               • boost (bool) – if True, boosting is used.
               • stop (str) – Stopping criterion ('adf', 'bic', 'aic', 'hq').
               • dAlpha (float) – The significance level for the stopping criterion 'adf'.
               • verbose (bool) – Whether to display a progress bar.
          Returns
               • vbHP (np.ndarray) – The estimated trend.
               • vCurrentRes (np.ndarray) – The residuals.
plot()
     Plots the true data against estimated trend
summary()
     Prints a summary of the results.
```

#### **Module contents**

#### PyTimeVar.datasets package

#### **Subpackages**

#### PyTimeVar.datasets.co2 package

#### **Submodules**

## PyTimeVar.datasets.co2.data module

PyTimeVar.datasets.co2.data.load(start\_date=None, end\_date=None, regions=None)

Load the CO2 emissions dataset and optionally filter by date range and/or countries. This dataset contains the emissions data from 1900 to 2017, for a range of countries.

#### **Parameters**

- start\_date (str, optional) The start\_year to filter the data. Format 'YYYY'. Minimum start year is 1900.
- end\_date (str, optional) The end\_year to filter the data. Format 'YYYY'.
- **regions** (list, optional) Regions to be selected from data.

#### Returns

DataFrame containing the filtered data with columns 'Date' and regions.

#### **Return type**

pandas.DataFrame

#### Warning

Prints warnings if any provided regions are not found in the dataset. Prints warnings if the start\_year is earlier than the minimum year in the data or the end\_year is later than the maximum year in the data.

#### **Module contents**

## PyTimeVar.datasets.gold package

#### **Submodules**

#### PyTimeVar.datasets.gold.data module

PyTimeVar.datasets.gold.data.load(currencies=None, start\_date=None, end\_date=None)

Load the gold dataset and optionally filter by specific currencies and date range.

#### **Parameters**

• **currencies** (list, optional) – List of currency codes to filter the dataset by. Available options are: ['USD', 'EUR', 'JPY', 'GBP', 'CAD', 'CHF', 'INR', 'CNY', 'TRY', 'SAR',

```
'IDR', 'AED', 'THB', 'VND', 'EGP', 'KRW', 'RUB', 'ZAR', 'AUD']
```

- **start\_date**(*str*, *optional*) The start date to filter the data. Format 'YYYY-MM-DD'.
- end\_date (str, optional) The end date to filter the data. Format 'YYYY-MM-DD'.

DataFrame containing the filtered data.

#### Return type

pandas.DataFrame



#### Warning

Prints warnings if any provided currencies are not found in the dataset. Prints warnings if the start\_date is earlier than the minimum date in the data or the end date is later than the maximum date in the data.

#### Module contents

## PyTimeVar.datasets.herding package

#### **Submodules**

#### PyTimeVar.datasets.herding.data module

PyTimeVar.datasets.herding.data.load(start\_date=None, end\_date=None, data\_replication=False)

Load the Herding dataset and optionally filter by date range. This dataset contains the herding data from Jan 5 2015 to Apr 29 2022.

#### **Parameters**

- start\_date (str, optional) The start\_year to filter the data. Format 'YYYY-MM-DD'. Minimum start year is 1900.
- end\_date (str, optional) The end\_year to filter the data. Format 'YYYY'.

#### Returns

DataFrame containing the filtered data with columns 'Date' and 'Herding'.

#### Return type

pandas.DataFrame



#### Warning

Prints warnings if any provided regions are not found in the dataset. Prints warnings if the start\_year is earlier than the minimum year in the data or the end\_year is later than the maximum year in the data.

#### **Module contents**

#### PyTimeVar.datasets.temperature package

#### **Submodules**

#### PyTimeVar.datasets.temperature.data module

PyTimeVar.datasets.temperature.data.load(regions=None, start\_date=None, end\_date=None)

Load the temperature dataset and optionally filter by specific regions and date range. This dataset contains the average yearly temperature change in degrees Celsius for different regions of the world from 1961 to 2023. :param regions: List of regions to filter the dataset by. Available options are:

['World', 'Africa', 'Asia', 'Europe', 'North America', 'Oceania', 'South America']

#### **Parameters**

- **start\_date** (*str*, *optional*) The start date to filter the data. Format 'YYYY-MM-DD'.
- end\_date (str, optional) The end date to filter the data. Format 'YYYY-MM-DD'.

#### Returns

DataFrame containing the filtered data.

#### Return type

pandas.DataFrame



#### Warning

Prints warnings if any provided regions are not found in the dataset. Prints warnings if the start\_year is earlier than the minimum year in the data or the end\_year is later than the maximum year in the data.

#### **Module contents**

## PyTimeVar.datasets.usd package

#### **Submodules**

#### PyTimeVar.datasets.usd.data module

PyTimeVar.datasets.usd.data.load(type='Open', start\_date=None, end\_date=None)

Load the USD index dataset and optionally filter by date range.

- type (str, optional) The type of data to load. Available options are: ['Open', 'High', 'Low', 'Close']
- **start\_date** (*str*, *optional*) The start date to filter the data. Format 'YYYY-MM-DD'.
- end\_date (str, optional) The end date to filter the data. Format 'YYYY-MM-DD'.

DataFrame containing the filtered data.

#### **Return type**

pandas.DataFrame



#### Warning

Prints warnings if any provided currencies are not found in the dataset. Prints warnings if the start\_date is earlier than the minimum date in the data or the end\_date is later than the maximum date in the data.

#### Module contents

#### **Submodules**

## PyTimeVar.datasets.utils module

PyTimeVar.datasets.utils.load\_csv(base\_file, csv\_name, sep=',', convert\_float=False) Standard simple csv loader

#### Module contents

Dataset module for PyTimeVar package.

#### PyTimeVar.gas package

#### **Submodules**

#### PyTimeVar.gas.GAS module

class PyTimeVar.gas.GAS.GAS(vY: ndarray, mX: ndarray, method: str = 'none', vgamma0: ndarray | None = *None, bounds: list* | None = None, options: dict | None = None, maxiter: int = 5)

Bases: object

Class for performing score-driven (GAS) filtering.

- **vY** (*np.ndarray*) The dependent variable (response) array.
- **mX** (*np.ndarray*) The independent variable (predictor) matrix.
- **method** (*string*) Method to estimate GAS model.
- **vgamma0** (*np.ndarray*) Initial parameter vector.
- **bounds** (*list*) List to define parameter space.
- **options** (*dict*) Stopping criteria for optimization.
- maxiter (int) Maximum number of repitions of the optimization algorithm. If not provided, default is set to five repitions with different initial parameters.

```
vΥ
     The dependent variable (response) array.
         Type
              np.ndarray
mΧ
     The independent variable (predictor) matrix.
         Type
             np.ndarray
n
     The length of vY.
         Type
             int
n_est
     The number of coefficients.
         Type
             int
method
     Method to estimate GAS model.
         Type
             string
vgamma0
     The initial parameter vector.
         Type
              np.ndarray
maxiter
     Maximum number of repitions of the optimization algorithm.
         Type
             int
bounds
     List to define parameter space.
         Type
             list
options
     Stopping criteria for optimization.
         Type
             dict
success
     If True, optimization was successful.
         Type
```

bool

#### betas

The estimated coefficients.

#### **Type**

np.ndarray

#### params

The estimated GAS parameters.

#### **Type**

np.ndarray

#### fit()

Fit score-driven model, according to the specified method ('gaussian' or 'student')

#### plot()

Plot estimated coefficients against true data

#### construct\_likelihood(vbeta0, vpara)

Calculated the log-likelihood value, according to the specified self.method.

#### **Parameters**

- **vbeta0** (*np.ndarray*) Initial coefficients at time zero.
- **vpara** (*np.ndarray*) Array of GAS parameters.

#### Returns

lhVal – Log-likelihood value.

#### **Return type**

float

### fit()

Fit score-driven model, according to the specified method ('gaussian' or 'student')

#### **Returns**

- **mBetaHat** (*np.ndarray*) The estimated coefficients.
- **vparaHat** (*np.ndarray*) The estimated GAS parameters.

#### plot()

Plot the beta coefficients over a normalized x-axis from 0 to 1.

#### **Module contents**

#### PyTimeVar.kalman package

#### **Submodules**

#### PyTimeVar.kalman.kalman module

```
class PyTimeVar.kalman.kalman.Kalman(vY: ndarray \mid None = None, T: ndarray \mid None = None, R: ndarray \mid None = None, sigma_u: float \mid None = None, b_1: ndarray \mid None = None, P_1: ndarray \mid None = None, mX: ndarray \mid None = None)
```

Bases: object

Class for performing Kalman filtering and smoothing.

#### **Parameters**

- **vY** (*np.ndarray*) The dependent variable (response) array.
- **T** (*np.ndarray*, *optional*) The transition matrix of the state space model.
- **R** (*np.ndarray*, *optional*) The transition correlation matrix of the state space model.
- Q (np.ndarray, optional) The transition covariance matrix of the state space model.
- **sigma\_u** (*np.ndarray*, *optional*) The observation noise variance of the state space model.
- **b\_1** (*np.ndarray*, *optional*) The initial mean of the state space model.
- **P\_1** (*np.ndarray*, *optional*) The initial covariance matrix of the state space model.
- mX (np.ndarray, optional) The regressors to use in the model. If provided, the model will be a linear regression model.

vΥ

The dependent variable (response) array.

```
Type
```

np.ndarray

n

The length of vY.

#### Type

int

#### isReg

If True, regressors are provided by the user.

#### **Type**

bool

Т

The transition matrix of the state space model.

#### **Type**

np.ndarray

Z

Auxiliary (1,1)-vector of a scalar 1. This is used in case there are no regressors.

## Type

np.ndarray

R

The transition correlation matrix of the state space model.

#### Type

np.ndarray

```
Q
     The transition covariance matrix of the state space model.
          Type
              np.ndarray
Н
     The observation noise variance of the state space model.
          Type
              np.ndarray
a_1
     The initial mean of the state space model.
          Type
              np.ndarray, optional
P_1
     The initial covariance matrix of the state space model.
          Type
              np.ndarray
mΧ
     The regressors to use in the model. If provided, the model will be a linear regression model.
          Type
              np.ndarray
Z_reg
     The regressors matrix in correct format to use in filtering.
          Type
              np.ndarray
p_dim
     The number of coefficients.
          Type
              int
m_dim
     The number of response variables. This is always 1.
          Type
              int
filt
     The filtered coefficients.
          Type
              np.ndarray
smooth
     The smoothed coefficients.
fit()
     Fit state-space model by Kalman filter or smoother, according to the specified option ('filter' or 'smoother')
```

#### summary()

Print a summary of the Kalman filter/smoother specifications, including the values of H, Q, R and T

#### plot()

Plot filtered/smoothed estimates against true data

#### compute\_likelihood\_LL(vTheta)

Computes the negative log-likelihood value for a given parameter vector.

#### **Parameters**

**vTheta** (*np.ndarray*) – The parameter vector.

#### **Returns**

The negative log-likelihood value.

#### Return type

float

#### filter()

Performs the filtering step of the Kalman filter.

#### Returns

The filtered state means at each time step.

#### **Return type**

np.ndarray

#### fit(option)

Fits the Kalman filter or smoother to the data.

#### **Parameters**

**option** (*string*) – Denotes the fitted trend: filter or smoother.

#### Raises

**ValueError** – No valid option is provided.

#### **Returns**

Estimated trend.

#### **Return type**

np.ndarray

#### plot()

Plot the beta coefficients over a normalized x-axis from 0 to 1 or over a date range.

#### smoother()

Performs the smoothing step of the Kalman filter.

#### Returns

The smoothed state means at each time step.

#### Return type

np.ndarray

#### summary()

Prints a summary of the state-space model specification.

#### **Module contents**

#### PyTimeVar.locallinear package

#### **Submodules**

#### PyTimeVar.locallinear.LLR module

```
class PyTimeVar.locallinear.LLR.LocalLinear(vY: ndarray, mX: ndarray, h: float = 0, bw\_selection: str | None = None, tau: ndarray | None = None, kernel: str = 'epanechnikov', LB\_bw: float | None = None, UB\_bw: float | None = None)
```

Bases: object

Class for performing local linear regression (LLR).

Local linear regression is a non-parametric regression method that fits linear models to localized subsets of the data to form a regression function. The code is based on the code provided by Lin et al. [1].

#### **Parameters**

- **vY** (*np.ndarray*) The dependent variable (response) array.
- **mX** (*np.ndarray*) The independent variable (predictor) matrix.
- **h** (*float*) The bandwidth parameter controlling the size of the local neighborhood. If not provided, it is estimated as the average of all methods in the package.
- **bw\_selection** (*string*) The name of the bandwidth selection method to be used. Choice between 'aic', 'gcv', 'lmcv-l' with l=0,2,4,6,etc., or 'all'. If not provided, it is set to 'all'.
- **tau** (*np.ndarray*) The array of points at which predictions are made. If not provided, it is set to a linear space between 0 and 1 with the same length as *vY*.
- **kernel** (*string*) The name of the kernel function used for estimation. If not provided, it is set to 'epanechnikov' for the Epanechnikov kernel.
- **LB\_bw** (*float*) The lower bound for the bandwidth selection. If not provided, it is set to 0.06.
- **UB\_bw** (*float*) The upper bound for the bandwidth selection. If not provided, it is set to 0.2 for LMCV-1 and to 0.7 for AIC and GCV.

vΥ

The response variable array.

```
Type
```

np.ndarray

 $\mathbf{m}\mathbf{X}$ 

The predictor matrix.

Type

np.ndarray

n

The length of vY.

Type

int

#### times

Linearly spaced time points for the local regression.

## Type

np.ndarray

#### tau

Points at which the regression is evaluated.

#### Type

np.ndarray

#### n\_est

The number of coefficients.

#### **Type**

int

#### kernel

The name of the kernel function.

#### Type

string

#### bw\_selection

The name of the bandwidth selection.

## Type

string

#### lmcv\_type

If LMCV is used for bandwidth selection, this attribute denotes the l in leave-2\*l+1-out.

## Type

float

#### dict\_bw

The dictionary that contains the optimnal bandwidth values for each individual method.

#### **Type**

dict

## h

The bandwidth used for local linear regression.

#### **Type**

float

#### betahat

The estimated coefficients.

#### Type

np.ndarray

#### predicted\_y

The fitted values for the response variable.

### Type

np.ndarray

#### residuals

The residuals resulting from the local linear regression.

#### **Type**

np.ndarray

#### fit()

Fit the model by local linear estimation and return estimated coefficients.

#### summary()

Print a summary of local linear regression results, including bandwidth, number of observations, and beta coefficients.

#### plot\_betas()

Plot estimated coefficients curve over a normalized x-axis from 0 to 1.

#### plot\_predicted()

Plot true data against fitted values.

#### plot\_residuals()

Plot residuals.

#### confidence\_bands()

Construct and plot bootstrap confidence intervals/bands for each coefficient curve.

#### **Notes**

The local linear regression is computed at each point specified in tau. The bandwidth h controls the degree of smoothing.

#### References

#### [1] Lin Y, Song M, van der Sluis B (2024),

Bootstrap inference for linear time-varying coefficient models in locally stationary time series, Journal of Computational and Graphical Statistics, Forthcoming.

#### ABS\_value(qtau, diff, tau, alpha, B)

Calculate the absolute value for quantiles.

#### **Parameters**

- qtau (np.ndarray) Array of quantiles.
- **diff** (*np.ndarray*) Difference array.
- tau (np.ndarray) Array of tau values.
- **alpha** (*float*) The significance level.
- **B** (*int*) The number of bootstrap samples.

#### Returns

Absolute value for quantiles.

#### Return type

float

#### AICmodx(h)

Computes the AIC value for a given mean squared error and trace.

#### **Parameters**

**h** (*float*) – The bandwidth parameter.

#### Returns

AIC value.

### Return type

float

AR(zhat, T, ic=None)

Estimate the AR model and compute residuals.

#### **Parameters**

- **zhat** (*np.ndarray*) Array of predicted values.
- T (int) Number of observations.
- ic (string) Information criterion to select number of lags. Default criterion is AIC

#### Returns

- **epsilonhat** (*np.ndarray*) Array of residuals.
- max\_lag (int) Maximum lag order.
- **armodel** (*AutoReg*) Fitted autoregressive model.

AW\_BT(zhat: ndarray, mX: ndarray, betatilde: ndarray, T: int, h: float, gamma: float)

Autoregressive Wild Bootstrap Compute a bootstrap sample using the autoregressive wild bootstrap.

#### **Parameters**

- **zhat** (*np.ndarray*) Array of residuals.
- **mX** (*np.ndarray*) Array of exogenous variables.
- **betatilde** (*np.ndarray*) Array of estimated coefficients.
- T (int) Total number of observations.
- **h** (*float*) The bandwidth parameter.
- gamma (float) The AR(1) coefficient and the standard deviation of the wild component in the AWB.

#### Returns

**vYstar** – Transformed response variable.

## Return type

np.ndarray

#### GCVmodx(h)

Computes the GCV value for a bandwidth value.

#### **Parameters**

**h** (*float*) – The bandwidth parameter.

#### Returns

GCV value.

#### Return type

float

#### $K_ZW_Q(vTi\ t,h)$

Kernel function for Multiplier Bootstrap quantile.

#### **Parameters**

- **vTi\_t** (*np.ndarray*) The array of time indices.
- **h** (*float*) The bandwidth parameter.

#### Returns

Array of kernel values.

#### Return type

np.ndarray

LBW\_BT(zhat: ndarray, mX: ndarray, betatilde: ndarray, T: int, h: float, gamma: float)

Local Blockwise Wild Bootstrap Performs the local blockwise wild bootstrap algorithm to generate a bootstrap sample.

#### **Parameters**

- **zhat** (*np.ndarray*) The input array of shape (T, 1) containing the original data.
- **mX** (*np.ndarray*) The input array of shape (T, k) containing the covariates.
- **betatilde** (*np.ndarray*) The input array of shape (k,) or (k, 1) containing the estimated coefficients.
- **T** (*int*) The number of observations.
- h(float) The bandwidth parameter.
- gamma (*float*) The AR(1) coefficient and the standard deviation of the wild component in the AWB.

#### Returns

vYstar – The bootstrap sample generated by the LBW\_BT algorithm.

#### Return type

np.ndarray

#### $MC_ZW(alpha, h, vY, mX, T, B)$

Perform the Multiplier Bootstrap bootstrap algorithm. Zhou, Z., & Wu, W. B. (2010). Simultaneous inference of linear models with time varying coefficients. Journal of the Royal Statistical Society. Series B (Statistical Methodology), 72(4), 513-531. http://www.jstor.org/stable/40802223

#### **Parameters**

- **alpha** The significance level for the bootstrap.
- **h** (*float*) Bandwidth parameter.
- **vY** (*np.ndarray*) Array of dependent variable values.
- mX (np.ndarray) Array of covariates.
- T (int) Number of observations.
- **B** (*int*) Number of bootstrap iterations.

#### Returns

Lower and upper confidence bands and beta coefficients.

#### Return type

tuple

SW\_BT(epsilontilde: ndarray, max\_lag: int, armodel, mX: ndarray, betatilde: ndarray, T: int)

Sieve Wild Bootstrap Calculate the transformed response variable using the local linear regression model.

#### **Parameters**

- **epsilontilde** (*np.ndarray*) Array of residuals.
- max\_lag (int) Maximum lag order.
- armodel (AutoReg) Fitted autoregressive model.
- **mX** (*np.ndarray*) Array of exogenous variables.
- **betatilde** (*np.ndarray*) Array of estimated coefficients.
- **T** (*int*) Total number of observations.

#### Returns

vYstar - Transformed response variable.

#### Return type

np.ndarray

**S\_BT**(epsilontilde: ndarray, max\_lag: int, armodel, mX: ndarray, betatilde: ndarray, T: int)

Sieve Bootstrap Calculate the transformed response variable using the local linear regression model.

#### **Parameters**

- **epsilontilde** (*np.ndarray*) Array of residuals.
- max\_lag (int) Maximum lag order for the autoregressive model.
- armodel (AutoReg) Fitted autoregressive model.
- **mX** (*np.ndarray*) Array of exogenous variables.
- **betatilde** (*np.ndarray*) Array of estimated coefficients.
- **T** (*int*) Total number of observations.

#### **Returns**

vYstar - Transformed response variable.

#### Return type

np.ndarray

**W\_BT**(zhat: ndarray, mX: ndarray, betatilde: ndarray, T: int, h: float, gamma: float)

Wild Bootstrap Calculate the transformed response variable using the local linear regression model.

#### **Parameters**

- **zhat** (*np.ndarray*) Array of residuals.
- **mX** (*np.ndarray*) Array of exogenous variables.
- **betatilde** (*np.ndarray*) Array of estimated coefficients.
- T (int) Total number of observations.
- **h** (*float*) The bandwidth parameter.
- **gamma** (*float*) The AR(1) coefficient and the standard deviation of the wild component in the AWB.

#### Returns

vYstar - Transformed response variable.

#### Return type

np.ndarray

#### bandwidth\_selection(LB\_bw, UB\_bw)

Calculate the optimal bandwidth for the local linear regression model using LMCV, AIC and GCV.

#### **Parameters**

- LB\_bw (float) The lower bound for the bandwidth selection.
- $UB_bw(float)$  The upper bound for the bandwidth selection

#### Returns

The optimal bandwidths for each individual method.

#### Return type

dict

confidence\_bands (bootstrap\_type: str = 'LBWB', alpha: float | None = None, gamma: float | None = None, ic: str | None = None, Gsubs=None, Chtilde: float = 2, B: float = 1299, plots: bool = False)

#### **Parameters**

- bootstraptype (str) Type of bootstrap to use ('SB', 'WB', 'SWB', 'MB', 'LBWB, 'AWB').
- **alpha** (*float*) Significance level for quantiles.
- gamma (float) Parameter value for Autoregressive Wild Bootstrap.
- **ic**(*str*) Type of information criterion to use for Sieve and Sieve Wild Bootstrap. Possible values are: 'aic', 'hqic', 'bic'
- **Gsubs** (*list of tuples*) List of sub-ranges for G. Each sub-range is a tuple (start\_index, end\_index). Default is None, which uses the full range (0, T).
- **Chtilde** (*float*) Multiplication constant to determine size of oversmoothing bandwidth htilde. Default is 2, if none or negative is specified.
- **B** (*int*) The number of bootstrap samples. Deafult is 1299, if not provided by the user.
- **plots** (*bool*) If True, plots are shown of the estimated coefficients and corresponding confidence bands.

#### Returns

- **S\_LB** (*np.ndarray*) The lower simultaneous confidence bands.
- **S\_UB** (*np.ndarray*) The upper simultaneous confidence bands.
- **P\_LB** (*np.ndarray*) The lower pointwise confidence intervals.
- **P\_UB** (*np.ndarray*) The upper pointwise confidence intervals.

```
construct_confidence_bands(bootstraptype: str, alpha: float | None = None, gamma: float | None = None, ic: str | None = None, Gsubs: list | None = None, Chtilde: float | None = None, B: float = 1299)
```

Construct confidence bands using bootstrap methods.

- bootstraptype (str) Type of bootstrap to use ('SB', 'WB', 'SWB', 'MB', 'LBWB, 'AWB').
- **alpha** (*float*) Significance level for quantiles.

- gamma (float) Parameter value for Autoregressive Wild Bootstrap.
- ic(str) Type of information criterion to use for Sieve and Sieve Wild Bootstrap. Possible values are: 'aic', 'hqic', 'bic'
- **Gsubs** (*list of tuples*) List of sub-ranges for G. Each sub-range is a tuple (start\_index, end\_index). Default is None, which uses the full range (0, T).
- **Chtilde** (*float*) Multiplication constant to determine size of oversmoothing bandwidth htilde. Default is 2, if none or negative is specified.
- **B** (*int*) The number of bootstrap samples. Deafult is 1299, if not provided by the user.

Each tuple contains simultaneous and pointwise lower and upper bands for each sub-range, and beta coefficients for each sub-range.

#### Return type

list of tuples

#### fit()

Fits the local linear regression model to the data.

#### Returns

**self.betahat** – The estimated coefficients.

#### Return type

np.ndarray

#### getDelta(mX, vEps, iM)

Calculate delta values for Multiplier Bootstrap samples.

#### **Parameters**

- **mX** (*np.ndarray*) Array of covariates.
- **vEps** (*np.ndarray*) Array of residuals.
- iM (int) Number of blocks.

#### **Returns**

Array of delta values.

#### Return type

np.ndarray

getLambda(mmDelta, iN, iM, taut, dT, dTau, dGamma)

Calculate lambda values for Multiplier Bootstrap samples.

- mmDelta (np.ndarray) Array of delta values.
- **iN** (*int*) Number of observations.
- **iM** (*int*) Number of blocks.
- taut (np.ndarray) Array of tau values.
- **dT** (*float*) Time parameter.
- dTau (float) Tau parameter.
- dGamma (float) Gamma parameter.

Array of lambda values.

#### **Return type**

np.ndarray

```
getM(mX, T, dT, h)
```

Calculate M values for Multiplier Bootstrap samples.

#### **Parameters**

- mX (np.ndarray) Array of covariates.
- T (int) Number of observations.
- **dT** (*float*) Time parameter.
- **h** (*float*) Bandwidth parameter.

#### **Returns**

Array of M values.

#### Return type

np.ndarray

```
getQ(B, T, taut, h, alpha)
```

Calculate quantile for Multiplier Bootstrap samples.

#### **Parameters**

- **B** (*int*) The number of bootstrap samples.
- **T** (*int*) the number of observations.
- taut (np.ndarray) The points at which the regression is evaluated.
- **h** (*float*) Bandwidth parameter.
- alpha (float) Alpha level for quantiles.

#### **Returns**

dQ - Quantile value.

#### **Return type**

float

```
getSigma(mM, mLam)
```

Calculate sigma values for Multiplier Bootstrap samples.

#### **Parameters**

- mM (np.ndarray) Array of M values.
- mLam (np.ndarray) Array of lambda values.

#### Returns

Array of sigma values.

#### Return type

np.ndarray

#### min\_alphap(diff, tau, alpha, B)

Calculate the minimum alpha value for confidence bands.

- **diff** (*np.ndarray*) Difference array.
- tau (np.ndarray) Array of tau values.
- alpha (float) The significance level.
- **B** (*int*) The number of bootstrap samples.

Minimum alpha value.

#### Return type

float

#### plot\_betas()

Plot the beta coefficients over a normalized x-axis from 0 to 1.

#### plot\_predicted()

Plot the actual values of Y against the predicted values of Y over a normalized x-axis from 0 to 1.

#### plot\_residuals()

Plot the residuals over a normalized x-axis from 0 to 1.

#### Returns

self.residuals - Array of residuals.

#### **Return type**

np.ndarray

#### summary()

Print a summary of the regression results.

#### Module contents

#### PyTimeVar.powerlaw package

#### **Submodules**

#### PyTimeVar.powerlaw.pwr module

```
class PyTimeVar.powerlaw.pwr.PowerLaw(vY: ndarray, n\_powers: float \mid None = None, vgamma0: ndarray \mid None = None, options: dict \mid None = None)
```

Bases: object

Class for implementing the Power-Law method.

#### **Parameters**

- **vY** (*np.ndarray*) The dependent variable (response) array.
- **n\_powers** (*int*) The number of powers.
- **vgamma0** (*np.ndarray*) The initial parameter vector.
- **options** (*dict*) Stopping criteria for optimization.

vΥ

The dependent variable (response) array.

```
Type
              np.ndarray
n
     The length of vY.
          Type
              int
p
     The number of powers. Default is set to 2.
          Type
              int
vgamma0
     The initial parameter vector.
          Type
              np.ndarray
bounds
     List to define parameter space.
          Type
              list
cons
     Dictionary to define constraints.
         Type
              dict
trendHat
     The estimated trend.
         Type
              np.ndarray
gammaHat
     The estimated power parameters.
          Type
              np.ndarray
coeffHat
     The estimated coefficients.
          Type
              np.ndarray
fit()
     Fit by power-law model and return trend estimates and parameter estimates .
summary()
     Print fitted prediction equation.
plot()
     Plot true data against estimated trend
```

fit()

## Returns

- **self.trendHat** (*np.ndarray*) The estimated trend.
- **self.gammaHat** (*np.ndarray*) The estimated power parameters.

## plot()

Plots the original series and the trend component.

## summary()

Print the mathematical equation for the fitted model

#### **Module contents**

## 1.1.2 Module contents

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