



# Clustering



# Clustering

- Clustering uses **unlabeled data** and looks for similarities between groups (clusters) in order to attempt to segment the data into separate clusters.
- Keep in mind that we don't actually know the true correct label for this data!



# Clustering

- How could we cluster this data together?

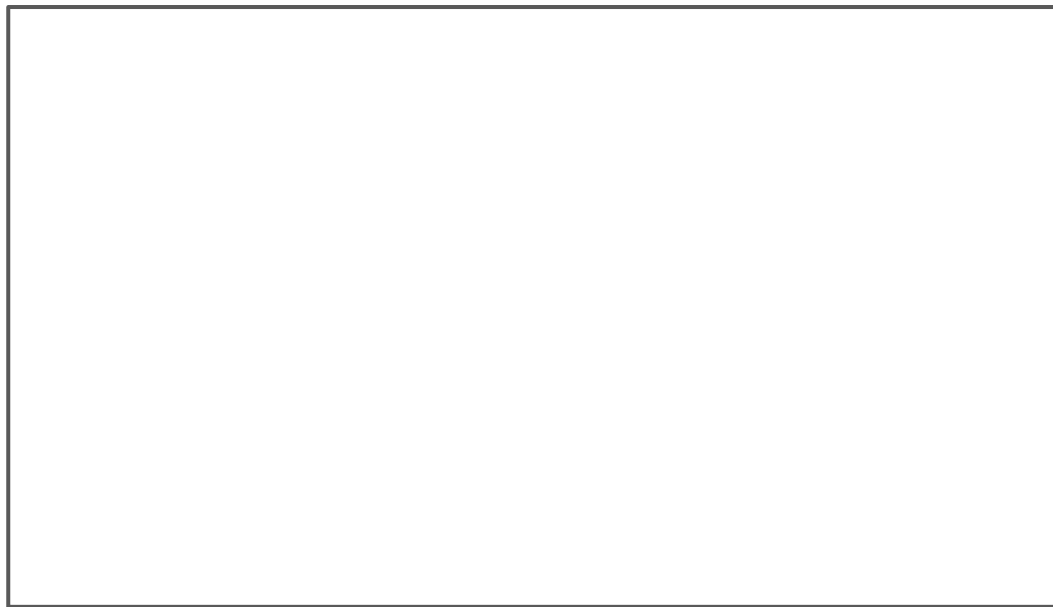
X1	X2
2	4
6	3
...	...
1	2



# Clustering

- Could simply plot and discover patterns:

x2

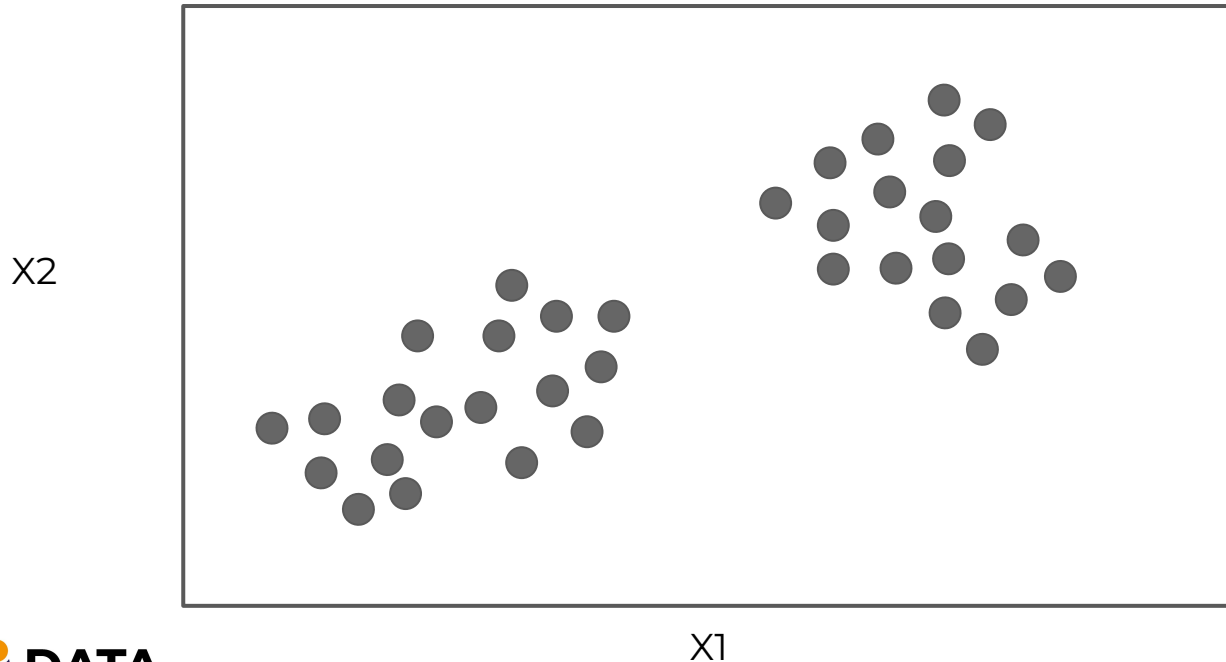


x1



# Clustering

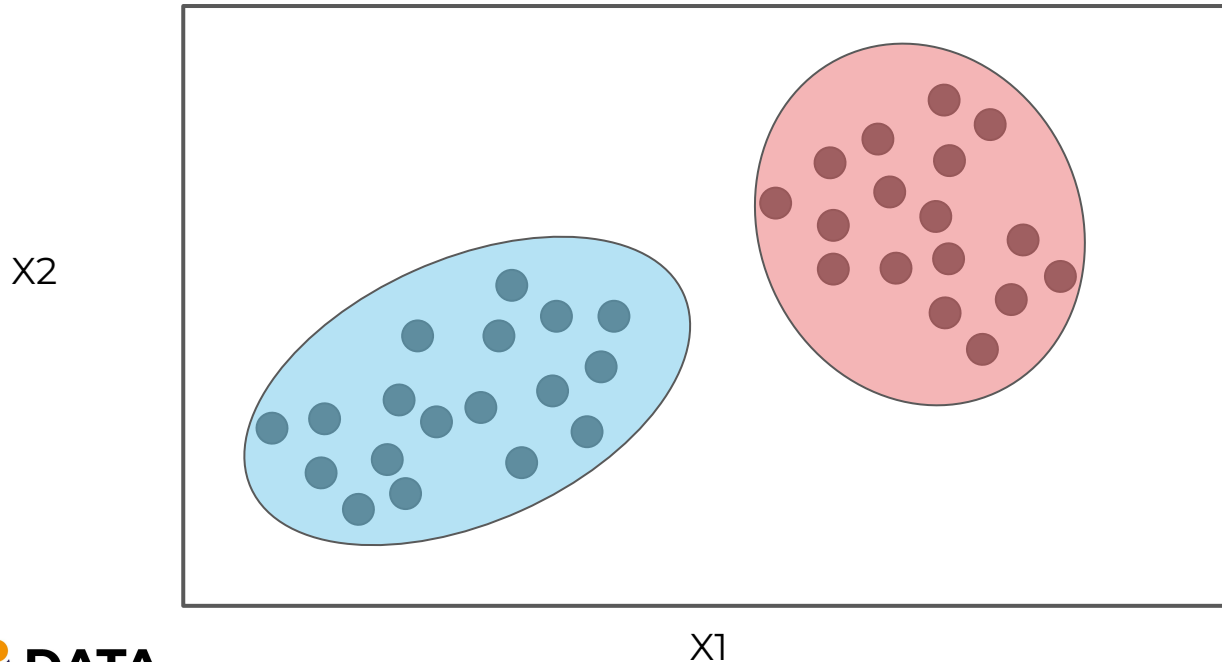
- Here we intuitively see 2 groupings:





# Clustering

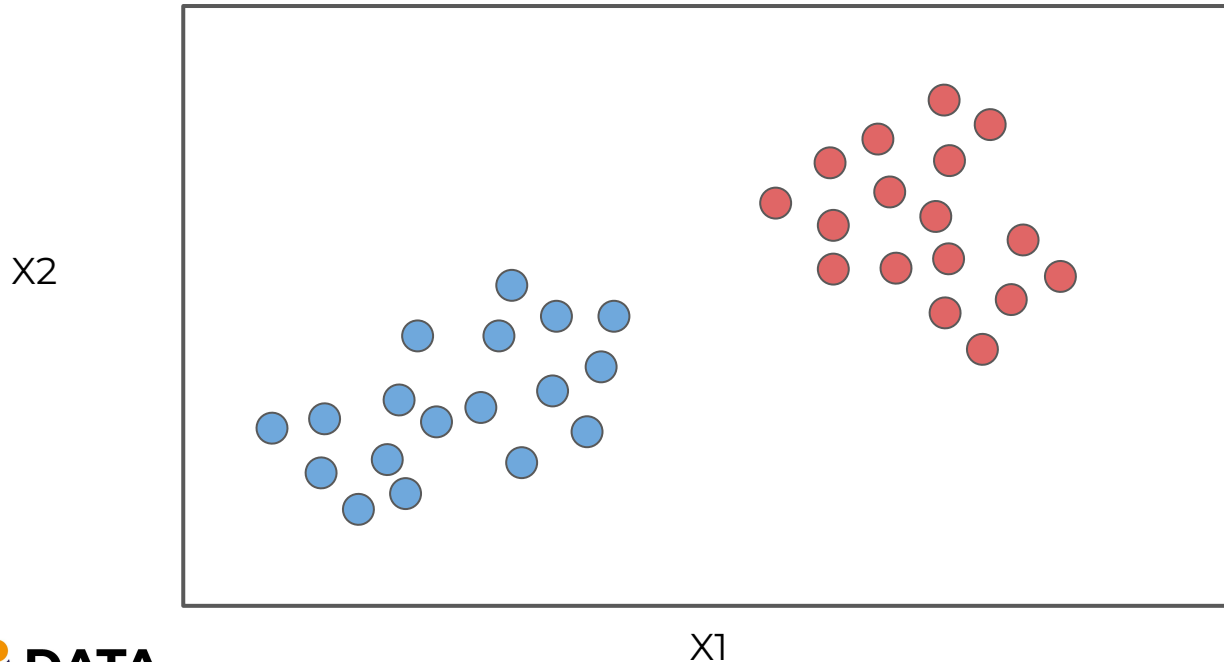
- Note how distance is the intuitive metric:





# Clustering

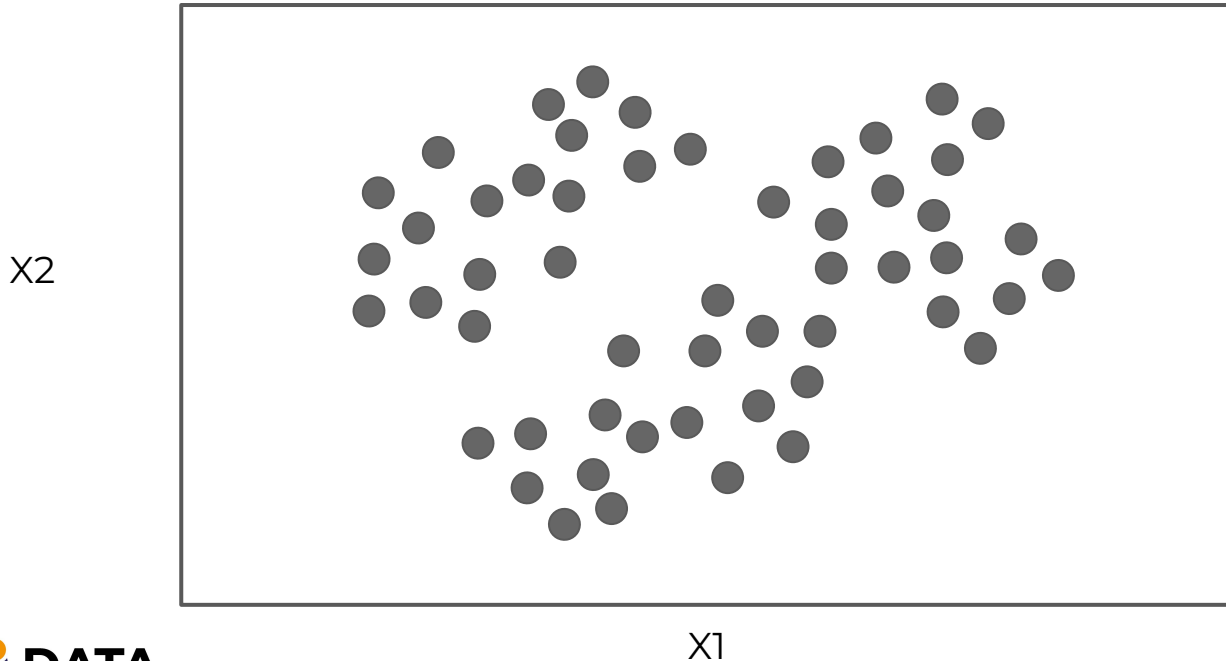
- We could then assign clusters:





# Clustering

- 2 or 3 clusters could both be reasonable:

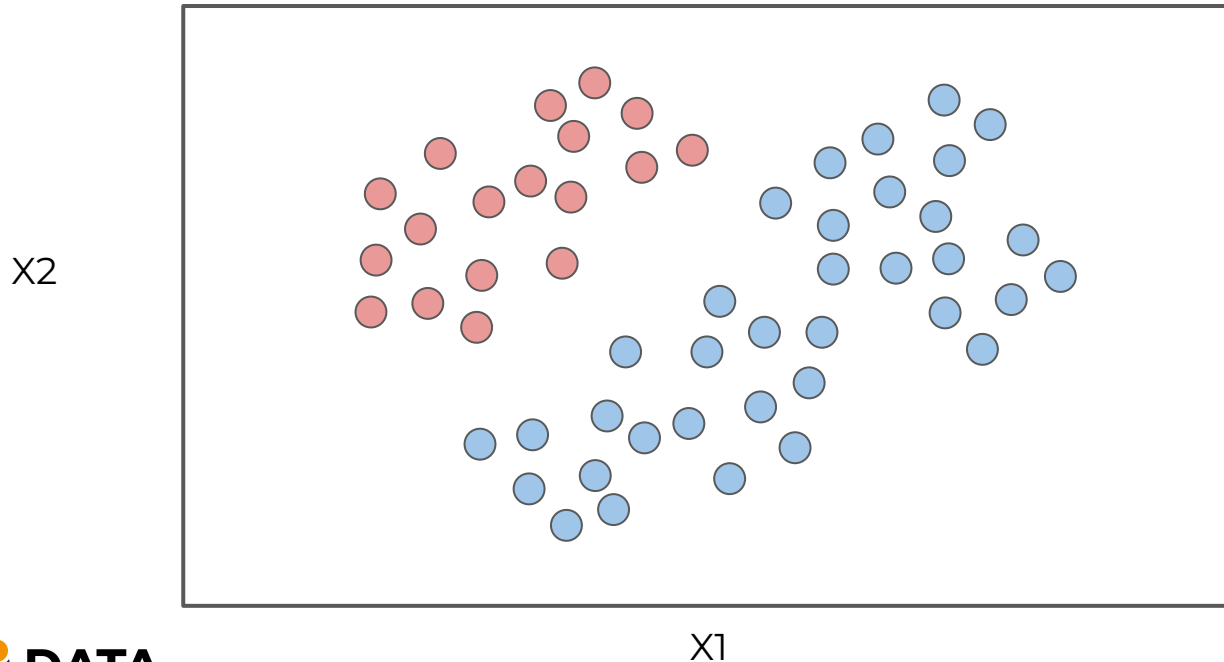






# Clustering

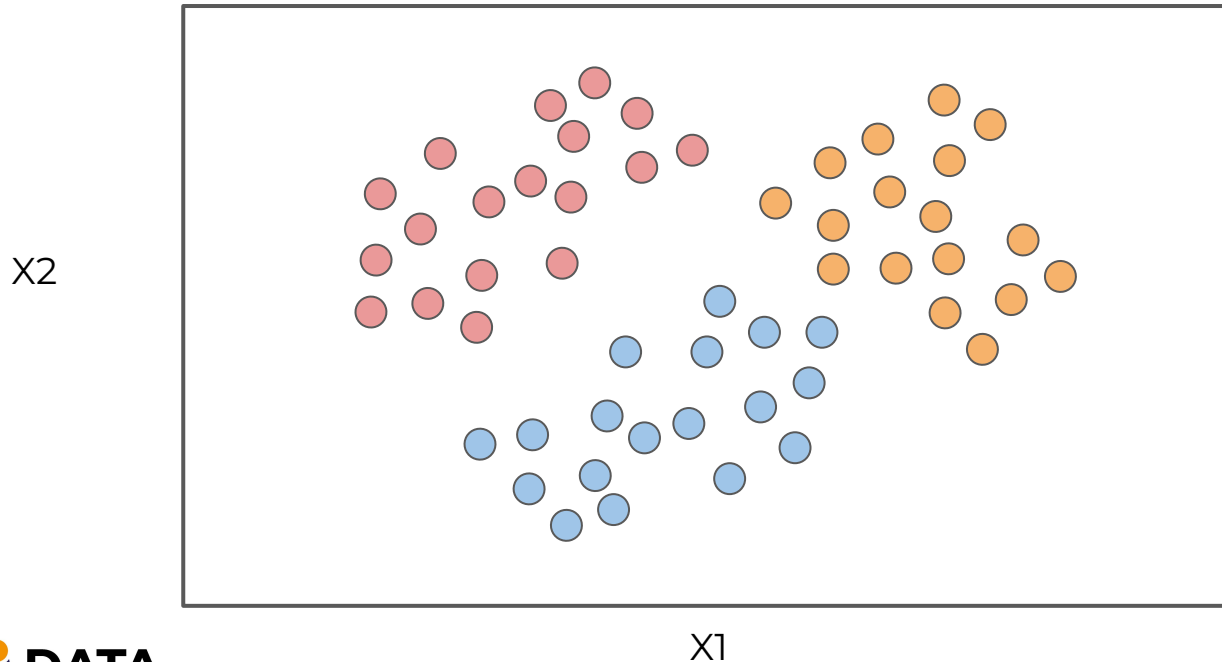
- 2 or 3 clusters could both be reasonable:





# Clustering

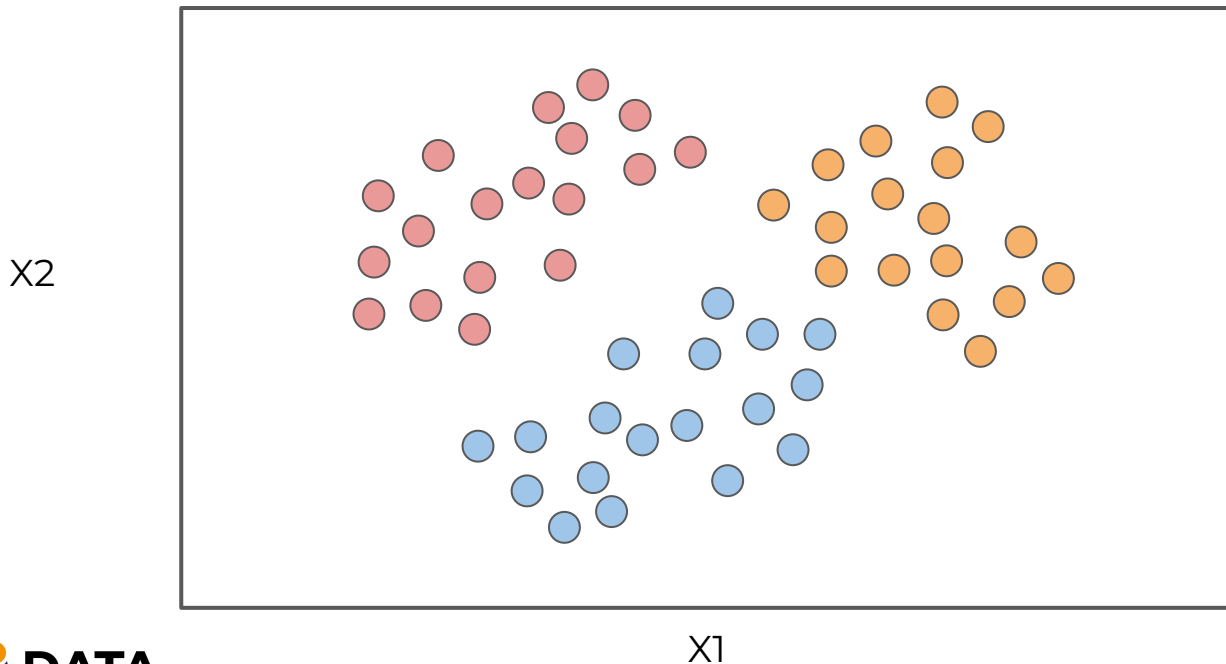
- 2 or 3 clusters could both be reasonable:





# Clustering

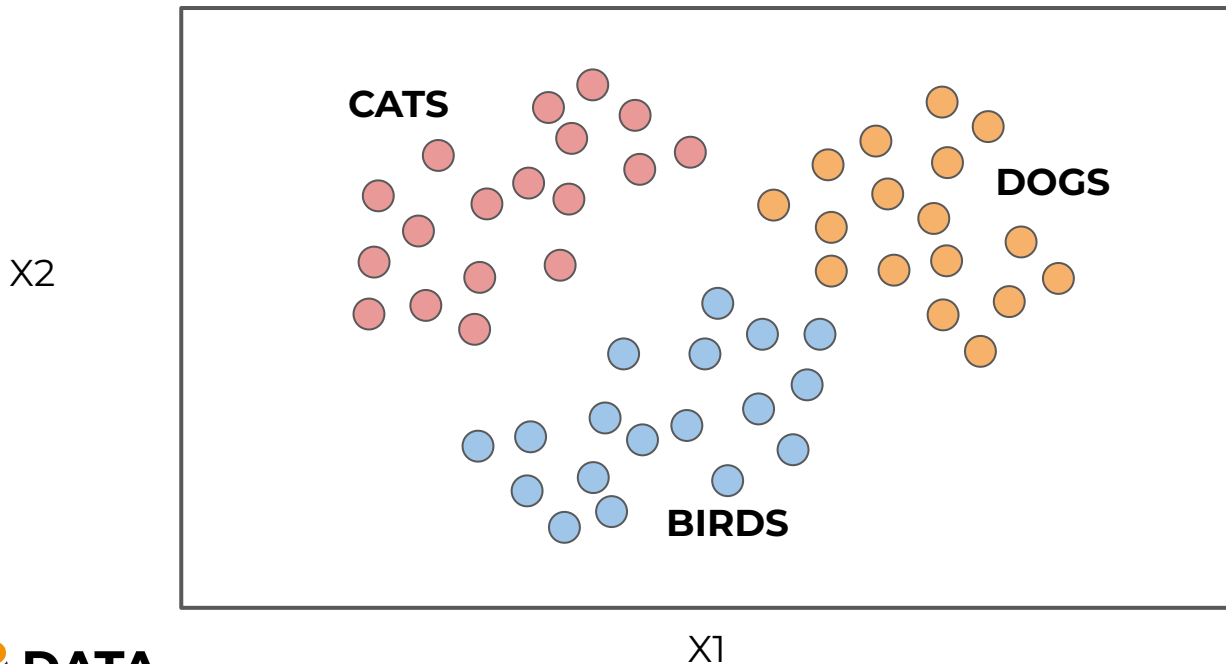
- Different methods can be used to decide!





# Clustering

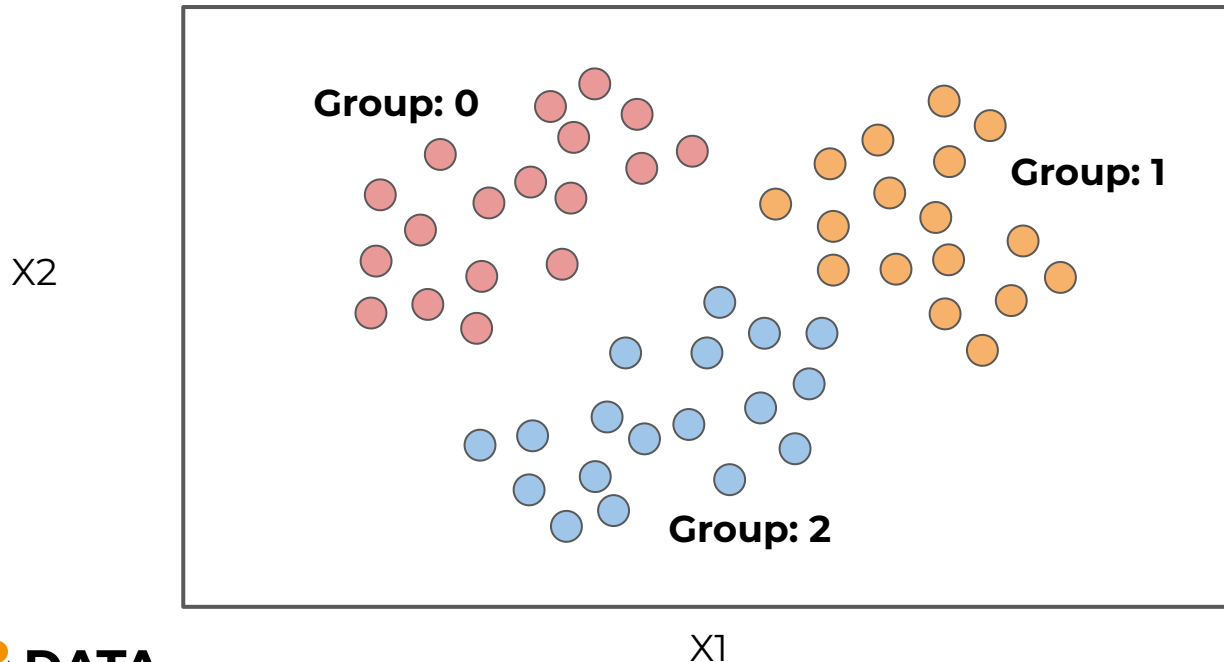
- Clustering doesn't "label" these for you!





# Clustering

- Clustering doesn't “label” these for you!





# Clustering

- Unsupervised Learning Paradigm Shift:
  - *If we've discovered these new cluster labels, could we use that as a **y** for supervised training?*
    - Yes! We can use unsupervised learning to discover possible labels, then apply supervised learning on new data points.



# Clustering

- It's much harder to compare unsupervised algorithms against each other due to the lack of ground truth based performance metrics (e.g. can't use accuracy or RMSE).



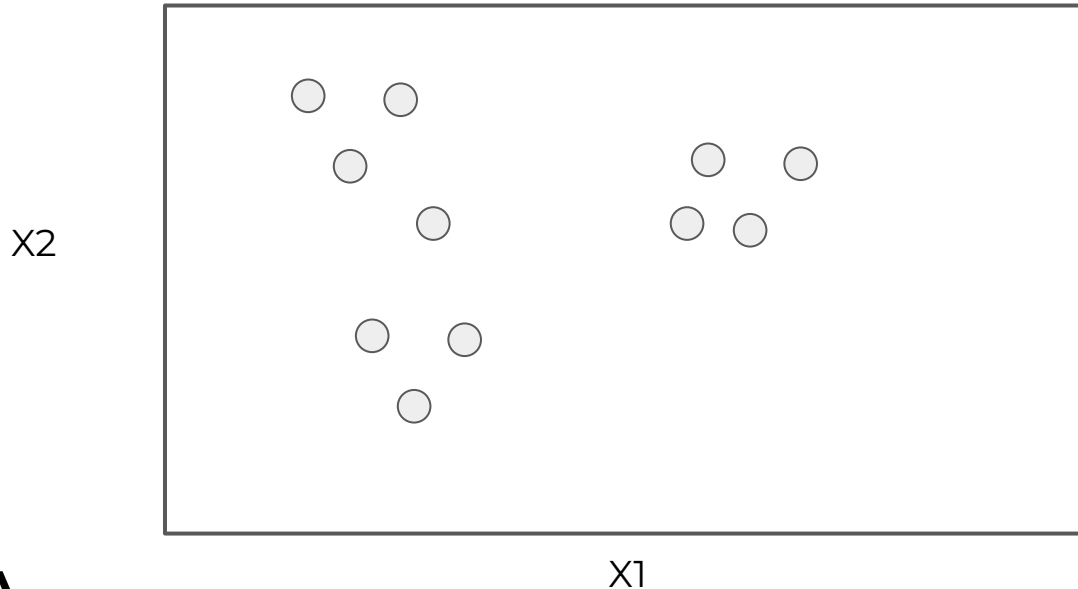
# K-Means Clustering





# K-Means Clustering

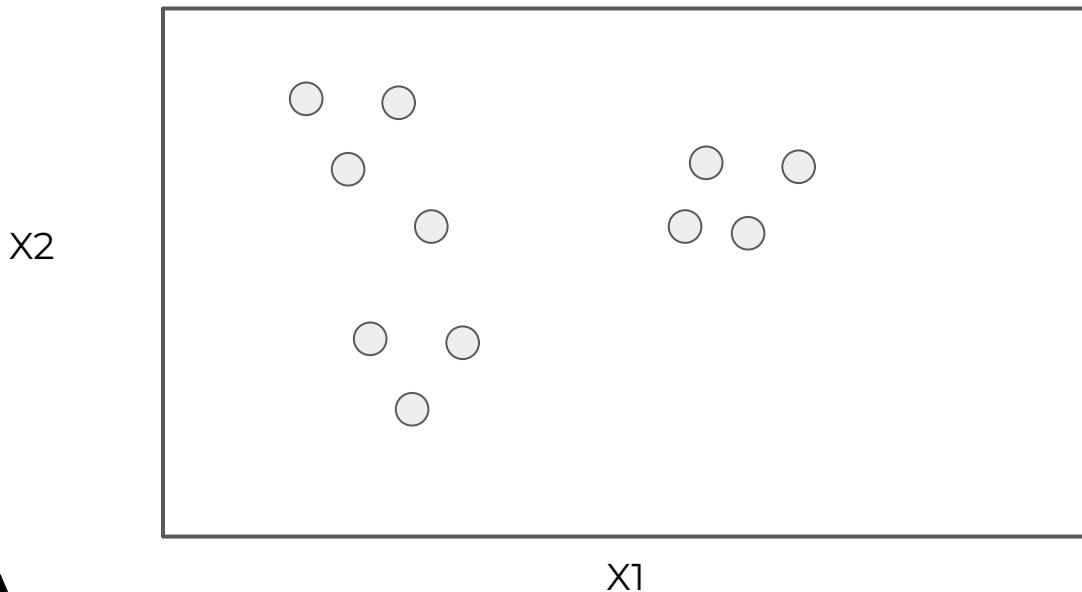
- Step 1: Choose the number of clusters to create (this is the K value).





# K-Means Clustering

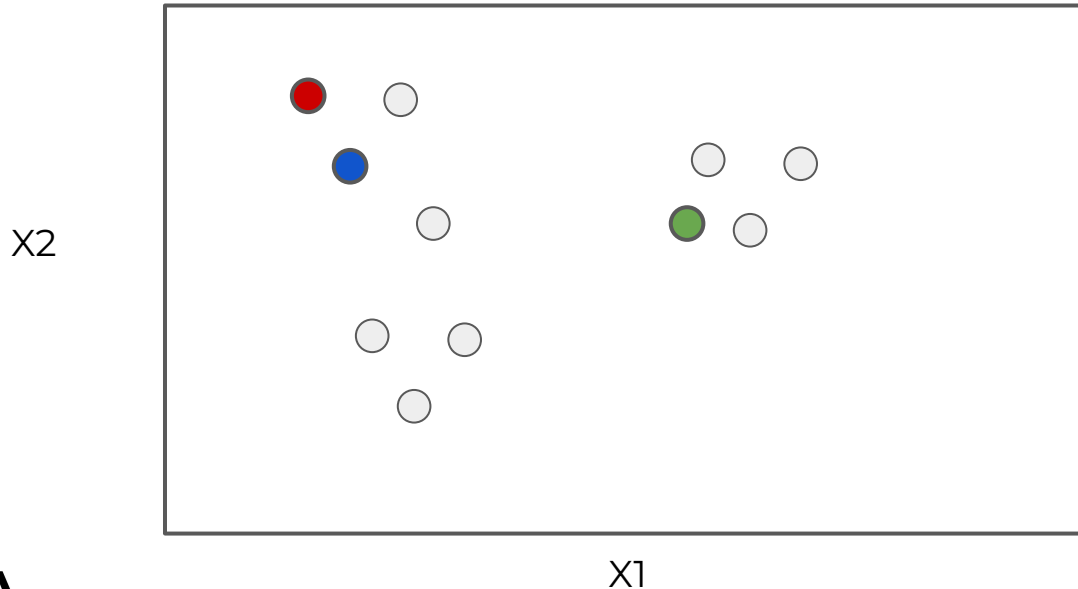
- Step 1: We'll choose  $K=3$ . Note in most situations you won't visualize the data.





# K-Means Clustering

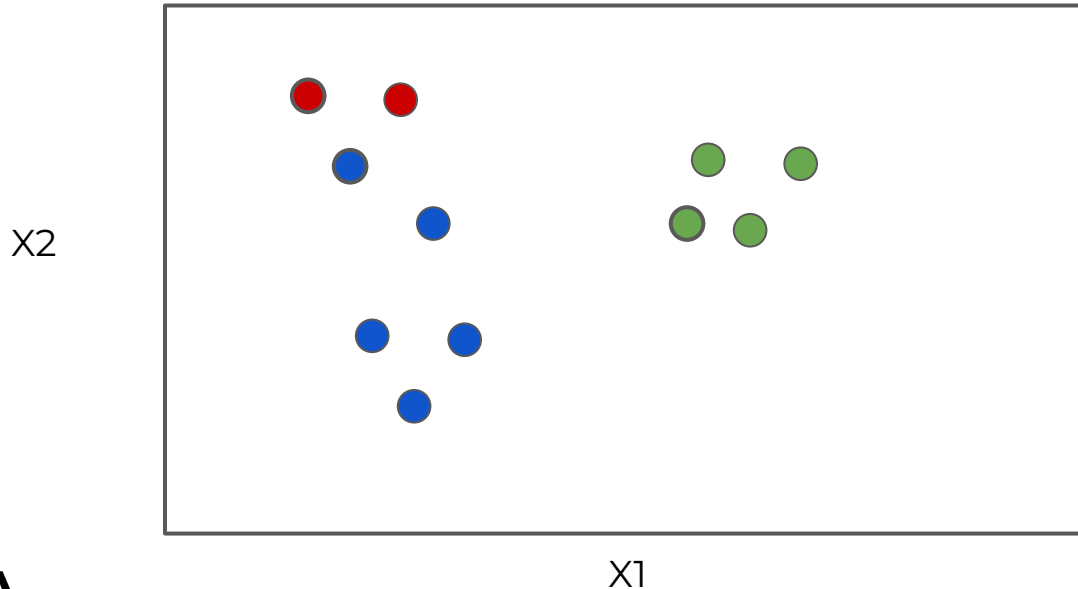
- Step 2: Randomly select  $K=3$  distinct data points.





# K-Means Clustering

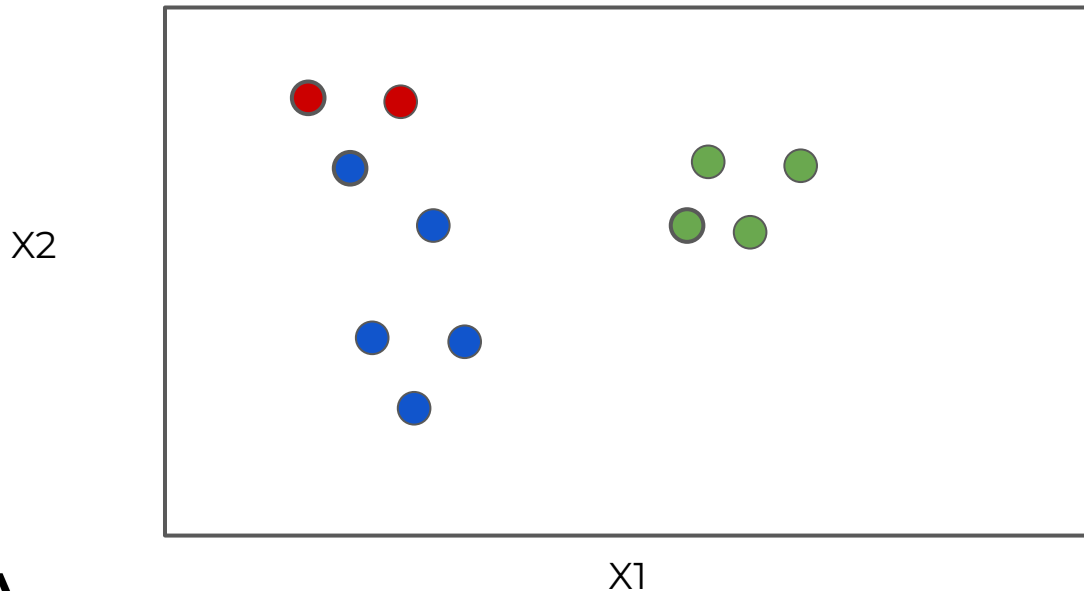
- Step 3: Assign each remaining point to the nearest “cluster” point.





# K-Means Clustering

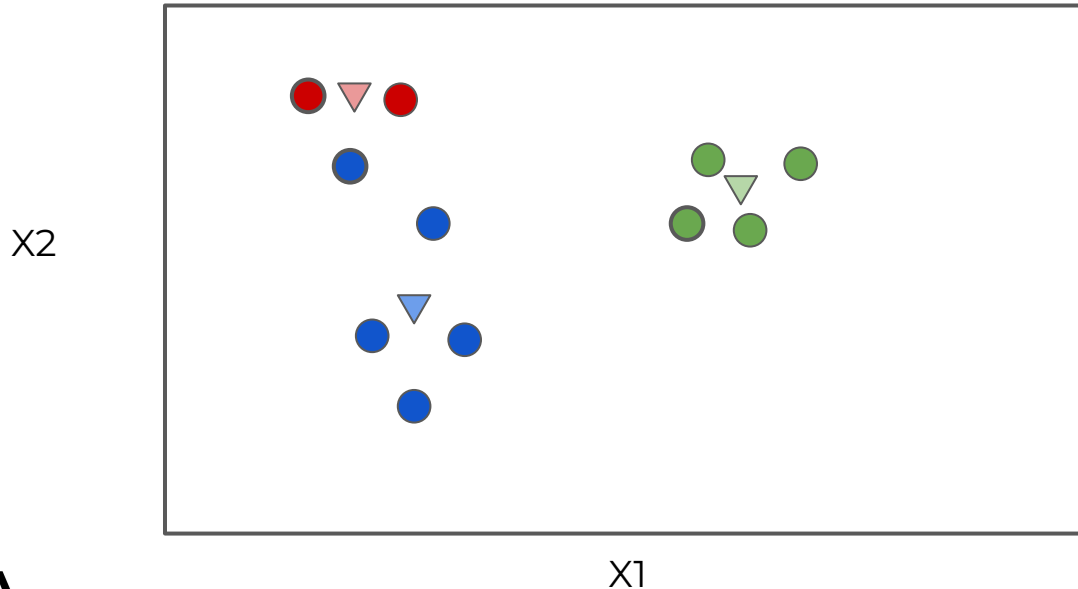
- Step 3: Note how this is using a distance metric to judge the nearest point.





# K-Means Clustering

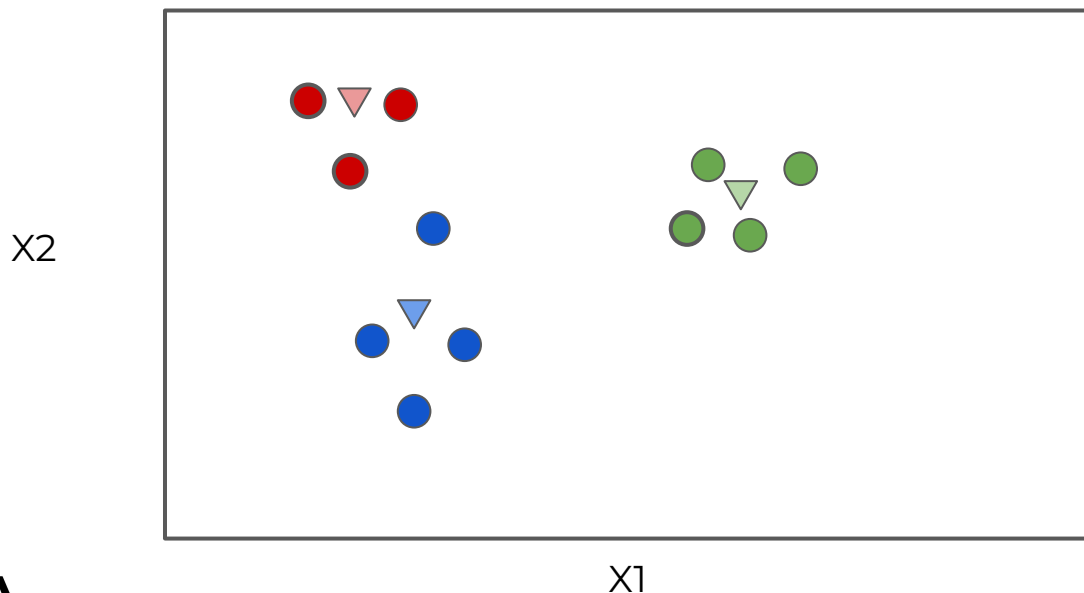
- Step 4: Calculate the center of the cluster points (mean value of point vectors).





# K-Means Clustering

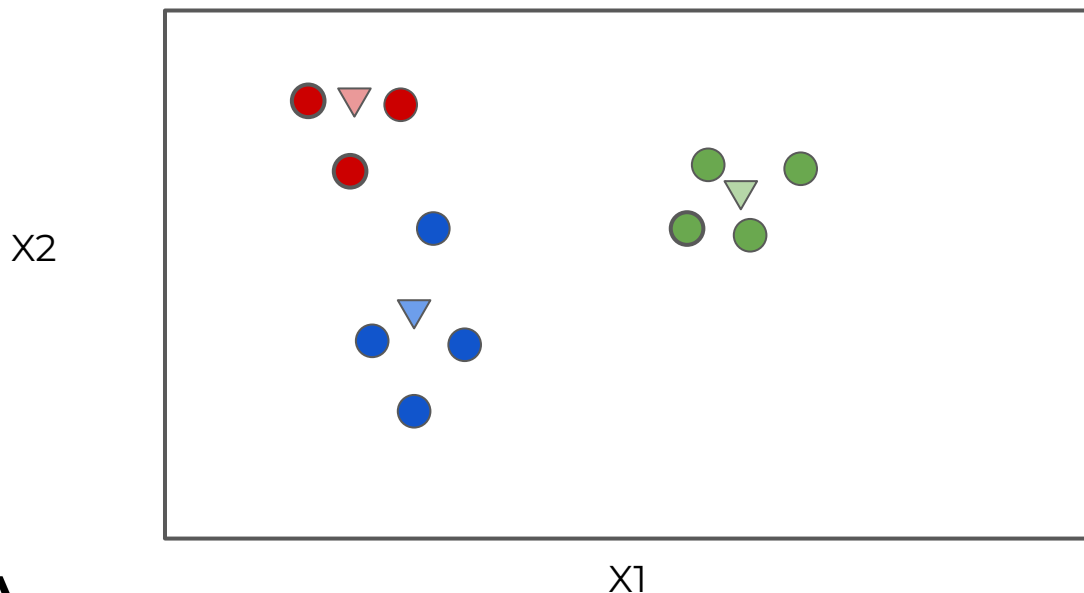
- Step 5: Now assign each point to the nearest cluster center.





# K-Means Clustering

- We repeat steps 4 and 5 until there are no more cluster reassignments.

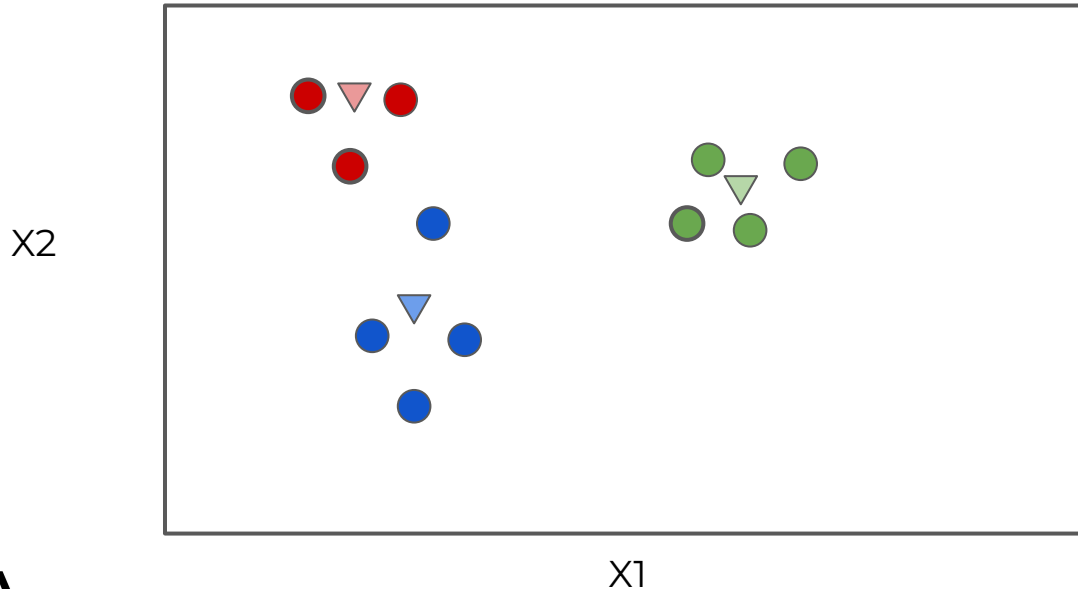






# K-Means Clustering

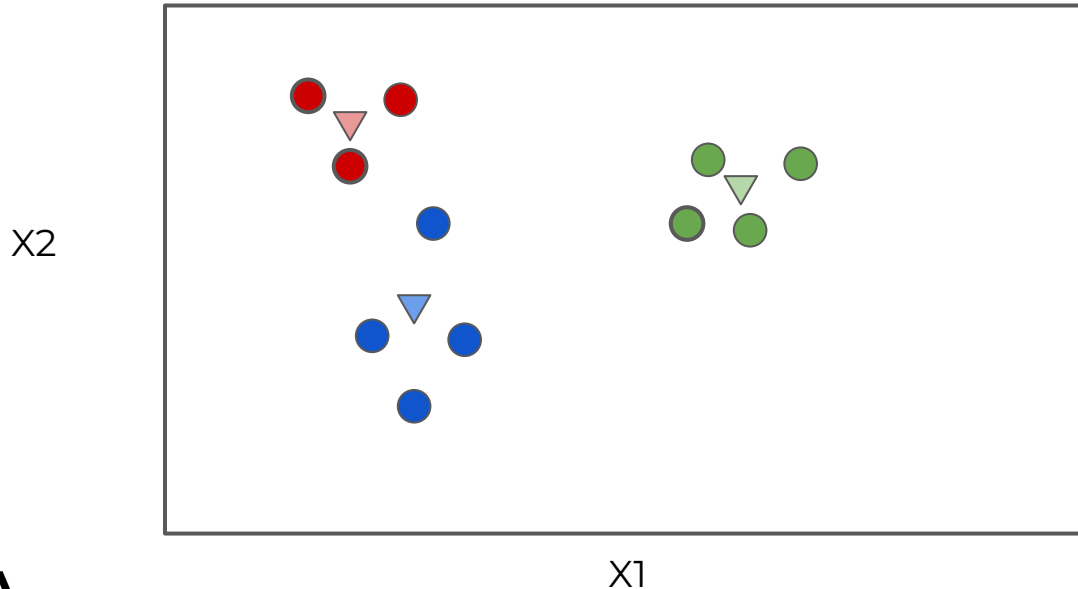
- Step 4b: Recalculate new cluster centers:





# K-Means Clustering

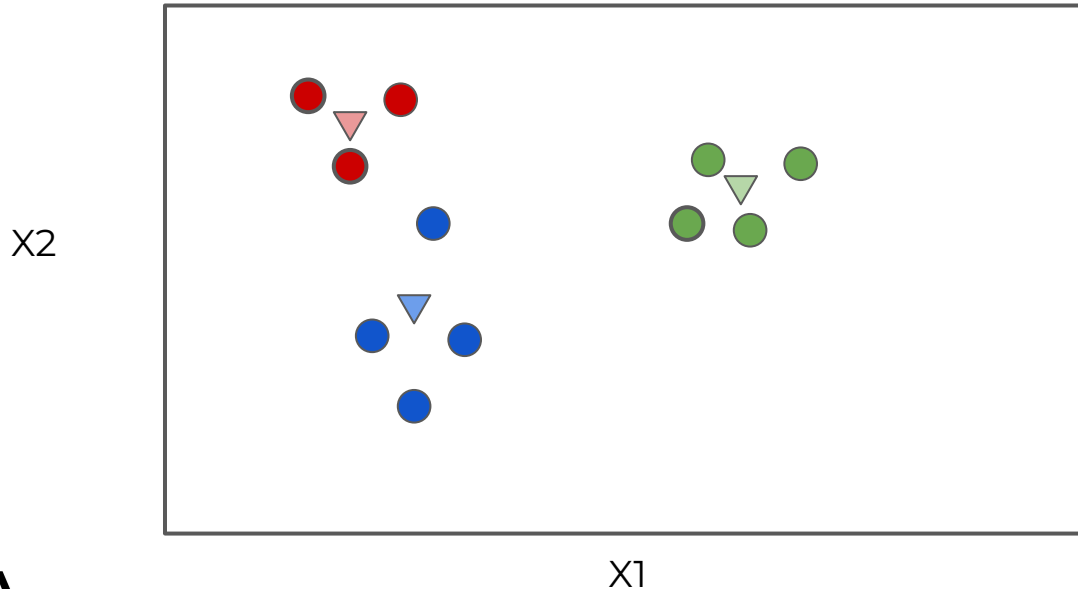
- Step 4b: Recalculate new cluster centers:





# K-Means Clustering

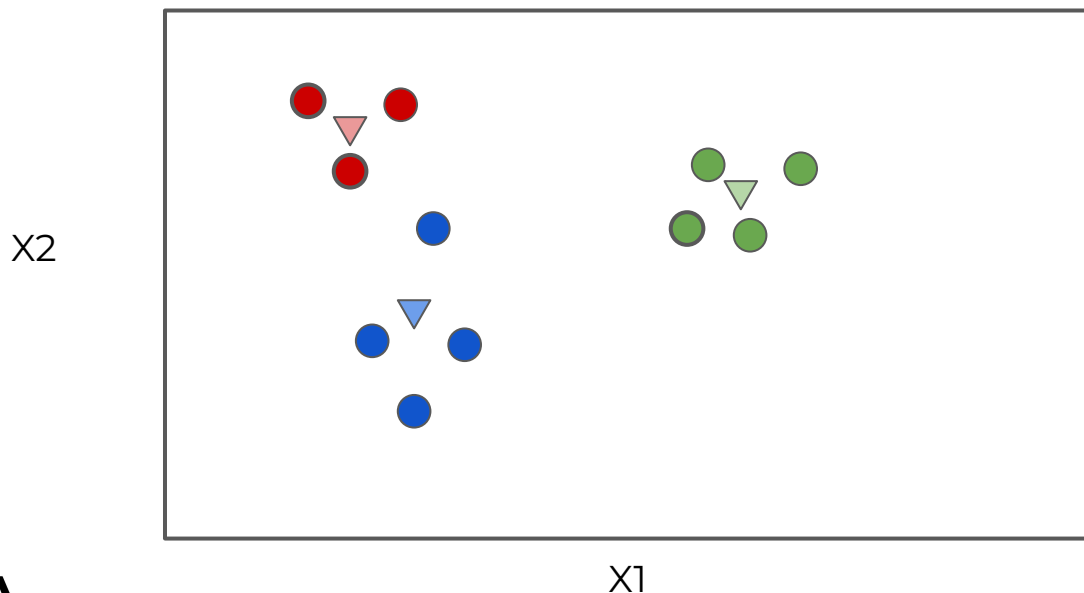
- Step 5b: Assign points to nearest cluster center.





# K-Means Clustering

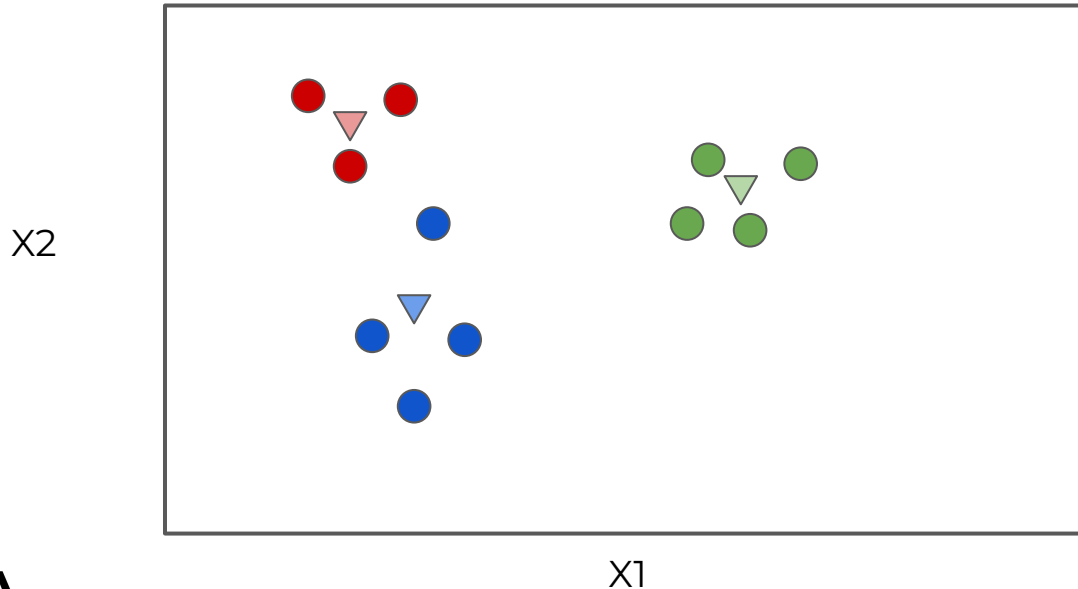
- If there are no more reassignments, we're done! The clusters have been found.





# K-Means Clustering

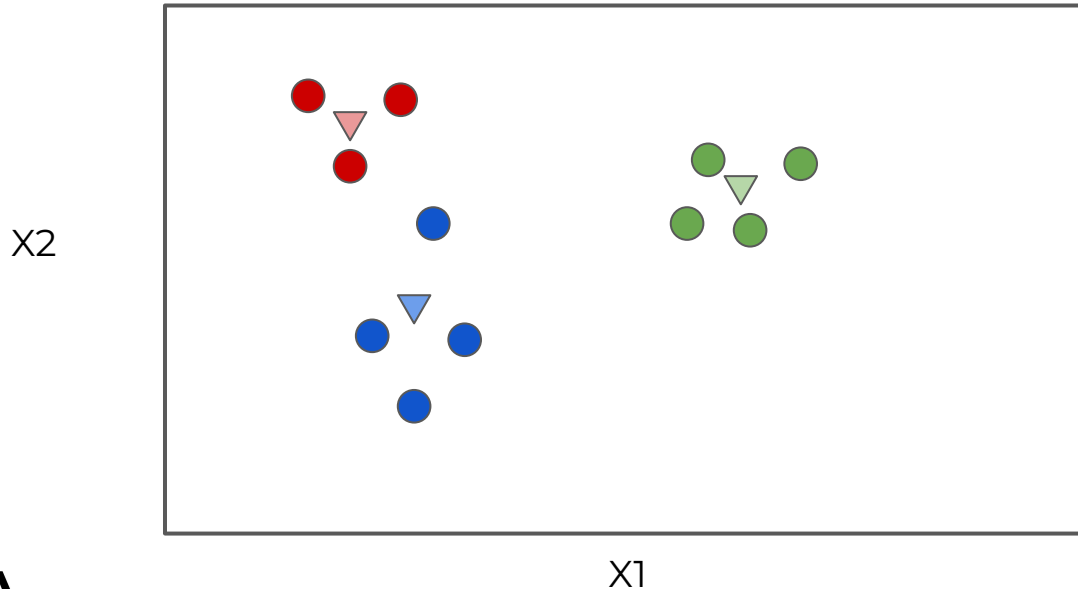
- How can we measure “goodness of fit”?





# K-Means Clustering

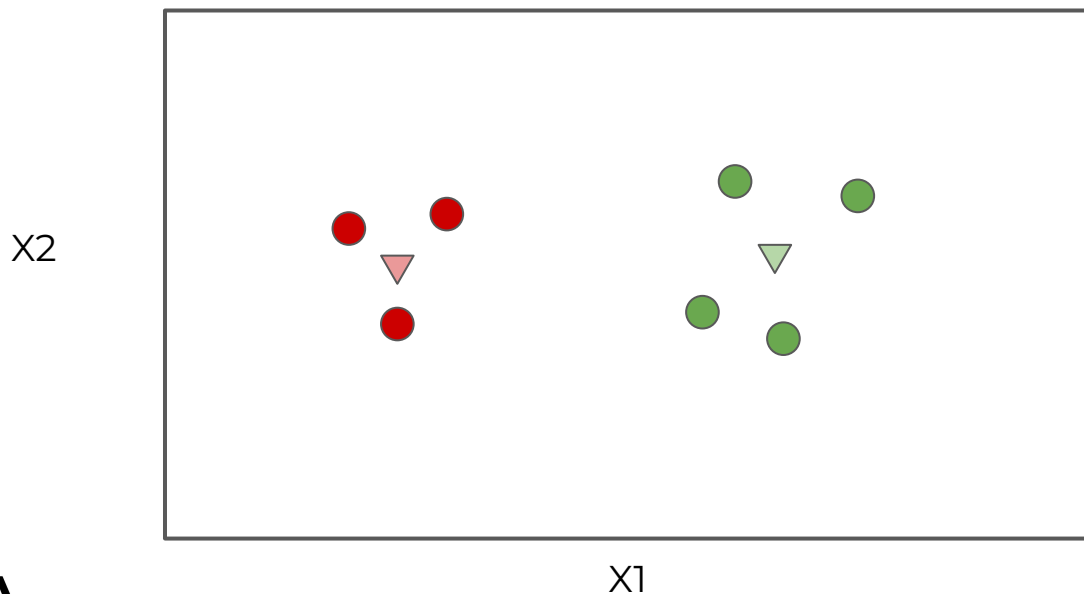
- We could measure the sum of the distances from points to cluster centers.





# K-Means Clustering

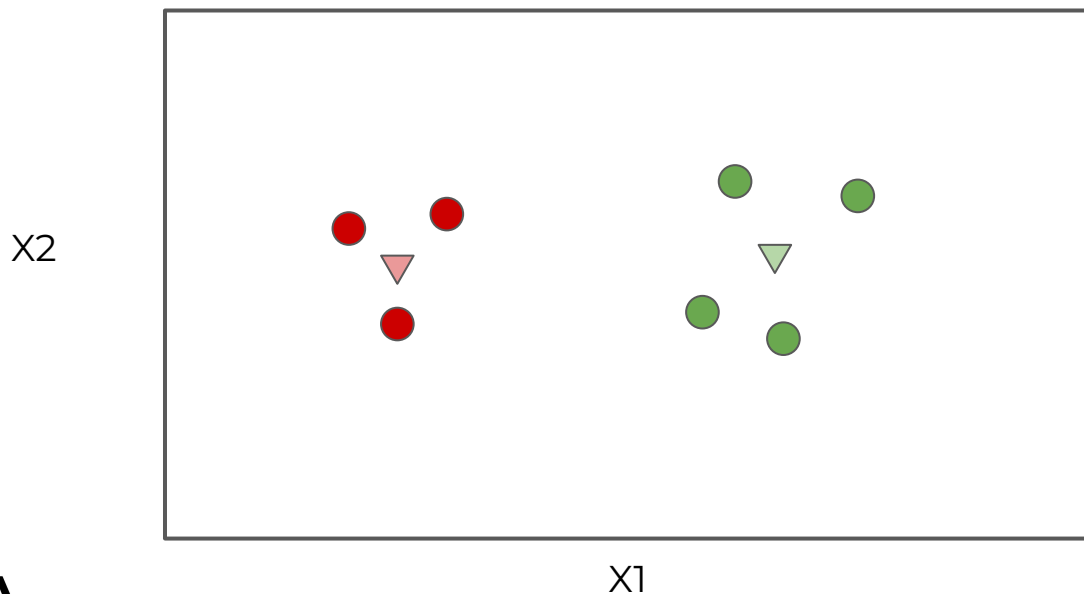
- Imagine a simple example starting with  $K=2$ .





# K-Means Clustering

- We measure the sum of the squared distances from points to the cluster center:



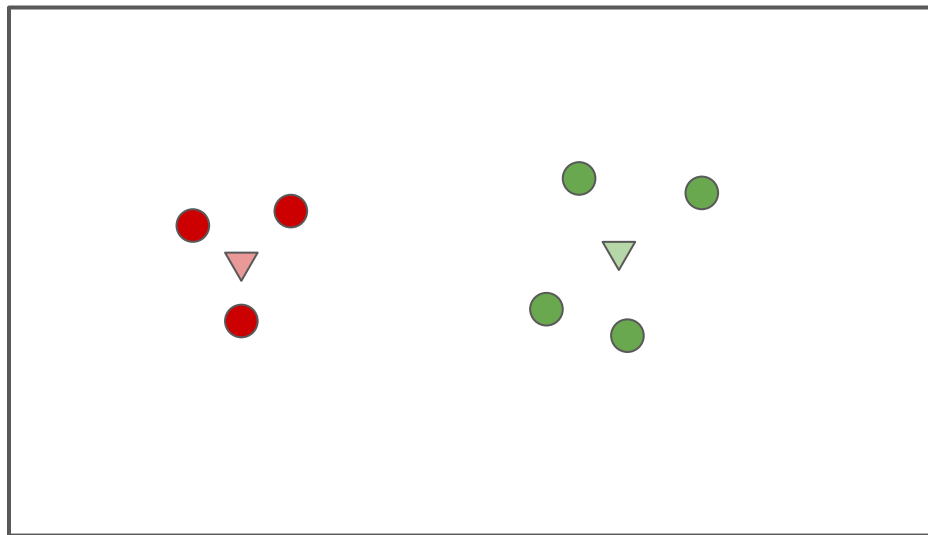




# Clustering

- Then we fit an entirely new KMeans model with  $K+1$ :

x2

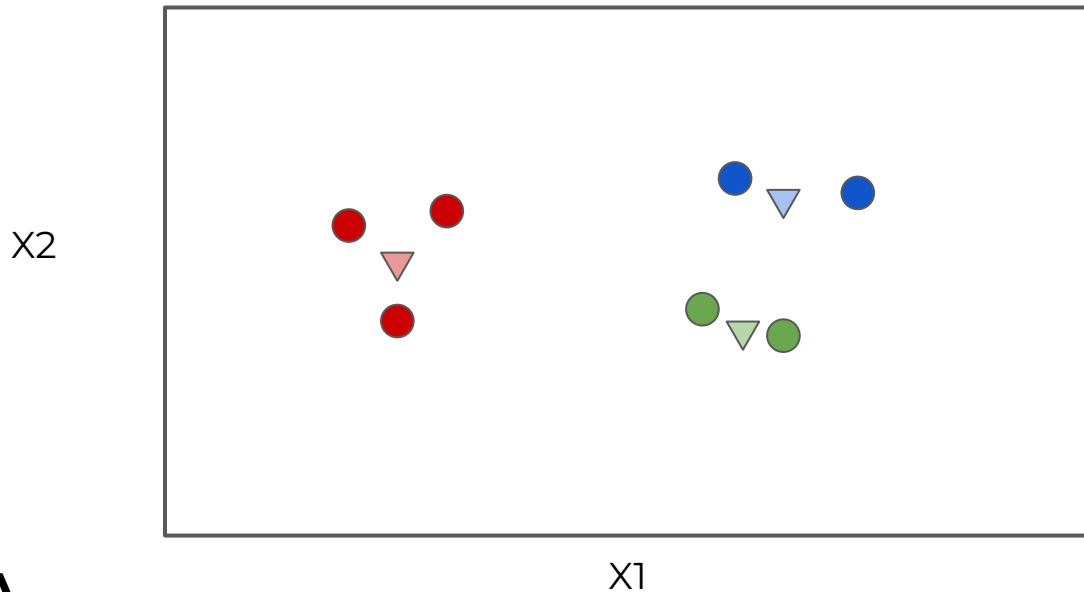


x1



# Clustering

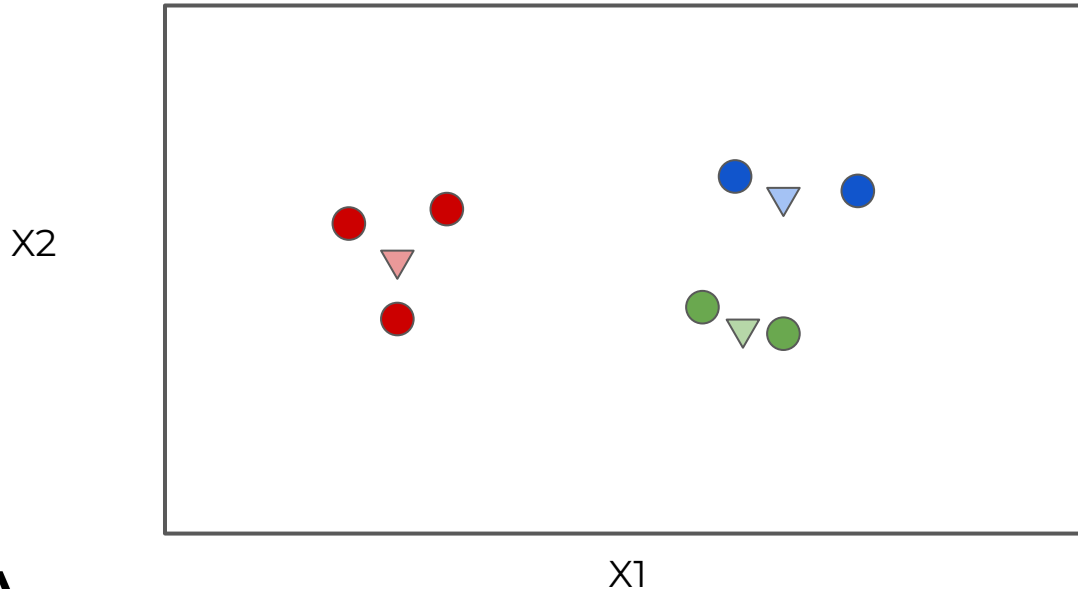
- Then we fit an entirely new KMeans model with  $K+1$ :





# Clustering

- Then measure again the sum of the squared distance (SSD) to center.

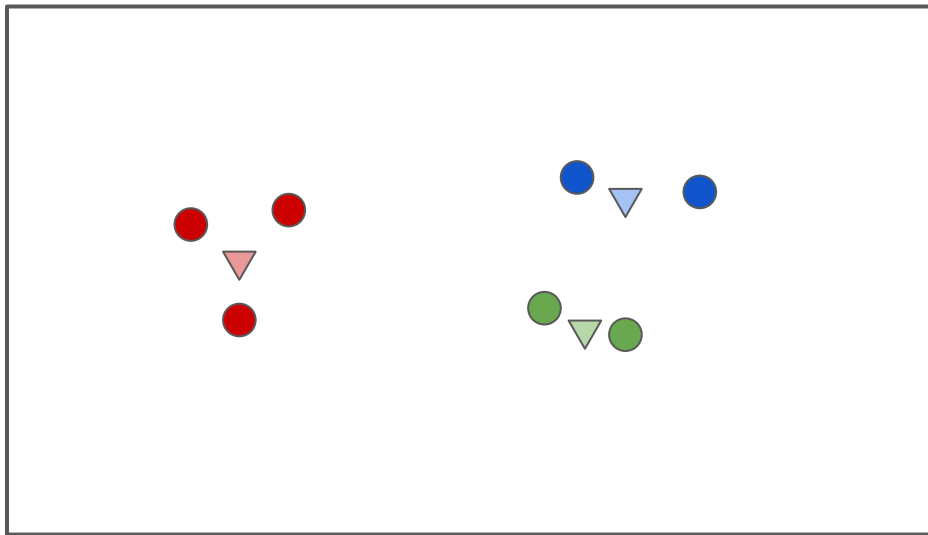




# Clustering

- In theory this SSD would go to zero once  $K$  is equal to the number of points.

x2



x1



# Clustering

- You would have a cluster for each point!  
SSD would be perfect at 0!

x2



x1



# Clustering

- We keep track of this SSD value for a range of different K values.
- We then look for a K value where **rate of reduction in SSD** begins to decline.
- This signifies that adding an extra cluster is **not** obtaining enough clarity of cluster separation to justify increasing K.



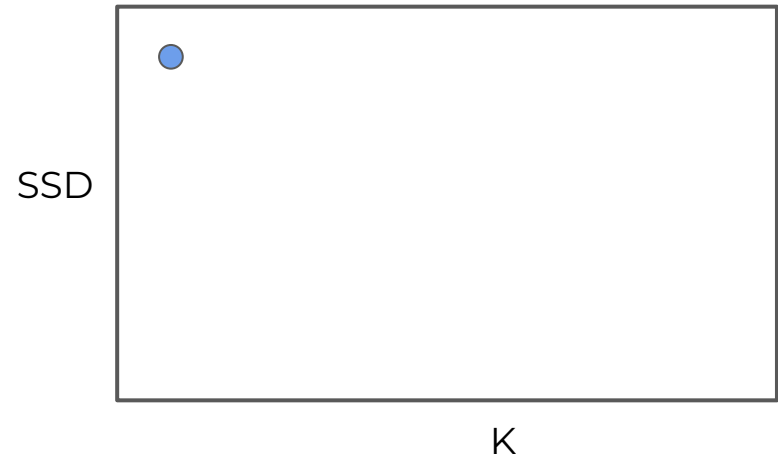
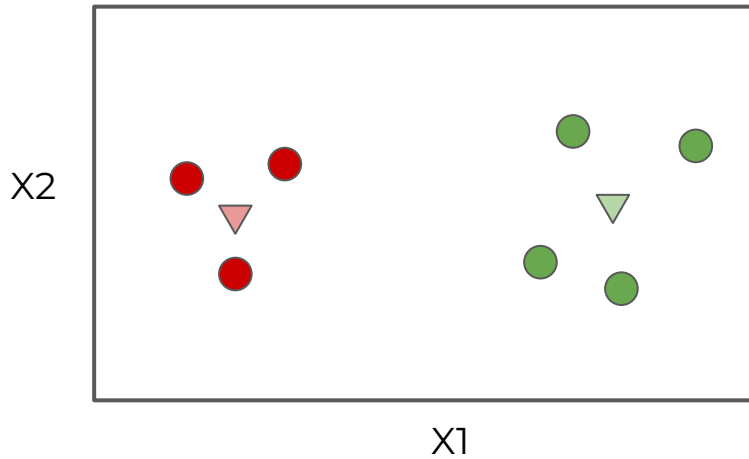
# Clustering

- This is known as the “elbow” method since we will track where decrease in SSD begins to flatten out compared to increasing K values.
- Let’s walk through what this chart would look like...



# Clustering

- Start with  $K=2$ :

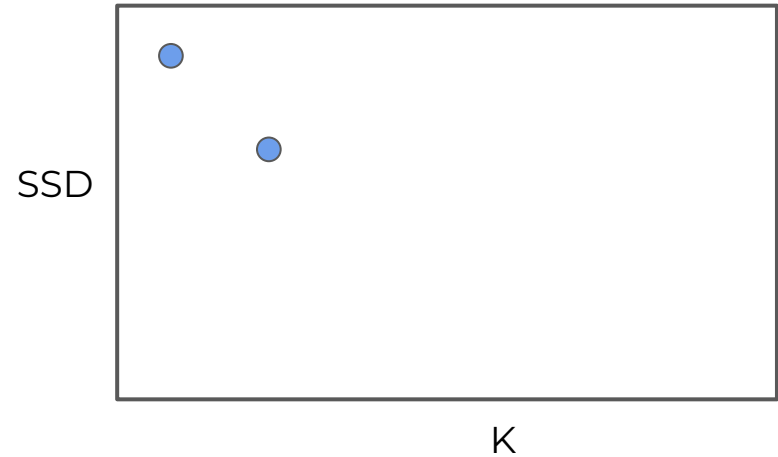
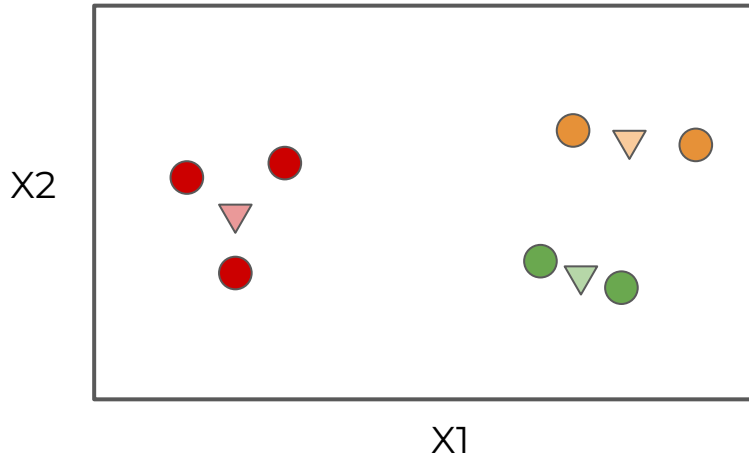






# Clustering

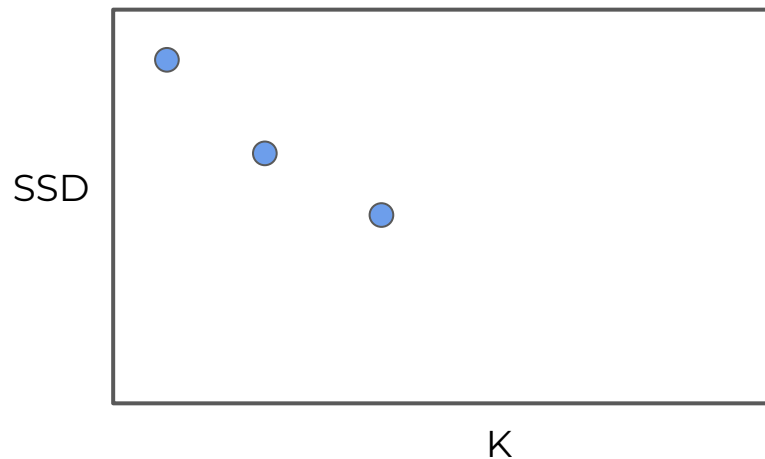
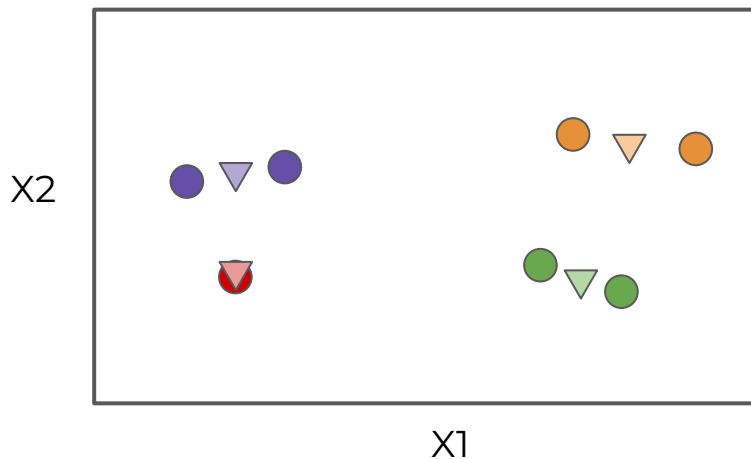
- Increase  $K$  and measure SSD:





# Clustering

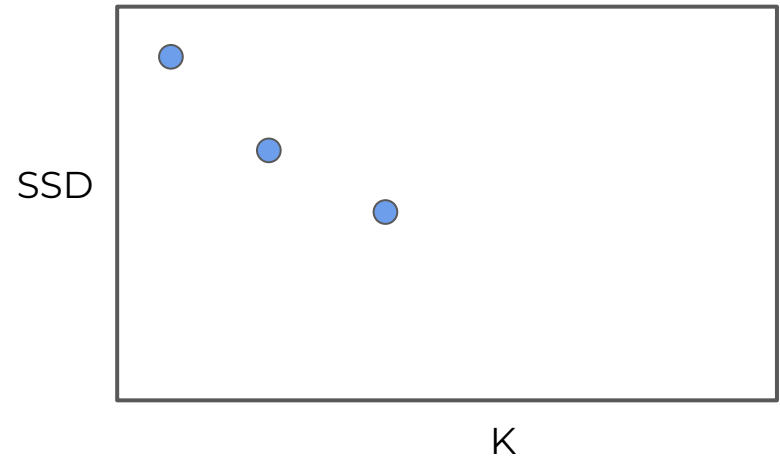
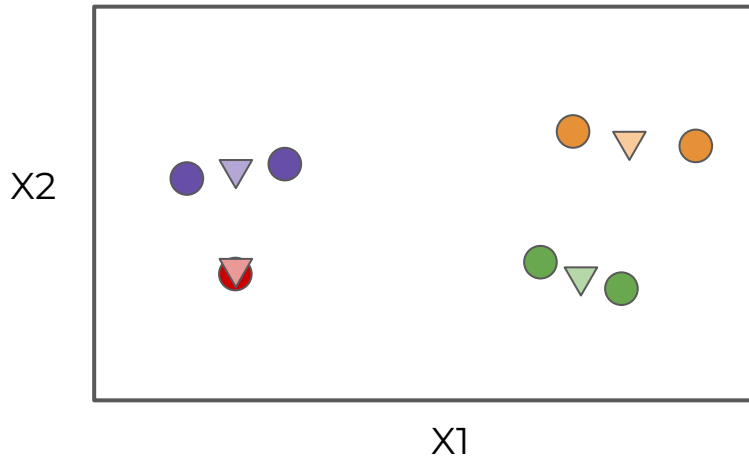
- Increase  $K$  and measure SSD:





# Clustering

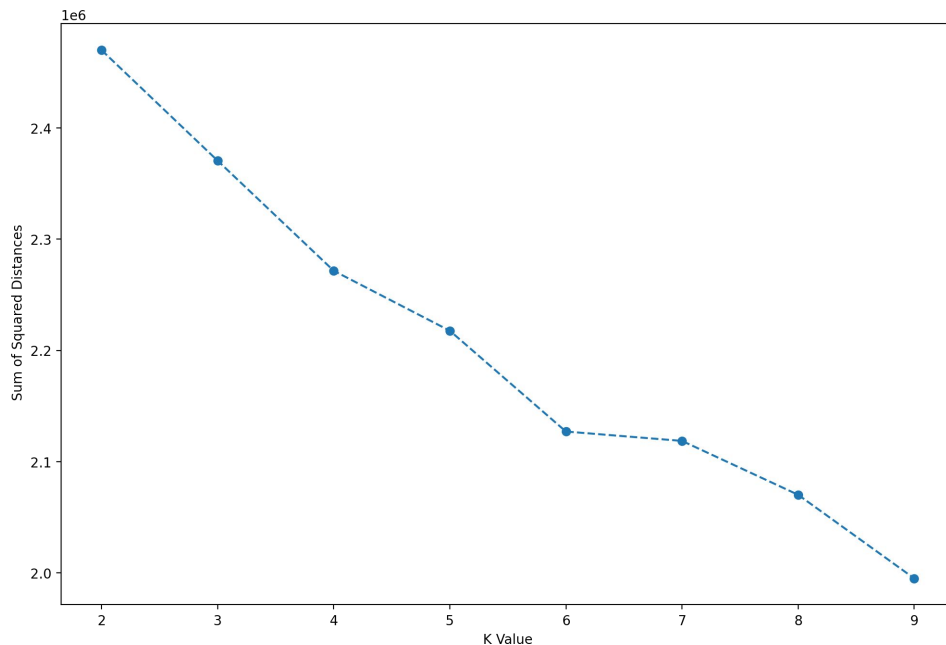
- Repeat this process for some set number of K values:





# K Means Clustering

- You will see a continuous decline.





# K Means Clustering

- Eventually you will see “elbow” points:
- These points are strong indicators that increasing K further is no longer justified as it is not revealing more “signal”.

