

FACULTY OF MATHEMATICS, COMPUTER SCIENCE AND
NATURAL SCIENCES RESEARCH GROUP COMPUTER SCIENCE 2

RWTH AACHEN UNIVERSITY, GERMANY

Bachelor Thesis

Analyzing runtime complexity of non-ndg Term Rewrite Systems

submitted by

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Coming soon

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Statutory Declaration in Lieu of an Oath

Abstract

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Chapter 1

Introduction

Term rewrite systems have been extensively studied, with the main problem concerning their complexity analysis. In recent decades many automated tools have been developed to infer upper bounds on runtime complexity (rc), which considers the longest rewrite sequence starting with a basic term disregarding any evaluation strategy. In contrast to rc, innermost runtime complexity (irc) makes use of an innermost evaluation strategy that can be much easier to analyse. While the analysis of irc has some uses, it is rc that is of greater interest.

Recently a technique has been developed to overapproximate some TRSs as non-dup generalized (ndg), with a corresponding proof of the equality of rc and irc for such ndg TRSs. The mentioned criteria combined with the much more powerful analysis of irc allowed inferring upper/lower bounds on rc from upper/lower bounds on irc. This method however makes no claims regarding all the TRSs that are non-ndg. It is the goal of this thesis to extend the technique to non-ndg TRSs.

Presented here is a transformation of the original non-ndg TRS into an encoded version, that shares the same rc. The goal of the encoding is to create a TRS, for which also holds that $\text{irc} = \text{rc}$. While the encoded version may not ndg, what is important is that we can apply the techniques used in the analysis of irc to infer the rc of the original non-ndg TRS.

As it will be shown, not all encodings are equal and some yield substantially better results. Two algorithms have been developed to improve the results of the automated analysis. The first - overapproximating the TRS positions that require encoding and a second - detecting when to alter the encoding to not add any non-terminating rules.

The structure of the thesis is as follows. Chapter 2 introduces some of the preliminary knowledge regarding TRSs. Chapter 3 contains a description of the first mentioned algorithm, which is used as the foundation, on which the encoding, described in Chapter 4, is built. Chapter 5 is dedicated to the second algorithm and the changes that come up from its result. In Chapter 6 are presented the results from the implementation of the technique in the tool AProVE and it also serves as a summary.

Chapter 2

Preliminaries

Chapter 3

Algorithm for finding non-ndg locations

Chapter 4

Encoding

Chapter 5

Encoding with terminating rules

Chapter 6

Results