

Table 1: Performance Results for GoldsteinPrice\\$\_2DProblem

Optimizer	Mean Final Value	Std Dev	Best Value	Worst Value	Mean Func Evals	Success Rate (%)	Mean Time (s)
QQN-StrongWolfe	$8.40 \times 10^1$	$2.01 \times 10^{-5}$	$8.40 \times 10^1$	$8.40 \times 10^1$	496.1	45.0	0.011
L-BFGS	$3.60 \times 10^3$	$1.28 \times 10^4$	$9.89 \times 10^1$	$5.94 \times 10^4$	130.6	45.0	0.002
GD-Momentum	$1.07 \times 10^3$	$8.72 \times 10^2$	$1.06 \times 10^2$	$4.35 \times 10^3$	19.1	20.0	0.000
QQN-Bisection-1	$1.22 \times 10^2$	$1.65 \times 10^2$	$8.40 \times 10^1$	$8.40 \times 10^2$	306.4	17.5	0.008
L-BFGS-Conservative	$8.12 \times 10^2$	$1.64 \times 10^2$	$9.89 \times 10^1$	$9.01 \times 10^2$	235.7	5.0	0.003
QQN-GoldenSection	$8.40 \times 10^1$	$1.93 \times 10^{-11}$	$8.40 \times 10^1$	$8.40 \times 10^1$	370.4	0.0	0.005
QQN-Backtracking	$8.59 \times 10^1$	1.32	$8.43 \times 10^1$	$8.86 \times 10^1$	787.9	0.0	0.016
QQN-Bisection-2	$1.97 \times 10^2$	$2.75 \times 10^2$	3.00	$8.40 \times 10^2$	34.4	0.0	0.001
QQN-CubicQuadraticInterpolation	$3.30 \times 10^2$	$3.54 \times 10^2$	$7.66 \times 10^1$	$8.40 \times 10^2$	374.3	0.0	0.012
Adam-WeightDecay	$8.40 \times 10^2$	$4.61 \times 10^{-1}$	$8.40 \times 10^2$	$8.42 \times 10^2$	215.0	0.0	0.004
GD	$8.51 \times 10^2$	6.46	$8.42 \times 10^2$	$8.77 \times 10^2$	25.4	0.0	0.001
Adam-Fast	$8.52 \times 10^2$	$1.39 \times 10^1$	$8.40 \times 10^2$	$9.15 \times 10^2$	36.1	0.0	0.001
GD-Nesterov	$8.58 \times 10^2$	$2.15 \times 10^1$	$8.41 \times 10^2$	$9.21 \times 10^2$	25.9	0.0	0.001
GD-WeightDecay	$8.64 \times 10^2$	$2.37 \times 10^1$	$8.40 \times 10^2$	$9.32 \times 10^2$	19.5	0.0	0.001
Adam	$8.78 \times 10^2$	$7.84 \times 10^1$	$8.40 \times 10^2$	$1.12 \times 10^3$	420.1	0.0	0.008
Adam-AMSGrad	$9.00 \times 10^2$	$8.79 \times 10^1$	$8.40 \times 10^2$	$1.14 \times 10^3$	444.2	0.0	0.010
QQN-MoreThuente	$1.11 \times 10^3$	$8.77 \times 10^2$	$9.73 \times 10^1$	$3.10 \times 10^3$	483.2	0.0	0.008
L-BFGS-Aggressive	$1.68 \times 10^3$	$1.48 \times 10^3$	$9.11 \times 10^1$	$6.78 \times 10^3$	774.3	0.0	0.006
Trust Region-Standard	$1.79 \times 10^3$	$1.27 \times 10^3$	$8.40 \times 10^2$	$4.76 \times 10^3$	526.4	0.0	0.003
Trust Region-Conservative	$2.22 \times 10^3$	$1.14 \times 10^3$	$8.45 \times 10^2$	$4.77 \times 10^3$	602.0	0.0	0.004
Trust Region-Adaptive	$2.51 \times 10^3$	$1.37 \times 10^3$	$1.11 \times 10^3$	$5.74 \times 10^3$	602.0	0.0	0.004