

Table 1: Performance Results for Sphere\2DPproblem

Optimizer	Mean Final Value	Std Dev	Best Value	Worst Value	Mean Func Evals	Success Rate (%)	Mean Time (s)
QQN-MoreThuente	0.00	0.00	0.00	0.00	13.0	100.0	0.000
QQN-Bisection-2	0.00	0.00	0.00	0.00	14.0	100.0	0.000
QQN-Backtracking	0.00	0.00	0.00	0.00	12.0	100.0	0.000
QQN-CubicQuadraticInterpolation	0.00	0.00	0.00	0.00	13.0	100.0	0.000
QQN-Bisection-1	0.00	0.00	0.00	0.00	16.0	100.0	0.000
L-BFGS	0.00	0.00	0.00	0.00	14.1	100.0	0.000
QQN-StrongWolfe	0.00	0.00	0.00	0.00	12.0	100.0	0.000
L-BFGS-Aggressive	0.00	0.00	0.00	0.00	12.6	100.0	0.000
QQN-GoldenSection	$3.16 \times 10^{-14}$	$5.52 \times 10^{-15}$	$2.25 \times 10^{-14}$	$4.41 \times 10^{-14}$	47.0	100.0	0.000
GD-WeightDecay	$3.67 \times 10^{-10}$	$1.54 \times 10^{-11}$	$3.44 \times 10^{-10}$	$3.96 \times 10^{-10}$	160.2	100.0	0.005
L-BFGS-Conservative	$1.65 \times 10^{-7}$	$4.21 \times 10^{-7}$	$2.42 \times 10^{-13}$	$1.86 \times 10^{-6}$	550.3	10.0	0.015
GD	$3.06 \times 10^{-6}$	$5.27 \times 10^{-7}$	$2.06 \times 10^{-6}$	$3.95 \times 10^{-6}$	335.0	0.0	0.008
GD-Nesterov	$9.93 \times 10^{-2}$	$1.35 \times 10^{-2}$	$7.20 \times 10^{-2}$	$1.24 \times 10^{-1}$	23.0	0.0	0.001
Adam-Fast	$1.26 \times 10^{-1}$	$6.68 \times 10^{-3}$	$1.10 \times 10^{-1}$	$1.38 \times 10^{-1}$	37.4	0.0	0.001
GD-Momentum	$1.54 \times 10^{-1}$	$2.80 \times 10^{-2}$	$1.09 \times 10^{-1}$	$1.99 \times 10^{-1}$	23.0	0.0	0.001
Adam-WeightDecay	$2.23 \times 10^{-1}$	$5.13 \times 10^{-2}$	$1.20 \times 10^{-1}$	$3.13 \times 10^{-1}$	502.0	0.0	0.010
Adam	1.21	$2.12 \times 10^{-1}$	$7.82 \times 10^{-1}$	1.59	502.0	0.0	0.010
Adam-AMSGrad	1.24	$2.50 \times 10^{-1}$	$7.07 \times 10^{-1}$	1.69	502.0	0.0	0.011
Trust Region-Conservative	3.06	3.99	$5.03 \times 10^{-2}$	$1.79 \times 10^1$	578.6	0.0	0.004
Trust Region-Standard	$1.02 \times 10^3$	$1.67 \times 10^3$	$4.40 \times 10^2$	$6.05 \times 10^3$	28.9	0.0	0.000
Trust Region-Adaptive	$1.03 \times 10^3$	$4.34 \times 10^2$	$3.80 \times 10^{-1}$	$1.22 \times 10^3$	47.7	0.0	0.000