Table 1: Performance Results for Michalewicz\\_2Dn\_m10Problem

|                                 |                        |                       |                        |                         | \2 -116            |                     |                  |
|---------------------------------|------------------------|-----------------------|------------------------|-------------------------|--------------------|---------------------|------------------|
| Optimizer                       | Mean Final<br>Value    | Std Dev               | Best<br>Value          | Worst<br>Value          | Mean Func<br>Evals | Success<br>Rate (%) | Mean Time<br>(s) |
| Trust Region-Conservative       | $-7.95 \times 10^{-7}$ | $1.30 \times 10^{-6}$ | $-4.80 \times 10^{-6}$ | $-3.63 \times 10^{-13}$ | 4.7                | 65.0                | 0.000            |
| Adam-Fast                       | $-5.87 \times 10^{-1}$ | $4.80 \times 10^{-1}$ | -1.00                  | $-4.68 \times 10^{-14}$ | 210.8              | 60.0                | 0.004            |
| Adam-WeightDecay                | $-2.43 \times 10^{-7}$ | $4.33 \times 10^{-7}$ | $-1.62 \times 10^{-6}$ | $-3.85 \times 10^{-14}$ | 13.0               | 55.0                | 0.000            |
| Trust Region-Standard           | $-7.75 \times 10^{-7}$ | $1.95 \times 10^{-6}$ | $-8.56 \times 10^{-6}$ | $-8.29 \times 10^{-14}$ | 4.4                | 40.0                | 0.000            |
| Adam-AMSGrad                    | $-6.48 \times 10^{-2}$ | $1.96 \times 10^{-1}$ | $-7.13 \times 10^{-1}$ | $-8.04 \times 10^{-14}$ | 61.9               | 30.0                | 0.001            |
| GD-Momentum                     | $-1.48 \times 10^{-6}$ | $6.08 \times 10^{-6}$ | $-2.80 \times 10^{-5}$ | $-1.18 \times 10^{-12}$ | 19.6               | 25.0                | 0.001            |
| GD                              | $-1.23 \times 10^{-6}$ | $3.18 \times 10^{-6}$ | $-1.33 \times 10^{-5}$ | $-3.39 \times 10^{-14}$ | 44.5               | 25.0                | 0.001            |
| Trust Region-Adaptive           | $-7.71 \times 10^{-7}$ | $2.55 \times 10^{-6}$ | $-1.17 \times 10^{-5}$ | $-4.35 \times 10^{-13}$ | 4.4                | 25.0                | 0.000            |
| GD-Nesterov                     | $-4.11 \times 10^{-7}$ | $8.04 \times 10^{-7}$ | $-3.19 \times 10^{-6}$ | $-4.77 \times 10^{-14}$ | 19.6               | 25.0                | 0.001            |
| QQN-CubicQuadraticInterpolation | $-3.46 \times 10^{-6}$ | $1.03 \times 10^{-5}$ | $-5.46 \times 10^{-5}$ | $-7.39 \times 10^{-14}$ | 137.6              | 17.5                | 0.004            |
| GD-WeightDecay                  | $-8.47 \times 10^{-7}$ | $2.02 \times 10^{-6}$ | $-6.96 \times 10^{-6}$ | $-7.95 \times 10^{-14}$ | 57.0               | 15.0                | 0.002            |
| L-BFGS-Aggressive               | $-9.02 \times 10^{-2}$ | $2.72 \times 10^{-1}$ | $-9.88 \times 10^{-1}$ | $-3.71 \times 10^{-14}$ | 298.7              | 2.5                 | 0.004            |
| Adam                            | $-1.03 \times 10^{-1}$ | $2.07 \times 10^{-1}$ | $-5.86 \times 10^{-1}$ | $-3.32 \times 10^{-13}$ | 452.2              | 0.0                 | 0.009            |
| QQN-Backtracking                | $-4.01 \times 10^{-2}$ | $1.75 \times 10^{-1}$ | $-8.01 \times 10^{-1}$ | $-1.48 \times 10^{-13}$ | 301.1              | 0.0                 | 0.006            |
| QQN-Bisection-1                 | $-8.51 \times 10^{-7}$ | $1.73 \times 10^{-6}$ | $-6.13 \times 10^{-6}$ | $-3.40 \times 10^{-13}$ | 212.4              | 0.0                 | 0.005            |
| QQN-StrongWolfe                 | $-7.90 \times 10^{-7}$ | $2.85 \times 10^{-6}$ | $-1.32 \times 10^{-5}$ | $-4.73 \times 10^{-14}$ | 226.9              | 0.0                 | 0.005            |
| QQN-Bisection-2                 | $-5.73 \times 10^{-7}$ | $1.93 \times 10^{-6}$ | $-8.75 \times 10^{-6}$ | $-7.35 \times 10^{-13}$ | 74.4               | 0.0                 | 0.001            |
| L-BFGS                          | $-5.62 \times 10^{-7}$ | $1.78 \times 10^{-6}$ | $-8.06 \times 10^{-6}$ | $-3.14 \times 10^{-13}$ | 197.7              | 0.0                 | 0.003            |
| QQN-GoldenSection               | $-3.69 \times 10^{-7}$ | $1.64 \times 10^{-6}$ | $-1.26\times10^{-5}$   | $-2.91 \times 10^{-14}$ | 320.4              | 0.0                 | 0.005            |
| QQN-MoreThuente                 | $-3.50 \times 10^{-7}$ | $8.09 \times 10^{-7}$ | $-3.18 \times 10^{-6}$ | $-9.53 \times 10^{-13}$ | 151.8              | 0.0                 | 0.004            |
| L-BFGS-Conservative             | $-2.69\times10^{-7}$   | $5.81\times10^{-7}$   | $-1.88\times10^{-6}$   | $-1.50 \times 10^{-13}$ | 143.9              | 0.0                 | 0.002            |