Table 1: Performance Results for PenaltyI\_5D\_alpha1e6 Problem

| Optimizer                     | Mean Final<br>Value | Std Dev  | Best<br>Value     | Worst<br>Value | Mean Func Evals | Success<br>Rate (%)                     | Mean Time (s) |
|-------------------------------|---------------------|----------|-------------------|----------------|-----------------|---|---------------|
|                               |                     | 7.61 - 5 |                   |                |                 | • |               |
| QQN-<br>GoldenSection         | 2.81e0              | 7.61e-5  | 2.81e0            | 2.81e0         | 3026.4          | 0.0                                     | 0.056         |
| QQN-                          | 2.81e0              | 7.09e-16 | 2.81e0            | 2.81e0         | 38.0            | 0.0                                     | 0.001         |
| CubicQuadraticIn              |                     | 7.09e-10 | 2.8160            | 2.8160         | 36.0            | 0.0                                     | 0.001         |
| L-BFGS-                       | 2.85e0              | 5.01e-2  | 2.81e0            | 3.03e0         | 3087.5          | 0.0                                     | 0.033         |
| Conservative                  | 2.6560              | 5.01e-2  | 2.0160            | <b>3.03e0</b>  | 3007.3          | 0.0                                     | 0.055         |
| QQN-Bisection-                | 2.81e0              | 6.12e-4  | 2.81e0            | 2.81e0         | 2178.7          | 0.0                                     | 0.071         |
| Adam-<br>AMSGrad              | 2.85e0              | 9.04e-2  | 2.82e0            | 3.24e0         | 747.3           | 0.0                                     | 0.017         |
| Adam-Robust                   | 2.16e1              | 2.85e1   | 2.82e0            | 1.26e2         | 120.4           | 0.0                                     | 0.003         |
| Adam Adam                     | 2.90e0              | 1.17e-1  | 2.82e0            | 3.24e0         | 733.5           | 0.0                                     | 0.005 $0.015$ |
| L-BFGS-                       | 2.96e0              | 9.11e-2  | 2.84e0            | 3.13e0         | 4259.2          | 0.0                                     | 0.036         |
| Limited                       | 2.5000              | 5.110 2  | 2.0400            | 0.1000         | 1200.2          | 0.0                                     | 0.000         |
| Adam-<br>WeightDecay          | 7.65e0              | 7.96e0   | 2.86e0            | 3.08e1         | 260.1           | 0.0                                     | 0.006         |
| QQN-<br>StrongWolfe           | 4.21e0              | 1.19e0   | 2.86e0            | 7.74e0         | 3121.1          | 0.0                                     | 0.086         |
| GD                            | 8.04e1              | 1.22e2   | 3.17e0            | 4.27e2         | 17.1            | 0.0                                     | 0.000         |
| GD-Nesterov                   | 3.89e2              | 8.55e2   | 3.28e0            | 3.56e3         | 14.1            | 0.0                                     | 0.000         |
| Adam-Fast                     | 4.69e2              | 8.74e2   | 3.30e0            | 2.81e3         | 29.0            | 0.0                                     | 0.001         |
| GD-                           | 5.87e2              | 9.45e2   | 3.36e0            | 2.82e3         | 13.9            | 0.0                                     | 0.000         |
| AdaptiveMomenti               |                     |          |                   |                |                 |   |               |
| L-BFGS-                       | 2.82e5              | 2.24e5   | 3.49e0            | 6.03e5         | 1110.7          | 0.0                                     | 0.022         |
| Aggressive                    |                     |          |                   |                |                 |   |               |
| GD-                           | 3.50e1              | 9.28e1   | 3.50e0            | 4.19e2         | 14.5            | 0.0                                     | 0.000         |
| WeightDecay                   |                     |          |                   |                |                 |   |               |
| L-BFGS-                       | 1.29e1              | 4.81e0   | 3.57e0            | 1.92e1         | 2860.6          | 0.0                                     | 0.036         |
| MoreThuente                   |                     |          |                   |                |                 |   |               |
| QQN-Bisection-                | 1.03e1              | 5.36e0   | 3.91e0            | 2.42e1         | 469.8           | 0.0                                     | 0.011         |
| GD-Momentum                   | 9.24e1              | 2.66e2   | 3.99e0            | 1.22e3         | 14.4            | 0.0                                     | 0.000         |
| L-BFGS                        | 7.00e4              | 1.12e5   | 4.88e0            | 5.16e5         | 95.2            | 0.0                                     | 0.001         |
| Trust Region-                 | 3.71e5              | 1.47e5   | 9.78e4            | 6.40e5         | 3002.0          | 0.0                                     | 0.019         |
| Adaptive                      |                     |          |                   |                |                 |   |               |
| Trust Region-<br>Standard     | 3.74e5              | 1.32e5   | 1.16e5            | 7.18e5         | 3002.0          | 0.0                                     | 0.019         |
| Trust Region-<br>Conservative | 3.90e5              | 1.18e5   | 1.47e5            | 5.82e5         | 3002.0          | 0.0                                     | 0.022         |
| Trust Region-<br>Aggressive   | 3.61e5              | 1.19e5   | 1.76e5            | 5.61e5         | 3002.0          | 0.0                                     | 0.020         |
| Trust Region-<br>Precise      | 4.20e5              | 1.11e5   | $2.36\mathrm{e}5$ | 6.26e5         | 3002.0          | 0.0                                     | 0.020         |