

Table 1: Performance Results for PenaltyI\10Dn\_alpha1e6Problem

| Optimizer                       | Mean Final Value   | Std Dev               | Best Value         | Worst Value        | Mean Func Evals | Success Rate (%) | Mean Time (s) |
|---------------------------------|--------------------|-----------------------|--------------------|--------------------|-----------------|------------------|---------------|
| QQN-GoldenSection               | 5.63               | $9.72 \times 10^{-4}$ | 5.63               | 5.63               | 909.6           | 0.0              | 0.016         |
| QQN-Bisection-1                 | 5.64               | $3.69 \times 10^{-3}$ | 5.63               | 5.64               | 442.6           | 0.0              | 0.014         |
| L-BFGS-Conservative             | 5.73               | $1.04 \times 10^{-1}$ | 5.63               | 6.00               | 683.1           | 0.0              | 0.009         |
| GD                              | 8.44               | $1.42 \times 10^1$    | 5.68               | $9.67 \times 10^1$ | 18.3            | 0.0              | 0.000         |
| Adam-WeightDecay                | 9.80               | 6.26                  | 5.72               | $3.18 \times 10^1$ | 269.4           | 0.0              | 0.006         |
| QQN-Bisection-2                 | $2.38 \times 10^1$ | 9.61                  | 9.95               | $4.07 \times 10^1$ | 590.8           | 0.0              | 0.014         |
| QQN-Backtracking                | $2.39 \times 10^1$ | $1.01 \times 10^1$    | 9.57               | $4.18 \times 10^1$ | 709.7           | 0.0              | 0.023         |
| QQN-CubicQuadraticInterpolation | $3.13 \times 10^1$ | $1.46 \times 10^1$    | $1.10 \times 10^1$ | $6.19 \times 10^1$ | 396.8           | 0.0              | 0.016         |
| QQN-StrongWolfe                 | $3.35 \times 10^1$ | $1.63 \times 10^1$    | $1.35 \times 10^1$ | $7.22 \times 10^1$ | 593.2           | 0.0              | 0.017         |
| GD-WeightDecay                  | $5.39 \times 10^1$ | $1.22 \times 10^2$    | 6.87               | $5.40 \times 10^2$ | 15.9            | 0.0              | 0.000         |
| GD-Nesterov                     | $1.82 \times 10^2$ | $3.92 \times 10^2$    | 6.83               | $1.60 \times 10^3$ | 14.7            | 0.0              | 0.000         |
| GD-Momentum                     | $3.14 \times 10^2$ | $5.37 \times 10^2$    | 7.48               | $1.85 \times 10^3$ | 15.2            | 0.0              | 0.000         |
| Adam-Fast                       | $1.43 \times 10^3$ | $1.48 \times 10^3$    | 6.84               | $5.21 \times 10^3$ | 32.1            | 0.0              | 0.001         |
| Adam                            | $6.19 \times 10^4$ | $3.79 \times 10^4$    | $3.61 \times 10^3$ | $1.53 \times 10^5$ | 502.0           | 0.0              | 0.011         |
| Adam-AMSGrad                    | $6.67 \times 10^4$ | $3.34 \times 10^4$    | $1.06 \times 10^4$ | $1.33 \times 10^5$ | 502.0           | 0.0              | 0.012         |
| QQN-MoreThuente                 | $1.15 \times 10^5$ | $2.49 \times 10^4$    | $4.71 \times 10^4$ | $1.60 \times 10^5$ | 487.0           | 0.0              | 0.011         |
| L-BFGS                          | $2.47 \times 10^5$ | $3.39 \times 10^5$    | $1.09 \times 10^1$ | $9.93 \times 10^5$ | 112.9           | 0.0              | 0.002         |
| L-BFGS-Aggressive               | $3.92 \times 10^5$ | $4.12 \times 10^5$    | 8.21               | $1.06 \times 10^6$ | 387.1           | 0.0              | 0.004         |
| Trust Region-Adaptive           | $7.29 \times 10^5$ | $1.87 \times 10^5$    | $3.99 \times 10^5$ | $1.24 \times 10^6$ | 602.0           | 0.0              | 0.004         |
| Trust Region-Conservative       | $7.49 \times 10^5$ | $2.29 \times 10^5$    | $3.55 \times 10^5$ | $1.26 \times 10^6$ | 602.0           | 0.0              | 0.004         |
| Trust Region-Standard           | $8.13 \times 10^5$ | $1.70 \times 10^5$    | $5.09 \times 10^5$ | $1.09 \times 10^6$ | 602.0           | 0.0              | 0.004         |