Table 1: Performance Results for Griewank\ $_5DProblem$ 

| 0                               | 3.6 79: 1            | G. I.D.               | D /                  | ***                  | 10                 | -                   | 3.6 m:           |
|---------------------------------|----------------------|-----------------------|----------------------|----------------------|--------------------|---------------------|------------------|
| Optimizer                       | Mean Final<br>Value  | Std Dev               | Best<br>Value        | Worst<br>Value       | Mean Func<br>Evals | Success<br>Rate (%) | Mean Time<br>(s) |
| QQN-StrongWolfe                 | 9.98                 | 2.96                  | 3.87                 | $1.33 \times 10^{1}$ | 457.9              | 0.0                 | 0.020            |
| QQN-Backtracking                | $1.13 \times 10^{1}$ | 1.62                  | 6.27                 | $1.25 \times 10^{1}$ | 578.1              | 0.0                 | 0.029            |
| QQN-Bisection-1                 | $1.17 \times 10^{1}$ | 1.74                  | 4.41                 | $1.31 \times 10^{1}$ | 295.1              | 0.0                 | 0.007            |
| QQN-CubicQuadraticInterpolation | $1.18 \times 10^{1}$ | 1.94                  | 2.78                 | $1.31 \times 10^{1}$ | 367.9              | 0.0                 | 0.014            |
| L-BFGS-Aggressive               | $1.20 \times 10^{1}$ | 1.03                  | 6.96                 | $1.23 \times 10^{1}$ | 348.9              | 0.0                 | 0.006            |
| GD-Momentum                     | $1.22 \times 10^{1}$ | $3.09 \times 10^{-7}$ | $1.22 \times 10^{1}$ | $1.22 \times 10^{1}$ | 335.0              | 0.0                 | 0.010            |
| GD-Nesterov                     | $1.22 \times 10^{1}$ | $3.81 \times 10^{-7}$ | $1.22 \times 10^{1}$ | $1.22 \times 10^{1}$ | 335.0              | 0.0                 | 0.011            |
| L-BFGS-Conservative             | $1.22 \times 10^{1}$ | $4.27 \times 10^{-5}$ | $1.22 \times 10^{1}$ | $1.22 \times 10^{1}$ | 557.4              | 0.0                 | 0.014            |
| L-BFGS                          | $1.23 \times 10^{1}$ | $4.14 \times 10^{-2}$ | $1.22 \times 10^{1}$ | $1.24 \times 10^{1}$ | 259.4              | 0.0                 | 0.006            |
| Trust Region-Conservative       | $1.23 \times 10^{1}$ | $2.83 \times 10^{-3}$ | $1.23 \times 10^{1}$ | $1.23 \times 10^{1}$ | 379.6              | 0.0                 | 0.003            |
| QQN-GoldenSection               | $1.23 \times 10^{1}$ | $8.03 \times 10^{-1}$ | 8.34                 | $1.31 \times 10^{1}$ | 716.1              | 0.0                 | 0.014            |
| Adam-Fast                       | $1.23 \times 10^{1}$ | $1.92 \times 10^{-2}$ | $1.22 \times 10^{1}$ | $1.23 \times 10^{1}$ | 68.8               | 0.0                 | 0.001            |
| QQN-MoreThuente                 | $1.24 \times 10^{1}$ | $3.06 \times 10^{-1}$ | $1.21 \times 10^{1}$ | $1.31 \times 10^{1}$ | 349.6              | 0.0                 | 0.012            |
| GD-WeightDecay                  | $1.24 \times 10^{1}$ | $6.67 \times 10^{-2}$ | $1.23 \times 10^{1}$ | $1.25 \times 10^{1}$ | 335.0              | 0.0                 | 0.011            |
| QQN-Bisection-2                 | $1.26 \times 10^{1}$ | $3.71 \times 10^{-1}$ | $1.22 \times 10^{1}$ | $1.31 \times 10^{1}$ | 422.4              | 0.0                 | 0.010            |
| Adam-WeightDecay                | $1.31 \times 10^{1}$ | $5.38 \times 10^{-2}$ | $1.31 \times 10^{1}$ | $1.32 \times 10^{1}$ | 502.0              | 0.0                 | 0.011            |
| GD                              | $1.32 \times 10^{1}$ | $1.04 \times 10^{-1}$ | $1.30 \times 10^{1}$ | $1.34 \times 10^{1}$ | 335.0              | 0.0                 | 0.009            |
| Adam                            | $1.34 \times 10^{1}$ | $2.57 \times 10^{-2}$ | $1.33 \times 10^{1}$ | $1.34 \times 10^{1}$ | 502.0              | 0.0                 | 0.010            |
| Adam-AMSGrad                    | $1.34 \times 10^{1}$ | $3.75 \times 10^{-2}$ | $1.33 \times 10^{1}$ | $1.35 \times 10^{1}$ | 502.0              | 0.0                 | 0.012            |
| Trust Region-Adaptive           | $1.35 \times 10^{1}$ | $2.50 \times 10^{-2}$ | $1.35 \times 10^{1}$ | $1.35 \times 10^{1}$ | 5.0                | 0.0                 | 0.000            |
| Trust Region-Standard           | $1.35 \times 10^{1}$ | $2.18\times10^{-2}$   | $1.35 \times 10^{1}$ | $1.35 \times 10^{1}$ | 5.0                | 0.0                 | 0.000            |