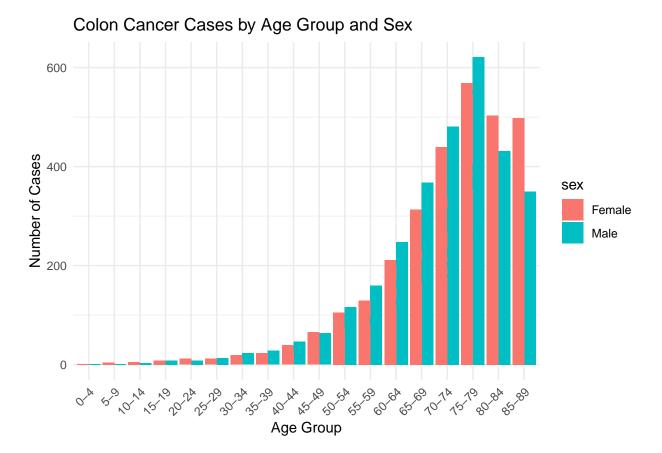
ki

Chen Chen Michelle

2024-11-18

We have variables are below: AgeGroup Year Sex The number of cases

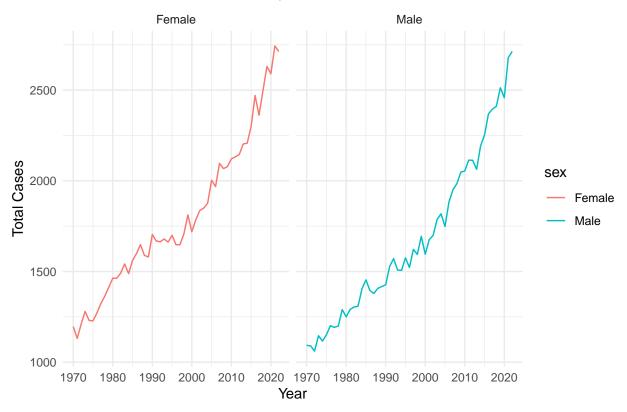
Conclusion: when age increases, the number of the cancer cases are increasing too. The colon cancer tends to happen to the old aged group. We can guess age may be positively related to the colon cancer rate. In the plot, the age group 75-79 has the highest number of cases. And the age group over 80, the incidence rate tends to decrease.



The trend of the total cases of both sexes has continuously increased over the years.

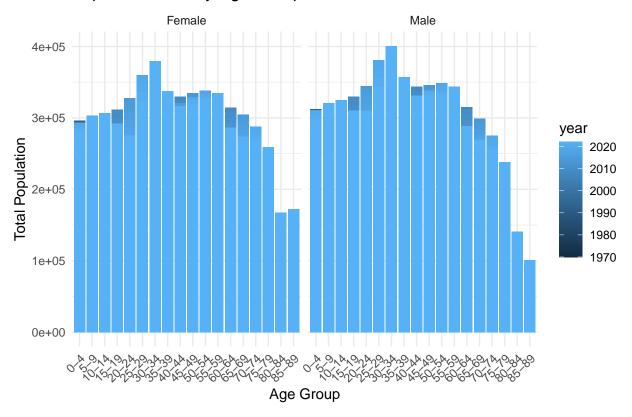
```
#question 2
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
# Summarize the data
summary_data <- data %>%
  group_by(year, sex) %>%
  summarize(total_cases = sum(n, na.rm = TRUE))
## `summarise()` has grouped output by 'year'. You can override using the
## `.groups` argument.
```

Total Colon Cancer Cases by Year and Sex



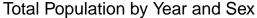
The two datasets have the same age group and calendar years.

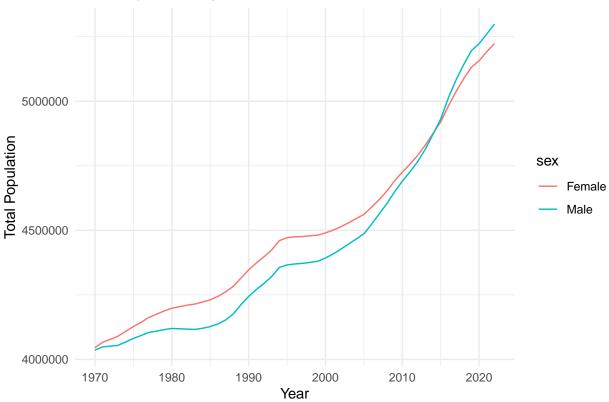
Population Size by Age Group, Year, and Sex



```
#question 4
# Merge the datasets
merged_data <- merge(data, population, by = c("year", "agegroup", "sex"))
# Summarize the total number of cases and population by year and sex
summary_data <- merged_data %>%
    group_by(year, sex) %>%
```

```
summarize(
   total_cases = sum(n, na.rm = TRUE),
   total_population = sum(n_pop, na.rm = TRUE)
## `summarise()` has grouped output by 'year'. You can override using the
## `.groups` argument.
# Check the summarized data
head(summary_data)
## # A tibble: 6 x 4
## # Groups: year [3]
## year sex total_cases total_population
## <int> <chr> <int>
                                      <int>
                     1196
## 1 1970 Female
                                    4045318
## 2 1970 Male
                      1093
                                  4035911
                    1131
1090
## 3 1971 Female
                                   4066592
## 4 1971 Male
                                    4048573
## 5 1972 Female
                      1210
                                    4077814
## 6 1972 Male
                      1061
                                    4051315
# Plot total population by year and sex
ggplot(summary_data, aes(x = year, y = total_population, color = sex)) +
  geom_line() +
  labs(title = "Total Population by Year and Sex",
      x = "Year",
      y = "Total Population") +
  theme_minimal()
```





```
#question 5
# Add a new variable for incidence rate in the merged data
new_merged_data <- merged_data %>%
    mutate(incidence_rate = n / n_pop)

# Check the updated data
head(new_merged_data)
```

```
sex n n_pop incidence_rate
##
    year agegroup
## 1 1970
              0-4 Female 0 280468
                                     0.000000e+00
                                     0.000000e+00
## 2 1970
              0 - 4
                    Male 0 296143
## 3 1970
            10-14 Female 1 257746
                                     3.879789e-06
## 4 1970
            10-14
                     Male 0 272559
                                     0.000000e+00
## 5 1970
            15-19 Female 1 269428
                                     3.711567e-06
## 6 1970
            15-19
                    Male 1 281997
                                     3.546137e-06
```

```
# Add a new variable for incidence rate in the summarized data
new_summary_data <- summary_data %>%
   mutate(incidence_rate = total_cases / total_population)
# Check the updated data
head(new_summary_data)
```

A tibble: 6 x 5
Groups: year [3]

```
##
                  total_cases total_population incidence_rate
      year sex
##
     <int> <chr>
                         <int>
                                          <int>
                                                          <dbl>
## 1 1970 Female
                         1196
                                        4045318
                                                      0.000296
                         1093
## 2 1970 Male
                                        4035911
                                                      0.000271
## 3
     1971 Female
                         1131
                                        4066592
                                                       0.000278
## 4 1971 Male
                         1090
                                                      0.000269
                                        4048573
## 5 1972 Female
                                        4077814
                                                       0.000297
                         1210
## 6 1972 Male
                          1061
                                        4051315
                                                      0.000262
```

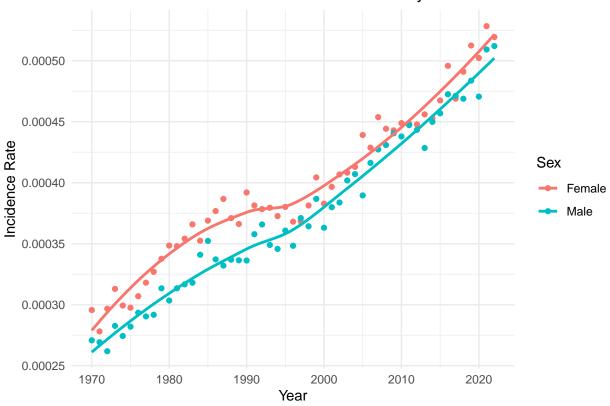
Definition of the incident rate = (total cases /total population) *100

Yes, it looks appropriate.

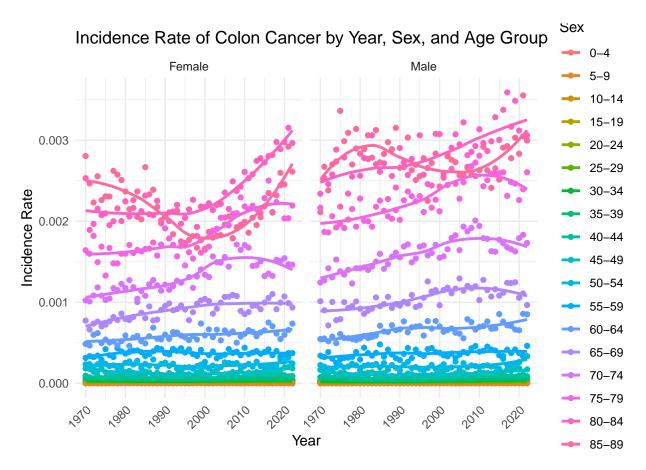
The incidence rate of colon cancer has steadily increased over calendar time for both males and females. Females consistently have a higher incidence rate of colon cancer compared to males throughout the period.

```
## `geom_smooth()` using formula = 'y ~ x'
```

Incidence Rate of Colon Cancer Over Time by Sex



`geom_smooth()` using formula = 'y ~ x'



The Poisson model estimates the total number of cases as the dependent variable, using population size as an offset and calendar year and sex as independent variables.

The estimated intercept is -29.69, representing the baseline log-incidence rate when the year is 0 and the reference category for sex (likely Female). The coefficient for the variable year is 0.01094 (p < 0.001), indicating a 1.1% annual increase in the incidence rate ((e^(0.01094) - 1) * 100), holding sex constant. The coefficient for sex (Male) is -0.05592 (p < 0.001), implying a 5.6% lower incidence rate for males compared to females, holding year constant.

```
#question 7 assume: main effect model the effect of exposure is the same in all levels of
poisson_model <- glm(
  total_cases ~ year + sex,
  offset = log(total_population),
  family = poisson(link = "log"),
  data = new_summary_data
)
summary(poisson_model)</pre>
```

```
##
## Call:
## glm(formula = total_cases ~ year + sex, family = poisson(link = "log"),
## data = new_summary_data, offset = log(total_population))
##
## Coefficients:
## Estimate Std. Error z value Pr(>|z|)
```

```
## (Intercept) -2.969e+01 3.071e-01 -96.68
                                             <2e-16 ***
              1.094e-02 1.536e-04 71.25
## year
                                             <2e-16 ***
## sexMale
              -5.592e-02 4.658e-03 -12.01
                                             <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
##
      Null deviance: 5505.07 on 105 degrees of freedom
## Residual deviance: 222.81 on 103 degrees of freedom
## AIC: 1211.4
##
## Number of Fisher Scoring iterations: 3
```

Based on the model output, the estimated incidence rates in 1970 are 0.0002933 for females and 0.0002774 for males. In 2020, the incidence rates are 0.0005070 for females and 0.0004794 for males. The model assumes that the log-incidence rate changes linearly with the calendar year, leading to an annual incidence rate increase of 1.1% ((e^(0.01094) - 1) * 100).

The key assumptions made in this model:

0.0002933271

- A linear relationship between year and log-incidence rate: log() = _0 + _1(year) + _2(sex).
- A constant difference between males and females: $_2 = -0.0559$, males have 5.5% lower incidence rates than females.
- No interactions among year, sex, age group.
- Accurate population size as an offset: the population size is accurately measured and representative of the population at risk for both sexes and years.
- Poisson distribution of the dependent variable: the variance in the number of cases increases with the expected number of cases.

```
#question 8
# Extract model coefficients
coefficients <- coef(poisson_model)</pre>
intercept <- coefficients["(Intercept)"]</pre>
year_coeff <- coefficients["year"]</pre>
sex_coeff <- coefficients["sexMale"]</pre>
# Calculate log incidence rate and incidence rate for 1970 and 2020
incidence_1970_male <- exp(intercept + year_coeff * 1970 + sex_coeff)</pre>
incidence_1970_female <- exp(intercept + year_coeff * 1970 )</pre>
incidence_2020_male <- exp(intercept + year_coeff * 2020 + sex_coeff)</pre>
incidence_2020_female <- exp(intercept + year_coeff * 2020)</pre>
# Print results
incidence_1970_male
   (Intercept)
## 0.0002773751
incidence_1970_female
## (Intercept)
```

```
incidence_2020_male

## (Intercept)
## 0.0004794199

incidence_2020_female

## (Intercept)
```

Colon cancer is more common in older age groups, and the age distribution has shifted over time. To better estimate incidence rates, we refit the Poisson model by including interaction terms: "year * sex," "year * age group," and "sex * age group."

0.0005069918

Based on the updated model output, the estimated incidence rates in 1970 for the 70-74 age group are 0.001350 for males and 0.001098 for females. In 2020, the incidence rates for the same age group are 0.001846 for males and 0.001544 for females.

```
#question9
# Fit a Poisson regression model with interaction terms for flexibility
poisson_model_age <- glm(
    n ~ year * sex + year * agegroup + sex * agegroup,
    offset = log(n_pop),
    family = poisson(link = "log"),
    data = new_merged_data  # Ensure merged_data has cases, population, year, sex, and agegroup)

# View the summary of the model
summary(poisson_model_age)</pre>
```

```
##
## Call:
## glm(formula = n ~ year * sex + year * agegroup + sex * agegroup,
##
      family = poisson(link = "log"), data = new merged data, offset = log(n pop))
##
## Coefficients:
##
                         Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                       -6.879e+01 9.627e+01 -0.715 0.4749
## year
                        2.618e-02 4.807e-02 0.545
                                                     0.5860
## sexMale
                        1.086e+00 1.545e+00 0.703
                                                     0.4819
                        5.897e+01 9.865e+01
                                             0.598
## agegroup5-9
                                                     0.5500
## agegroup10-14
                        7.020e+01 9.684e+01 0.725
                                                     0.4685
## agegroup15-19
                        3.521e+01 9.654e+01 0.365
                                                     0.7153
                        4.121e+01 9.648e+01
                                             0.427
                                                     0.6693
## agegroup20-24
## agegroup25-29
                        4.711e+01 9.643e+01
                                            0.489
                                                     0.6252
## agegroup30-34
                        3.562e+01 9.637e+01 0.370 0.7117
## agegroup35-39
                        4.877e+01 9.634e+01 0.506 0.6127
                        4.329e+01 9.631e+01 0.449
## agegroup40-44
                                                     0.6531
## agegroup45-49
                        5.194e+01 9.629e+01 0.539
                                                     0.5897
## agegroup50-54
                        5.354e+01 9.628e+01 0.556
                                                     0.5782
## agegroup55-59
                       5.598e+01 9.628e+01 0.581
                                                     0.5609
## agegroup60-64
                        4.976e+01 9.628e+01 0.517
                                                     0.6053
```

```
## agegroup65-69
                         4.985e+01 9.627e+01
                                                0.518
                                                        0.6046
## agegroup70-74
                         4.853e+01 9.627e+01
                                                0.504
                                                        0.6142
## agegroup75-79
                         4.823e+01 9.627e+01
                                                0.501
                                                        0.6164
## agegroup80-84
                         4.867e+01 9.627e+01
                                                0.505
                                                        0.6132
## agegroup85-89
                         6.130e+01
                                    9.627e+01
                                                0.637
                                                        0.5243
## year:sexMale
                        -5.696e-04 3.104e-04 -1.835
                                                        0.0665
## year:agegroup5-9
                        -2.792e-02 4.927e-02 -0.567
                                                        0.5710
## year:agegroup10-14
                        -3.283e-02 4.836e-02
                                               -0.679
                                                        0.4972
## year:agegroup15-19
                        -1.496e-02 4.821e-02
                                               -0.310
                                                        0.7563
## year:agegroup20-24
                        -1.788e-02 4.818e-02 -0.371
                                                        0.7106
## year:agegroup25-29
                        -2.080e-02 4.815e-02
                                               -0.432
                                                        0.6658
## year:agegroup30-34
                        -1.484e-02 4.812e-02
                                               -0.308
                                                        0.7578
                                              -0.440
## year:agegroup35-39
                        -2.117e-02 4.811e-02
                                                        0.6599
                                                        0.7056
## year:agegroup40-44
                        -1.816e-02 4.809e-02 -0.378
## year:agegroup45-49
                        -2.220e-02 4.808e-02
                                               -0.462
                                                        0.6443
## year:agegroup50-54
                         -2.274e-02
                                    4.808e-02
                                               -0.473
                                                        0.6362
## year:agegroup55-59
                        -2.372e-02 4.808e-02 -0.493
                                                        0.6217
## year:agegroup60-64
                        -2.037e-02 4.807e-02
                                               -0.424
                                                        0.6717
## year:agegroup65-69
                        -2.020e-02 4.807e-02 -0.420
                                                        0.6743
                                               -0.403
## year:agegroup70-74
                        -1.935e-02 4.807e-02
                                                        0.6873
## year:agegroup75-79
                        -1.904e-02 4.807e-02 -0.396
                                                        0.6921
## year:agegroup80-84
                        -1.914e-02 4.807e-02 -0.398
                                                        0.6905
## year:agegroup85-89
                        -2.552e-02 4.807e-02 -0.531
                                                        0.5956
## sexMale:agegroup5-9
                        -7.823e-01 1.460e+00
                                               -0.536
                                                        0.5921
                                                        0.6447
## sexMale:agegroup10-14 -6.568e-01 1.424e+00
                                               -0.461
## sexMale:agegroup15-19 -4.856e-01 1.419e+00
                                               -0.342
                                                        0.7322
## sexMale:agegroup20-24 -4.125e-01 1.418e+00
                                               -0.291
                                                        0.7711
## sexMale:agegroup25-29 -1.100e-01 1.417e+00
                                               -0.078
                                                        0.9381
## sexMale:agegroup30-34 -3.506e-02 1.416e+00
                                               -0.025
                                                        0.9802
## sexMale:agegroup35-39 -7.101e-02 1.415e+00
                                               -0.050
                                                        0.9600
## sexMale:agegroup40-44 1.914e-02 1.415e+00
                                                0.014
                                                        0.9892
## sexMale:agegroup45-49 -5.963e-02 1.415e+00
                                               -0.042
                                                        0.9664
## sexMale:agegroup50-54 -4.559e-04 1.414e+00
                                                0.000
                                                        0.9997
                                                0.035
## sexMale:agegroup55-59 4.903e-02 1.414e+00
                                                        0.9723
## sexMale:agegroup60-64 1.673e-01
                                                0.118
                                                        0.9058
                                    1.414e+00
## sexMale:agegroup65-69 1.981e-01 1.414e+00
                                                0.140
                                                        0.8886
## sexMale:agegroup70-74 2.426e-01
                                    1.414e+00
                                                0.172
                                                        0.8638
## sexMale:agegroup75-79
                         2.643e-01 1.414e+00
                                                0.187
                                                        0.8517
## sexMale:agegroup80-84
                                                0.178
                                                        0.8588
                         2.516e-01
                                    1.414e+00
## sexMale:agegroup85-89 3.263e-01 1.414e+00
                                                0.231
                                                        0.8175
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 406971.1
                                        degrees of freedom
                               on 1907
## Residual deviance:
                        2749.5
                               on 1853 degrees of freedom
## AIC: 11967
## Number of Fisher Scoring iterations: 6
# Extract model coefficients
coefficients <- coef(poisson_model_age)</pre>
```

```
# males
rate_1970_male <- exp(</pre>
  #intercept
  coefficients["(Intercept)"] +
    coefficients["year"] * 1970 +
    #male
    coefficients["sexMale"] * 1 +
    #age 70-74
    coefficients["agegroup70-74"] * 1 +
    # year*sex
    coefficients["year:sexMale"] * 1970 * 1 +
    # year*age 70-74
    coefficients["year:agegroup70-74"] * 1970 * 1 +
    # sex*age 70-74
    coefficients["sexMale:agegroup70-74"] * 1 * 1)
rate_1970_female <- exp(</pre>
  #intercept
  coefficients["(Intercept)"] +
    #year
    coefficients["year"] * 1970 +
    #female
    coefficients["sexMale"] * 0 +
    #age 70-74
    coefficients["agegroup70-74"] * 1 +
    # year*sex
    coefficients["year:sexMale"] * 1970 * 0 +
    # year*age 70-74
    coefficients["year:agegroup70-74"] * 1970 * 1 +
    # sex*age 70-74
    coefficients["sexMale:agegroup70-74"] * 0 * 1)
rate_2020_male <- exp(</pre>
  #intercept
  coefficients["(Intercept)"] +
  #year
  coefficients["year"] * 2020 +
  #male
  coefficients["sexMale"] * 1 +
  #age 70-74
  coefficients["agegroup70-74"] * 1 +
  # year*sex
  coefficients["year:sexMale"] * 2020 * 1 +
  # year*age 70-74
  coefficients["year:agegroup70-74"] * 2020 * 1 +
  # sex*age 70-74
  coefficients["sexMale:agegroup70-74"] * 1 * 1)
rate_2020_female <- exp(</pre>
```

```
#intercept
  coefficients["(Intercept)"] +
    #year
    coefficients["year"] * 2020 +
    #female
    coefficients["sexMale"] * 0 +
    #age 70-74
    coefficients["agegroup70-74"] * 1 +
    # year*sex
    coefficients["year:sexMale"] * 2020 * 0 +
    # year*age 70-74
    coefficients["year:agegroup70-74"] * 2020 * 1 +
    # sex*age 70-74
    coefficients["sexMale:agegroup70-74"] * 0 * 1)
rate_1970_male
## (Intercept)
## 0.001349865
rate_1970_female
## (Intercept)
## 0.001097564
rate_2020_male
## (Intercept)
## 0.001845669
rate_2020_female
## (Intercept)
## 0.001544049
```