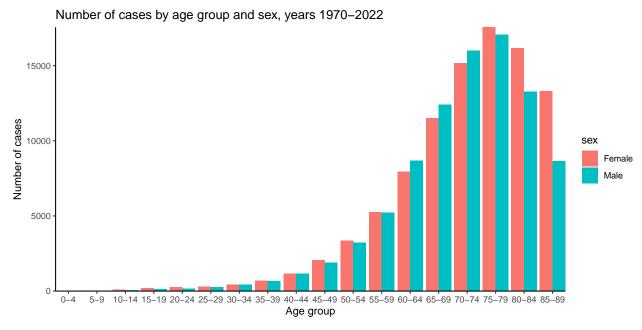
Assignment 1

```
library(readr)
library(tidyverse)
library(ggplot2)
library(splines)
cases <- readr::read_tsv("cases.tsv")</pre>
population <- readr::read_tsv("population.tsv")</pre>
##
      agegroup
                              year
                                             sex
                                                                    n
   Length: 1908
                                                                     : 0.00
##
                                :1970
                                         Length:1908
                        Min.
                                                             Min.
    Class : character
                         1st Qu.:1983
                                         Class : character
                                                             1st Qu.: 4.00
    Mode :character
                                         Mode :character
                         Median:1996
##
                                                             Median : 28.00
##
                         Mean
                                :1996
                                                             Mean
                                                                     : 96.73
##
                         3rd Qu.:2009
                                                             3rd Qu.:177.25
##
                         Max.
                                :2022
                                                             Max.
                                                                     :621.00
Dataset cases contains the yearly number of cancer cases (variable "n") by age group (variable "agegroup")
and sex (variable "sex"), with variable "year" ranging from 1970 to 2022. Eighteen different age groups are
defined, as:
## [1] 0-4
               5-9
                     10-14 15-19 20-24 25-29 30-34 35-39 40-44 45-49 50-54 55-59
## [13] 60-64 65-69 70-74 75-79 80-84 85-89
## 18 Levels: 0-4 5-9 10-14 15-19 20-24 25-29 30-34 35-39 40-44 45-49 ... 85-89
Two sex groups are defined, as:
## [1] "Male"
                 "Female"
```

Question 1: plot the number of cases by age group and sex



The plot shows that:

• both for females and males separately, the total number of cases registered between 1970 and 2022 increases with age, reaches a peak at age group 75-79 and then decreases with age.

We have variables are below:

AgeGroup

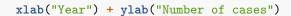
Year

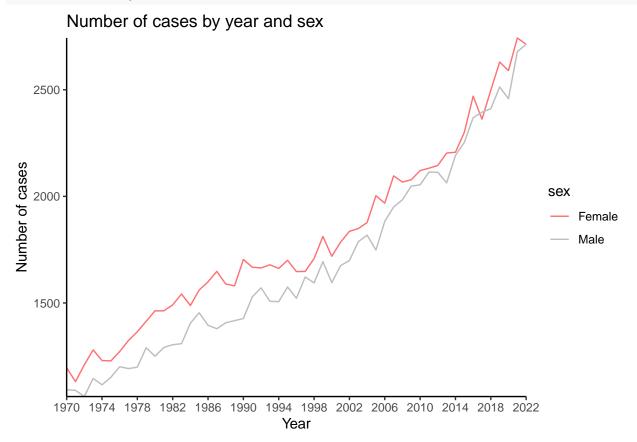
Sex

The number of cases

Conclusion: when age increases, the number of cancer cases are increasing too. Colon cancer tends to happen to the old aged group. We can guess age may be positively related to the colon cancer rate. In the plot, the age group 75-79 has the highest number of cases. And the age group over 80, the incidence rate tends to decrease.

Question 2: total number of cases in each calendar year by males and females.



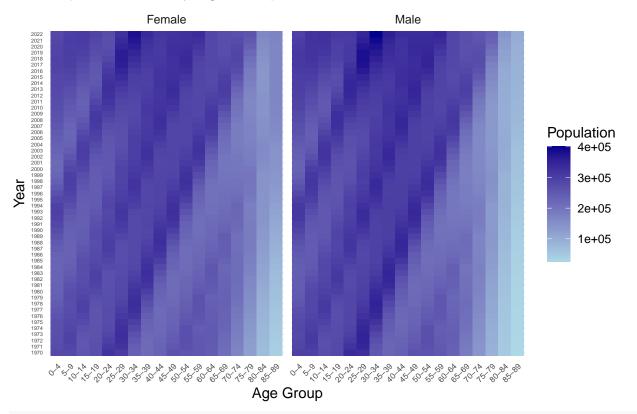


The graphs show an increasing trend in the yearly number of cases, both for females and males. The trend of the total cases of both sexes has continuously increased over the years. The total yearly number of reported cancer cases tends to be lower for males than for females.

Question 3: population, and plot of population size over age groups and calendar year simultaneously, separately by males and females.

The dataset

Population Size by Age Group and Year



head(population)

```
## # A tibble: 6 x 4
##
     agegroup sex
                     year n_pop
##
     <chr>
              <chr> <dbl>
                           <dbl>
## 1 0-4
              Male
                     1970 296143
## 2 5-9
              Male
                     1970 295092
## 3 10-14
              Male
                     1970 272559
## 4 15-19
              Male
                     1970 281997
## 5 20-24
                     1970 336648
              Male
## 6 25-29
              Male
                     1970 329316
```

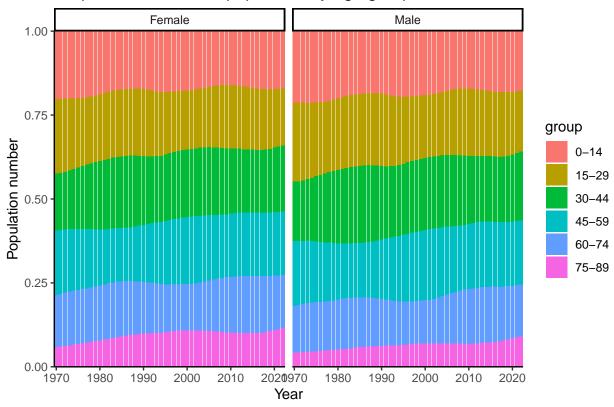
summary(population)

```
##
                                               year
      agegroup
                           sex
                                                             n_pop
##
   Length:1908
                       Length:1908
                                                                : 26513
                                          Min.
                                                 :1970
                                                         Min.
   Class :character
                       Class : character
                                          1st Qu.:1983
                                                         1st Qu.:215564
##
   Mode :character
##
                                          Median:1996
                                                         Median :269226
                       Mode :character
##
                                          Mean
                                                 :1996
                                                         Mean
                                                                 :248347
##
                                          3rd Qu.:2009
                                                         3rd Qu.:299042
##
                                                 :2022
                                                                 :400939
                                                         Max.
```

Compare age groups
all(unique(cases\$agegroup) %in% unique(population\$agegroup))

```
## [1] TRUE
# Compare calendar years
all(unique(cases$year) %in% unique(population$year))
## [1] TRUE
Dataset population includes the same age groups and calendar years as dataset cases.
population <- population %>% mutate(agegroup = factor(agegroup, levels = factor_groups))
population %>%
  mutate(group = case_when(
   agegroup %in% factor_groups[1:3] ~ "0-14",
   agegroup %in% factor_groups[4:6] ~ "15-29",
   agegroup %in% factor_groups[7:9] ~ "30-44",
   agegroup %in% factor_groups[10:12] ~ "45-59",
   agegroup %in% factor_groups[13:15] ~ "60-74",
   agegroup %in% factor_groups[16:18] ~ "75-89",
   TRUE ~ NA
   )
   ) %>%
  ggplot(aes(x = year, y = n_pop, fill = group)) +
  facet_wrap(~sex, ncol = 2) +
  geom_bar(position="fill", stat="identity") +
  theme_classic() +
  coord_cartesian(expand = FALSE) +
  # add labels and title
  ggtitle("Proportion of swedish population by age group.") +
  xlab("Year") + ylab("Population number")
```

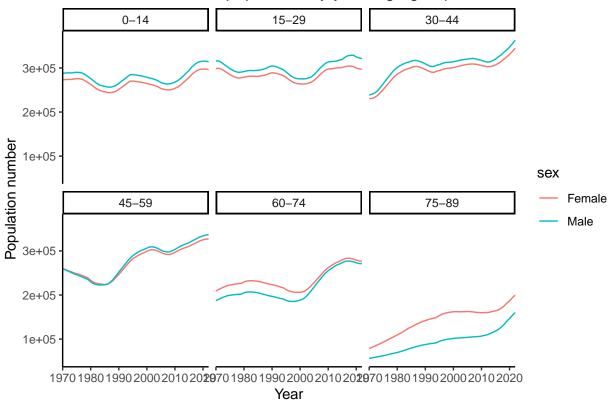
Proportion of swedish population by age group.



Plot, males and females bigger age groups

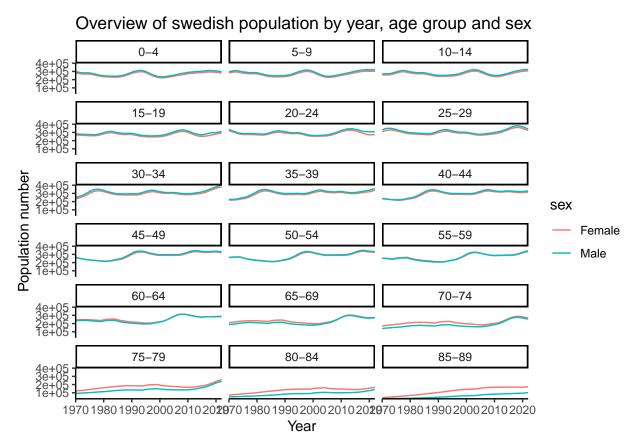
```
population %>%
  mutate(group = case when(
    agegroup %in% factor_groups[1:3] ~ "0-14",
    agegroup %in% factor_groups[4:6] ~ "15-29",
    agegroup %in% factor_groups[7:9] ~ "30-44",
    agegroup %in% factor_groups[10:12] ~ "45-59",
    agegroup %in% factor_groups[13:15] ~ "60-74",
    agegroup %in% factor_groups[16:18] ~ "75-89",
    TRUE ~ NA
    )
    ) %>%
  ggplot(aes(x = year, y = n_pop, color = sex)) +
  facet_wrap(~group, ncol = 3) +
  stat_summary(geom="line")+
  theme_classic() +
  coord_cartesian(expand = FALSE) +
  # add labels and title
  ggtitle("Overview of swedish population by year, age group and sex") +
  xlab("Year") + ylab("Population number")
```





Plot, males and females

```
population %>%
  ggplot(aes(x = year, y = n_pop, color = sex)) +
  facet_wrap(~agegroup, ncol = 3) +
  stat_summary(geom="line")+
  theme_classic() +
  coord_cartesian(expand = FALSE) +
  # add labels and title
  ggtitle("Overview of swedish population by year, age group and sex") +
  xlab("Year") + ylab("Population number")
```



Yes, the two datasets have the same age group and calendar years.

Question 4: merge the datasets

merged dataframe, with age

```
# merging datasets
cases_pop <- cases %>% left_join(population)
# ## check
# cases %>% nrow() == cases_pop %>% nrow()
# population %>% nrow() == cases_pop %>% nrow()
cases_pop %>% head()
## # A tibble: 6 x 5
     agegroup year sex
                              n n_pop
##
     <fct>
              <dbl> <chr> <dbl> <dbl> <dbl>
## 1 0-4
               2022 Male
                              0 296183
## 2 5-9
               2022 Male
                              0 319820
## 3 10-14
               2022 Male
                              1 325003
               2022 Male
## 4 15-19
                              8 310539
## 5 20-24
               2022 Male
                              5 310354
## 6 25-29
               2022 Male
                              4 342974
```

Cases and population datasets summarized. Will be merged in question 5

```
# cases by year and sex
cases_ys <- cases %>%
  group_by(year, sex) %>%
  summarize(n = sum(n)) %>%
  ungroup()

# population by year and sex
population_ys <- population %>%
  group_by(year, sex) %>%
  summarize(n_pop = sum(n_pop)) %>%
  ungroup()
```

Question 5: Incidence rate

Interpretation:

Definition of incidence rate: "for a specific follow-up period, the number of new cases of the outcome divided by the total person-time at risk" (Adina Feldman, Lecture 2). In our case, for each period of one year, the number of new cases of cancer in that year, divided by the total person-time (1 year times population in that year).

In this question, the definition of the incident rate = (total cases /total population) 100. (In the previous plots (total cases/total population) 10^4) Yes, it's a standard way to calculate the incidence rate, but it does't not consider the age distribution since colon cancer risk varies by age.

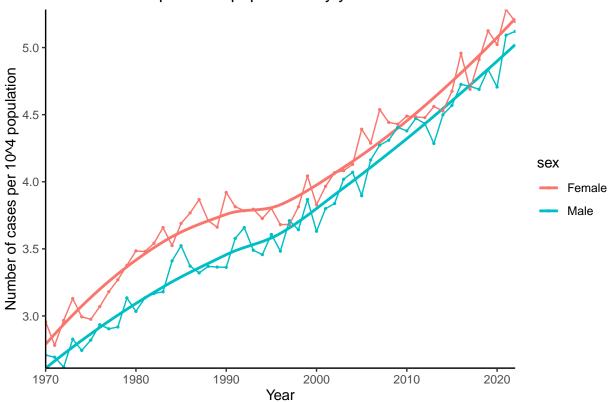
Question 6: Plot the incidence rate of colon cancer over calendar time and apply a smoother, separately by males and females (here you can use the incidence rate based on the total number of cases and the total population size). Describe what you can conclude from the graphs. Create a graph of incidence rates over calendar year by sex and age group, and apply smoothers, what can you conclude

Summarized model

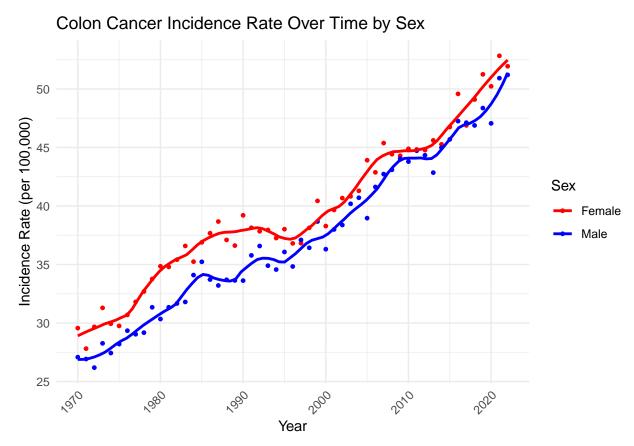
```
cases_pop_ys %>%
  ggplot(aes(x = year, y = rate, color = sex)) +
  # smooth the curve
  geom_smooth(se= FALSE) +
  # non smoothed data
```

```
geom_point(size = 0.5) +
stat_summary(geom="line") +
theme_classic() +
coord_cartesian(expand = FALSE) +
#scale_x_continuous(lim = c(1970, 2022), breaks = c(seq(1970, 2022, by = 4))) +
# add labels and title
ggtitle("Incidence rate per 10^4 population by year and sex") +
xlab("Year") + ylab("Number of cases per 10^4 population")
```

Incidence rate per 10⁴ population by year and sex



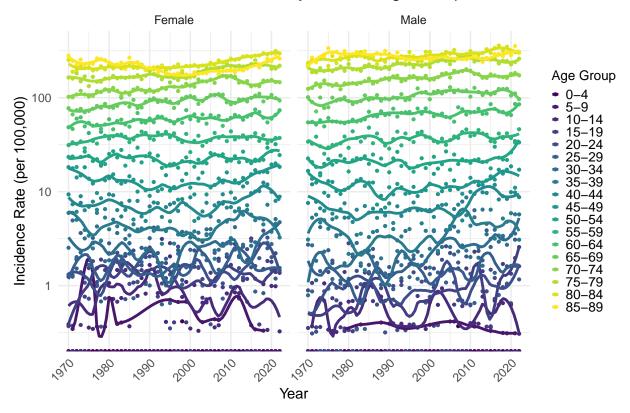
When I normalize by population size, I see that the incidence rate per ten thousand population shows an increasing trend in time, both for females and for males separately.



Yearly count per ten thousand population is lower for males than for females. \backslash

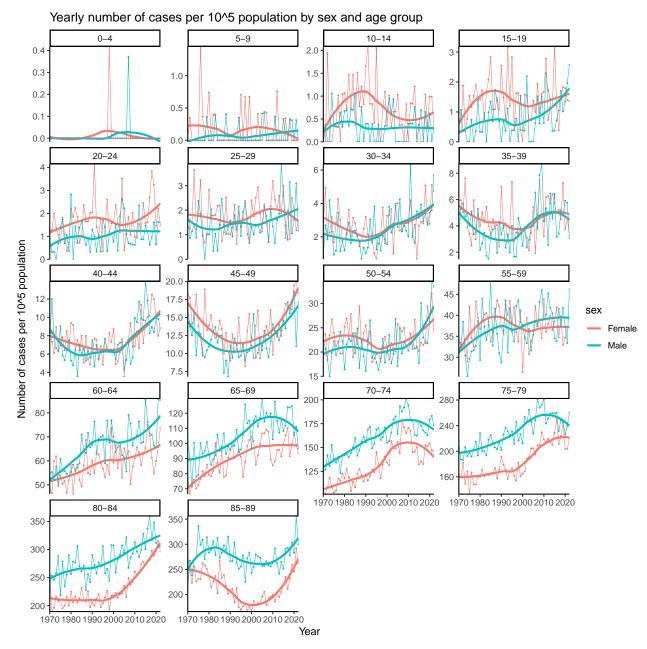
Age

Colon Cancer Incidence Rate by Sex and Age Group Over Time



Facet plot with age groups, y scale free

```
cases_pop %>%
  ggplot(aes(x = year, y = rate, color = sex)) +
  facet_wrap(~ agegroup , ncol = 4, scales = "free_y") +
  # smooth the curve
  geom_smooth(se = FALSE) +
  # non smoothed data
  geom_point(size = 0.2) +
  stat_summary(geom="line", size = 0.05) +
  theme_classic() +
  coord_cartesian(expand = FALSE) +
  #scale_x_continuous(lim = c(1970, 2022), breaks = c(seq(1970, 2022, by = 4))) +
  # add labels and title
  ggtitle(paste("Yearly number of cases per 10^5 population by sex and age group")) +
  xlab("Year") + ylab("Number of cases per 10^5 population")
```



- Comparing different ages, trends for age-specific incidence rates are different for different ages.\
- Comparing females and males, while the crude incidence rate values tend to be higher for females than for males, the age-specific incidence rates have a tendency to be higher for females than for males, when age groups are s.t. age < 55. They tend to be lower for females than for males when age groups are s.t. age => 60 years. \

See different age structures in population for males and females: \https://www.healthknowledge.org.uk/e-learning/epidemiology/specialists/standardisation

The incidence rate of colon cancer has steadily increased over calendar time for both males and females. Females consistently have a higher incidence rate of colon cancer compared to males throughout the period.

Question 7: Poisson model

```
poisson_model <- cases_pop_ys %>%
  glm(formula = n ~ year + sex + offset(log(n_pop)), family = "poisson")
summary(poisson_model)
##
## Call:
## glm(formula = n ~ year + sex + offset(log(n_pop)), family = "poisson",
##
       data = .)
##
## Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -2.969e+01 3.071e-01 -96.68
                                                <2e-16 ***
               1.094e-02 1.536e-04
                                       71.25
                                                <2e-16 ***
## year
## sexMale
               -5.592e-02 4.658e-03 -12.01
                                                <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 5505.07 on 105 degrees of freedom
## Residual deviance: 222.81 on 103 degrees of freedom
## AIC: 1211.4
##
## Number of Fisher Scoring iterations: 3
log(n/n \ pop) = -29.69415 + 0.01094 * year - 0.05592 * \delta_f(sex) with \delta_f(sex = "Female") = 0,
\delta_f(sex = "Male") = 1, since sex = "Male" was taken as a reference by the gml() function.
```

The Poisson model estimates the total number of cases as the dependent variable, using population size as an offset and calendar year and sex as independent variables.

The estimated intercept is -29.69, representing the baseline log-incidence rate when the year is 0 and the reference category for sex (likely Female). The coefficient for the variable year is 0.01094 (p < 0.001), indicating a 1.1% annual increase in the incidence rate ((e^(0.01094) - 1) * 100), holding sex constant. The coefficient for sex (Male) is -0.05592 (p < 0.001), implying a 5.6% lower incidence rate for males compared to females, holding year constant.

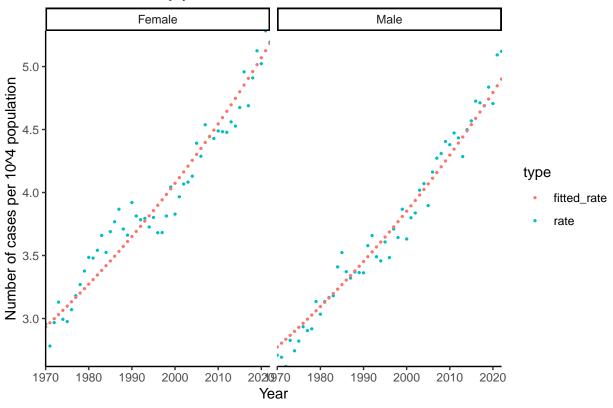
(e^(0.01094) - 1) * 100) in dataset used for the regression, factor 100 is 10^4 instead

```
toplot <- cases_pop_ys %>%
   add_column(fitted = poisson_model$fitted.values) %>%
   mutate(fitted_rate = 10^4* fitted/n_pop)

toplot %>%
   pivot_longer(cols = c(rate, fitted_rate), names_to = "type") %>%
   ggplot(aes(x = year, y = value)) +
   geom_point(aes(color = type), size = 0.5) +
   facet_wrap(~sex, ncol = 2) +
   theme_classic() +
   coord_cartesian(expand = FALSE) +
   #scale_x_continuous(lim = c(1970, 2022), breaks = c(seq(1970, 2022, by = 4))) +
   # add_labels_and_title
```

```
ggtitle("Incidence rate by year and sex, fitted and observed values") +
xlab("Year") + ylab("Number of cases per 10<sup>4</sup> population")
```

Incidence rate by year and sex, fitted and observed values



Question 8:

```
# Extract model coefficients
coefficients <- coef(poisson_model)</pre>
intercept <- coefficients["(Intercept)"]</pre>
year_coeff <- coefficients["year"]</pre>
sex_coeff <- coefficients["sexMale"]</pre>
# Calculate log incidence rate and incidence rate for 1970 and 2020
incidence_1970_male <- exp(intercept + year_coeff * 1970 + sex_coeff)</pre>
incidence_1970_female <- exp(intercept + year_coeff * 1970 )</pre>
incidence_2020_male <- exp(intercept + year_coeff * 2020 + sex_coeff)</pre>
incidence_2020_female <- exp(intercept + year_coeff * 2020)</pre>
# Print results
incidence_1970_male
## (Intercept)
## 0.0002773751
incidence_1970_female
    (Intercept)
## 0.0002933271
```

```
incidence_2020_male

## (Intercept)
## 0.0004794199
incidence_2020_female

## (Intercept)
## 0.0005069918
```

Based on the model output, the estimated incidence rates in 1970 are 0.0002933 for females and 0.0002774 for males. In 2020, the incidence rates are 0.0005070 for females and 0.0004794 for males.

3. Assumptions made regarding how the incidence rate changes over calendar years and difference between males and females

- Rates for males and females have the same time dependence, and differ just by a constant term (multiplicative).\
- Repeat with mixing year*sex
- The model assumes that the log-incidence rate changes linearly with the calendar year, leading to an annual incidence rate increase of 1.1% ((e^(0.01094) 1) * 100). //10^4 in the dataset used here

The key assumptions made in this model:

- A linear relationship between year and log-incidence rate: $\log() = _0 + _1(year) + _2(sex)$
- A constant difference between males and females: $_2 = -0.0559$, males have 5.5% lower incidence rates than females
- No interactions among year, sex, age group.
- Accurate population size as an offset: the population size is accurately measured and representative of the population at risk for both sexes and years.
- Poisson distribution of the dependent variable: the variance in the number of cases increases with the expected number of cases.
- A constant difference in log() between males and females: $_2 = -0.0559$, males have 5.5% lower incidence rates than females ((mu_males-mu_females)/mu_females = exp(-0.0559)-1 = -0.054)

Question 9

```
## year
                           2.618e-02
                                      4.807e-02
                                                    0.545
                                                            0.5860
## sexMale
                           1.086e+00
                                       1.545e+00
                                                   0.703
                                                            0.4819
## agegroup5-9
                           5.897e+01
                                       9.865e+01
                                                    0.598
                                                            0.5500
                           7.020e+01
                                       9.684e+01
                                                   0.725
                                                            0.4685
## agegroup10-14
## agegroup15-19
                           3.521e+01
                                       9.654e+01
                                                   0.365
                                                            0.7153
## agegroup20-24
                           4.121e+01
                                      9.648e+01
                                                   0.427
                                                            0.6693
## agegroup25-29
                           4.711e+01
                                       9.643e+01
                                                    0.489
                                                            0.6252
## agegroup30-34
                           3.562e+01
                                       9.637e+01
                                                   0.370
                                                            0.7117
   agegroup35-39
                           4.877e+01
                                       9.634e+01
                                                    0.506
                                                            0.6127
   agegroup40-44
                           4.329e+01
                                       9.631e+01
                                                    0.449
                                                            0.6531
## agegroup45-49
                           5.194e+01
                                       9.629e+01
                                                    0.539
                                                            0.5897
## agegroup50-54
                           5.354e+01
                                       9.628e+01
                                                   0.556
                                                            0.5782
## agegroup55-59
                           5.598e+01
                                      9.628e+01
                                                   0.581
                                                            0.5609
                                                    0.517
## agegroup60-64
                           4.976e+01
                                       9.628e+01
                                                            0.6053
                                       9.627e+01
                                                    0.518
## agegroup65-69
                           4.985e+01
                                                            0.6046
## agegroup70-74
                           4.853e+01
                                       9.627e+01
                                                    0.504
                                                            0.6142
                           4.823e+01
                                       9.627e+01
                                                   0.501
  agegroup75-79
                                                            0.6164
  agegroup80-84
                           4.867e+01
                                       9.627e+01
                                                    0.505
                                                            0.6132
## agegroup85-89
                           6.130e+01
                                      9.627e+01
                                                   0.637
                                                            0.5243
## year:sexMale
                          -5.696e-04
                                      3.104e-04
                                                  -1.835
                                                            0.0665
## year:agegroup5-9
                          -2.792e-02
                                      4.927e-02
                                                  -0.567
                                                            0.5710
## year:agegroup10-14
                          -3.283e-02
                                      4.836e-02
                                                  -0.679
                                                            0.4972
## year:agegroup15-19
                          -1.496e-02
                                       4.821e-02
                                                  -0.310
                                                            0.7563
   year:agegroup20-24
                          -1.788e-02
                                       4.818e-02
                                                  -0.371
                                                            0.7106
## year:agegroup25-29
                                                            0.6658
                          -2.080e-02
                                       4.815e-02
                                                  -0.432
## year:agegroup30-34
                          -1.484e-02
                                      4.812e-02
                                                  -0.308
                                                            0.7578
                                                  -0.440
                                                            0.6599
## year:agegroup35-39
                          -2.117e-02
                                       4.811e-02
## year:agegroup40-44
                          -1.816e-02
                                      4.809e-02
                                                  -0.378
                                                            0.7056
## year:agegroup45-49
                          -2.220e-02
                                      4.808e-02
                                                  -0.462
                                                            0.6443
## year:agegroup50-54
                          -2.274e-02
                                       4.808e-02
                                                  -0.473
                                                            0.6362
  year:agegroup55-59
                          -2.372e-02
                                       4.808e-02
                                                  -0.493
                                                            0.6217
  year:agegroup60-64
                          -2.037e-02
                                       4.807e-02
                                                  -0.424
                                                            0.6717
## year:agegroup65-69
                          -2.020e-02
                                       4.807e-02
                                                  -0.420
                                                            0.6743
## year:agegroup70-74
                          -1.935e-02
                                       4.807e-02
                                                  -0.403
                                                            0.6873
                                                  -0.396
## year:agegroup75-79
                          -1.904e-02
                                       4.807e-02
                                                            0.6921
## year:agegroup80-84
                          -1.914e-02
                                      4.807e-02
                                                  -0.398
                                                            0.6905
## year:agegroup85-89
                          -2.552e-02
                                       4.807e-02
                                                  -0.531
                                                            0.5956
## sexMale:agegroup5-9
                          -7.823e-01
                                       1.460e+00
                                                  -0.536
                                                            0.5921
## sexMale:agegroup10-14 -6.568e-01
                                                  -0.461
                                                            0.6447
                                       1.424e+00
## sexMale:agegroup15-19 -4.856e-01
                                       1.419e+00
                                                  -0.342
                                                            0.7322
## sexMale:agegroup20-24 -4.125e-01
                                       1.418e+00
                                                  -0.291
                                                            0.7711
## sexMale:agegroup25-29 -1.100e-01
                                                  -0.078
                                                            0.9381
                                       1.417e+00
                                                  -0.025
## sexMale:agegroup30-34 -3.506e-02
                                       1.416e+00
                                                            0.9802
## sexMale:agegroup35-39 -7.101e-02
                                                  -0.050
                                       1.415e+00
                                                            0.9600
## sexMale:agegroup40-44
                          1.914e-02
                                       1.415e+00
                                                   0.014
                                                            0.9892
                                                  -0.042
## sexMale:agegroup45-49 -5.963e-02
                                       1.415e+00
                                                            0.9664
## sexMale:agegroup50-54 -4.559e-04
                                       1.414e+00
                                                   0.000
                                                            0.9997
## sexMale:agegroup55-59
                           4.903e-02
                                       1.414e+00
                                                    0.035
                                                            0.9723
                                                   0.118
## sexMale:agegroup60-64
                           1.673e-01
                                       1.414e+00
                                                            0.9058
## sexMale:agegroup65-69
                           1.981e-01
                                       1.414e+00
                                                   0.140
                                                            0.8886
## sexMale:agegroup70-74
                           2.426e-01
                                       1.414e+00
                                                   0.172
                                                            0.8638
## sexMale:agegroup75-79
                           2.643e-01
                                       1.414e+00
                                                    0.187
                                                            0.8517
                                                   0.178
## sexMale:agegroup80-84
                           2.516e-01
                                       1.414e+00
                                                            0.8588
## sexMale:agegroup85-89
                           3.263e-01
                                      1.414e+00
                                                   0.231
                                                            0.8175
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for poisson family taken to be 1)
##
       Null deviance: 406971.1 on 1907 degrees of freedom
## Residual deviance:
                        2749.5 on 1853 degrees of freedom
## AIC: 11967
## Number of Fisher Scoring iterations: 6
# Extract model coefficients
coefficients <- coef(poisson_model_age)</pre>
# males
rate_1970_male <- exp(</pre>
  #intercept
  coefficients["(Intercept)"] +
  #year
  coefficients["year"] * 1970 +
  #male
  coefficients["sexMale"] * 1 +
  #age 70-74
  coefficients["agegroup70-74"] * 1 +
  # year*sex
  coefficients["year:sexMale"] * 1970 * 1 +
  # year*age 70-74
  coefficients["year:agegroup70-74"] * 1970 * 1 +
  # sex*age 70-74
  coefficients["sexMale:agegroup70-74"] * 1 * 1)
rate_1970_female <- exp(</pre>
  #intercept
  coefficients["(Intercept)"] +
  #year
  coefficients["year"] * 1970 +
  #female
  coefficients["sexMale"] * 0 +
  #age 70-74
  coefficients["agegroup70-74"] * 1 +
  # year*sex
  coefficients["year:sexMale"] * 1970 * 0 +
  # year*age 70-74
  coefficients["year:agegroup70-74"] * 1970 * 1 +
  # sex*age 70-74
  coefficients["sexMale:agegroup70-74"] * 0 * 1)
rate_2020_male <- exp(</pre>
  #intercept
  coefficients["(Intercept)"] +
  #year
  coefficients["year"] * 2020 +
  coefficients["sexMale"] * 1 +
```

```
#age 70-74
  coefficients["agegroup70-74"] * 1 +
  # year*sex
  coefficients["year:sexMale"] * 2020 * 1 +
  # year*age 70-74
  coefficients["year:agegroup70-74"] * 2020 * 1 +
  # sex*age 70-74
  coefficients["sexMale:agegroup70-74"] * 1 * 1)
rate 2020 female <- exp(
  #intercept
  coefficients["(Intercept)"] +
  #year
  coefficients["year"] * 2020 +
  #female
  coefficients["sexMale"] * 0 +
  #age 70-74
  coefficients["agegroup70-74"] * 1 +
  # year*sex
  coefficients["year:sexMale"] * 2020 * 0 +
  # year*age 70-74
  coefficients["year:agegroup70-74"] * 2020 * 1 +
  # sex*age 70-74
  coefficients["sexMale:agegroup70-74"] * 0 * 1)
rate_1970_male
## (Intercept)
## 0.001349865
rate_1970_female
## (Intercept)
## 0.001097564
rate_2020_male
## (Intercept)
## 0.001845669
rate_2020_female
## (Intercept)
## 0.001544049
```

Colon cancer is more common in older age groups, and the age distribution has shifted over time. To better estimate incidence rates, we refit the Poisson model by including interaction terms: "year * sex," "year * age group," and "sex * age group."

Based on the updated model output, the estimated incidence rates in 1970 for the 70-74 age group are 0.001350 for males and 0.001098 for females. In 2020, the incidence rates for the same age group are 0.001846 for males and 0.001544 for females.

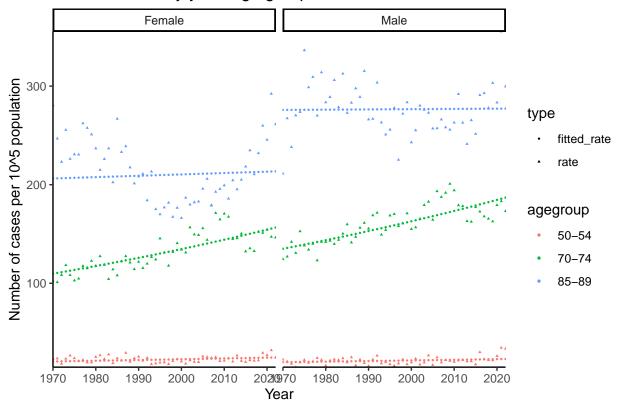
• For 70-74 age group, the estimated incidence rates for females are lower than the estimated incidence rates for males

Plot of the fit

```
toplot <- cases_pop %>%
  add_column(fitted = poisson_model_age$fitted.values) %>%
  mutate(fitted_rate = 10^5* fitted/n_pop)

toplot %>%
  pivot_longer(cols = c(rate, fitted_rate), names_to = "type") %>%
  filter(agegroup %in% c("50-54", "70-74", "85-89")) %>%
  ggplot(aes(x = year, y = value, color = agegroup)) +
  geom_point(aes(shape = type), size = 0.5) +
  facet_wrap(-sex, ncol = 2) +
  theme_classic() +
  coord_cartesian(expand = FALSE) +
  #scale_x_continuous(lim = c(1970, 2022), breaks = c(seq(1970, 2022, by = 4))) +
  # add labels and title
  ggtitle("Incidence rate by year, age group and sex, fitted and observed values") +
  xlab("Year") + ylab("Number of cases per 10^5 population")
```

Incidence rate by year, age group and sex, fitted and observed values



Question 10: splines

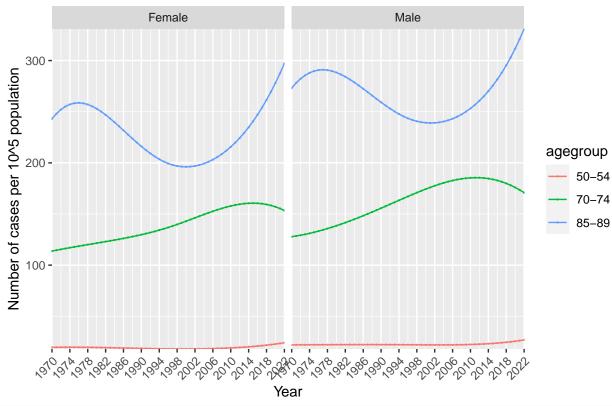
A model with splines on year and age, with 4 degrees of freedom is fitted.

```
age <- seq(2,87,5)
age_df <- data.frame(agegroup = factor_groups, age = age)
splines_to_fit <- cases_pop %>%
```

```
inner_join(age_df)
splines_model <- splines_to_fit %>%
  glm(formula = n \sim bs(year, df = 4)*sex + bs(year, df = 4)*bs(age, df = 4) + offset(log(n_pop)), family
summary(splines_model)
##
## Call:
## glm(formula = n \sim bs(year, df = 4) * sex + bs(year, df = 4) *
       bs(age, df = 4) + offset(log(n_pop)), family = "poisson",
##
       data = .)
##
## Coefficients:
##
                                        Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                     -15.738712
                                                   0.671231 -23.448 < 2e-16 ***
## bs(year, df = 4)1
                                        3.694552
                                                   1.208697
                                                              3.057 0.00224 **
## bs(year, df = 4)2
                                        2.068501
                                                  0.851414
                                                              2.429 0.01512 *
## bs(year, df = 4)3
                                                  1.099291
                                                              0.322 0.74734
                                       0.354132
## bs(year, df = 4)4
                                       1.584977
                                                  0.781170
                                                              2.029 0.04246 *
## sexMale
                                       0.116708
                                                   0.024714
                                                              4.722 2.33e-06 ***
## bs(age, df = 4)1
                                       4.101335
                                                   0.834264
                                                              4.916 8.83e-07 ***
                                                              9.995 < 2e-16 ***
## bs(age, df = 4)2
                                       6.246528
                                                  0.624982
## bs(age, df = 4)3
                                       9.368812
                                                  0.691320 13.552 < 2e-16 ***
## bs(age, df = 4)4
                                       9.719233
                                                  0.668235
                                                            14.545 < 2e-16 ***
## bs(year, df = 4)1:sexMale
                                                  0.048833 -0.503 0.61506
                                      -0.024556
## bs(year, df = 4)2:sexMale
                                       0.172448
                                                  0.036831
                                                             4.682 2.84e-06 ***
## bs(year, df = 4)3:sexMale
                                                              0.331 0.74086
                                       0.013093
                                                  0.039589
## bs(year, df = 4)4:sexMale
                                       -0.009055
                                                   0.028459
                                                            -0.318 0.75035
## bs(year, df = 4)1:bs(age, df = 4)1 -4.349044
                                                   1.525640
                                                            -2.851 0.00436 **
## bs(year, df = 4)2:bs(age, df = 4)1 -3.261222
                                                   1.095106
                                                            -2.978 0.00290 **
## bs(year, df = 4)3:bs(age, df = 4)1
                                       1.360035
                                                   1.373562
                                                             0.990 0.32210
                                                            -1.226 0.22034
## bs(year, df = 4)4:bs(age, df = 4)1 -1.193387
                                                  0.973687
## bs(year, df = 4)1:bs(age, df = 4)2 -3.388194
                                                   1.129417
                                                            -3.000 0.00270 **
## bs(year, df = 4)2:bs(age, df = 4)2 -2.509392
                                                   0.798650
                                                            -3.142 0.00168 **
## bs(year, df = 4)3:bs(age, df = 4)2 -1.963695
                                                            -1.917 0.05524 .
                                                   1.024384
## bs(year, df = 4)4:bs(age, df = 4)2 -1.623920
                                                   0.728446
                                                            -2.229 0.02579 *
## bs(year, df = 4)1:bs(age, df = 4)3 -3.733949
                                                   1.246274
                                                            -2.996 0.00273 **
## bs(year, df = 4)2:bs(age, df = 4)3 -1.506318
                                                   0.878186
                                                            -1.715 0.08630 .
## bs(year, df = 4)3:bs(age, df = 4)3
                                       0.788503
                                                   1.130687
                                                             0.697 0.48557
## bs(year, df = 4)4:bs(age, df = 4)3 -1.157147
                                                  0.803596
                                                            -1.440 0.14988
## bs(year, df = 4)1:bs(age, df = 4)4 -3.499444
                                                   1.203637
                                                            -2.907 0.00364 **
## bs(year, df = 4)2:bs(age, df = 4)4 -2.514658
                                                   0.848316
                                                            -2.964 0.00303 **
## bs(year, df = 4)3:bs(age, df = 4)4 -0.450302
                                                   1.095107
                                                            -0.411
                                                                    0.68093
## bs(year, df = 4)4:bs(age, df = 4)4 -1.383982
                                                   0.778095 - 1.779 0.07529.
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 406971.1 on 1907 degrees of freedom
## Residual deviance:
                       3136.5 on 1878 degrees of freedom
## AIC: 12304
##
```

```
## Number of Fisher Scoring iterations: 6
toplot <- splines_to_fit %>%
  add_column(fitted = splines_model$fitted.values) %>%
  mutate(fitted_rate = 10^5* fitted/n_pop)
toplot %>%
  filter(age %in% c(52,72,87)) %>%
  ggplot(aes(x = year, y = fitted_rate, color = agegroup)) +
  facet_wrap(~sex, ncol = 2) +
  geom_point(size = 0.1) +
  stat_summary(geom="line") +
  theme(axis.text.x = element_text(angle=45, hjust=1)) +
  coord_cartesian(expand = FALSE) +
  scale_x_continuous(lim = c(1970, 2022), breaks = c(seq(1970, 2022, by = 4))) +
  \# add labels and title
  ggtitle("Incidence rate by year, age and sex, fitted model") +
  xlab("Year") + ylab("Number of cases per 10^5 population")
```

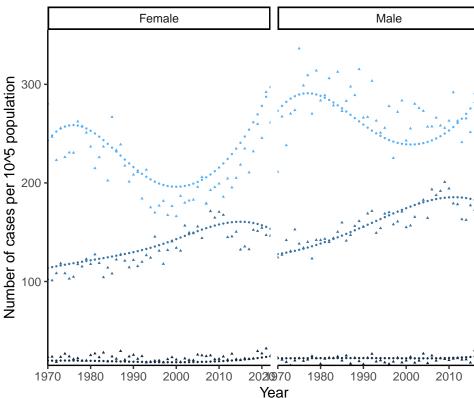
Incidence rate by year, age and sex, fitted model



```
toplot %>%
  pivot_longer(cols = c(rate, fitted_rate), names_to = "type") %>%
  filter(age %in% c(52,72,87)) %>%
  ggplot(aes(x = year, y = value, color = age)) +
  geom_point(aes(shape = type), size = 0.5) +
  facet_wrap(~sex, ncol = 2) +
  theme_classic() +
  coord_cartesian(expand = FALSE) +
```

```
#scale_x_continuous(lim = c(1970, 2022), breaks = c(seq(1970, 2022, by = 4))) +
# add labels and title
ggtitle("Incidence rate by year, age and sex, fitted and observed values") +
xlab("Year") + ylab("Number of cases per 10^5 population")
```

Incidence rate by year, age and sex, fitted and observed

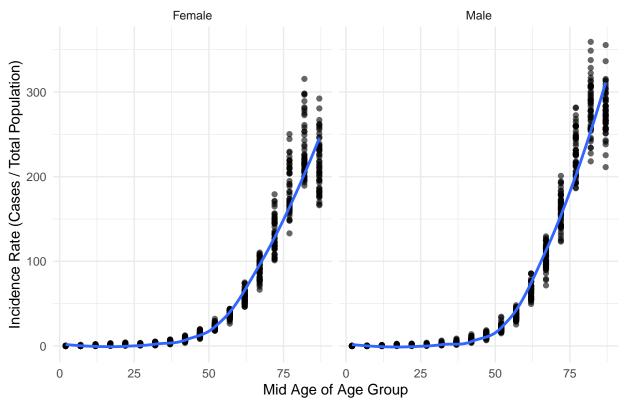


observed-fitted-1.pdf observed-fitted-1.bb

Question 10

```
# Merge cases and population data frames
merged_data <- merge(cases, population, by = c("agegroup", "sex", "year"))</pre>
print(head(merged_data, n=5))
##
     agegroup
                 sex year n n_pop
## 1
          0-4 Female 1970 0 280468
## 2
          0-4 Female 1971 0 275596
          0-4 Female 1972 0 270765
          0-4 Female 1973 0 267532
## 4
          0-4 Female 1974 0 269260
merged_data <- merged_data %>%
 mutate(
    incidence_rate = (n / n_pop) * 100000,
    age_midpoint = as.numeric(sub("-.*", "", agegroup)) + 2,
    sex = factor(sex)
      )
# Print column names to verify
```

Incidence Rate by Age



```
# Fitting a generalized linear model using splines
splines_model <- glm(
  formula = n ~ bs(year, df = 4)*bs(age_midpoint, df = 4) * sex + offset(log(n_pop)),
  data = merged_data,
  family = poisson()
)
summary(splines_model)</pre>
```

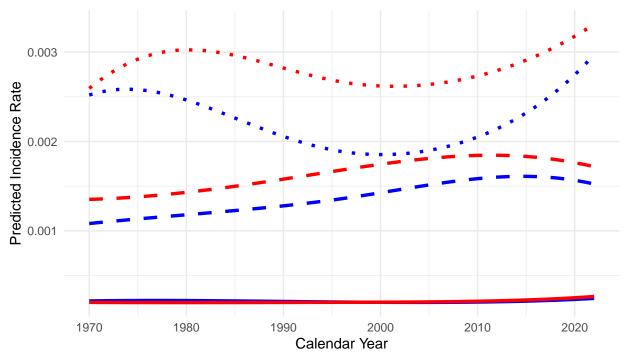
```
##
## Call:
## glm(formula = n ~ bs(year, df = 4) * bs(age_midpoint, df = 4) *
## sex + offset(log(n_pop)), family = poisson(), data = merged_data)
```

```
## Coefficients:
                                                          Estimate Std. Error
##
## (Intercept)
                                                                      0.748865
                                                        -14.569275
## bs(year, df = 4)1
                                                           2.501508
                                                                      1.390446
## bs(year, df = 4)2
                                                          2.037596
                                                                      1.019856
## bs(year, df = 4)3
                                                          -0.494946
                                                                      1.326696
## bs(year, df = 4)4
                                                          0.284297
                                                                      0.956309
## bs(age_midpoint, df = 4)1
                                                          2.803894
                                                                      0.959586
## bs(age_midpoint, df = 4)2
                                                          5.501598
                                                                      0.698437
## bs(age_midpoint, df = 4)3
                                                          7.992804
                                                                      0.775120
## bs(age_midpoint, df = 4)4
                                                          8.585834
                                                                      0.745947
## sexMale
                                                         -3.346662
                                                                      1.545262
## bs(year, df = 4)1:bs(age_midpoint, df = 4)1
                                                         -2.558816
                                                                      1.807307
## bs(year, df = 4)2:bs(age_midpoint, df = 4)1
                                                         -2.906208
                                                                      1.344734
## bs(year, df = 4)3:bs(age_midpoint, df = 4)1
                                                           2.492452
                                                                      1.692620
## bs(year, df = 4)4:bs(age_midpoint, df = 4)1
                                                          0.560981
                                                                      1.213426
## bs(year, df = 4)1:bs(age_midpoint, df = 4)2
                                                         -2.409901
                                                                      1.302262
## bs(year, df = 4)2:bs(age_midpoint, df = 4)2
                                                         -2.599417
                                                                      0.959793
## bs(year, df = 4)3:bs(age_midpoint, df = 4)2
                                                         -1.518627
                                                                      1.236974
## bs(year, df = 4)4:bs(age_midpoint, df = 4)2
                                                         -0.820693
                                                                      0.892561
## bs(year, df = 4)1:bs(age_midpoint, df = 4)3
                                                         -2.427657
                                                                      1.440452
## bs(year, df = 4)2:bs(age_midpoint, df = 4)3
                                                         -1.326466
                                                                      1.055886
## bs(year, df = 4)3:bs(age_midpoint, df = 4)3
                                                           1.882810
                                                                      1.368446
## bs(year, df = 4)4:bs(age_midpoint, df = 4)3
                                                          0.350943
                                                                      0.985957
## bs(year, df = 4)1:bs(age_midpoint, df = 4)4
                                                          -2.382935
                                                                      1.385469
## bs(year, df = 4)2:bs(age_midpoint, df = 4)4
                                                          -2.578386
                                                                      1.016811
## bs(year, df = 4)3:bs(age_midpoint, df = 4)4
                                                          0.301665
                                                                      1.322407
## bs(year, df = 4)4:bs(age_midpoint, df = 4)4
                                                          -0.119462
                                                                      0.953222
## bs(year, df = 4)1:sexMale
                                                          3.875116
                                                                      2.704734
## bs(year, df = 4)2:sexMale
                                                          0.421600
                                                                      1.861218
## bs(year, df = 4)3:sexMale
                                                          3.127299
                                                                      2.382851
## bs(year, df = 4)4:sexMale
                                                          3.666262
                                                                      1.731212
## bs(age_midpoint, df = 4)1:sexMale
                                                          3.933159
                                                                      1.879343
## bs(age_midpoint, df = 4)2:sexMale
                                                          2.504288
                                                                      1.444037
## bs(age_midpoint, df = 4)3:sexMale
                                                          3.918359
                                                                      1.586555
## bs(age midpoint, df = 4)4:sexMale
                                                          3.375753
                                                                      1.538658
## bs(year, df = 4)1:bs(age_midpoint, df = 4)1:sexMale
                                                         -5.465763
                                                                      3.346095
## bs(year, df = 4)2:bs(age_midpoint, df = 4)1:sexMale
                                                         -1.040530
                                                                      2.353886
## bs(year, df = 4)3:bs(age_midpoint, df = 4)1:sexMale
                                                          -3.969268
                                                                      2.936333
## bs(year, df = 4)4:bs(age_midpoint, df = 4)1:sexMale
                                                         -4.775214
                                                                      2.122510
## bs(year, df = 4)1:bs(age_midpoint, df = 4)2:sexMale
                                                         -3.315179
                                                                      2.533808
## bs(year, df = 4)2:bs(age_midpoint, df = 4)2:sexMale
                                                          0.186232
                                                                      1.747198
## bs(year, df = 4)3:bs(age_midpoint, df = 4)2:sexMale
                                                         -2.131003
                                                                      2.225754
## bs(year, df = 4)4:bs(age_midpoint, df = 4)2:sexMale
                                                         -2.572030
                                                                      1.618188
## bs(year, df = 4)1:bs(age_midpoint, df = 4)3:sexMale
                                                         -4.184404
                                                                      2.781225
## bs(year, df = 4)2:bs(age_midpoint, df = 4)3:sexMale
                                                         -0.638061
                                                                      1.915849
## bs(year, df = 4)3:bs(age_midpoint, df = 4)3:sexMale
                                                         -3.674431
                                                                      2.446820
## bs(year, df = 4)4:bs(age_midpoint, df = 4)3:sexMale
                                                         -4.133885
                                                                      1.777236
## bs(year, df = 4)1:bs(age_midpoint, df = 4)4:sexMale
                                                         -3.700081
                                                                      2.693826
## bs(year, df = 4)2:bs(age_midpoint, df = 4)4:sexMale
                                                         -0.001042
                                                                      1.854556
## bs(year, df = 4)3:bs(age midpoint, df = 4)4:sexMale
                                                         -2.878592
                                                                      2.373886
## bs(year, df = 4)4:bs(age_midpoint, df = 4)4:sexMale -3.586707
                                                                      1.724491
##
                                                        z value Pr(>|z|)
```

```
## (Intercept)
                                                       -19.455 < 2e-16 ***
## bs(year, df = 4)1
                                                         1.799
                                                                0.07201 .
## bs(year, df = 4)2
                                                         1.998
                                                                0.04572 *
## bs(year, df = 4)3
                                                        -0.373
                                                                0.70910
## bs(year, df = 4)4
                                                         0.297
                                                                0.76625
## bs(age midpoint, df = 4)1
                                                        2.922 0.00348 **
## bs(age_midpoint, df = 4)2
                                                        7.877 3.35e-15 ***
## bs(age_midpoint, df = 4)3
                                                        10.312 < 2e-16 ***
## bs(age_midpoint, df = 4)4
                                                        11.510
                                                                < 2e-16 ***
## sexMale
                                                        -2.166
                                                                0.03033 *
## bs(year, df = 4)1:bs(age_midpoint, df = 4)1
                                                        -1.416
                                                                0.15683
## bs(year, df = 4)2:bs(age_midpoint, df = 4)1
                                                        -2.161
                                                                0.03068 *
## bs(year, df = 4)3:bs(age_midpoint, df = 4)1
                                                        1.473
                                                                0.14087
                                                        0.462
## bs(year, df = 4)4:bs(age_midpoint, df = 4)1
                                                                0.64386
## bs(year, df = 4)1:bs(age_midpoint, df = 4)2
                                                       -1.851
                                                                0.06423
## bs(year, df = 4)2:bs(age_midpoint, df = 4)2
                                                        -2.708
                                                                0.00676 **
## bs(year, df = 4)3:bs(age_midpoint, df = 4)2
                                                       -1.228
                                                                0.21956
## bs(year, df = 4)4:bs(age midpoint, df = 4)2
                                                       -0.919
                                                                0.35784
## bs(year, df = 4)1:bs(age_midpoint, df = 4)3
                                                       -1.685
                                                                0.09192
## bs(year, df = 4)2:bs(age_midpoint, df = 4)3
                                                       -1.256
                                                                0.20902
## bs(year, df = 4)3:bs(age_midpoint, df = 4)3
                                                        1.376
                                                                0.16886
## bs(year, df = 4)4:bs(age_midpoint, df = 4)3
                                                        0.356
                                                                0.72188
## bs(year, df = 4)1:bs(age_midpoint, df = 4)4
                                                       -1.720
                                                                0.08544
## bs(year, df = 4)2:bs(age_midpoint, df = 4)4
                                                       -2.536
                                                                0.01122 *
## bs(year, df = 4)3:bs(age_midpoint, df = 4)4
                                                        0.228
                                                                0.81955
## bs(year, df = 4)4:bs(age_midpoint, df = 4)4
                                                        -0.125
                                                                0.90027
## bs(year, df = 4)1:sexMale
                                                         1.433
                                                                0.15194
## bs(year, df = 4)2:sexMale
                                                         0.227
                                                                0.82080
## bs(year, df = 4)3:sexMale
                                                         1.312
                                                                0.18938
## bs(year, df = 4)4:sexMale
                                                         2.118
                                                                0.03420 *
## bs(age_midpoint, df = 4)1:sexMale
                                                         2.093
                                                                0.03636 *
## bs(age_midpoint, df = 4)2:sexMale
                                                         1.734
                                                                0.08288
## bs(age_midpoint, df = 4)3:sexMale
                                                         2.470
                                                                0.01352 *
## bs(age_midpoint, df = 4)4:sexMale
                                                         2.194
                                                                0.02824 *
## bs(year, df = 4)1:bs(age_midpoint, df = 4)1:sexMale -1.633
                                                                0.10237
## bs(year, df = 4)2:bs(age_midpoint, df = 4)1:sexMale -0.442
                                                                0.65845
## bs(year, df = 4)3:bs(age_midpoint, df = 4)1:sexMale -1.352
## bs(year, df = 4)4:bs(age_midpoint, df = 4)1:sexMale -2.250
                                                                0.02446 *
## bs(year, df = 4)1:bs(age_midpoint, df = 4)2:sexMale -1.308
                                                                0.19075
## bs(year, df = 4)2:bs(age_midpoint, df = 4)2:sexMale
                                                        0.107
                                                                0.91511
## bs(year, df = 4)3:bs(age_midpoint, df = 4)2:sexMale -0.957
## bs(year, df = 4)4:bs(age_midpoint, df = 4)2:sexMale -1.589
                                                                0.11196
## bs(year, df = 4)1:bs(age_midpoint, df = 4)3:sexMale -1.505
                                                                0.13245
## bs(year, df = 4)2:bs(age_midpoint, df = 4)3:sexMale -0.333
                                                                0.73910
## bs(year, df = 4)3:bs(age_midpoint, df = 4)3:sexMale -1.502
                                                                0.13317
## bs(year, df = 4)4:bs(age_midpoint, df = 4)3:sexMale -2.326
                                                                0.02002 *
## bs(year, df = 4)1:bs(age_midpoint, df = 4)4:sexMale -1.374
                                                                0.16958
## bs(year, df = 4)2:bs(age_midpoint, df = 4)4:sexMale -0.001
                                                                0.99955
## bs(year, df = 4)3:bs(age_midpoint, df = 4)4:sexMale -1.213
                                                                0.22528
## bs(year, df = 4)4:bs(age_midpoint, df = 4)4:sexMale -2.080
                                                                0.03754 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
```

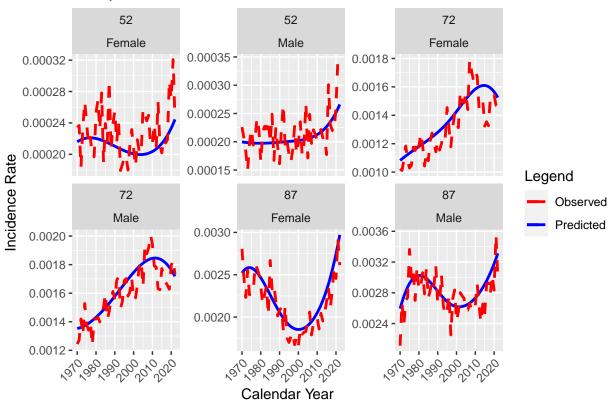
```
##
##
       Null deviance: 406971.1 on 1907 degrees of freedom
## Residual deviance:
                        2572.3 on 1858 degrees of freedom
## AIC: 11780
## Number of Fisher Scoring iterations: 6
# Assuming you have your merged data as 'merged_data' and fitted model as 'model'
# Create a new data frame for predictions
age groups \leftarrow c(52, 72, 87)
sex_groups <- c("Female", "Male")</pre>
years <- unique(merged_data$year) # Get all unique years from your data
# Create an empty data frame to store predictions
prediction data <- expand.grid(</pre>
 year = years,
 age_midpoint = age_groups,
 sex = sex_groups
# Add population to avoid warnings (use dummy values as predictions will standardize population)
prediction_data$n_pop <- 1</pre>
# Use the predict() function to generate predicted values
prediction_data$predicted_incidence <- predict(splines_model, newdata = prediction_data, type = "respon</pre>
# Plotting the incidence rates over time for each sex at ages 52, 72, and 87
library(ggplot2)
ggplot(prediction_data, aes(x = year, y = predicted_incidence, color = sex, linetype = as.factor(age_mi-
 geom_line(size = 1.2) +
 labs(title = "Predicted Incidence Rates Across Calendar Time",
       x = "Calendar Year",
       y = "Predicted Incidence Rate") +
  scale_color_manual(values = c("blue", "red")) +
  scale_linetype_manual(values = c("solid", "dashed", "dotted")) +
  theme_minimal() +
  theme(legend.title = element_blank()) +
  theme(legend.position = "bottom")
```

Predicted Incidence Rates Across Calendar Time



```
Female — Male
                                                      52 - 72 - 87
# Compare with observed values
observed_data <- merged_data %>%
  filter(age_midpoint %in% c(52, 72, 87)) %>%
  group_by(year, age_midpoint, sex) %>%
  summarize(observed_rate = sum(n) / sum(n_pop))
# Combine predicted and observed data
comparison_data <- left_join(prediction_data, observed_data, by = c("year", "age_midpoint", "sex"))</pre>
ggplot(comparison_data, aes(x = year)) +
  geom_line(aes(y = predicted_incidence, color = "Predicted"), size = 1) +
  geom_line(aes(y = observed_rate, color = "Observed"), size = 1, linetype = "dashed") +
  facet_wrap(~ age_midpoint + sex, scales = "free_y") +
 labs(
   title = "Comparison of Predicted and Observed Incidence Rates",
   x = "Calendar Year",
   y = "Incidence Rate",
   color = "Legend"
  scale_color_manual(values = c("Predicted" = "blue", "Observed" = "red")) +
  theme(axis.text.x = element_text(angle=45, hjust=1))
```

Comparison of Predicted and Observed Incidence Rates



Question 11: direct age standardised rate

```
# reference values for male and female population
standard_pop <- population %>%
    filter(year == 2022) %>%
    rename(ref_pop = n_pop) %>%
    select(-year)

# reference value for total male population
tot_male <- standard_pop %>%
    filter(sex == "Male") %>%
    pull(ref_pop) %>% sum()

# reference value for total female population
tot_female <- standard_pop %>%
    filter(sex == "Female") %>%
    pull(ref_pop) %>% sum()
```

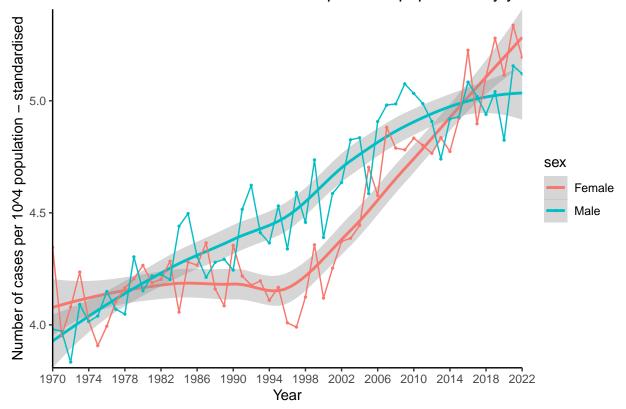
Standardised incidence rates:

```
age_standardised_rates <- cases_pop %>%
select(-rate) %>%
left_join(standard_pop) %>%
# add number of cases obtained if population number was ref_pop
mutate(cases_ref_pop = ref_pop * n/n_pop) %>%
```

Plot of age standardised rates

```
age_standardised_rates %>%
    ggplot(aes(x = year, y = standardised_rate, color = sex)) +
# smooth the curve
geom_smooth() +
# non smoothed data
geom_point(size = 0.5) +
stat_summary(geom="line") +
theme_classic() +
coord_cartesian(expand = FALSE) +
scale_x_continuous(lim = c(1970, 2022), breaks = c(seq(1970, 2022, by = 4))) +
# add labels and title
ggtitle("Standardised incidence rate: cases per 10^4 population by year and sex") +
xlab("Year") + ylab("Number of cases per 10^4 population - standardised")
```

Standardised incidence rate: cases per 10⁴ population by year and sex

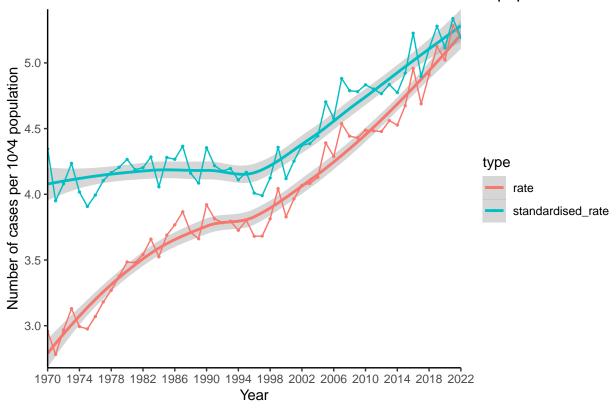


Comparison with non standardised rates

Females:

```
cases_pop_ys %>%
  filter(sex == "Female") %>%
 left_join(age_standardised_rates) %>%
  select(year, sex, rate, standardised_rate) %>%
  pivot_longer(cols = c(rate, standardised_rate), names_to = "type") %>%
  ggplot(aes(x = year, y = value, color = type))+
  # smooth the curve
  geom_smooth() +
  # non smoothed data
  geom_point(size = 0.5) +
  stat_summary(geom="line") +
  theme_classic() +
  coord cartesian(expand = FALSE) +
  scale_x_continuous(lim = c(1970, 2022), breaks = c(seq(1970, 2022, by = 4))) +
  # add labels and title
  ggtitle("Standardised vs non standarsised incidence rate - female population") +
  xlab("Year") + ylab("Number of cases per 10<sup>4</sup> population")
```

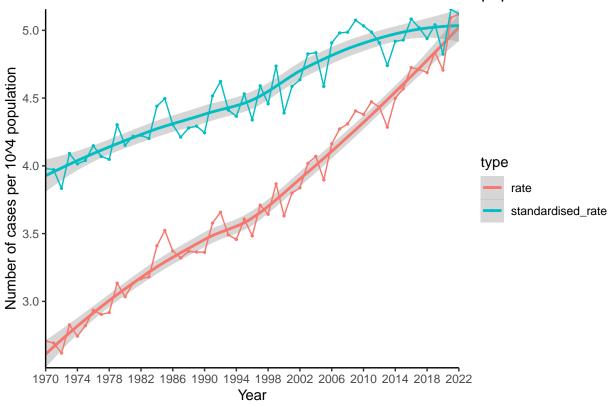
Standardised vs non standarsised incidence rate – female population



Males

```
cases_pop_ys %>%
 filter(sex == "Male") %>%
 left_join(age_standardised_rates) %>%
  select(year, sex, rate, standardised_rate) %>%
  pivot_longer(cols = c(rate, standardised_rate), names_to = "type") %>%
  ggplot(aes(x = year, y = value, color = type))+
  # smooth the curve
  geom_smooth() +
  # non smoothed data
  geom_point(size = 0.5) +
  stat_summary(geom="line") +
  theme_classic() +
  coord_cartesian(expand = FALSE) +
  scale_x_continuous(lim = c(1970, 2022), breaks = c(seq(1970, 2022, by = 4))) +
  # add labels and title
  ggtitle("Standardised vs non standarsised incidence rate - male population") +
  xlab("Year") + ylab("Number of cases per 10<sup>4</sup> population")
```

Standardised vs non standarsised incidence rate – male population



Question 12: direct age standardised rate on predicted data

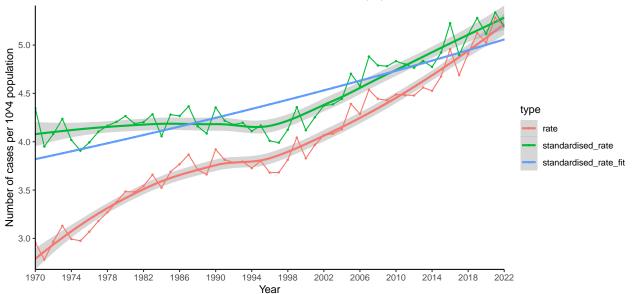
```
cases_pop_fit <- cases_pop %>%
  select(-rate, -n) %>%
  # replace number of cases with fitted number of cases, which should already be in the right order
  add column(n fit = poisson model age$fitted.values)
# repeat question 11
age_standardised_rates_fit <- cases_pop_fit %>%
 left_join(standard_pop) %>%
  # add number of cases obtained if population number was ref pop
  mutate(cases_ref_pop = ref_pop * n_fit/n_pop) %>%
  # for each year, compute total (sum over agegroups) and divide by total reference population
  # keep male and female categories
  group_by(year, sex) %>%
  # sum over agegroups
  summarize(sum_ages = sum(cases_ref_pop, na.rm = TRUE)) %>%
  ungroup() %>%
  mutate(standardised_rate_fit = case_when(sex == "Female" ~ sum_ages/tot_female,
                                       sex == "Male" ~ sum_ages/tot_male,
                                       TRUE ~ NA)
         ) %>%
  select(-sum_ages) %>%
  # rescale
  mutate(standardised_rate_fit = 10^4 * standardised_rate_fit)
```

Comparison of standardised rates obtained with fitted data, with standardised rates from the original dataset.

Females:

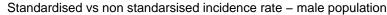
```
cases_pop_ys %>%
  filter(sex == "Female") %>%
  left_join(age_standardised_rates) %>%
  left_join(age_standardised_rates_fit) %>%
  select(year, sex, rate, standardised_rate, standardised_rate_fit) %>%
  pivot_longer(cols = c(rate, standardised_rate, standardised_rate_fit), names_to = "type") %>%
  #filter(type == "standardised_rate_fit") %>%
  ggplot(aes(x = year, y = value, color = type))+
  # smooth the curve
  geom smooth() +
  # non smoothed data
  geom_point(size = 0.5) +
  stat_summary(geom="line") +
  theme classic() +
  coord_cartesian(expand = FALSE) +
  scale_x_continuous(lim = c(1970, 2022), breaks = c(seq(1970, 2022, by = 4))) +
  # add labels and title
  ggtitle("Standardised vs non standarsised incidence rate - female population") +
  xlab("Year") + ylab("Number of cases per 10<sup>4</sup> population")
```

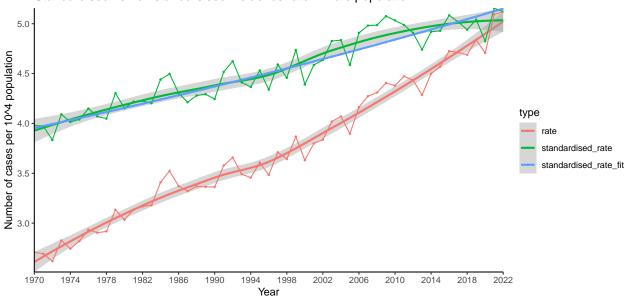
Standardised vs non standarsised incidence rate - female population



```
cases_pop_ys %>%
  filter(sex == "Male") %>%
  left_join(age_standardised_rates) %>%
  left_join(age_standardised_rates_fit) %>%
  select(year, sex, rate, standardised_rate, standardised_rate_fit) %>%
  pivot_longer(cols = c(rate, standardised_rate, standardised_rate_fit), names_to = "type") %>%
  ggplot(aes(x = year, y = value, color = type))+
  # smooth the curve
  geom_smooth() +
  # non smoothed data
```

```
geom_point(size = 0.5) +
stat_summary(geom="line") +
theme_classic() +
coord_cartesian(expand = FALSE) +
scale_x_continuous(lim = c(1970, 2022), breaks = c(seq(1970, 2022, by = 4))) +
# add labels and title
ggtitle("Standardised vs non standarsised incidence rate - male population") +
xlab("Year") + ylab("Number of cases per 10^4 population")
```





Rephrase:

Both for females and for males, compared to the original rates, the curve for the standardised rates has a greater value of the intercept and a smaller slope: standardized rates are higher than the original rates, and the maximum difference between the curves occurs the more distant in time from the current year. The difference between the curves decreases in time.

This can be explained by the aging of the population: the proportion of swedish population aged 75 or more increases in time (see plot with age proportions), and it's the highest in 2022, the reference year. This implies that when computing the standardised rate in year y, that year's rates for older population, which are in general the highest among the age groups, are weighted more.

 $standardised\ rate(y,sex) = \sum_{agegroups} rate(y,agegroup,sex) \cdot population\ proportion(2022,agegroup,sex)$

Question 13: conclusions

Incidence rates of colon cancer vary significantly across age groups, with older age groups generally having higher incidence rates as seen in the plot "Colon Cancer Incidence Rate by Sex and Age Group Over Time" in question 6. 1. For age group 0-4 and 85-89 the incidence rate is more constant over the time period 1970- 2020 for males than for females. 2. For age group 40-44 there was an increase by a factor of ten or so between the years 2000 and 2020 whereas there was no such change for females.

Over time, there is an overall increase in incidence rates for most age groups, particularly for middle-aged and older adults.

The overall incidence rates of colon cancer have increased steadily for both males and females over the years.

Females consistently show slightly higher crude incidence rates compared to males throughout the observed time period.

When we take age into account females tend to have lower incidence rate than males (agegroup 75 up): this could be related to the fact, that, for these agegroups the female population is more numerous than men population