



**UNSW**  
**S Y D N E Y**

CANDIDATE

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TEST

# Quiz 3

Subject code	--
Evaluation type	--
Test opening time	28.02.2024 07:00
End time	06.03.2024 07:00
Grade deadline	--
PDF created	13.08.2024 06:33

Question	Status	Marks	Question type
1.1	Correct	1/1	Multiple Choice
1.2	Partially Correct	0.25/1	Multiple Response
1.3	Correct	1/1	Multiple Response
1.4	Correct	1/1	Multiple Response
1.5	Partially Correct	0.2800000011920929/1	Multiple Response
2.1	Correct	1/1	Multiple Response
2.2	Correct	1/1	Multiple Response
2.3	Correct	1/1	Multiple Response
2.4	Correct	1/1	True / False
2.5	Wrong	0/1	True / False

1.1 Consider the graph with:

- vertex set  $\{0,1\} \times \{0,1\} \times \{0,1\}$
- an edge between two vertices if they differ in exactly two co-ordinates

What is the degree sequence of this graph?

Select one alternative:

☐ 1,1,1,1,1,1,1,1

☐ 0,0,2,2,2,2,0,0

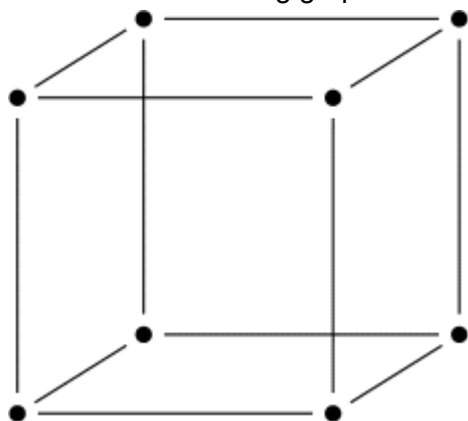
☐ 0,4,4,0,0,0,0,0

☒ 0,0,0,8,0,0,0,0

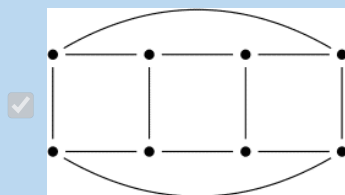
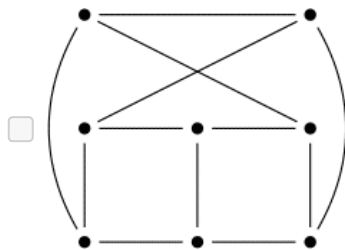
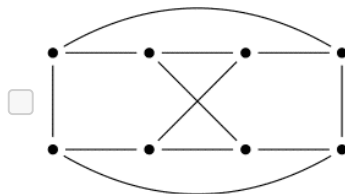
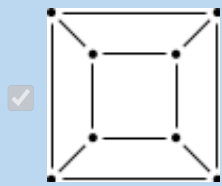
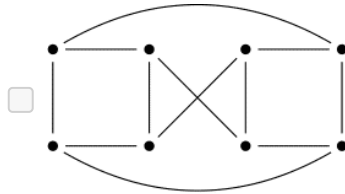
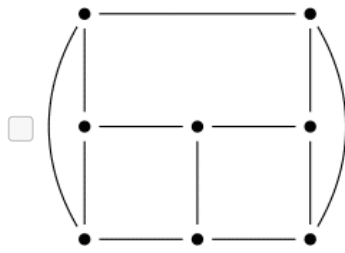


☐ None of the above

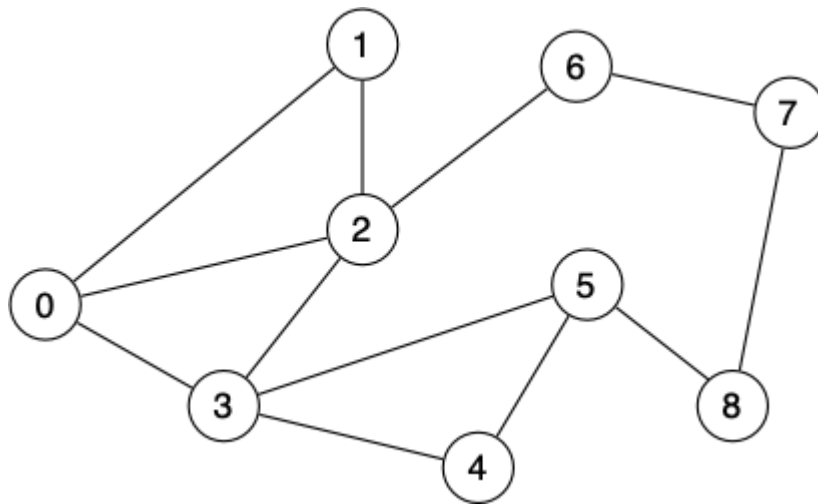
**1.2** Which of the following graphs are isomorphic to this graph:



Select all that apply:



1.3 Consider the following graph:



Starting from Vertex 0, which of the following sequences of vertices *could* arise as a sequence of **explored** vertices when performing a **breadth-first traversal** (according to lectures)?

Select all that apply:

☐ 0,2,1,3,5,4,8,6,7

☒ 0,1,2,3,6,5,4,7,8



☐ 0,1,3,4,5,8,7,6,2

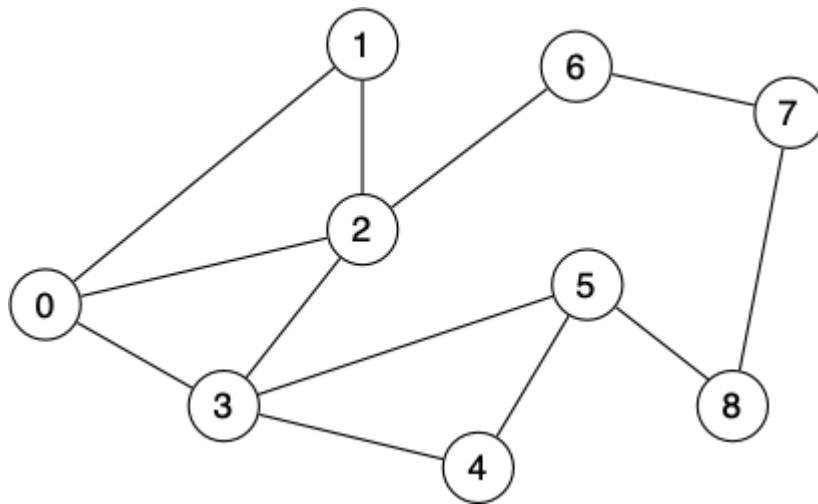
☒ 0,3,2,1,4,5,6,8,7



☐ 0,1,2,3,4,5,6,7,8

☐ 0,3,5,8,7,6,4,2,1

1.4 Consider the following graph:



Starting from Vertex 0, which of the following sequences of vertices could arise as a sequence of **explored** vertices when performing a **depth-first traversal** (according to lectures)?

Select all that apply:

☒ 0,1,3,4,5,8,7,6,2



☐ 0,1,2,3,6,5,4,7,8

☐ 0,2,1,3,5,4,8,6,7

☐ 0,1,2,3,4,5,6,7,8

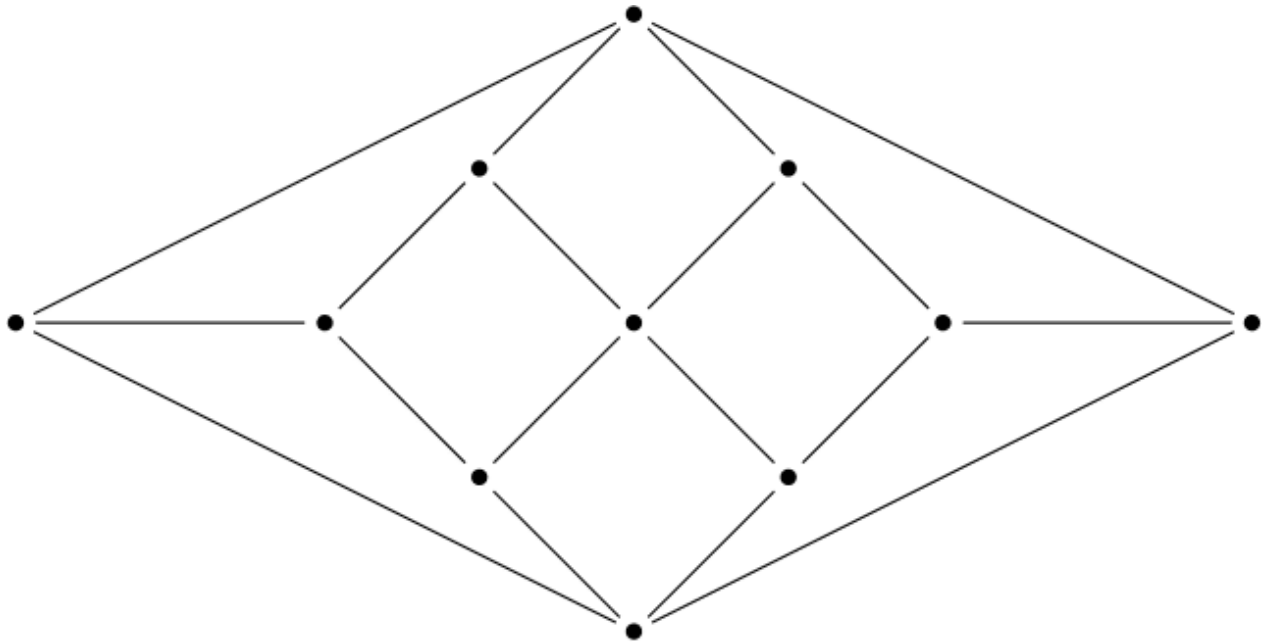
☐ 0,3,2,1,4,5,6,8,7

☒ 0,3,5,8,7,6,4,2,1





1.5 Consider the following graph:



Which of the following properties does this graph have?

**Select all that apply:**

<input checked="" type="checkbox"/> Clique number 2	<input checked="" type="checkbox"/>
<input checked="" type="checkbox"/> Hamiltonian path	<input checked="" type="checkbox"/>
<input checked="" type="checkbox"/> Planar	<input checked="" type="checkbox"/>
<input checked="" type="checkbox"/> Eulerian path	<input type="checkbox"/>
<input checked="" type="checkbox"/> Bipartite	<input checked="" type="checkbox"/>
<input checked="" type="checkbox"/> Contains a cycle of length 10	<input checked="" type="checkbox"/>
<input type="checkbox"/> Chromatic number 3	
<input checked="" type="checkbox"/> Connected	<input checked="" type="checkbox"/>

**2.1** Which of the following statements are true for any graph with  $n \geq 1$  vertices and  $m \geq 0$  edges?

**Select all that apply:**

☒ If  $m < n-1$  then the graph is not connected



☐ If  $m < n$  then the graph is acyclic

☐ If  $m \geq n-1$  then the graph is connected

☒ If  $m \geq n$  then the graph contains a cycle



**2.2** Let  $D_0, D_1, D_2, D_3$  be the degree sequence of a **tree** with  $n \geq 2$  vertices (assume  $D_k = 0$  for  $k \geq 4$ )

Which of the following must necessarily hold:

**Select all that apply**

☒  $D_0 = 0$



☐  $D_2 \geq D_3$

☐  $D_3 \geq D_2$

☒  $D_1 \geq 2$



☐  $D_1$  is even

☒  $D_1 = 2 + D_3$



**2.3** Which of the following graphs have an Eulerian circuit?

**Select all that apply**

☐  $K_{5,5}$

☒  $K_{5,5,5}$



☐ All graphs with degree sequence 0,0,5,0,5

☒ All graphs with degree sequence 0,0,3,0,3,0,3



☒ All regular graphs with 5 vertices and 10 edges



☒  $K_5$



**2.4** Let  $G$  be a finite directed graph where every vertex has in-degree and out-degree at most 1.

True or false:

$G$  has a vertex of out-degree 0 if and only if  $G$  has a vertex of in-degree 0.

☒ True



☐ False

**2.5** True or false:

If a graph has chromatic number at least 3, then it must contain a subdivision of  $K_3$

☐ True



☐ False

