

The use of reaction equations for the simulation of physical phenomena

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Words:

Abstract

Tis but a placeholder

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1 Introduction

Hello [Knuth, 2001a]. [Einstein, 1905] [Goossens et al., 1993] asjkldf [Knuth, 2001b]

2 Calculus

3 Diffusion

4 Reaction

5 Reaction Diffusion

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Listing 1: Diffusion

```
1 import numpy as np
2 from mpl_toolkits.mplot3d import Axes3D
3 import matplotlib.pyplot as plt
4
5 # Simulation constants
6 alpha = 0.00001 # Laplician multiplier
7 dx = 0.01 # Simulation speed/accuracy
8 n = 2000 # number of iterations
9
10 # Matrix initialization
11 M = np.empty((100, 100))
12 M.fill(0)
13 x, y = M.shape
14 # Hotspot Seeding
15 M[20:30, 45:50] = 90
16 M[70:80, 45:50] = 90
17 np.set_printoptions(precision=1)
18
19
20 # Implementation of the decretized laplacian operator
21 def laplacian(Z):
22     Ztop = Z[0:-2, 1:-1]
23     Zleft = Z[1:-1, 0:-2]
24     Zbottom = Z[2:, 1:-1]
25     Zright = Z[1:-1, 2:]
26     Zcenter = Z[1:-1, 1:-1]
27     return (Ztop + Zleft + Zbottom + Zright - (4 * Zcenter)) / dx**2
28
29
30 # Iterations through PDE
31 for _ in range(n):
32     Mn = M[1:-1, 1:-1]
33     M[1:-1, 1:-1] = Mn + np.multiply(laplacian(M), alpha)
34
35 # Graph Data
36 plt.imshow(M, cmap=plt.cm.coolwarm,
37             interpolation='bilinear', extent=[-1, 1, -1, 1])
```

Bibliography

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- [Knuth, 2001a] Knuth, D. (2001a). Knuth: Computers and typesetting.
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