Notebook

April 29, 2023

1 Bigrams - MakeMore pt.1 (12/04/2023)

We now move on to see some interesting applications of the theory we developed earlier on.

Mostly, we will see how to construct a language model, character based, able to 'learn' how to 'reproduce' $\mu(x_n|x_1,\ldots,x_{n-1})$. We will develop such model following "chronological" steps, in the sense that we'll start from an older programming structure and later improve the latest feature in Artificial Intelligence.

Almost all the material presented is taken from A. Karpathy's course and GitHub repository.

First, we start with *counting approach* (not to be confused with the counting technique earlier presented) to implement a bigram approximation of our "language" model (a "2-Markov" approximation).

We want to learn something from a dataset of words. First of all, we need a machine which generates these data (the so-called words).

```
[22]: words = open('data/nomi_italiani.txt').read().splitlines()
```

Let's figure out the length of each word in our dataset.

```
[23]: L = [len(w) for w in words]
print(words[L.index(max(L))])
```

marie-odette-rose-gabrielle

```
[24]: import numpy as np print(np.mean(L))
```

7.088193300384404

```
[25]: import random
  random.seed(154)
  random.shuffle(words)
  print(words[:10])
```

```
['castorino', 'ella', 'irmo', 'leoluca', 'sankhare', 'galvano', 'faleria',
'germando', 'illo', 'romilde']
```

```
[26]: for w in words[:1]:
          for ch1, ch2 in zip(w, w[1:]):
               print(ch1, ch2)
     са
     a s
     s t
     t o
     o r
     r i
     i n
     n o
[27]: print(w)
      list(w)
      print(w[1:])
     castorino
     astorino
     To get all bigrams of, for example, the last three words one can do something like that
[28]: for w in words[:3]:
          chs = [' < S >'] + list(w) + [' < E >']
          for ch1, ch2 in zip(chs, chs[1:]):
               print(ch1, ch2)
     <S> c
     са
     a s
     s t
     t o
     o r
     r i
     i n
     n o
     o <E>
     <S> e
     e l
     1 1
     l a
     a <E>
     <S> i
     i r
     r m
     m o
     o <E>
```

How many often does a bigram happen?

```
[29]: b = {}
    for w in words[:3]:
        chs = ['<S>'] + list(w) + ['<E>']
        for ch1, ch2 in zip(chs, chs[1:]):
            b[(ch1, ch2)] = b.get((ch1, ch2), 0) + 1
        print(b)
```

```
{('<S>', 'c'): 1, ('c', 'a'): 1, ('a', 's'): 1, ('s', 't'): 1, ('t', 'o'): 1, ('o', 'r'): 1, ('r', 'i'): 1, ('i', 'n'): 1, ('n', 'o'): 1, ('o', '<E>'): 2, ('<S>', 'e'): 1, ('e', 'l'): 1, ('l', 'l'): 1, ('l', 'a'): 1, ('a', '<E>'): 1, ('<S>', 'i'): 1, ('i', 'r'): 1, ('r', 'm'): 1, ('m', 'o'): 1}
```

We can do it for all words

```
[30]: b = {}
for w in words:
    chs = ['<S>'] + list(w) + ['<E>']
    for ch1, ch2 in zip(chs, chs[1:]):
        b[(ch1, ch2)] = b.get((ch1, ch2), 0) + 1
```

We now want to construct a machine which tells us the probability of the next character. Let's sort all by frequency

```
[31]: print(sorted(b.items(), key=lambda z: -z[1]))
```

```
[(('o', '<E>'), 4235), (('a', '<E>'), 3831), (('i', 'n'), 1935), (('a', 'n'),
1497), (('r', 'i'), 1483), (('n', 'a'), 1429), (('i', 'o'), 1380), (('i', 'a'),
1344), (('n', 'o'), 1269), (('1', 'i'), 1261), (('e', 'r'), 1149), (('<S>',
'a'), 1095), (('e', 'l'), 1070), (('a', 'r'), 957), (('o', 'r'), 920), (('<S>',
'f'), 885), (('a', 'l'), 856), (('<S>', 'o'), 789), (('d', 'o'), 754), (('i',
'l'), 712), (('r', 'o'), 705), (('e', 'n'), 699), (('r', 'a'), 686), (('l',
'a'), 682), (('m', 'a'), 663), (('<S>', 'g'), 657), (('n', 'i'), 649), (('e',
'<E>'), 630), (('<S>', 'e'), 629), (('<S>', 'r'), 626), (('<S>', 'm'), 595),
(('o', 'n'), 591), (('r', 'e'), 584), (('t', 'a'), 580), (('d', 'a'), 565),
(('t', 'o'), 559), (('d', 'i'), 552), (('o', 'l'), 545), (('d', 'e'), 540),
(('1', '1'), 537), (('m', 'i'), 532), (('s', 'i'), 531), (('<S>', 'c'), 520),
(('l', 'e'), 511), (('g', 'i'), 496), (('i', 's'), 482), (('l', 'o'), 474),
(('<S>', '1'), 446), (('n', 'e'), 437), (('n', 'd'), 433), (('t', 'i'), 430),
(('l', 'd'), 405), (('i', 'd'), 403), (('v', 'i'), 398), (('t', 't'), 392),
(('<S>', 's'), 391), (('f', 'i'), 387), (('e', 't'), 386), (('t', 'e'), 378),
(('c', 'o'), 364), (('<S>', 'd'), 351), (('z', 'i'), 350), (('<S>', 'p'), 345),
(('i', 'c'), 342), (('m', 'e'), 335), (('n', 't'), 334), (('c', 'a'), 333),
(('s', 'a'), 333), (('e', 's'), 331), (('c', 'i'), 326), (('o', 's'), 322),
(('<S>', 'i'), 319), (('<S>', 'n'), 313), (('i', 'e'), 311), (('s', 't'), 307),
(('<S>', 'v'), 297), (('<S>', 'b'), 293), (('f', 'e'), 283), (('v', 'a'), 279),
(('g', 'e'), 272), (('i', 'r'), 268), (('m', 'o'), 263), (('a', 't'), 255),
(('b', 'e'), 255), (('a', 'm'), 254), (('a', 'd'), 251), (('v', 'e'), 245),
(('e', 'd'), 245), (('r', 'd'), 237), (('n', 'z'), 237), (('a', 's'), 236),
(('c', 'e'), 235), (('r', 't'), 234), (('<S>', 't'), 226), (('i', 'm'), 225),
```

```
(('s', 'e'), 220), (('e', 'o'), 219), (('n', 'n'), 217), (('e', 'm'), 215),
(('i', 't'), 206), (('i', 'g'), 195), (('e', 'a'), 189), (('f', 'a'), 187),
(('r', 'm'), 182), (('o', 'd'), 181), (('o', 'm'), 177), (('c', 'c'), 175),
(('s', 'o'), 167), (('f', 'r'), 166), (('p', 'i'), 164), (('u', 'r'), 163),
(('l', 'm'), 160), (('g', 'a'), 156), (('b', 'a'), 155), (('u', 'c'), 154),
(('o', 'v'), 145), (('i', '<E>'), 143), (('p', 'a'), 142), (('l', 'v'), 140),
(('p', 'e'), 139), (('l', 'f'), 139), (('a', 'u'), 138), (('c', 'h'), 137),
(('i', 'v'), 132), (('b', 'i'), 126), (('a', 'c'), 123), (('f', 'o'), 121),
(('g', 'o'), 121), (('u', 'i'), 117), (('s', 's'), 116), (('a', 'v'), 115),
(('b', 'r'), 113), (('s', 'c'), 113), (('u', 'l'), 113), (('r', 'u'), 112),
(('l', 'u'), 110), (('z', 'a'), 109), (('c', 'l'), 109), (('o', 't'), 107),
(('a', 'b'), 106), (('f', 'l'), 105), (('h', 'i'), 103), (('u', 's'), 103),
(('n', 'u'), 102), (('t', 'r'), 102), (('n', 'c'), 100), (('e', 'g'), 100),
(('a', 'z'), 99), (('d', 'r'), 97), ((' < S > ', 'z'), 97), (('g', 'l'), 94), (('a', 'l'), 94))
'g'), 93), (('r', 'n'), 93), (('n', 'g'), 91), (('s', '<E>'), 90), (('p', 'r'),
90), (('p', 'o'), 90), (('i', 'z'), 90), (('u', 'n'), 89), (('z', 'o'), 86),
(('t', 'u'), 86), (('e', 'v'), 82), (('e', 'u'), 81), (('b', 'o'), 80), (('<S>',
'u'), 80), (('z', 'e'), 79), (('r', 'c'), 77), (('r', 'r'), 75), (('z', 'z'),
75), (('r', 'g'), 74), (('a', 'i'), 74), (('q', 'u'), 73), (('i', 'b'), 72),
(('o', 'b'), 71), (('r', 's'), 70), (('h', 'e'), 68), (('l', 'b'), 68), (('u',
'd'), 68), (('s', 'p'), 67), (('o', 'c'), 67), (('g', 'u'), 65), (('a', 'f'),
61), (('n', 's'), 61), (('i', 'u'), 59), (('c', 'r'), 59), (('l', 'c'), 58),
(('l', 't'), 57), (('r', 'l'), 57), (('s', 'm'), 57), (('v', 'o'), 56), (('f',
'f'), 56), (('g', 'r'), 56), (('m', 'b'), 55), (('<S>', 'w'), 55), (('u', 'e'),
53), (('u', 'a'), 53), (('r', '<E>'), 52), (('m', 'm'), 50), (('d', 'u'), 50),
(('p', 'p'), 49), (('s', 'u'), 48), (('u', 't'), 47), (('e', 'f'), 47), (('<S>',
'q'), 47), (('e', 'z'), 47), (('r', 'v'), 46), (('e', 'p'), 46), (('a', '-'),
45), (('o', 'p'), 45), (('i', 'p'), 44), (('o', 'f'), 44), (('l', 'g'), 44),
(('a', 'o'), 42), (('e', 'c'), 41), (('r', 'z'), 40), (('u', 'g'), 39), (('a', 'c'), 40), (('a', 'c'
'e'), 37), (('n', '<E>'), 37), (('m', 'p'), 35), (('f', 'u'), 34), (('u', 'b'),
33), (('d', 'd'), 33), (('g', 'h'), 31), (('<S>', 'j'), 31), (('o', 'i'), 31),
(('w', 'a'), 30), (('g', 'n'), 29), (('c', 'u'), 29), (('g', 'g'), 29), (('b',
'b'), 28), (('m', 'u'), 28), (('n', 'f'), 28), (('e', 'b'), 28), (('u', 'm'),
27), (('a', 'p'), 26), (('i', 'f'), 26), (('h', 'a'), 25), (('r', 'f'), 25),
(('o', 'g'), 25), (('o', 'a'), 24), (('s', 'l'), 24), (('j', 'a'), 24), (('s',
'v'), 23), (('l', 's'), 23), (('u', 'f'), 22), (('r', 'b'), 22), (('e', 'i'),
21), (('p', 'l'), 19), (('o', 'e'), 19), (('w', 'i'), 17), (('u', 'p'), 17),
(('b', 'u'), 16), (('l', '<E>'), 16), (('o', '-'), 16), (('u', 'z'), 16), (('k',
'a'), 15), (('d', '<E>'), 15), (('j', 'o'), 14), (('e', '-'), 14), (('u', 'o'),
13), (('-', 'm'), 13), (('-', 'a'), 13), (('p', 'u'), 13), (('l', 'p'), 12),
(('-', 'r'), 12), (('u', '<E>'), 12), (('s', 'q'), 12), (('r', 'p'), 11),
(('<S>', 'k'), 11), (('b', 'l'), 11), (('n', 'r'), 10), (('n', '-'), 10), (('w',
'e'), 9), (('-', 'g'), 9), (('d', 'm'), 9), (('t', 'h'), 9), (('l', 'z'), 8),
(('m', '<E>'), 8), (('a', 'h'), 8), (('n', 'm'), 8), (('s', 'd'), 7), (('z',
'u'), 7), (('n', 'l'), 7), (('-', 'e'), 7), (('e', 'e'), 6), (('t', '<E>'), 6),
(('s', 'f'), 6), (('y', 'n'), 6), (('-', 'j'), 6), (('r', 'k'), 6), (('v', 'v'),
6), (('v', 'r'), 6), (('s', 'z'), 6), (('n', 'p'), 6), (('g', 'd'), 5), (('s',
'b'), 5), (('a', 'q'), 5), (('o', 'h'), 5), (('i', 'k'), 5), (('b', 'd'), 5),
```

```
(('k', 'o'), 5), (('o', 'z'), 5), (('g', 'f'), 5), (('-', 'p'), 5), (('s', 'h'),
5), (('o', 'u'), 5), (('r', 'q'), 5), (('k', 'h'), 4), (('-', 'd'), 4), (('-',
'i'), 4), (('<S>', 'y'), 4), (('z', 'b'), 4), (('x', 'a'), 4), (('y', '<E>'),
4), (('h', 'r'), 4), (('k', 'r'), 4), (('t', 'y'), 4), (('l', 'r'), 4), (('a',
'w'), 4), (('j', 'u'), 4), (('z', '<E>'), 4), (('d', 'v'), 4), (('h', '<E>'),
4), (('-', '1'), 4), (('-', 'c'), 4), (('-', 'o'), 3), (('y', 'o'), 3), (('1',
('v'), 3), (('v', 'l'), 3), (('r', 'v'), 3), (('v', 's'), 3), (('-', 's'), 3),
(('f', 'n'), 3), (('l', 'k'), 3), (('w', 'o'), 3), (('k', 'i'), 3), (('e', 'x'), 3))
3), (('n', 'v'), 3), (('j', 'e'), 3), (('x', 'i'), 3), (('w', '<E>'), 3), (('p',
'h'), 3), (('i', 'j'), 3), (('h', 'o'), 3), (('e', 'w'), 3), (('<S>', 'h'), 3),
(('r', 'x'), 3), (('k', '<E>'), 3), (('s', 'r'), 3), (('n', 'q'), 3), (('d',
'g'), 3), (('z', 'y'), 3), (('n', 'k'), 2), (('c', 'y'), 2), (('y', 'u'), 2),
(('v', '<E>'), 2), (('e', 'j'), 2), (('j', 'i'), 2), (('-', 'b'), 2), (('-',
'v'), 2), (('-', 'h'), 2), (('w', 'l'), 2), (('z', 'k'), 2), (('y', 'a'), 2),
(('s', '-'), 2), (('d', '-'), 2), (('-', 'k'), 2), (('v', 'u'), 2), (('t', '-'),
2), (('a', 'y'), 2), (('l', 'n'), 2), (('s', 'k'), 2), (('n', 'b'), 2), (('e',
'k'), 2), (('m', 'l'), 2), (('-', 'n'), 2), (('f', '<E>'), 2), (('n', 'j'), 2),
(('y', 'l'), 2), (('u', 'j'), 2), (('c', 't'), 2), (('t', 's'), 2), (('u', 'k'),
2), (('r', '-'), 2), (('c', '<E>'), 2), (('x', '<E>'), 2), (('c', 'm'), 1),
(('o', 'x'), 1), (('b', '-'), 1), (('y', 'v'), 1), (('m', 'y'), 1), (('y', 'r'),
1), (('-', 'y'), 1), (('s', 'n'), 1), (('i', 'x'), 1), (('-', 'f'), 1), (('t',
'l'), 1), (('r', 'j'), 1), (('m', '-'), 1), (('t', 'b'), 1), (('d', 'j'), 1),
(('k', 'e'), 1), (('k', 'b'), 1), (('a', 'j'), 1), (('t', 'g'), 1), (('-', 'w'),
1), (('k', '-'), 1), (('-', 'z'), 1), (('n', 'w'), 1), (('b', '<E>'), 1), (('o',
'k'), 1), (('k', 's'), 1), (('j', '<E>'), 1), (('y', 'k'), 1), (('m', 'n'), 1),
(('l', '-'), 1), (('i', '-'), 1), (('m', 's'), 1), (('t', 'p'), 1), (('o', 'y'),
1), (('y', 'c'), 1), (('w', 'u'), 1), (('d', 'y'), 1), (('z', 't'), 1), (('f',
'-'), 1), (('z', '-'), 1), (('n', 'y'), 1), (('a', 'a'), 1), (('d', 'h'), 1),
(('-', '<E>'), 1), (('u', '-'), 1), (('d', 'w'), 1), (('u', 'v'), 1), (('j',
'n'), 1), (('h', '-'), 1), (('t', 'm'), 1), (('j', 'j'), 1), (('a', 'x'), 1),
(('c', 'q'), 1), (('l', 'h'), 1), (('h', 'm'), 1), (('k', 't'), 1), (('g',
'<E>'), 1)]
```

With the set function built-in python one can get the unique elements of a list

```
[32]: w = set(list(words[1]))
print(w)
```

{'e', 'a', 'l'}

Now we want to code this information Let's take only the unique elements of a word, then of all words, i.e. our finite alphabet

```
[33]: chars = sorted(list(set(''.join(words))))
    chars.append('<S>')
    chars.append('<E>')
    print(chars)
```

['-', 'a', 'b', 'c', 'd', 'e', 'f', 'g', 'h', 'i', 'j', 'k', 'l', 'm', 'n', 'o',

```
'p', 'q', 'r', 's', 't', 'u', 'v', 'w', 'x', 'y', 'z', '<S>', '<E>']
```

At this point we should have 27 characters, 26 letters of the alphabet and the dash from composite names

```
[34]: print(len(chars))
```

29

Actually we need 29 characters, i.e. the 27 previously discussed plus the initial and final of a word

```
[35]: import torch

N = torch.zeros(29, 29)
```

Let's now build an encoder, which assigns an integer value to each character of our alphabet. This will be a dictionary.

```
[36]: stoi = {s: i for i, s in enumerate(chars)}
stoi['<S>'] = 27
stoi['<E>'] = 28
print(stoi)
```

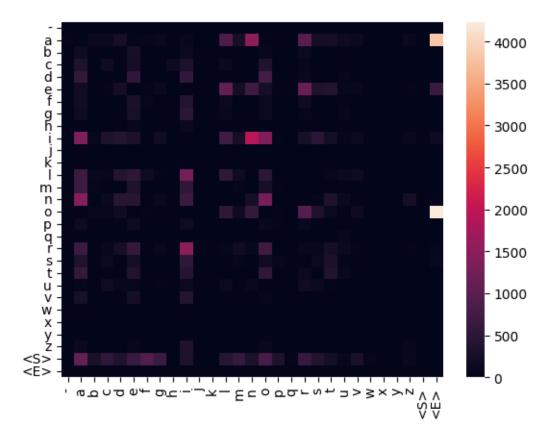
```
{'-': 0, 'a': 1, 'b': 2, 'c': 3, 'd': 4, 'e': 5, 'f': 6, 'g': 7, 'h': 8, 'i': 9, 'j': 10, 'k': 11, 'l': 12, 'm': 13, 'n': 14, 'o': 15, 'p': 16, 'q': 17, 'r': 18, 's': 19, 't': 20, 'u': 21, 'v': 22, 'w': 23, 'x': 24, 'y': 25, 'z': 26, '<S>': 27, '<E>': 28}
```

Now let's count the frequency of each bigram and put it in our tensor.

```
[37]: for w in words:
    chs = ['<S>'] + list(w) + ['<E>']
    for ch1, ch2 in zip(chs, chs[1:]):
        N[stoi[ch1], stoi[ch2]] += 1
N[28, 27] = 1 # <E> <S>
```

```
[38]: import seaborn as sns sns.heatmap(N, xticklabels=chars, yticklabels=chars)
```

[38]: <Axes: >



Now one can also build a decoder

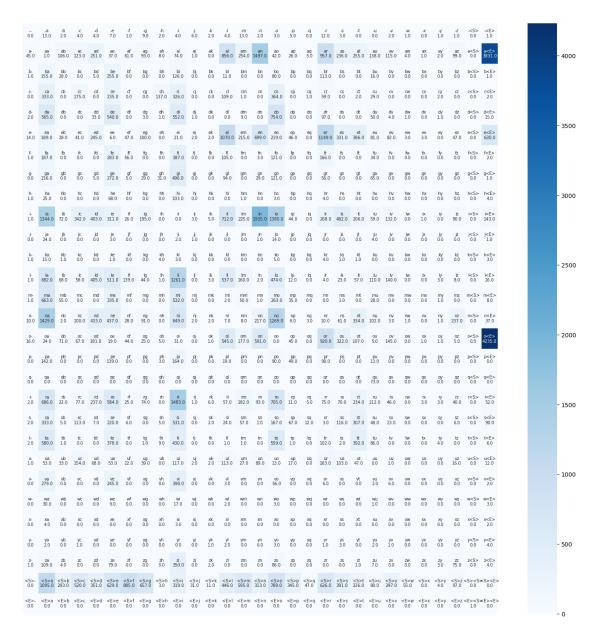
```
[39]: itos = {i: s for s, i in stoi.items()} print(itos)
```

```
{0: '-', 1: 'a', 2: 'b', 3: 'c', 4: 'd', 5: 'e', 6: 'f', 7: 'g', 8: 'h', 9: 'i', 10: 'j', 11: 'k', 12: 'l', 13: 'm', 14: 'n', 15: 'o', 16: 'p', 17: 'q', 18: 'r', 19: 's', 20: 't', 21: 'u', 22: 'v', 23: 'w', 24: 'x', 25: 'y', 26: 'z', 27: '<S>', 28: '<E>'}
```

Notice that **stoi** is associating to any character a number, so they are enumerated from 0 to 26 (the dimension of our alphabet is 29). On the other hand, **itos** is decoding a number into a character.

For a better visualization we can plot the whole matrix together with the bigrams and their frequencies

[40]: <Axes: >



How can we use counting to infer our probability? How can we reproduce the probability distribution of these numbers?

Let's start by computing the probability of the first character. First, normalize all the rows of the tensor, then sample using frequencies. It is possible, with PyTorch, to normalize all the rows of a matrix (stochastic on the row) by doing M/M.sum(...). Assume that \vec{p} is now our 27th row normalized, i.e. '<S>' + '%c' string, which represents the frequency of starting letters. Using the conditional probability known by the dataset one can start to generate words basing on bigrams, actually in a Markov chain approximation. However, the result is not properly good (is very, very bad ngl). Words must be extracted with repetition from our \vec{p} vector. Actually, an integer is

generated, not a word.

TRIVIA ChatGPT has a vocabulary of words (chunks - word pieces), not characters.

```
[41]: p = N / N.sum(axis=1, keepdims=True)
      g = torch.Generator().manual_seed(123450)
      for i in range(10):
          out = []
          ix = 27
          while True:
              pix = p[ix]
              ix = torch.multinomial(
                  pix, num_samples=1, replacement=True, generator=g).item()
              out.append(itos[ix])
              if ix == 28:
                  break
          print(''.join(out))
     epucia<E>
     o<E>
     lgomenzano<E>
     a<E>
     ginttio<E>
     s<E>
     ciniglclalirermo<E>
     feonedo<E>
     mola<E>
     ndo<E>
     What if the probability distribution was uniform?
[42]: for i in range(10):
          out = []
          ix = 27
          while True:
              pix = torch.ones(29)/29.0
              ix = torch.multinomial(
                  pix, num_samples=1, replacement=True, generator=g).item()
              out.append(itos[ix])
              if ix == 28:
                  break
          print(''.join(out))
     aaognqusx<E>
     sx<S>ukksqzwca<S><E>
     zvksvkbglkndtjxwfra<S>fotxorg<S>x<S>mytxlnvdrqordxkclczhn-ynrqjp-1<E>
     xwcsruntl-rdkfbzexahxcxoxa-ucfnoae<E>
     natlmee<S>yxjtpynrn-zsps<E>
```

```
zmpaaxp<E>
cidlwhsmmllkndpzawmdxkhnnyghb<E>
cchgmhzv<S>lf<S>sfwrwwolpb<S>-itrmv-j-lld<S>gouh<E>
mmuykixwsdddbaopvxqldjwwy<S>my-trkjwbjdoqkkxepmw<S>cjv<E>
lzyywd<S>kwu<E>
```

Words generated with uniform distribution are way worse, so just using the probability of the dataset (simple information - just counting) one can achieve a quite good result with respect to the total randomness.

How to evaluate an algorithm like this one? (just one char memory) How can we do better?

2 Trigrams - MakeMore2 (19/04/2023)

What if we wanted to guess the fourth character by knowing the first 3 ones? We should have a counting matrix N of size (in this case) $28 \cdot 28 \cdot 28 = 21952$. For some applications we would like to look at strings of 9,10 characters or even more: the situation becomes exponentially untreatable.

We must find another way to "train" our system, one that does not involve counting since the latter is not scalable to n—grams. We are going to ask a **Neural Network** to predict the (conditioned) probability distribution over all characters. Furthermore, we are going to see the most simple case of Neural Network now, but then we are going to complexify it and get incredible results.

```
[443]: # https://youtu.be/TCH_1BHY58I
# https://github.com/karpathy/makemore
```

Now we'll try to build a multilayer perceptron (MLP). Each character is going to be embedded in a 2D space. We've three vectors 30D, so 90D as total dimension (28 chars + 2). Training the network the embedding will change. We'll have a linear transformation which transpose in an intermediate layer we can see as 100D vector. Transforming this non-linearly (with a hyperbolic tangent) it will construct the derivatives (back propagation). With another linear transform we'll connect all. Exponentiating and normalizing we'll get the desired probability distribution. Hyperparameters are the a priori defined parameters. To do things in a good way one needs to know how to tune the hyperparameters.

```
[445]: # read in all the words random.seed(158)
```

```
words = open('data/nomi_italiani.txt', 'r').read().splitlines()
random.shuffle(words)
print(words[0:10])
print(len(words))
```

['argento', 'giovannino', 'licurga', 'elvira', 'marena', 'sirio', 'emilia', 'bisio', 'preziosa', 'perpetua']
9105

```
[446]: # build the vocabulary of characters and mapping to/from integers
    chars = sorted(list(set(''.join(words))))

stoi = {s: i+1 for i, s in enumerate(chars)}
    stoi['.'] = 0
    itos = {i: s for s, i in stoi.items()}
    print(itos)
    print(stoi)
```

```
{1: '-', 2: 'a', 3: 'b', 4: 'c', 5: 'd', 6: 'e', 7: 'f', 8: 'g', 9: 'h', 10: 'i', 11: 'j', 12: 'k', 13: 'l', 14: 'm', 15: 'n', 16: 'o', 17: 'p', 18: 'q', 19: 'r', 20: 's', 21: 't', 22: 'u', 23: 'v', 24: 'w', 25: 'x', 26: 'y', 27: 'z', 0: '.'}
{'-': 1, 'a': 2, 'b': 3, 'c': 4, 'd': 5, 'e': 6, 'f': 7, 'g': 8, 'h': 9, 'i': 10, 'j': 11, 'k': 12, 'l': 13, 'm': 14, 'n': 15, 'o': 16, 'p': 17, 'q': 18, 'r': 19, 's': 20, 't': 21, 'u': 22, 'v': 23, 'w': 24, 'x': 25, 'y': 26, 'z': 27, '.': 0}
```

Previous example - Markov chain, so the block size was 1. Updating the contest means shift over the string and add the last character. X contains the samples (what I'm looking at). Each row of X is a trigram. Y contains the correct answers.

Y = torch.tensor(Y)

```
argento
... ---> a
..a ---> r
.ar ---> g
arg ---> e
rge ---> n
gen ---> t
ent ---> o
nto ---> .
giovannino
... ---> g
..g ---> i
.gi ---> o
gio ---> v
iov ---> a
ova ---> n
van ---> n
ann ---> i
nni ---> n
nin ---> o
ino ---> .
licurga
... ---> 1
..1 ---> i
.li ---> c
lic ---> u
icu ---> r
cur ---> g
urg ---> a
rga ---> .
elvira
... ---> e
..e ---> 1
.el ---> v
elv ---> i
lvi ---> r
vir ---> a
ira ---> .
marena
... ---> m
..m ---> a
.ma ---> r
mar ---> e
are ---> n
ren ---> a
```

```
ena ---> .
```

If I present to my system $0 = \cdot$ I expect to find 2 = a, and so on.

```
[448]: print(X) print(Y)
```

```
Ο,
tensor([[ 0,
                 0],
        [ 0,
                 2],
             Ο,
        [ 0,
             2, 19],
        [ 2, 19,
                 8],
        [19,
             8,
                 6],
        [8, 6, 15],
        [6, 15, 21],
        [15, 21, 16],
        [0,0,0],
        [ 0,
             0, 8],
        [0, 8, 10],
        [8, 10, 16],
        [10, 16, 23],
        [16, 23, 2],
        [23, 2, 15],
        [2, 15, 15],
        [15, 15, 10],
        [15, 10, 15],
        [10, 15, 16],
        [0, 0, 0],
        [0, 0, 13],
        [ 0, 13, 10],
        [13, 10, 4],
        [10,
             4, 22],
        [4, 22, 19],
        [22, 19, 8],
             8,
        [19,
                 2],
        [ 0,
             Ο,
                 0],
        [ 0,
             0, 6],
        [0, 6, 13],
        [6, 13, 23],
        [13, 23, 10],
        [23, 10, 19],
        [10, 19, 2],
        [0, 0, 0],
        [ 0, 0, 14],
        [0, 14, 2],
             2, 19],
        [14,
        [2, 19, 6],
        [19, 6, 15],
        [ 6, 15,
                 2]])
```

```
tensor([ 2, 19, 8, 6, 15, 21, 16, 0, 8, 10, 16, 23, 2, 15, 15, 10, 15, 16, 0, 13, 10, 4, 22, 19, 8, 2, 0, 6, 13, 23, 10, 19, 2, 0, 14, 2, 19, 6, 15, 2, 0])
```

```
[449]: print(X.shape, X.dtype, Y.shape, Y.dtype)
```

```
torch.Size([41, 3]) torch.int64 torch.Size([41]) torch.int64
```

Now we want to predict the next character starting from trigrams. We're going to take a 2D embedding of the 28 characters. There are many pre-calculated embeddings in the world.

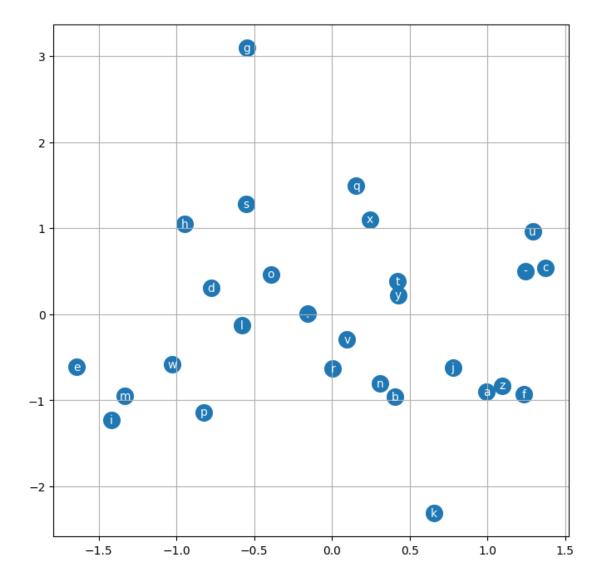
We can generate a random (normal) matrix 28x2. In deep data analysis (what we're doing) the world is going really fast. There is a lot of material, 99% of which are bullshits.

```
[450]: # https://pytorch.org/docs/stable/generated/torch.randn.html
C = torch.randn((28, 2))
```

```
[451]: print(C[5]) print(C.shape)
```

```
tensor([-0.7776, 0.3077])
torch.Size([28, 2])
```

Here is a plot of the embedding. Letters are random, after the training this picture is going to change. From this plot we can learn how characters are related each other.



Another way to embed characters is the **one-hot encoding** discussed last lecture. We can see this embedding as the first layer of our network, even if there's no linearity in it. In fact, they're completely equivalent. One can also see all the embeddings.

```
[0.0061, -0.6300],
[-0.5460, 3.0955],
[-1.6397, -0.6131],
[0.3087, -0.8025],
[0.4220, 0.3822],
[-0.3936,
          0.4641],
[-0.1584,
          0.0036],
[-0.5460,
          3.0955],
[-1.4187, -1.2333],
[-0.3936, 0.4641],
[0.0970, -0.2923],
[0.9940, -0.8991],
[0.3087, -0.8025],
[0.3087, -0.8025],
[-1.4187, -1.2333],
[0.3087, -0.8025],
[-0.3936, 0.4641],
[-0.1584, 0.0036],
[-0.5780, -0.1284],
[-1.4187, -1.2333],
[ 1.3726, 0.5412],
[ 1.2897, 0.9605],
[0.0061, -0.6300],
[-0.5460, 3.0955],
[0.9940, -0.8991],
[-0.1584, 0.0036],
[-1.6397, -0.6131],
[-0.5780, -0.1284],
[0.0970, -0.2923],
[-1.4187, -1.2333],
[0.0061, -0.6300],
[0.9940, -0.8991],
[-0.1584, 0.0036],
[-1.3297, -0.9474],
[0.9940, -0.8991],
[0.0061, -0.6300],
[-1.6397, -0.6131],
[0.3087, -0.8025],
[0.9940, -0.8991],
[-0.1584, 0.0036]])
```

How to embed the 41 trigrams we have?

```
[454]: emb = C[X] print(emb.shape)
```

torch.Size([41, 3, 2])

Moreover, we can differentiate C! Input has dimension 6 = 3 * 2

```
[455]: | \# construct the Layer.... x.W+ b... so the input has dimension 6=3*2 for <math>(say)_{\sqcup}
       →100 neurons...
       W1 = torch.randn(6, 100)
       b1 = torch.randn(100)
      We want to concatenate tensors. And maybe unbind them.
[456]: # https://putorch.org/docs/stable/torch.html search for concatenate...
       print(torch.cat([emb[:, 0, :], emb[:, 1, :], emb[:, 2, :]], 1)[1])
       print(emb[1])
      tensor([-0.1584, 0.0036, -0.1584, 0.0036, 0.9940, -0.8991])
      tensor([[-0.1584, 0.0036],
              [-0.1584, 0.0036],
              [ 0.9940, -0.8991]])
[457]: # we want a code for general n-grams.....
       # use 'unbind' https://pytorch.org/docs/stable/generated/torch.unbind.
       →html#torch.unbind
       len(torch.unbind(emb, 1))
[457]: 3
[458]: # and this work fore any context length......
       torch.cat(torch.unbind(emb, 1), 1)
[458]: tensor([[-0.1584, 0.0036, -0.1584, 0.0036, -0.1584, 0.0036],
               [-0.1584, 0.0036, -0.1584, 0.0036, 0.9940, -0.8991],
               [-0.1584, 0.0036, 0.9940, -0.8991, 0.0061, -0.6300],
               [0.9940, -0.8991, 0.0061, -0.6300, -0.5460, 3.0955],
               [0.0061, -0.6300, -0.5460, 3.0955, -1.6397, -0.6131],
               [-0.5460, 3.0955, -1.6397, -0.6131, 0.3087, -0.8025],
               [-1.6397, -0.6131, 0.3087, -0.8025, 0.4220, 0.3822],
               [0.3087, -0.8025, 0.4220, 0.3822, -0.3936, 0.4641],
               [-0.1584, 0.0036, -0.1584, 0.0036, -0.1584,
                                                             0.0036],
               [-0.1584, 0.0036, -0.1584, 0.0036, -0.5460, 3.0955],
               [-0.1584, 0.0036, -0.5460, 3.0955, -1.4187, -1.2333],
               [-0.5460, 3.0955, -1.4187, -1.2333, -0.3936, 0.4641],
               [-1.4187, -1.2333, -0.3936, 0.4641, 0.0970, -0.2923],
               [-0.3936, 0.4641, 0.0970, -0.2923, 0.9940, -0.8991],
               [0.0970, -0.2923, 0.9940, -0.8991, 0.3087, -0.8025],
               [0.9940, -0.8991, 0.3087, -0.8025, 0.3087, -0.8025],
               [0.3087, -0.8025, 0.3087, -0.8025, -1.4187, -1.2333],
               [0.3087, -0.8025, -1.4187, -1.2333, 0.3087, -0.8025],
               [-1.4187, -1.2333, 0.3087, -0.8025, -0.3936, 0.4641],
```

```
[-0.1584, 0.0036, -0.1584, 0.0036, -0.1584, 0.0036],
[-0.1584, 0.0036, -0.1584, 0.0036, -0.5780, -0.1284],
[-0.1584, 0.0036, -0.5780, -0.1284, -1.4187, -1.2333],
[-0.5780, -0.1284, -1.4187, -1.2333, 1.3726, 0.5412],
[-1.4187, -1.2333, 1.3726, 0.5412, 1.2897, 0.9605],
[1.3726, 0.5412, 1.2897, 0.9605, 0.0061, -0.6300],
[ 1.2897, 0.9605, 0.0061, -0.6300, -0.5460,
                                             3.0955],
[0.0061, -0.6300, -0.5460, 3.0955, 0.9940, -0.8991],
[-0.1584, 0.0036, -0.1584, 0.0036, -0.1584, 0.0036],
[-0.1584, 0.0036, -0.1584, 0.0036, -1.6397, -0.6131],
[-0.1584, 0.0036, -1.6397, -0.6131, -0.5780, -0.1284],
[-1.6397, -0.6131, -0.5780, -0.1284, 0.0970, -0.2923],
[-0.5780, -0.1284, 0.0970, -0.2923, -1.4187, -1.2333],
[0.0970, -0.2923, -1.4187, -1.2333, 0.0061, -0.6300],
[-1.4187, -1.2333, 0.0061, -0.6300, 0.9940, -0.8991],
[-0.1584, 0.0036, -0.1584, 0.0036, -0.1584, 0.0036],
[-0.1584, 0.0036, -0.1584, 0.0036, -1.3297, -0.9474],
[-0.1584, 0.0036, -1.3297, -0.9474, 0.9940, -0.8991],
[-1.3297, -0.9474, 0.9940, -0.8991, 0.0061, -0.6300],
[0.9940, -0.8991, 0.0061, -0.6300, -1.6397, -0.6131],
[0.0061, -0.6300, -1.6397, -0.6131, 0.3087, -0.8025],
[-1.6397, -0.6131, 0.3087, -0.8025, 0.9940, -0.8991]])
```

Let's see a better way.

```
[459]: | # https://pytorch.org/docs/stable/generated/torch.Tensor.view.html
       # https://pytorch.org/docs/stable/generated/torch.Tensor.stride.html
      a = torch.arange(18)
      print(a)
      print(a.shape)
      print(a.view(9, 2))
      print(a.view(2, 9))
      print(a.untyped_storage()) # very efficient in torch
      tensor([0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17])
      torch.Size([18])
      tensor([[ 0, 1],
              [ 2,
                   3],
              [4,
                   5],
              [6,
                   7],
              [8, 9],
              [10, 11],
              [12, 13],
              [14, 15],
              [16, 17]])
      tensor([[ 0, 1, 2, 3, 4, 5, 6, 7, 8],
```

```
[ 9, 10, 11, 12, 13, 14, 15, 16, 17]])
       0
       1
       2
       3
       4
       5
       6
       7
       8
       9
       10
       11
       12
       13
       14
       15
       16
       17
      [torch.storage.TypedStorage(dtype=torch.int64, device=cpu) of size 18]
      /tmp/ipykernel_494/1622729900.py:12: UserWarning: TypedStorage is deprecated. It
      will be removed in the future and UntypedStorage will be the only storage class.
      This should only matter to you if you are using storages directly. To access
      UntypedStorage directly, use tensor.untyped_storage() instead of
      tensor.storage()
        print(a.storage()) # very efficient in torch
[460]: print(emb.view(41, 6) == torch.cat(torch.unbind(emb, 1), 1))
      tensor([[True, True, True, True, True, True],
              [True, True, True, True, True],
              [True, True, True, True, True],
              [True, True, True, True, True],
```

```
[True, True, True, True, True, True],
              [True, True, True, True, True],
              [True, True, True, True, True],
              [True, True, True, True, True, True]])
      So we can use
[461]: h = emb.view(41, 6) @ W1 + b1
[462]: print(h)
       print(h.shape)
       # -1 means 'infer' the dimension from the other dimensions (sort-of auto)
       print(emb.view(-1, 6) @ W1 + b1)
      tensor([[-0.0127, -1.5797, 0.3777, ..., 0.8798, 0.8424,
                                                                  0.3150],
              [0.4762, -1.6867,
                                  2.4601,
                                           ..., -1.1835,
                                                        1.1385,
                                                                  1.0527],
              [-2.4161, -1.6783,
                                  2.7843, ..., -1.8970, -1.9951,
                                                                 0.8419],
              [0.0383, -0.0525,
                                  3.2570,
                                          ..., 2.5062, -3.9853, -0.9087],
              [1.8422, -0.6354,
                                  2.8349,
                                           ..., 1.2162, -0.9053, -1.1034],
              [-0.7111, -4.3180, 3.8939, ..., -3.6111, 0.0440, 2.0282]])
      torch.Size([41, 100])
      tensor([[-0.0127, -1.5797,
                                 0.3777, ..., 0.8798, 0.8424,
                                                                 0.3150],
              [0.4762, -1.6867, 2.4601, ..., -1.1835, 1.1385,
                                                                  1.0527],
              [-2.4161, -1.6783,
                                 2.7843,
                                           ..., -1.8970, -1.9951,
                                                                 0.8419],
              [0.0383, -0.0525,
                                 3.2570,
                                           ..., 2.5062, -3.9853, -0.9087],
              [1.8422, -0.6354,
                                  2.8349, ..., 1.2162, -0.9053, -1.1034],
```

[True, True, True, True, True, True], [True, True, True, True, True, True, True],

[-0.7111, -4.3180, 3.8939, ..., -3.6111, 0.0440, 2.0282]])

Embed (glue) + apply matrix + add b1. Now apply a non-linear transformation like hyperbolic tangent.

```
[463]: # first layer

# https://pytorch.org/docs/stable/generated/torch.tanh.html

h = torch.tanh(emb.view(-1, 6) @ W1 + b1)
```

```
[464]: print(h)
```

Second layer must take in 100D vector and give out a 28D vector.

```
[465]: # second layer

W2 = torch.randn((100, 28))
b2 = torch.randn(28)
```

h is coming out from the first layer, then we feed with h the layer here.

```
[466]: logits = h @ W2 + b2 print(logits.shape)
```

torch.Size([41, 28])

Logits means log of the counting...

```
[467]: counts = logits.exp()
```

Normalize to interpret this as a measure, i.e. a probability distribution coming out from the network when fed with three chars.

```
[468]: prob = counts / counts.sum(1, keepdims=True)
```

```
[469]: print(prob[0])
    print(prob[0].sum())
    print(prob[0, 1])
    print(prob[[0, 1], [2, 5]])
```

```
tensor([9.7717e-07, 1.1903e-09, 1.1622e-03, 1.3884e-04, 1.2119e-07, 1.4373e-08, 3.7337e-08, 5.9759e-07, 4.1920e-10, 1.5534e-08, 9.1641e-01, 4.8512e-11, 6.0606e-07, 1.0638e-03, 9.7434e-06, 3.2012e-06, 3.8229e-08, 1.5657e-07,
```

```
3.3748e-03, 1.0385e-06, 2.4357e-05, 6.0491e-09, 2.8107e-14, 7.6021e-12, 7.7808e-02, 1.6660e-08, 2.7311e-11, 9.1822e-10])
tensor(1.0000)
tensor(1.1903e-09)
tensor([1.1622e-03, 1.7094e-10])
```

Model is initialized with random weights, so it's making mistakes.

```
[470]: print(Y)
      print(torch.arange(41))
      print(prob[torch.arange(41), Y])
      tensor([ 2, 19, 8, 6, 15, 21, 16, 0, 8, 10, 16, 23, 2, 15, 15, 10, 15, 16,
              0, 13, 10, 4, 22, 19, 8, 2, 0, 6, 13, 23, 10, 19, 2, 0, 14, 2,
              19, 6, 15, 2, 0])
      tensor([0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17,
              18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35,
              36, 37, 38, 39, 40])
      tensor([1.1622e-03, 1.3647e-10, 1.2721e-10, 7.4825e-06, 4.3084e-15, 2.0606e-09,
              4.9061e-08, 5.3828e-07, 4.1920e-10, 7.6886e-08, 4.0766e-01, 1.1818e-09,
              2.8867e-08, 3.2134e-04, 5.7727e-05, 3.4768e-12, 1.0444e-11, 7.0611e-15,
              1.1958e-08, 1.0638e-03, 9.8603e-01, 5.7557e-09, 1.4726e-06, 7.5069e-07,
              5.9529e-17, 3.8195e-05, 4.3590e-09, 3.7337e-08, 1.0221e-06, 1.0162e-11,
              3.0114e-01, 4.2972e-04, 5.7576e-08, 1.1595e-06, 9.7434e-06, 1.8131e-09,
              6.9818e-13, 2.9324e-11, 1.8745e-15, 9.2900e-11, 6.4576e-09])
```

We, of course, want the model to predict the right answer. Probability going to one implies loss going to zero.

```
[471]: loss = - prob[torch.arange(41), Y].log().mean() print(loss) # very bad of course.....
```

tensor(17.5833)

Let's put things together. Parameters will contain all the objects we're going to change. Why is the embedding dimension 2? We'll try with 10... tanh 0 = 0 and that will be important.

```
[472]: g = torch.Generator().manual_seed(123456780) # for reproducibility
C = torch.randn((28, 2), generator=g)
W1 = torch.randn((6, 100), generator=g)
b1 = torch.randn(100, generator=g)
W2 = torch.randn((100, 28), generator=g)
b2 = torch.randn(28, generator=g)
parameters = [C, W1, b1, W2, b2]
```

How many parameters are fixable?

```
[473]: print(sum(p.nelement() for p in parameters)) # number of parameter in total...
```

3584

For each sample I compute the $\log \rightarrow \text{high loss}$.

```
[474]: emb = C[X]  # torch.Size([41, 3, 2])
h = torch.tanh(emb.view(-1, 6) @ W1 + b1)  # (41,100)
logits = h @ W2 + b2  # (41,27)
counts = logits.exp()
prob = counts/counts.sum(1, keepdims=True)
loss = -prob[torch.arange(41), Y].log().mean()
print(loss)
```

tensor(17.2342)

Very efficient and can compute the exponential of big terms

```
[475]: print(F.cross_entropy(logits, Y))
```

tensor(17.2342)

Now the loss has to be minimized.

tensor(17.2342)

We'll use the cross entropy function because the exponentiation of just -500 will result in 0

```
[477]: # two very good reasons to use 'cross_entropy': more efficient (no tensor) and substract the maximum to avoid nan...discuss....

logits = torch.tensor([-5, -3, 0, 10]) # -100
counts = logits.exp()
prob = counts/counts.sum()
print(counts)
print(prob)
```

```
tensor([6.7379e-03, 4.9787e-02, 1.0000e+00, 2.2026e+04])
tensor([3.0589e-07, 2.2602e-06, 4.5398e-05, 9.9995e-01])
```

Put the gradient to zero, then compute the backward derivative and update all parameters in order to decrease the loss. 41 trigrams are going in layers, then calculate the loss.

Backward pass means compute the derivative of the loss for each parameter. It's a very complex stuff. We're not happy with back propagation but, by now, it's the only thing which works.

Learning rate -0.1 (negative direction). This is a magic number.

```
for p in parameters:
    p.requires_grad = True

for _ in range(1000):
    # now we learn...forward bass
    emb = C[X] # torch.Size([41, 3, 2])
    h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (41,100)
    logits = h @ W2 + b2 # (41,27)
    loss = F.cross_entropy(logits, Y)
    # backward pass
    for p in parameters:
        p.grad = None
    loss.backward()
    # update
    for p in parameters:
        p.data += -0.1*p.grad
```

Low loss means overfitting, then the model is going to give me one of the sample I provided. This is not useful at all.

```
[479]: # sampling from the model.....
       g = torch.Generator().manual_seed(12345678+10)
       for _ in range(20):
           out = []
           context = [0]*block_size
           while True:
               emb = C[torch.tensor([context])]
               h = torch.tanh(emb.view(1, -1) @ W1 + b1)
               logits = h @ W2 + b2
               probs = F.softmax(logits, dim=1)
               ix = torch.multinomial(probs, num_samples=1, generator=g).item()
               context = context[1:]+[ix]
               out.append(ix)
               if ix == 0:
                   break
           print(''.join(itos[i] for i in out))
```

```
elvira.
marena.
giovannino.
giovannino.
giovannino.
giovannino.
elvira.
marena.
```

```
argento.
argento.
elvira.
argento.
licurga.
licurga.
marena.
giovannino.
marena.
giovannino.
```

What is happening? Our model has gone in **overfitting**: it is spitting out the same names we put in, since we trained it only on those small samples (we've given it only 5 samples out of 7000+...)! So the loss is low enough now to sample, but of course our model is still useless. How can we fix this?

If we try to train the system with the whole data set (so that all the 41's are changed to the dimension of the dataset, that's the only change in the code) we fix the overfitting problem, but the algorithm will of course slow down in order to make the same calculations for such high dimensionality.

To fix this problem, we need to use **minibatches**.

```
[480]: for p in parameters:
           p.requires_grad = True
       for _ in range(1000):
           # now we learn...forward bass
           emb = C[X] # torch.Size([41, 3, 2])
           h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (41,100)
           logits = h @ W2 + b2 # (41,27)
           loss = F.cross_entropy(logits, Y)
           # print(loss.item())
           # backward pass
           for p in parameters:
               p.grad = None
           loss.backward()
           # update
           for p in parameters:
               p.data += -0.1*p.grad
       print(loss.item())
```

0.19916315376758575

Logits are the neurons coming out from the last layer. They'll be transformed into probability.

```
[481]: print(logits.max(1)) print(Y)
```

Taking all words we get a very big example dataset.

```
[483]: print(X.shape, Y.shape)
```

torch.Size([73643, 3]) torch.Size([73643])

Again, a hidden layer of 100 neurons.

```
[484]: # exactly as before....
g = torch.Generator().manual_seed(123456780) # for reproducibility
C = torch.randn((28, 2), generator=g)
W1 = torch.randn((6, 100), generator=g)
b1 = torch.randn(100, generator=g)
W2 = torch.randn((100, 28), generator=g)
b2 = torch.randn(28, generator=g)
parameters = [C, W1, b1, W2, b2]
```

```
[485]: for p in parameters:
           p.requires_grad = True
       for _ in range(10):
           # now we learn...forward bass -- = 73643
           emb = C[X] \# torch.Size([--, 3, 2])
           h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--, 100)
           logits = h @ W2 + b2 # (--,27)
           loss = F.cross_entropy(logits, Y)
           print(loss.item())
           # backward pass
           for p in parameters:
               p.grad = None
           loss.backward()
           # update
           for p in parameters:
               p.data += -0.1*p.grad
      17.754497528076172
      15.824398040771484
      14.187443733215332
      13.052313804626465
      12.071905136108398
      11.263842582702637
      10.603142738342285
      10.075033187866211
      9.627379417419434
      9.222493171691895
      See how it's slowing down... Every time we give all samples to it. Let's subdivide the dataset in
      minibatches.
[486]: \# try ix=torch.randint(0,X.shape[0],(10,2)) and explain
       ix = torch.randint(0, X.shape[0], (10,))
       # https://pytorch.org/docs/stable/generated/torch.randint.html
       print(ix)
      tensor([65739, 57246, 73039, 50426, 60229, 1076, 10994, 71617, 42058, 29497])
      Weird things happen with PyTorch...
[487]: ix = torch.randint(0, X.shape[0], (10, 1))
       print(ix)
      tensor([[57686],
               [8590],
               [18991],
               [31694],
               [56747],
```

```
[36820],
               [19621],
               [15325],
               [65718],
               [48395]])
[488]: for _ in range(10):
           # mini batch construct of size ...
           ix = torch.randint(0, X.shape[0], (32,))
           # now we learn...forward bass -- = 73643
           emb = C[X[ix]] # torch.Size([--, 3, 2])
           h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--,100)
           logits = h @ W2 + b2 # (--,27)
           loss = F.cross_entropy(logits, Y[ix])
           print(loss.item())
           # backward pass
           for p in parameters:
               p.grad = None
           loss.backward()
           # update
           for p in parameters:
               p.data += -0.1*p.grad
       print(loss.item())
      9.076169967651367
      8.107839584350586
      7.53472900390625
      8.057098388671875
      9.006769180297852
      6.839514255523682
      6.016563415527344
      7.071707725524902
      6.523996353149414
      6.122567653656006
      6.122567653656006
      Learning rate specifies how I move through gradient. Using 10, the system got completely lost (too
      big jumps).
[489]: | # how we define the 'learning rate' ? p.data += -0.1*p.grad
       # play with learning rate from .01 to 100.... and discuss
[490]: for _ in range(1000):
           # mini batch construct
           ix = torch.randint(0, X.shape[0], (100,))
           # now we learn...forward bass -- = 73643
           emb = C[X[ix]] # torch.Size([--, 3, 2])
```

h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--, 100)

```
logits = h @ W2 + b2 # (--,27)
loss = F.cross_entropy(logits, Y[ix])
# print(loss.item())
# backward pass
for p in parameters:
    p.grad = None
loss.backward()
# update
for p in parameters:
    p.data += -.1*p.grad
print(loss.item())
```

2.3013787269592285

```
[491]: lre = torch.linspace(-3, 0, 1000)
lrs = 10**lre # from 10**-3 to 10**0 = 1. The exponents are linearly_
distributed, not the values
print(lrs.shape)
```

torch.Size([1000])

```
[492]: for p in parameters:
           p.requires_grad = True
       lri = []
       lriex = []
       lossi = []
       for i in range(1000):
          # mini batch construct
           ix = torch.randint(0, X.shape[0], (100,))
           # now we learn...forward bass -- = 73643
           emb = C[X[ix]] # torch.Size([--, 3, 2])
           h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--,100)
           logits = h @ W2 + b2 # (--,27)
           loss = F.cross_entropy(logits, Y[ix])
           # backward pass
           for p in parameters:
               p.grad = None
           loss.backward()
           # update
           lr = lrs[i]
           # lr= .01
           for p in parameters:
               p.data += -lr*p.grad
```

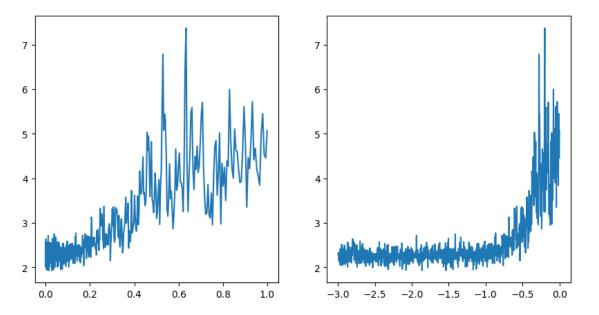
```
# track stats
    lri.append(lr) # learning rate
    lriex.append(lre[i]) # exponent
    lossi.append(loss.item()) # loss function
print(loss.item())
```

5.072561264038086

Plotting the loss function we notice that it's growing... not good.

```
[493]: fig, ax = plt.subplots(1, 2, figsize=(10, 5))
ax[0].plot(lri, lossi)
ax[1].plot(lriex, lossi)
```

[493]: [<matplotlib.lines.Line2D at 0x7f0c8eb10520>]



What is happening to the loss? There are some values of the learning rate which do better for our loss function than others. Also, it's very much fluctuating: there is a brilliant solution for this problem which we will see later on.

Usually, the convention with the training data is to have it split into 80% to train, a 10% to validate the hyperparameters and then a final 10% to keep there and use only once to see if the Neural Network is actually doing good.

How to validate that the network is doing something good? It may seem good while being completely wrong. We should have a test set of data to use when the hyperparameters are fixed.

```
[494]: emb = C[X] # torch.Size([41, 3, 2])
h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (41,100)
logits = h @ W2 + b2 # (41,27)
loss = F.cross_entropy(logits, Y)
print(loss)
```

tensor(4.5317, grad_fn=<NllLossBackward0>)

Typically, data are divided into 80-10-10 part (test/tune/validation) This function shuffles the words and builds the three wanted datasets.

First let's define the function build dataset.

```
[495]: # be careful with the test eugene.....
       def build_dataset(words):
           block size = 3 # context length: how many characters do we take to predict,
        →the next one ... change it !!
           X, Y = [], [] # input & label
           for w in words:
               context = [0]*block_size
               for ch in w + '.':
                   ix = stoi[ch]
                   X.append(context)
                   Y.append(ix)
             # print(''.join(itos[i] for i in context), '--->', itos[ix])
                   context = context[1:]+[ix] # shift: crop and append
           X = torch.tensor(X)
           Y = torch.tensor(Y)
           print(X.shape, Y.shape)
           return X, Y
```

```
[496]: import random
  random.seed(42)
  random.shuffle(words)
  n1 = int(0.8*len(words))
  n2 = int(0.9*len(words))

Xtr, Ytr = build_dataset(words[:n1]) # train
  Xdev, Ydev = build_dataset(words[n1:n2]) # tune hyperparameters
  Xte, Yte = build_dataset(words[n2:]) # validate
```

```
torch.Size([58867, 3]) torch.Size([58867])
torch.Size([7404, 3]) torch.Size([7404])
torch.Size([7372, 3]) torch.Size([7372])
```

```
[497]: # and we do it again with the new datasets......
       print(Xtr.shape, Ytr.shape)
       # exactly as before....
       g = torch.Generator().manual_seed(123456780) # for reproducibility
       C = torch.randn((28, 2), generator=g)
       W1 = torch.randn((6, 100), generator=g)
       b1 = torch.randn(100, generator=g)
       W2 = torch.randn((100, 28), generator=g)
       b2 = torch.randn(28, generator=g)
       parameters = [C, W1, b1, W2, b2]
      torch.Size([58867, 3]) torch.Size([58867])
[498]: for p in parameters:
           p.requires_grad = True
       lre = torch.linspace(-3, 0, 1000)
       lrs = 10**lre
[499]: # now we train only on Xtr
       lri = []
       lriex = \Pi
       lossi = ∏
       for i in range(10000):
           # mini batch construct
           ix = torch.randint(0, Xtr.shape[0], (40,))
           # now we learn...forward bass -- = 73643
           emb = C[Xtr[ix]] # torch.Size([--, 3, 2])
           h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--, 100)
           logits = h @ W2 + b2 # (--,27)
           loss = F.cross_entropy(logits, Ytr[ix])
          # print(i,loss.item())
           # backward pass
           for p in parameters:
               p.grad = None
           loss.backward()
           # update
           # lr=lrs[i]
           lr = .1
           for p in parameters:
               p.data += -lr*p.grad
       print(loss.item())
```

```
# track stats
# lri.append(lr)
# lriex.append(lre[i])
# lossi.append(loss.item())
```

2.018704652786255

Now evaluate on the validation test (and also on the test).

```
[500]: # now we evaluate on Xdev
emb = C[Xdev]
h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--,100)
logits = h @ W2 + b2 # (--,27)
loss = F.cross_entropy(logits, Ydev)
print(loss.item())
```

2.1819050312042236

```
[501]: # now we evaluate on Xtr.... we are NOT overfitting
emb = C[Xtr]
h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--,100)
logits = h @ W2 + b2 # (--,27)
loss = F.cross_entropy(logits, Ytr)
print(loss.item())
```

2.172853708267212

So now we know that our model has a low loss **and** we are not overfitting, my system is able to reproduce not only the data I show it in the training but also other data it has never seen before. Nice...

Now we can change the hyperparameters: this is a very simple case, so it's not going to change much, but still we do it for pedagogical reasons. Even in such a simple model, changing the hyperparameters makes our parameters go from ~ 3000 to ~ 10000 . Let's take a look at what happens now to the loss...

```
[502]: g = torch.Generator().manual_seed(123456780) # for reproducibility
C = torch.randn((28, 2), generator=g)
W1 = torch.randn((6, 300), generator=g)
b1 = torch.randn(300, generator=g)
W2 = torch.randn((300, 28), generator=g)
b2 = torch.randn(28, generator=g)
parameters = [C, W1, b1, W2, b2]
```

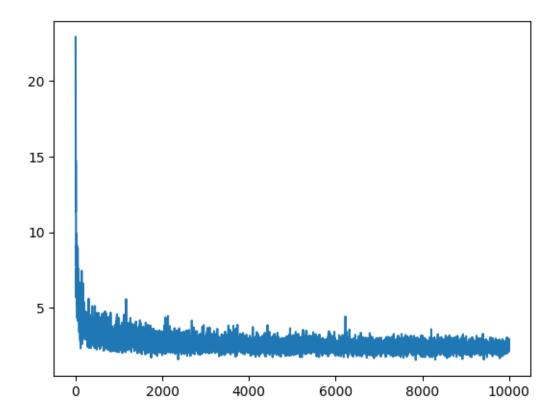
```
[503]: # number of parameter in total... before 3584
print(sum(p.nelement() for p in parameters))
```

10584

```
[504]: | lri = []
       lriex = []
       lossi = []
       stepi = []
       for p in parameters:
           p.requires_grad = True
       for i in range(10000):
          # mini batch construct
           ix = torch.randint(0, Xtr.shape[0], (40,))
           # now we learn...forward bass -- = 73643
           emb = C[Xtr[ix]] # torch.Size([--, 3, 2])
           h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--,100)
           logits = h @ W2 + b2 # (--,27)
           loss = F.cross_entropy(logits, Ytr[ix])
           # backward pass
           for p in parameters:
               p.grad = None
           loss.backward()
           # update
           # lr=lrs[i]
           lr = .1
           for p in parameters:
              p.data += -lr*p.grad
           stepi.append(i)
           lossi.append(loss.item())
```

```
[505]: plt.plot(stepi, lossi)
```

[505]: [<matplotlib.lines.Line2D at 0x7f0cb9541de0>]



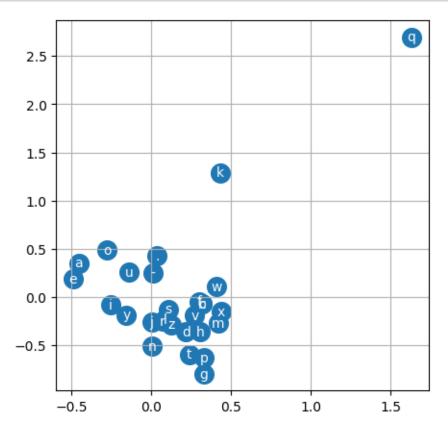
We can see how the loss starts very high and then decreases very much with training, but still it is fluctuating: this shouldn't be very surprising, since even with training our model is based on random number and processes, so fluctuations are guaranteed. But as we said before, there is a nice way to reduce these fluctuations, which is called **batch normalization**.

This is a transformation we make our data undergo in order to have a "gaussian" activity of our neurons. In this way we avoid 2 things: 1. we avoid our neurons' activity being too high, i.e. we do not want values which would mostly fall into the plateaus of our hyperbolic tangent and thus cause the "freezing" of our neurons, i.e. their inability to learn, since their output would always be +1 or -1 and no in between; 2. we avoid large fluctuations in our data, since gaussian data fluctuations scale as we know with $\frac{1}{\sqrt{N}}$ where N is the number of samples. Such transformation is (roughly speaking) just gaussian normalization of data (actually there are more complex operations going on in the batch-normalization functions of libraries like PyTorch, and we actually do not know much about the precise statistical effectiveness of such processes, we use them as kind of "black box"), before feeding them to the linear layer, i.e. data are normalized before the hyperbolic tangent application. This means that we take the sample mean of our data $\bar{x} = \sum_i^N \frac{x_i}{N}$, compute the sample standard deviation σ_s and then transform each point x of our set by

$$x \longrightarrow \frac{x - \bar{x}}{\sigma_s}$$

We will use batch normalization later on.

Now we can visualize the result of the embedding. The letters are clustered, e.g. vowels are clustered.



Now increase to 10 the embedding dimension...

```
[507]: g = torch.Generator().manual_seed(123456780) # for reproducibility
C = torch.randn((28, 10), generator=g)
W1 = torch.randn((30, 200), generator=g)
b1 = torch.randn(200, generator=g)
W2 = torch.randn((200, 28), generator=g)
b2 = torch.randn(28, generator=g)
parameters = [C, W1, b1, W2, b2]
```

[508]: print(sum(p.nelement() for p in parameters)) # number of parameter in total

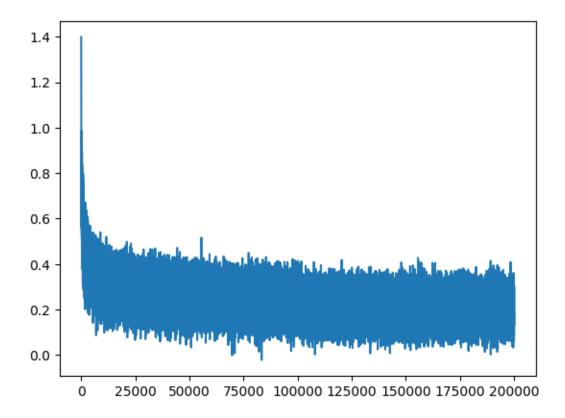
12108

Now change the learning rate...

```
[510]: for i in range(200000):
           # mini batch construct
          ix = torch.randint(0, Xtr.shape[0], (40,))
           # now we learn...forward bass -- = 73643
          emb = C[Xtr[ix]] # torch.Size([--, 3, 2])
          h = torch.tanh(emb.view(-1, 30) @ W1 + b1) # (--,100)
          logits = h @ W2 + b2 # (--,27)
          loss = F.cross_entropy(logits, Ytr[ix])
          # backward pass
          for p in parameters:
              p.grad = None
          loss.backward()
          # update
          lr = .1 if i < 100000 else 0.01
          for p in parameters:
              p.data += -lr*p.grad
          stepi.append(i)
          lossi.append(loss.log10().item()) # note the log10 !!
```

```
[511]: plt.plot(stepi, lossi)
```

[511]: [<matplotlib.lines.Line2D at 0x7f0cbbff3b50>]



We're doing well and not overfitting.

```
[512]: emb = C[Xtr]
h = torch.tanh(emb.view(-1, 30) @ W1 + b1) # (--,100) 30 not 6 !
logits = h @ W2 + b2 # (--,27)
loss = F.cross_entropy(logits, Ytr)
print(loss.item())
```

1.6529531478881836

```
[513]: emb = C[Xdev]
h = torch.tanh(emb.view(-1, 30) @ W1 + b1) # (--,100)
logits = h @ W2 + b2 # (--,27)
loss = F.cross_entropy(logits, Ydev)
print(loss.item())
```

1.8500275611877441

Once trained the model we can sample from it. **NOTE**: there are many (many many) hyperparameters to play with, like the number of layer, numbers of neurons from layers, embedding dimensions, dimension of the batches, learning rate....

We can now see words that are not in the dataset.

```
[514]: # g = torch.Generator().manual_seed(12345678+10)

for _ in range(30):
    out = []
    context = [0]*block_size
    while True:
        emb = C[torch.tensor([context])]
        h = torch.tanh(emb.view(1, -1) @ W1 + b1)
        logits = h @ W2 + b2
        probs = F.softmax(logits, dim=1)
        ix = torch.multinomial(probs, num_samples=1, generator=g).item()
        context = context[1:]+[ix]
        out.append(ix)
        if ix == 0:
            break

        print(''.join(itos[i] for i in out))
```

```
ade.
galdina.
crescenzu.
erto.
marinanto.
divia.
deciano.
ermiro.
dircolo.
arleolomurita.
gusina.
ristofelastrrino.
chrica.
mea.
pina.
pedermen.
ave.
alimolando.
gertaudino.
speramina.
orlino.
orlide.
venzion-idalma.
is.
asdina.
clemiglia.
zelminio.
brunino.
esio.
```

doluttunaa.

Not bad! We see names that were not in the original dataset, and much more "name-like" than the previous examples.

3 Concatenated Network - MakeMore pt.3 (21/04/2023)

We are now ready to move on to Multilayer Perceptrons models: in order to do it we are going to reproduce the results of an "old" paper.

We are going to see the procedure of **embedding**, which is one of the most powerful tools in Neural Networks architectures: basically, we choose to encode (randomly at the beginning) our words into vectors in a euclidean space of a certain dimension (there are no general rules to choose such dimension), and see how with training our network clusterizes automatically the words. In our case we are actually going to see it working on just characters instead of words. As a matter of fact, we are going to consider a 3—gram approximation of our language model.

We have as input the characters at time t-1, t-2 and t-3 (we are considering tri-grams) which get embedded by a matrix C in a 30-dimensional vector as chosen by the authors of the paper. Then we put together these three 30-dimensional vectors to get a 90-dimensional one. We feed this vector to an intermediate layer with a nonlinear transformation (tanh). The output of such "hidden" layer gets then fed to a last layer which linearly transforms it by $\hat{W} \cdot \vec{x} + \hat{B}$.

We will see that there are many parameters in such system: the coefficients in the embedding matrix C and the matrix W, which will change with training in order to minimize the loss, but also some numbers which we a priori choose, which define the structure of our Multi-Layer Perceptron. For example, the dimension of the embedding, or the gradient descent rate. These are the so-called hyperparameters.

```
[2]: # https://youtu.be/P6sfmUTpUmc
# https://github.com/karpathy/makemore
```

```
[3]: # we now want to dig more into neural activity and learning to understand the ∴RNN and LSTM architecture and properties...

import random import torch import torch.nn.functional as F import matplotlib.pyplot as plt #for making figures %matplotlib inline
```

```
[5]: # read in all the words
random.seed(158)
words = open("data/nomi_italiani.txt", "r").read().splitlines()
random.shuffle(words)
words[0:8]
```

```
[5]: ['argento', 'giovannino',
```

```
'licurga',
      'elvira',
      'marena',
      'sirio',
      'emilia',
      'bisio']
[6]: print(len(words))
    9105
[7]: # build the vocabulary of characters and mapping to/from integers
     chars = sorted(list(set("".join(words))))
     stoi = {s: i + 1 for i, s in enumerate(chars)}
     stoi["."] = 0
     itos = {i: s for s, i in stoi.items()}
     vocab_size = len(itos)
     print(itos)
    print(vocab_size)
    {1: '-', 2: 'a', 3: 'b', 4: 'c', 5: 'd', 6: 'e', 7: 'f', 8: 'g', 9: 'h', 10:
    'i', 11: 'j', 12: 'k', 13: 'l', 14: 'm', 15: 'n', 16: 'o', 17: 'p', 18: 'q', 19:
    'r', 20: 's', 21: 't', 22: 'u', 23: 'v', 24: 'w', 25: 'x', 26: 'y', 27: 'z', 0:
    '.'}
    28
[8]: # build the dataset
     block_size = (
         # context length: how many characters do we take to predict the next one ...
         3
     def build_dataset(words):
        X, Y = [], [] # input & label
         for w in words:
             context = [0] * block_size
             for ch in w + ".":
                 ix = stoi[ch]
                 X.append(context)
                 Y.append(ix)
                 # print(''.join(itos[i] for i in context), '--->', itos[ix])
                 context = context[1:] + [ix] # shift: crop and append
```

```
X = torch.tensor(X)
Y = torch.tensor(Y)
print(X.shape, Y.shape)
return X, Y
```

```
[9]: import random

random.seed(42)
random.shuffle(words)
n1 = int(0.8 * len(words))
n2 = int(0.9 * len(words))

Xtr, Ytr = build_dataset(words[:n1])
Xdev, Ydev = build_dataset(words[n1:n2])
Xte, Yte = build_dataset(words[n2:])
```

```
torch.Size([58867, 3]) torch.Size([58867])
torch.Size([7404, 3]) torch.Size([7404])
torch.Size([7372, 3]) torch.Size([7372])
```

We now construct the first layer: the input of such layer will have dimension $3 \cdot 2 = 6$, i.e. the multiplied dimension of the *n*-gram and the embedding dimension. We will consider 100 neurons (another hyperparameter).

```
[10]: # MLP revisited
    n_embd = 10  # the dimensionality of the character embedding vectors
    n_hidden = 200  # the number of neurons in the hidden layer of MLP

g = torch.Generator().manual_seed(123456780)  # for reproducibility
C = torch.randn((vocab_size, n_embd), generator=g)
W1 = torch.randn((n_embd * block_size, n_hidden), generator=g)  # neurons
b1 = torch.randn(n_hidden, generator=g)  # bias
W2 = torch.randn((n_hidden, vocab_size), generator=g)
b2 = torch.randn(vocab_size, generator=g)
parameters = [C, W1, b1, W2, b2]
print(sum(p.nelement() for p in parameters))  # number of parameter in total...
for p in parameters:
    p.requires_grad = True
```

12108

Now we would like to compute the product $emb \cdot W1 + b1$. But emb has a different dimension (or shape) with regard to W1: we need to **concatenate** the elements of emb in order to get the same dimension. Now, there would be many ways to do this: with PyTorch we have the function cat (together with unbind) which could do the work for us... but there is actually a much less time-costing way.

As a matter of fact, PyTorch has a built-in method *view* which re-organizes the elements of a tensor in the shape we choose: and it does this operation just (roughly) re-arranging the allocated

memory for each term, and not allocating new memory: therefore this is far more efficient than using other PyTorch functions. This is what we are going to use.

```
[11]: # same optimization as last time
      max_steps = 200000
      batch_size = 32
      lossi = []
      for i in range(max_steps):
          # mini batch construct
          ix = torch.randint(0, Xtr.shape[0], (batch_size,), generator=g)
          Xb, Yb = Xtr[ix], Ytr[ix] # batch X, Y
          # forward bass
          emb = C[Xb] # embed characters into vectors
          embcat = emb.view(emb.shape[0], -1) # concatenate the vectors
          hpreact = embcat @ W1 + b1 # hidden layer pre-activation
          h = torch.tanh(hpreact) # hidden layer
          logits = h @ W2 + b2 # output layer
          loss = F.cross_entropy(logits, Yb) # loss function
          # backward pass
          for p in parameters:
              p.grad = None
          loss.backward()
          # update
          lr = 0.1 if i < 100000 else 0.01 # step learning rate decay</pre>
          for p in parameters:
              p.data += -lr * p.grad
          # track stats
          if i % 10000 == 0: # print every once in a while
              print(f"{i:7d}/{max_steps:7d}:{loss.item():.4f}")
          lossi.append(loss.log10().item())
```

```
0/ 200000:25.2234
10000/ 200000:2.2865
20000/ 200000:2.1045
30000/ 200000:2.1319
40000/ 200000:1.8164
50000/ 200000:1.8491
70000/ 200000:1.9464
80000/ 200000:1.9799
90000/ 200000:2.3608
100000/ 200000:1.3078
```

```
110000/ 200000:1.9567

120000/ 200000:1.5188

130000/ 200000:1.7088

140000/ 200000:2.0892

160000/ 200000:1.2948

170000/ 200000:1.3657

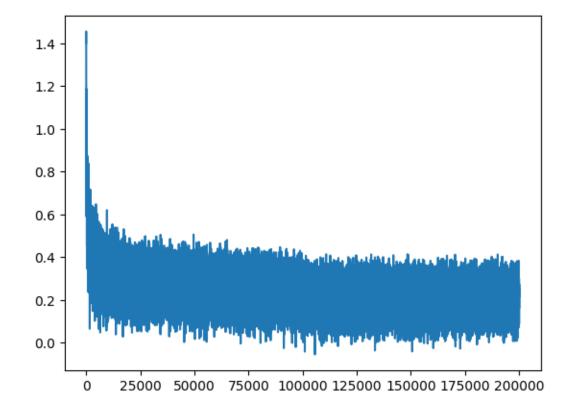
180000/ 200000:1.7789

190000/ 200000:1.5764

[12]: print(-torch.tensor(1 / 28).log())

tensor(3.3322)

[14]: plt.plot(lossi)
```



```
[15]: # this decorator disables gradient tracking....discuss in class....
@torch.no_grad()
def split_loss(split):
    x, y = {
        "train": (Xtr, Ytr),
        "val": (Xdev, Ydev),
```

```
"test": (Xte, Yte),
}[split]
emb = C[x] # (N,block_size, n_embd)
embcat = emb.view(emb.shape[0], -1) # concat into (N,block_size*n_embd)
hpreact = embcat @ W1 + b1 # hidden layer pre-activation
h = torch.tanh(hpreact) # hidden layer (N, h_hidden)
logits = h @ W2 + b2 # output layer (N, vocab_size)
loss = F.cross_entropy(logits, y) # loss function
print(split, loss.item())
```

```
[16]: split_loss("train")
split_loss("val")
```

train 1.6465035676956177 val 1.8481979370117188

```
[17]: # sampling from the model.....
      g = torch.Generator().manual_seed(12345678 + 10)
      for _ in range(20):
          out = []
          context = [0] * block_size
          while True:
              emb = C[torch.tensor([context])] # (1,block_size,n_embed)
              h = torch.tanh(emb.view(1, -1) @ W1 + b1)
              logits = h @ W2 + b2
              probs = F.softmax(logits, dim=1)
              # sample from the distribuion
              ix = torch.multinomial(probs, num_samples=1, generator=g).item()
              # shift the context window and track the samples
              context = context[1:] + [ix]
              out.append(ix)
              # if we sample the special '.' token, break
              if ix == 0:
                  break
          print("".join(itos[i] for i in out)) # decode and print the generated word
```

albo.
giovanno.
rizio.
siside.
polina.
gio.
assimo.
cecchiarosinda.

```
benuartinaippirenziana.
     peppio.
     abdocchia.
     bella.
     benio.
     moheo.
     lauretilla.
     rinieronino.
     filosca.
     esaro.
     euto.
     giliana.
[21]: # let us focus on the last layer ....logits and then softmax
      logits = torch.randn(4) * 100
      # logits = view(2, 2, 2, 20)
      probs = torch.softmax(logits, dim=0)
      loss = -probs[2].log()
      print("logits:", logits)
      print("probs:", probs)
      print("loss:", loss)
     logits: tensor([-14.4960, -31.7004, 124.3944, 179.8049])
     probs: tensor([0.0000e+00, 0.0000e+00, 8.6204e-25, 1.0000e+00])
     loss: tensor(55.4105)
[22]: # back to our examples and look at the logit just after the first pass and
       understand normalization....
      # MLP revisited
      n_{embd} = 10 # the dimensionality of the character embedding vectors
      n_hidden = 200 # the number of neurons in the hidden layer of MLP
      g = torch.Generator().manual_seed(123456780) # for reproducibility
      C = torch.randn((vocab_size, n_embd), generator=g)
      W1 = torch.randn((n_embd * block_size, n_hidden), generator=g) # *0.20
      b1 = torch.randn(n_hidden, generator=g) # *0.01
      W2 = torch.randn((n_hidden, vocab_size), generator=g) # *0.01
      b2 = torch.randn(vocab_size, generator=g) # *0
      parameters = [C, W1, b1, W2, b2]
      print(sum(p.nelement() for p in parameters)) # number of parameter in total...
      for p in parameters:
          p.requires_grad = True
```

```
[23]: |# same optimization as last time...try, look at logits then go up and change W2_{\square}
       ⇔and b2 normalization....
      \max \text{ steps} = 200000
      batch size = 32
      lossi = ∏
      for i in range(max_steps):
          # mini batch construct
          ix = torch.randint(0, Xtr.shape[0], (batch_size,), generator=g)
          Xb, Yb = Xtr[ix], Ytr[ix] # batch X,Y
          # forward bass
          emb = C[Xb] # embed characters into vectors
          embcat = emb.view(emb.shape[0], -1) # concatenate the vectors
          hpreact = embcat @ W1 + b1 # hidden layer pre-activation
          h = torch.tanh(hpreact) # hidden layer
          logits = h @ W2 + b2 # output layer
          loss = F.cross_entropy(logits, Yb) # loss function
          # backward pass
          for p in parameters:
              p.grad = None
          loss.backward()
          # update
          lr = 0.1 if i < 100000 else 0.01 # step learning rate decay
          for p in parameters:
              p.data += -lr * p.grad
          # track stats
          if i % 10000 == 0: # print every once in a while
              print(f"{i:7d}/{max_steps:7d}:{loss.item():.4f}")
          lossi.append(loss.log10().item())
          break
           0/ 200000:25.2234
```

```
[26]: print(
    logits[1]
) # confidently wrong... but with weight is better... 'squashing down the
    →neurons...'
```

```
tensor([ 10.6530, -7.2423, 31.2924, -15.8263, 7.0554, -0.8957, 10.4593, 8.9841, 13.3143, -2.6116, 14.7497, 17.5647, 17.0676, 1.1002, 14.7031, -13.5323, -19.1125, -21.7921, 21.1479, 8.6535, 7.4713, -3.2913, 3.2052, 1.8503, 12.2664, -3.8606, 3.1228, 4.6715],
```

grad_fn=<SelectBackward0>)

```
[29]: # Now we focus on the first layer (show pict): h & hpreact

# remember to intialize and run again

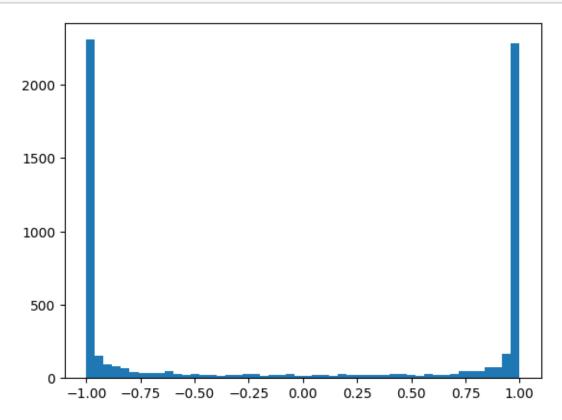
# look at the +- 1 in h
print(h.shape)
```

torch.Size([32, 200])

[28]: print(len(h.view(-1).tolist())) # 32*200

6400

[30]: plt.hist(h.view(-1).tolist(), 50)
a lot of neurons are 'saturated'

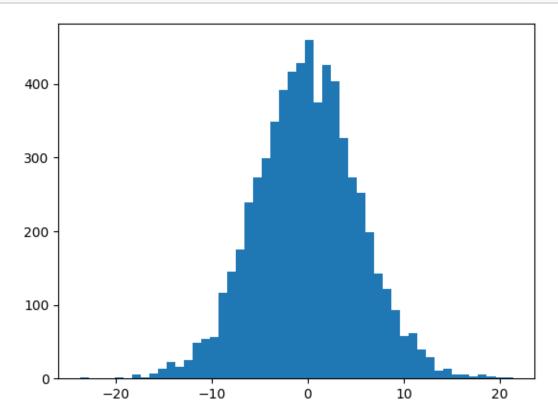


```
[31]: # now look at the "broad" shape of the 'hpreact' distribution....and this is_bad for learning...we want 'normality' for our brain...

# tgh'(x) = (1-tgh(x)^2).... saturation bring to vanish gradient...no learning...

plt.hist(hpreact.view(-1).tolist(), 50)

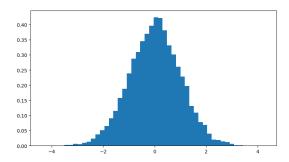
# a lot of neurons are ' saturated'
```

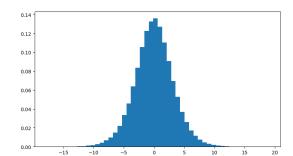




```
[34]: # why we do not to have to worry too much about inizialization....bach
       \hookrightarrow normalization..
      # since 2015
      # https://arxiv.org/abs/1502.03167
      # if the problems are fluctuations and saturations (discuss in class)...then_{f U}
       ⇒just gaussain normalize at each layer...
      # simple as that !!!...and normalizing is differentiable !!....
      x = torch.randn(1000, 10)
      w = torch.randn(10, 200) # *.2 #*1/10**0.5
      y = x @ w
      print(y.shape)
      print(x.mean(), x.std())
      print(y.mean(), y.std())
      plt.figure(figsize=(20, 5))
      plt.subplot(121)
      plt.hist(x.view(-1).tolist(), 50, density=True)
      plt.subplot(122)
      plt.hist(y.view(-1).tolist(), 50, density=True)
```

```
torch.Size([1000, 200])
tensor(0.0148) tensor(0.9958)
tensor(-0.0002) tensor(3.1940)
```





4 Convolutional Network - MakeMore pt.4 (28/04/2023)

For real the 4th was about back propagation, but we skip it in this course. For the final exam one may go deeper into this algorithm, maybe by hand.

Last time we implemented a multilayer perceptron (with actually two layers), working at character level and building a probability distribution. The pipeline was: - embedding (2 - 10 dimensional vectors) - glue them together, but this is not the best thing one can do

Instead of looking at 3 previous char we can look at 8 previous char and so on... We'll see it doesn't change much. Idea: feed the net with information in a hierarchical way. Notice that we'll work with text, but we can expand this also to images. We want to construct a convolution network,

even if it's not related to the mathematical definition of convolution. Glue chars together, giving it to a layer, process, glue another char and give to the next layer and so on. The line behind all this is entropy, we skip the compression algorithm for lack of time. Probability distribution, entropy and compression are actually the same thing.

```
[1]: # now we want to enlarge the context length AND ''fuse information in au

hierarchical manner''

# see the approach in https://arxiv.org/abs/1609.03499
```

```
[2]: # The importance of embedding

# word2vec: skip-gram https://arxiv.org/pdf/1301.3781v3.pdf

# node2vec: https://arxiv.org/pdf/1607.00653.pdf
```

Data are not always linear, or a lattice, or on a euclidean space... Things are complicated. However, for some phenomena, they're naturally distributed in networks (or if you want, graph). The main concepts are neighbors, distances... As we can handle text we can handle images, which are just euclidean spaces.

This field is going extremely fast, keep going!

We deal with real numbers which can be positive, negative, very big, very small... The hyperbolic tangent help us to squeeze them. Otherwise, the neurons won't learn. There is still a lot to understand there... Take it as it is, $e \ più \ non \ dimandare$. Actually, there are many ways to squeeze without the hyperbolic tangent, but the meaning is the same.

We'll assume batch normalization and focus on the method. We'll hierarchically glue 8 char together. See also WaveNet for audio generation. We want to pass from $2+2+2 \rightarrow 6$ to $2 \rightarrow 3 \rightarrow ... \rightarrow 6$, i.e. gradually. Convolutional layers like this are very spread and useful for text analysis.

```
[3]: import random
import torch
import torch.nn.functional as F
import torch.nn as nn
import matplotlib.pyplot as plt
%matplotlib inline
```

```
[4]: # read in all the words
random.seed(158)
words = (
    open("data/nomi_italiani.txt", "r").read().splitlines()
) # each line is an element of the list
random.shuffle(words)
print(len(words))
print(words[0:8])
```

```
9105
['argento', 'giovannino', 'licurga', 'elvira', 'marena', 'sirio', 'emilia', 'bisio']
```

```
[5]: # build the vocabulary of characters and mappings to/from integers (encoder/
     ⇔decoder)
     chars = sorted(list(set("".join(words))))
     stoi = {s: i + 1 for i, s in enumerate(chars)}
     stoi["."] = 0
     itos = {i: s for s, i in stoi.items()}
     vocab size = len(stoi)
     print(itos)
    print(vocab_size)
    {1: '-', 2: 'a', 3: 'b', 4: 'c', 5: 'd', 6: 'e', 7: 'f', 8: 'g', 9: 'h', 10:
    'i', 11: 'j', 12: 'k', 13: 'l', 14: 'm', 15: 'n', 16: 'o', 17: 'p', 18: 'q', 19:
    'r', 20: 's', 21: 't', 22: 'u', 23: 'v', 24: 'w', 25: 'x', 26: 'y', 27: 'z', 0:
    '.'}
    28
[6]: # build the dataset
     block_size = 8 # 8 context length: how many characters do we take to predict
     →the next one?...start with 3!!
     def build dataset(words):
        X, Y = [], []
        for w in words:
             context = [0] * block_size
            for ch in w + ".":
                 ix = stoi[ch]
                 X.append(context)
                 Y.append(ix)
                 context = context[1:] + [ix] # crop and append
        X = torch.tensor(X)
        Y = torch.tensor(Y)
        print(X.shape, Y.shape)
        return X, Y
    n1 = int(0.8 * len(words))
    n2 = int(0.9 * len(words))
     Xtr, Ytr = build_dataset(words[:n1]) # 80%
     Xdev, Ydev = build_dataset(words[n1:n2]) # 10%
     Xte, Yte = build_dataset(words[n2:]) # 10%
    torch.Size([59049, 8]) torch.Size([59049])
    torch.Size([7332, 8]) torch.Size([7332])
    torch.Size([7262, 8]) torch.Size([7262])
```

```
[7]: for x, y in zip(Xtr[:20], Ytr[:20]):
         print("".join(itos[ix.item()] for ix in x), "-->", itos[y.item()])
    ... --> a
    ...a --> r
    ...ar --> g
    ...arg --> e
    ...arge --> n
    ...argen --> t
    ..argent --> o
    .argento --> .
    ... --> g
    ...g --> i
    ...gi --> o
    ...gio --> v
    ...giov --> a
    ...giova --> n
    ..giovan --> n
    .giovann --> i
    giovanni --> n
    iovannin --> o
    ovannino --> .
    ... --> 1
```

Let's do it in an object-oriented way. These things are already contained in PyTorch, so we don't need to write them by hand. All these classes are into _torch.nn.*_

```
[8]: # Near copy paste of the layers we have developed in Part 3
     # Comment on this! https://pytorch.org/docs/stable/nn.html
     # now just evaluate this then we will chage it and use torch functions!
     # all these definitions work as in PyTorch, but we won't use it as a black box
     #__
     class Linear:
         def __init__(self, fan_in, fan_out, bias=True):
             self.weight = (
                torch.randn((fan_in, fan_out)) / fan_in**0.5
             ) # note: kaiming init
             self.bias = torch.zeros(fan_out) if bias else None
         def __call__(self, x):
             self.out = x @ self.weight
             if self.bias is not None:
                 self.out += self.bias
             return self.out
```

```
def parameters(self):
        return [self.weight] + ([] if self.bias is None else [self.bias])
#__
class BatchNorm1d:
    def __init__(self, dim, eps=1e-5, momentum=0.1):
        self.eps = eps
        self.momentum = momentum
        self.training = True
        # parameters (trained with backprop)
        self.gamma = torch.ones(dim)
        self.beta = torch.zeros(dim)
        # buffers (trained with a running 'momentum update')
        self.running_mean = torch.zeros(dim)
        self.running_var = torch.ones(dim)
    def __call__(self, x):
        # calculate the forward pass
        if self.training:
            if x.ndim == 2:
                dim = 0
            elif x.ndim == 3:
                dim = (0, 1)
            xmean = x.mean(dim, keepdim=True) # batch mean
            xvar = x.var(dim, keepdim=True) # batch variance
        else:
            xmean = self.running_mean
            xvar = self.running_var
        # normalize to unit variance
        xhat = (x - xmean) / torch.sqrt(xvar + self.eps)
        self.out = self.gamma * xhat + self.beta
        # update the buffers
        if self.training:
            with torch.no_grad():
                self.running mean = (
                    1 - self.momentum
                ) * self.running_mean + self.momentum * xmean
                self.running_var = (
                    1 - self.momentum
                ) * self.running_var + self.momentum * xvar
        return self.out
    def parameters(self):
        return [self.gamma, self.beta]
```

```
#__
class Tanh:
   def __call__(self, x):
        self.out = torch.tanh(x)
        return self.out
    def parameters(self):
       return []
class Embedding:
    def __init__(self, num_embeddings, embedding_dim):
        self.weight = torch.randn((num_embeddings, embedding_dim))
    def __call__(self, IX):
        self.out = self.weight[IX]
        return self.out
    def parameters(self):
        return [self.weight]
#
class Flatten:
    def __init__(self, n):
        self.n = n
    def __call__(self, x):
        self.out = x.view(x.shape[0], -1)
        return self.out
    def parameters(self):
        return []
class FlattenConsecutive:
    def __init__(self, n):
        self.n = n
    def __call__(self, x):
```

```
B, T, C = x.shape
        x = x.view(B, T // self.n, C * self.n)
        if x.shape[1] == 1:
            x = x.squeeze(1)
        self.out = x
        return self.out
    def parameters(self):
        return []
#__
class Sequential:
    def __init__(self, layers):
        self.layers = layers
    def __call__(self, x):
        for layer in self.layers:
            x = layer(x)
        self.out = x
        return self.out
    def parameters(self):
        # get parameters of all layers and stretch them out into one list
        return [p for layer in self.layers for p in layer.parameters()]
```

```
[9]: torch.manual_seed(42)
```

[9]: <torch._C.Generator at 0x7f50c6067390>

C is our embedding matrix 28x10 which contains the 10 dimensional embedding for each of 28 chars. Context length is 3, multiply by 10 so 30 is the dimension of the input layer.

```
[10]: # original network https://jmlr.org/papers/volume3/tmp/bengio03a.pdf

n_embd = 10  # the dimensionality of the character embedding vectors
n_hidden = 200  # the number of neurons in the hidden layer of the MLP

C = torch.randn(vocab_size, n_embd)
layers = [
    Linear(n_embd * block_size, n_hidden, bias=False),
    BatchNorm1d(n_hidden),  # normalize, otherwise learning stops
    Tanh(),
    Linear(n_hidden, vocab_size),
]
```

```
# parameter initialization
with torch.no_grad():
    layers[-1].weight *= 0.1 # last layer make less confident

parameters = [C] + [p for layer in layers for p in layer.parameters()]
print(sum(p.nelement() for p in parameters)) # number of parameters in total
for p in parameters:
    p.requires_grad = True
```

```
[11]: # same optimization as last time
      \max \text{ steps} = 200000
      batch_size = 32
      lossi = []
      for i in range(max_steps):
          # minibatch construct
          ix = torch.randint(0, Xtr.shape[0], (batch_size,))
          Xb, Yb = Xtr[ix], Ytr[ix] # batch X, Y
          # forward pass
          emb = C[Xb] # embed the characters into vectors
          x = emb.view(
              emb.shape[0], -1
          ) # concatenate the vectors, view is not memory consuming
          for layer in layers:
              x = layer(x)
          loss = F.cross_entropy(x, Yb) # loss function
          # backward pass, now we're using our black box
          for p in parameters:
              p.grad = None
          loss.backward()
          # update: simple SGD
          lr = 0.1 if i < 150000 else 0.01 # step learning rate decay</pre>
          for p in parameters:
              p.data += -lr * p.grad
              # track stats
          if i % 10000 == 0: # print every once in a while
              print(f"{i:7d}/{max_steps:7d}: {loss.item():.4f}")
          lossi.append(loss.log10().item())
```

0/ 200000: 3.3371 10000/ 200000: 2.1734

```
20000/ 200000: 1.9819
 30000/ 200000: 1.6350
 40000/ 200000: 1.3981
 50000/ 200000: 1.6659
 60000/ 200000: 1.8349
 70000/ 200000: 1.6599
 80000/ 200000: 1.2059
 90000/ 200000: 1.6775
100000/ 200000: 1.3948
110000/ 200000: 1.3727
120000/ 200000: 1.7746
130000/ 200000: 1.5139
140000/ 200000: 1.3102
150000/ 200000: 1.4078
160000/ 200000: 1.3451
170000/ 200000: 1.2467
180000/ 200000: 1.4784
190000/ 200000: 1.3532
```

Why 3.3 at the beginning? Assuming all random, $-\log \frac{1}{28}$ is about that number...

NOTE that with 8 the decrease is very slow, we're fusing info too quickly!

Small batch implies fluctuating a lot, so we can use view to split in pieces of one thousand.

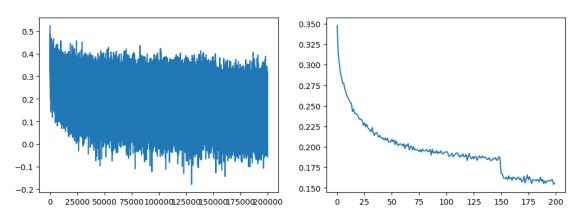
```
[12]: print(-torch.tensor(1 / 28).log())
# 32 batches are few... so you can get very lucky or unlucky

fig, ax = plt.subplots(ncols=2, figsize=(12, 4))

ax[0].plot(torch.tensor(lossi))
ax[1].plot(torch.tensor(lossi).view(-1, 1000).mean(1)) # mean on each row
```

tensor(3.3322)

[12]: [<matplotlib.lines.Line2D at 0x7f4ff1b2c1c0>]



But look now at the first plot of the loss function. It's very bad, but why? Because a size of 32 is very small for our batches, therefore we have that sometimes (luckily) the system is very right about its predictions and sometimes (unluckily) it is not. But we are physicists, we know tensors can be manipulated... what if we split the 200000 components of the loss into lines of length 1000? Then we could take the average of that and plot it... The second plot is much better, and we didn't change the data! So averaged over time, we are doing very good: H is decreasing, and also notice that at the 150 step it makes another downward jump (SGD).

Now our training is over, and we want to evaluate our results. We need to tell PyTorch that we're not in the training phase anymore. **BE CAREFUL**, or you'll get weird results due to batch normalization, which for us is a black box.

```
[13]: # put layers into eval mode (needed for batchnorm especially)
for layer in layers:
layer.training = False
```

```
[14]: # evaluate the loss
      @torch.no_grad() # this decorator disables gradient tracking inside pytorch
      def split_loss(split):
          x, y = {
              "train": (Xtr, Ytr),
              "val": (Xdev, Ydev),
              "test": (Xte, Yte),
          }[split]
          emb = C[x] # embed the characters into vectors (N, block_size)
          x = emb.view(emb.shape[0], -1) # concatenate the vectors
          for layer in layers:
              x = laver(x)
          loss = F.cross_entropy(x, y) # loss function
          print(split, loss.item())
      split_loss("train")
      split_loss("val")
```

train 1.3725385665893555 val 1.7553908824920654

```
[15]: # sample from the model
for _ in range(20):
    out = []
    context = [0] * block_size # initialize with all ...
    while True:
        # forward pass the neural net
        emb = C[
            torch.tensor([context])
        ] # embed the characters into vectors (N,block_size)
```

```
x = emb.view(emb.shape[0], -1) # concatenate the vectors
for layer in layers:
    x = layer(x)
logits = x
probs = F.softmax(logits, dim=1)
# sample from the distribution
ix = torch.multinomial(probs, num_samples=1).item()
# shift the context window and track the samples
context = context[1:] + [ix]
out.append(ix)
# if we sample the special '.' token, break
if ix == 0:
    break

print("".join(itos[i] for i in out)) # decode and print the generated word
```

```
amode.
leandro.
alfisio.
fabbions.
amperia.
oreino.
silvina.
wantie.
olderiza.
orea.
consolita.
mariacrostelfino.
emerande.
giandamaro.
fiero.
slorena-gettto.
morino.
morietta.
alcidisso.
artemine.
```

Not that bad. But still, we can improve this. We actually skipped the embedding, which we could now introduce with our classes defined earlier. But instead we want to "torchify" now our code, i.e. start to use Torch functions to improve the efficiency of our system.

```
[16]: # we can do better and use "Embedding" (as pytorch) to see C as a first layer

# original network https://jmlr.org/papers/volume3/tmp/bengio03a.pdf

n_embd = 10 # the dimensionality of the character embedding vectors
n_hidden = 200 # the number of neurons in the hidden layer of the MLP
```

```
# C= torch.randn(vocab size, n embd)
layers = [
   Embedding(vocab_size, n_embd),
   Flatten(block_size),
   Linear(n_embd * block_size, n_hidden, bias=False),
   BatchNorm1d(n hidden),
   Tanh(),
   Linear(n hidden, vocab size),
# parameter initialization
with torch.no_grad():
   layers[-1].weight *= 0.1 # last layer make less confident
# parameters=[C]+[p for layer in layers for p in layer.parameters()]
parameters = [p for layer in layers for p in layer.parameters()]
print(sum(p.nelement() for p in parameters)) # number of parameters in total
for p in parameters:
   p.requires_grad = True
```

In PyTorch one can write this as a sequential list of layer, with the same function names.

```
[17]: n_embd = 10  # the dimensionality of the character embedding vectors
    n_hidden = 200  # the number of neurons in the hidden layer of the MLP

model = nn.Sequential(
    nn.Embedding(vocab_size, n_embd),
    nn.Flatten(block_size),
    nn.Linear(n_embd * block_size, n_hidden, bias=False),
    nn.BatchNorm1d(n_hidden),
    nn.Tanh(),
    nn.Linear(n_hidden, vocab_size),
)

# number of parameters in total
print(sum(p.nelement() for p in model.parameters()))
for p in model.parameters():
    p.requires_grad = True
```

22308

```
[18]: # or with 'karpathy' definitions...

n_embd = 10 # the dimensionality of the character embedding vectors
```

```
n_hidden = 200  # the number of neurons in the hidden layer of the MLP

model = Sequential(
    [
        Embedding(vocab_size, n_embd),
        Flatten(block_size),
        Linear(n_embd * block_size, n_hidden, bias=False),
        BatchNorm1d(n_hidden),
        Tanh(),
        Linear(n_hidden, vocab_size),
    ]
)

# number of parameters in total
print(sum(p.nelement() for p in model.parameters()))
for p in model.parameters():
        p.requires_grad = True
```

```
[19]: # put layers into eval mode (needed for batchnorm especially)
# be back on this now keep it !!

for layer in model.layers:
    layer.training = True

# model.train(True)
```

```
[20]: # same optimization as before time
max_steps = 200000
batch_size = 32
lossi = []

for i in range(max_steps):
    # minibatch construct
    ix = torch.randint(0, Xtr.shape[0], (batch_size,))
    Xb, Yb = Xtr[ix], Ytr[ix] # batch X,Y

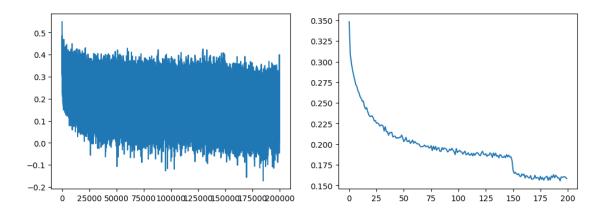
# forward pass
# emb=C[Xb] # embed the characters into vectors
# x=emb.view(emb.shape[0],-1) #concatenate the vectors
# for layer in layers:
# x=layer(x)

logits = model(Xb)
loss = F.cross_entropy(logits, Yb) # loss function
```

```
# backward pass
          for p in model.parameters():
              p.grad = None
          loss.backward()
          # update: simple SGD
          lr = 0.1 if i < 150000 else 0.01 # step learning rate decay</pre>
          for p in model.parameters():
              p.data += -lr * p.grad
          # track stats
          if i % 10000 == 0: # print every once in a while
              print(f"{i:7d}/{max_steps:7d}: {loss.item():.4f}")
          lossi.append(loss.log10().item())
      # break
           0/ 200000: 3.5427
       10000/ 200000: 1.6889
       20000/ 200000: 1.7099
       30000/ 200000: 1.7663
       40000/ 200000: 1.6661
       50000/ 200000: 1.5461
       60000/ 200000: 1.8788
       70000/ 200000: 1.7811
       80000/ 200000: 1.9472
       90000/ 200000: 1.3643
      100000/ 200000: 1.5458
      110000/ 200000: 1.4089
      120000/ 200000: 1.6715
      130000/ 200000: 2.0241
      140000/ 200000: 1.6338
      150000/ 200000: 1.5033
      160000/ 200000: 1.5036
      170000/ 200000: 1.5975
      180000/ 200000: 1.3502
      190000/ 200000: 1.6590
[21]: fig, ax = plt.subplots(ncols=2, figsize=(12, 4))
      ax[0].plot(torch.tensor(lossi))
```

[21]: [<matplotlib.lines.Line2D at 0x7f4ff1b2d660>]

ax[1].plot(torch.tensor(lossi).view(-1, 1000).mean(1)) # mean on each row



```
[22]: # put layers into eval mode (needed for batchnorm especially)
# be back on this now keep it !!

for layer in model.layers:
    layer.training = False
# model.train(True)
```

```
[23]: # evaluate the loss
      @torch.no_grad() # this decorator disables gradient tracking inside pytorch
      def split_loss(split):
          x, y = {
              "train": (Xtr, Ytr),
              "val": (Xdev, Ydev),
              "test": (Xte, Yte),
          }[split]
              emb=C[x] # embed the characters into vectors (N,block size) before
              x=emb.view(emb.shape[0],-1) #concatenate the vectors
                for layer in layers:
                    x=layer(x)
          logits = model(x)
          loss = F.cross_entropy(logits, y) # loss function
          print(split, loss.item())
      split_loss("train")
      split_loss("val")
```

train 1.3757604360580444 val 1.73955237865448

```
[24]: # sample from the model
      for _ in range(20):
          out = []
          context = [0] * block_size # initialize with all ...
          while True:
              # forward pass the neural net
                        emb=C[torch.tensor([context])] # embed the characters into_{\sqcup}
       →vectors (N,block_size)
              #
                        x=emb.view(emb.shape[0],-1) #concatenate the vectors
              #
                        for layer in layers:
              #
                            x=layer(x)
                        logits = x
              logits = model(torch.tensor([context]))
              probs = F.softmax(logits, dim=1)
              # sample from the distribution
              ix = torch.multinomial(probs, num_samples=1).item()
              # shift the context window and track the samples
              context = context[1:] + [ix]
              out.append(ix)
              # if we sample the special '.' token, break
              if ix == 0:
                  break
          print("".join(itos[i] for i in out)) # decode and print the generated word
```

```
tima.
andrea.
laurezio.
loriela.
anio.
lucido.
eriscondo.
guerriana.
ginepro.
umbra.
angeloce.
raffoso.
marziano.
erlene.
bonulana.
eva.
abelda.
riziaddino.
calaria.
eride.
```

Now embedding is accounted for, and we could generate names in this way. This is a little better, but still, there is room for improvement. We could for example add more layer and make ourselves a nice **deep network**: but this wouldn't improve much our system at the moment. Why is that? It's because we still didn't introduce any hierarchical organization in our data, which will be a definitive improvement for our Neural Network structure. We want to change the step between the embedding and the feeding to the hidden layer, in the sense that we do not want anymore to fuse the information coming from the data altogether into a single vector which is then fed to the tanh. We want instead to introduce a hierarchical structure of our embedded data.

```
[25]: # now we are going to try to do better...but because we crunch all the
      scharacters at the first layer (show picture language model),
      # adding deeper layer will not be useful...we need first to do as wavenet:
       →cluster characters in steps, hierarchialy...(convolution)
      # Progressive fusion along the layers: 2-gram -> 4->gram -> 8-gram....show
       ⇒picture in wavenet paper.....
      # first recreate the data set with block_size = 8
[26]: # let's look at a batch of just 4 example
      ix = torch.randint(0, Xtr.shape[0], (4,))
      Xb, Yb = Xtr[ix], Ytr[ix]
      logits = model(Xb)
      print(Xb.shape)
      print(Xb)
     torch.Size([4, 8])
     tensor([[ 0, 0, 0, 0, 7, 10, 15, 2],
             [0, 8, 2, 3, 19, 10, 6, 13],
             [0, 0, 0, 0, 0, 0, 0, 8],
             [10, 23, 2, 13, 5, 10, 15, 16]])
[27]: print(model.layers[0].out.shape) # output of the embedding layer
      print(model.layers[1].out.shape) # output of the Flatten layer
      print(model.layers[2].out.shape) # output of the Linear layer
     torch.Size([4, 8, 10])
     torch.Size([4, 80])
     torch.Size([4, 200])
     Now multiply each vector for the matrix and take a 200dim vector as output
[28]: # now a nice surprise about the Linear Layer https://pytorch.org/docs/stable/
       \hookrightarrow generated/torch.nn.Linear.html#torch.nn.Linear
```

```
[28]: torch.Size([4, 200])
     We can also add more dimensions... and PyTorch will work on the right dimension.
[29]: # but also !!
      print((torch.randn(4, 2, 80) @ torch.randn(80, 200) + torch.randn(200)).shape)
      # or also !!
      print((torch.randn(4, 4, 20) @ torch.randn(20, 200) + torch.randn(200)).shape)
     torch.Size([4, 2, 200])
     torch.Size([4, 4, 200])
     Instead of one vector of 80 we can use four vectors of 20.
[30]: # 1 2 3 4 5 6 7 8 -> (1 2) (3 4) (5 6) (7 8)
      # we want to fuse vectors in pairs and acts in parallel on the 4 pairs of \Box
       \hookrightarrow characters.
      # i.e. we go from (torch.randn(4,80)@ torch.randn(80,200)+torch.randn(200)).
      # ....second batch dimension...discuss in class...!!
      print((torch.randn(4, 4, 20) @ torch.randn(20, 200) + torch.randn(200)).shape)
     torch.Size([4, 4, 200])
[31]: # so now we need to change the Flatten layer to produce a (4,4,20) tensor and
       →NOT (4,80)
      e = torch.randn(
          4, 8, 10
      ) # goal: want this to be (4,4,20) where consecutive 10-d vectors
      # get concatenated (in pairs (1 2) (3 4) (5 6) (7 8))
[32]: # trick
      print(list(range(10)))
      print(list(range(10))[::2])
      print(list(range(10))[1::2])
      [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
      [0, 2, 4, 6, 8]
     [1, 3, 5, 7, 9]
[33]: # so we want this...
      print(e.shape)
      explicit = torch.cat([e[:, ::2, :], e[:, 1::2, :]], dim=2)
      print(explicit.shape)
```

).shape # broadcasting in the last term....

```
torch.Size([4, 8, 10])
     torch.Size([4, 4, 20])
[35]: input = torch.randn(4, 8, 10)
     print(input.shape)
      m = nn.Flatten()
      output = m(input)
      print(output.shape)
     torch.Size([4, 8, 10])
     torch.Size([4, 80])
[36]: #_
      class FlattenConsecutive:
          def __init__(self, n):
              self.n = n
          def __call__(self, x):
              B, T, C = x.shape
              x = x.view(B, T // self.n, C * self.n)
              if x.shape[1] == 1:
                  x = x.squeeze(1)
              self.out = x
              return self.out
          def parameters(self):
              return []
[37]: # Back to the Model...here we recover the previous one with
       →FlattenConsecutive(block_size)
      n_embd = 10 # the dimensionality of the character embedding vectors
      n_hidden = 200 # the number of neurons in the hidden layer of the MLP
      model = Sequential(
          Embedding(vocab_size, n_embd),
              FlattenConsecutive(block_size),
              Linear(n_embd * block_size, n_hidden, bias=False),
              BatchNorm1d(n_hidden),
              nn.Tanh(),
              Linear(n_hidden, vocab_size),
          ]
      )
```

```
# number of parameters in total
     print(sum(p.nelement() for p in model.parameters()))
     for p in model.parameters():
         p.requires_grad = True
     22308
[38]: # let's look at a batch of just 4 example
     ix = torch.randint(0, Xtr.shape[0], (4,))
     Xb, Yb = Xtr[ix], Ytr[ix]
     logits = model(Xb)
     print(Xb.shape)
     print(Xb)
     torch.Size([4, 8])
     tensor([[ 0, 0, 0, 0, 0, 0, 0],
             [0, 0, 0, 0, 0, 0, 4],
             [0, 0, 0, 0, 0, 0, 0, 0],
             [0, 0, 0, 16, 13, 10, 23]])
[39]: for layer in model.layers[:-2]:
         print(layer.__class__.__name__, ":", tuple(layer.out.shape))
     Embedding: (4, 8, 10)
     FlattenConsecutive: (4, 80)
     Linear: (4, 200)
     BatchNorm1d: (4, 200)
[40]: # we now move to a hierarchical approach
     n embd = 10  # the dimensionality of the character embedding vectors
     n hidden = 200 # the number of neurons in the hidden layer of the MLP
     model = Sequential(
          Embedding(vocab_size, n_embd),
             FlattenConsecutive(2),
             Linear(n_embd * 2, n_hidden, bias=False),
             BatchNorm1d(n_hidden),
             Tanh(),
             FlattenConsecutive(2),
             Linear(n_hidden * 2, n_hidden, bias=False),
             BatchNorm1d(n_hidden),
             Tanh(),
             FlattenConsecutive(2),
             Linear(n_hidden * 2, n_hidden, bias=False),
             BatchNorm1d(n_hidden),
```

```
Tanh(),
             Linear(n_hidden, vocab_size),
         ]
     )
     # number of parameters in total
     print(sum(p.nelement() for p in model.parameters()))
     for p in model.parameters():
         p.requires_grad = True
     171108
[41]: # let's look at a batch of just 4 example
     ix = torch.randint(0, Xtr.shape[0], (4,))
     Xb, Yb = Xtr[ix], Ytr[ix]
     logits = model(Xb)
     print(Xb.shape)
     print(Xb)
     torch.Size([4, 8])
     tensor([[ 0, 0, 0, 0, 14, 2, 19],
             [0, 0, 0, 0, 0, 0, 8],
             [0, 0, 0, 0, 0, 0, 0, 0],
             [0, 0, 0, 8, 22, 20, 21, 2]])
[42]: for layer in model.layers:
         print(layer.__class__.__name__, ":", tuple(layer.out.shape))
     Embedding : (4, 8, 10)
     FlattenConsecutive : (4, 4, 20)
     Linear: (4, 4, 200)
     BatchNorm1d : (4, 4, 200)
     Tanh: (4, 4, 200)
     FlattenConsecutive: (4, 2, 400)
     Linear: (4, 2, 200)
     BatchNorm1d : (4, 2, 200)
     Tanh: (4, 2, 200)
     FlattenConsecutive : (4, 400)
     Linear: (4, 200)
     BatchNorm1d: (4, 200)
     Tanh: (4, 200)
     Linear: (4, 28)
[43]: print(logits.shape)
     torch.Size([4, 28])
```

```
[44]: | # we now move to a hierarchical approach but resize to compare with the initial
       ∽onwe
      # we use n_hidden=68 to have almost the same number of parameters..,
      n_{embd} = 10 # the dimensionality of the character embedding vectors
      n_hidden = 200 # the number of neurons in the hidden layer of the MLP
      model = Sequential(
              Embedding(vocab_size, n_embd),
              FlattenConsecutive(2),
              Linear(n_embd * 2, n_hidden, bias=False),
              BatchNorm1d(n_hidden),
              Tanh(),
              FlattenConsecutive(2),
              Linear(n_hidden * 2, n_hidden, bias=False),
              BatchNorm1d(n hidden),
              Tanh(),
              FlattenConsecutive(2),
              Linear(n_hidden * 2, n_hidden, bias=False),
              BatchNorm1d(n_hidden),
              Tanh(),
              Linear(n_hidden, vocab_size),
          ]
      )
      # number of parameters in total
      print(sum(p.nelement() for p in model.parameters()))
      for p in model.parameters():
          p.requires_grad = True
```

```
[45]: # same optimization as before
max_steps = 200000
batch_size = 32
lossi = []

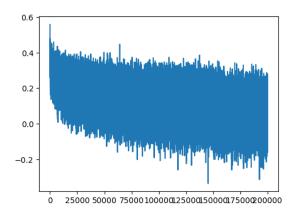
for i in range(max_steps):
    # minibatch construct
    ix = torch.randint(0, Xtr.shape[0], (batch_size,))
    Xb, Yb = Xtr[ix], Ytr[ix] # batch X,Y

# forward pass
logits = model(Xb)
```

```
loss = F.cross_entropy(logits, Yb) # loss function
          # backward pass
          for p in model.parameters():
              p.grad = None
          loss.backward()
          # update: simple SGD
          lr = 0.1 if i < 150000 else 0.01 # step learning rate decay</pre>
          for p in model.parameters():
              p.data += -lr * p.grad
          # track stats
          if i % 10000 == 0: # print every once in a while
              print(f"{i:7d}/{max_steps:7d}: {loss.item():.4f}")
          lossi.append(loss.log10().item())
      # break
           0/ 200000: 3.6123
       10000/ 200000: 1.8124
       20000/ 200000: 1.6373
       30000/ 200000: 1.7834
       40000/ 200000: 1.2532
       50000/ 200000: 1.8544
       60000/ 200000: 1.0383
       70000/ 200000: 1.5017
       80000/ 200000: 1.0546
       90000/ 200000: 1.0752
      100000/ 200000: 1.4752
      110000/ 200000: 1.1615
      120000/ 200000: 1.2915
      130000/ 200000: 1.1062
      140000/ 200000: 1.1331
      150000/ 200000: 1.4284
      160000/ 200000: 1.9482
      170000/ 200000: 1.2848
      180000/ 200000: 1.2159
      190000/ 200000: 1.3101
[46]: fig, ax = plt.subplots(ncols=2, figsize=(12, 4))
      ax[0].plot(torch.tensor(lossi))
```

[46]: [<matplotlib.lines.Line2D at 0x7f4fef808100>]

ax[1].plot(torch.tensor(lossi).view(-1, 1000).mean(1)) # mean on each row



```
0.35

0.30 -

0.25 -

0.10 -

0 25 50 75 100 125 150 175 200
```

```
[48]: # evaluate the loss
@torch.no_grad() # this decorator disables gradient tracking inside pytorch
def split_loss(split):
    x, y = {
        "train": (Xtr, Ytr),
        "val": (Xdev, Ydev),
        "test": (Xte, Yte),
        }[split]
    logits = model(x)
    loss = F.cross_entropy(logits, y) # loss function
    print(split, loss.item())

split_loss("train")
split_loss("val")
```

train 1.1616768836975098 val 1.8372830152511597

```
[49]: # sample from the model
for _ in range(20):
    out = []
    context = [0] * block_size # initialize with all ...
    while True:
        logits = model(torch.tensor([context]))
```

```
probs = F.softmax(logits, dim=1)
    # sample from the distribution
    ix = torch.multinomial(probs, num_samples=1).item()
    # shift the context window and track the samples
    context = context[1:] + [ix]
    out.append(ix)
    # if we sample the special '.' token, break
    if ix == 0:
        break

print("".join(itos[i] for i in out)) # decode and print the generated word
```

```
gaspawa.
waldemaro.
ambra.
aida.
eraldina.
isacco.
amadio.
mariso.
fabrina.
valdimaro.
gerarda.
opaldo.
firmanina.
melchiorino.
nicoletto.
lallo.
giommato.
callisto.
sostino.
cleontina.
```