MLM Nested Project D

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Question 1: data generating process

Question 2: fit the model

```
lmer_fit1 \leftarrow lmer(y \sim x + (1 | classid), data = dat)
summary(lmer_fit1)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
##
     Data: dat
## REML criterion at convergence: 71227.3
##
## Scaled residuals:
       Min
            1Q Median
                                ЗQ
                                       Max
## -4.0143 -0.6761 0.0024 0.6711 3.7584
##
## Random effects:
                         Variance Std.Dev.
## Groups
            Name
## classid (Intercept) 1.893
                                  1.376
                         2.008
## Residual
                                  1.417
## Number of obs: 20000, groups: classid, 100
##
## Fixed effects:
                 Estimate Std. Error
                                             df t value Pr(>|t|)
## (Intercept) -7.493e-03 1.391e-01 1.022e+02 -0.054
               9.864e-01 3.496e-02 1.990e+04 28.216
## x
                                                           <2e-16 ***
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
## (Intr)
## x -0.126
```

Question 2:

- a. The estimated coefficient of X is 0.986.
- b. The 95% confidence interval for this coefficient estimate is [0.986 1.96 * 0.035, 0.986 + 1.96 * 0.035] = [0.9174, 1.0546]. It covers the true coefficient, which is 1.

Question 3:

```
# 3a
dat_copy <- dat</pre>
# 3b
Z_Q3 \leftarrow rbinom(20000, 1, 0.5)
table(Z_Q3)
## Z_Q3
       0
## 9945 10055
# 3c
dat_copy <- dat_copy %>%
    mutate(y = replace(y, 1:n(), ifelse(Z_Q3 == 1, NA, y)))
lmer_fit_Q3 \leftarrow lmer(y \sim x + (1 \mid classid), data = dat_copy)
summary(lmer_fit_Q3)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
##
      Data: dat_copy
##
## REML criterion at convergence: 35607.1
##
## Scaled residuals:
##
       Min
                1Q Median
                                 ЗQ
                                         Max
## -3.9102 -0.6698 0.0146 0.6663 3.8709
##
## Random effects:
## Groups Name
                          Variance Std.Dev.
## classid (Intercept) 1.880
                                 1.371
## Residual
                          2.007
                                   1.417
## Number of obs: 9945, groups: classid, 100
##
## Fixed effects:
```

```
##
              Estimate Std. Error
                                       df t value Pr(>|t|)
              0.867
## (Intercept)
## x
               1.02485
                         0.04963 9846.41936 20.649
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Correlation of Fixed Effects:
##
    (Intr)
## x - 0.177
N_Q3 <- nrow(dat) - sum(is.na(dat_copy$y))</pre>
N_Q3
## [1] 9945
```

e.

The estimate coefficient is 1.02, which changes a little bit The 95% CI is [1.02 - 1.96 * 0.05, 1.02 + 1.96 * 0.05], which is [0.92, 1.12] almost converges to the true value

f.

The total sample size used in this Question is 9945

Question 4:

```
# 4a
dat_copy_4 <- dat
z \leftarrow rbinom(100 * 200, 1, dat_copy_4$x)
table(z)
## z
       0
## 10002 9998
dat_copy_4$y \leftarrow ifelse(z == 1, NA, dat_copy_4$y)
lmer_fit_4 <- lmer(y ~ x + (1 | classid), data = dat_copy_4)</pre>
summary(lmer_fit_4)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
##
      Data: dat_copy_4
##
## REML criterion at convergence: 35850.3
##
```

```
Min 1Q Median
                             3Q
## -3.8356 -0.6795 0.0052 0.6608 3.7058
##
## Random effects:
## Groups Name
                        Variance Std.Dev.
## classid (Intercept) 1.874
                                  1.369
                                  1.420
## Residual
                         2.015
## Number of obs: 10002, groups: classid, 100
##
## Fixed effects:
##
                Estimate Std. Error
                                          df t value Pr(>|t|)
## (Intercept) 3.442e-03 1.391e-01 1.034e+02 0.025
## x
              9.547e-01 6.031e-02 9.903e+03 15.831
                                                        <2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Correlation of Fixed Effects:
   (Intr)
## x - 0.147
d.
  i. The 95% confidence interval is [0.837,1.073], which covers the "truth".
e.
N <- nrow(dat) - sum(is.na(dat_copy_4$y))</pre>
```

Max

We use N = 10002 samples in the model fit.

Question 5:

8522 11478

Scaled residuals:

##

```
dat_copy_5 <- dat
### a
expit <- function(x) {</pre>
    \exp(x)/(1 + \exp(x))
### b
z <- rbinom(100 * 200, 1, expit(dat_copy_5$y))</pre>
table(z)
## z
##
```

```
dat_copy_5$y <- ifelse(z == 1, NA, dat_copy_5$y)</pre>
### d
lmer_fit_5 <- lmer(y ~ x + (1 | classid), data = dat_copy_5)</pre>
summary(lmer_fit_5)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
     Data: dat_copy_5
##
##
## REML criterion at convergence: 28257.5
##
## Scaled residuals:
##
      Min
               1Q Median
                                ЗQ
                                       Max
## -4.0870 -0.6596 0.0090 0.6679 3.1897
##
## Random effects:
## Groups Name
                        Variance Std.Dev.
## classid (Intercept) 1.078
                                1.038
                                 1.240
## Residual
                        1.539
## Number of obs: 8522, groups: classid, 100
##
## Fixed effects:
##
               Estimate Std. Error
                                          df t value Pr(>|t|)
## (Intercept) -0.7488 0.1074 105.0594 -6.972 2.86e-10 ***
                 0.7069
                            0.0475 8423.2269 14.881 < 2e-16 ***
## x
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
## (Intr)
## x -0.208
The new estimate for slope is 0.707.
```

The 95% confidence interval is [0.614,0.8], which does not cover the "truth", besides the intercept also change.

 \mathbf{f}

 \mathbf{e}

The total sample size is 8522, based on number of observations.