MLM Nested Project D

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Question 1: data generating process

Question 2: fit the model

```
lmer_fit1 <- lmer(y ~ x + (1|classid), data = dat)</pre>
summary(lmer_fit1)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
     Data: dat
##
##
## REML criterion at convergence: 71227.3
## Scaled residuals:
            1Q Median
##
      Min
                               3Q
                                      Max
## -4.0143 -0.6761 0.0024 0.6711 3.7584
##
## Random effects:
## Groups Name
                        Variance Std.Dev.
## classid (Intercept) 1.893 1.376
## Residual
                        2.008
                                 1.417
```

Question 2:

- a. The estimated coefficient of X is 0.986.
- b. The 95% confidence interval for this coefficient estimate is [0.986 1.96 * 0.035, 0.986 + 1.96 * 0.035] = [0.9174, 1.0546] cover the true coefficient, which is 1.

Question 3:

Question 4:

```
# 4a
z \leftarrow rbinom(100*200,1,dat$x)
# 4b
dat$y_q4 <- ifelse(z==1,NA,dat$y)</pre>
lmer_fit_mar \leftarrow lmer(y_q4 \sim x + (1|classid), data = dat)
summary(lmer_fit_mar)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y_q4 \sim x + (1 \mid classid)
      Data: dat
##
## REML criterion at convergence: 35559
##
## Scaled residuals:
##
       Min
               1Q Median
                                 3Q
                                        Max
## -3.9126 -0.6748 0.0037 0.6705 3.7484
##
## Random effects:
## Groups
             Name
                          Variance Std.Dev.
## classid (Intercept) 1.853
                                   1.361
                          2.004
                                   1.415
## Number of obs: 9936, groups: classid, 100
## Fixed effects:
                Estimate Std. Error
                                             df t value Pr(>|t|)
## (Intercept) 1.299e-03 1.384e-01 1.035e+02 0.009
```

```
## x 9.764e-01 6.065e-02 9.838e+03 16.100 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
## (Intr)
## x -0.148

d.
i. The 95% confidence interval is [0.858,1.095], which covers the "truth".</pre>
```

 $N \leftarrow sum(z==0)$

e.

We use N = 9936 samples in the model fit.

Question 5: