# MLM Nested Project D

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### Question 1: data generating process

## Question 2: fit the model

```
lmer_fit1 <- lmer(y ~ x + (1 | classid), data = dat)</pre>
summary_lmer_fit1 <- summary(lmer_fit1)</pre>
summary_lmer_fit1
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
      Data: dat
##
## REML criterion at convergence: 71227.3
##
## Scaled residuals:
      Min
            1Q Median
                                3Q
                                       Max
## -4.0143 -0.6761 0.0024 0.6711 3.7584
##
## Random effects:
## Groups Name
                         Variance Std.Dev.
## classid (Intercept) 1.893
                                  1.376
                         2.008
                                  1.417
## Number of obs: 20000, groups: classid, 100
## Fixed effects:
                 Estimate Std. Error
                                             df t value Pr(>|t|)
## (Intercept) -7.493e-03 1.391e-01 1.022e+02 -0.054
                                                           0.957
## x
               9.864e-01 3.496e-02 1.990e+04 28.216
                                                          <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Correlation of Fixed Effects:
## (Intr)
## x -0.126
estimate_x <- summary_lmer_fit1$coefficients[2, 1]
se_x <- summary_lmer_fit1$coefficients[2, 2]</pre>
```

#### Question 2:

- a. The estimated coefficient of X is 0.9864.
- b. The 95% confidence interval for this coefficient estimate is [0.986 1.96 \* 0.035, 0.986 + 1.96 \* 0.035] = [0.9179, 1.0549]. It covers the true coefficient, which is 1.

#### Question 3:

```
# 3a
dat_copy <- dat
# 3b
Z_Q3 \leftarrow rbinom(20000, 1, 0.5)
table(Z_Q3)
## Z_Q3
## 9945 10055
# 3c
dat_copy <- dat_copy %>%
   mutate(y = replace(y, 1:n(), ifelse(Z_Q3 == 1, NA, y)))
lmer_fit_Q3 <- lmer(y ~ x + (1 | classid), data = dat_copy)</pre>
summary(lmer_fit_Q3)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
##
      Data: dat_copy
##
## REML criterion at convergence: 35607.1
##
## Scaled residuals:
##
       Min
                1Q Median
                                ЗQ
                                       Max
## -3.9102 -0.6698 0.0146 0.6663 3.8709
##
## Random effects:
## Groups Name
                         Variance Std.Dev.
## classid (Intercept) 1.880
                                  1.371
## Residual
                         2.007
## Number of obs: 9945, groups: classid, 100
##
## Fixed effects:
                 Estimate Std. Error
                                              df t value Pr(>|t|)
## (Intercept)
                 -0.02359
                             0.14005 105.47622
                                                 -0.168
                                                            0.867
                             0.04963 9846.41936 20.649
## x
                  1.02485
                                                           <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Correlation of Fixed Effects:
## (Intr)
## x -0.177

# 3f
N_Q3 <- nrow(dat) - sum(is.na(dat_copy$y))
N_Q3
## [1] 9945</pre>
```

e.

The estimate coefficient is 1.02, which does not change too much The 95% CI is [1.02 - 1.96 \* 0.05, 1.02 + 1.96 \* 0.05], which is [0.92, 1.12] almost converges to the true value

f.

The total sample size used in this Question is 9945

## Question 4:

```
# 4a
dat_copy_4 <- dat</pre>
z <- rbinom(100 * 200, 1, dat_copy_4$x)
table(z)
## z
##
       0
## 10002 9998
dat_copy_4$y <- ifelse(z == 1, NA, dat_copy_4$y)</pre>
# 4c
lmer_fit_4 <- lmer(y ~ x + (1 | classid), data = dat_copy_4)</pre>
summary_lmer_fit4 <- summary(lmer_fit_4)</pre>
summary_lmer_fit4
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
##
      Data: dat_copy_4
##
## REML criterion at convergence: 35850.3
##
## Scaled residuals:
                                 ЗQ
       Min
                1Q Median
##
                                         Max
## -3.8356 -0.6795 0.0052 0.6608 3.7058
##
## Random effects:
                          Variance Std.Dev.
## Groups
            Name
## classid (Intercept) 1.874
                                   1.369
                                   1.420
## Residual
                          2.015
## Number of obs: 10002, groups: classid, 100
## Fixed effects:
```

```
##
                Estimate Std. Error df t value Pr(>|t|)
## (Intercept) 3.442e-03 1.391e-01 1.034e+02 0.025
                                                              0.98
               9.547e-01 6.031e-02 9.903e+03 15.831
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Correlation of Fixed Effects:
##
     (Intr)
## x - 0.147
estimate_x <- summary_lmer_fit4$coefficients[2, 1]</pre>
round(estimate_x, 4)
## [1] 0.9547
\mathbf{d}.
  i. The 95% confidence interval is [0.837,1.073], which covers the "truth".
e.
N <- nrow(dat) - sum(is.na(dat_copy_4$y))</pre>
We use N = 10002 samples in the model fit.
Question 5:
dat_copy_5 <- dat
### a
expit <- function(x) {</pre>
    \exp(x)/(1 + \exp(x))
}
z <- rbinom(100 * 200, 1, expit(dat_copy_5$y))</pre>
table(z)
## z
##
       0
## 8522 11478
dat_copy_5$y <- ifelse(z == 1, NA, dat_copy_5$y)</pre>
### d
lmer_fit_5 <- lmer(y ~ x + (1 | classid), data = dat_copy_5)</pre>
summary(lmer_fit_5)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
      Data: dat_copy_5
##
## REML criterion at convergence: 28257.5
```

##

## Scaled residuals:

```
##
      Min
               1Q Median
                               3Q
                                      Max
                  0.0090 0.6679
## -4.0870 -0.6596
                                   3.1897
##
## Random effects:
##
   Groups
            Name
                        Variance Std.Dev.
   classid (Intercept) 1.078
                                 1.038
##
   Residual
                        1.539
                                 1.240
## Number of obs: 8522, groups: classid, 100
##
## Fixed effects:
               Estimate Std. Error
                                          df t value Pr(>|t|)
                                    105.0594 -6.972 2.86e-10 ***
## (Intercept)
                -0.7488
                            0.1074
## x
                 0.7069
                            0.0475 8423.2269 14.881 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##
     (Intr)
## x -0.208
```

The new estimate for slope is 0.707.

 $\mathbf{e}$ 

The 95% confidence interval is [0.614,0.8], which does not cover the "truth", besides the intercept also change.

 $\mathbf{f}$ 

The total sample size is 8522, based on number of observations.