MLM Nested Project D

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Question 1: data generating process

Question 2: fit the model

```
lmer_fit1 <- lmer(y ~ x + (1|classid), data = dat)
summary(lmer_fit1)</pre>
```

```
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
##
     Data: dat
## REML criterion at convergence: 71227.3
##
## Scaled residuals:
##
               1Q Median
      Min
                                ЗQ
                                       Max
## -4.0143 -0.6761 0.0024 0.6711 3.7584
##
## Random effects:
## Groups
           Name
                         Variance Std.Dev.
## classid (Intercept) 1.893
                                  1.376
## Residual
                         2.008
                                  1.417
## Number of obs: 20000, groups: classid, 100
##
```

Question 2:

- a. The estimated coefficient of X is 0.986.
- b. The 95% confidence interval for this coefficient estimate is [0.986 1.96 * 0.035, 0.986 + 1.96 * 0.035] = [0.9174, 1.0546]. It covers the true coefficient, which is 1.

Question 3:

```
# 3a
dat_copy <- dat
# 3b
Z_Q3 \leftarrow rbinom(20000, 1, 0.5)
table(Z_Q3)
## Z_Q3
##
      0
## 9945 10055
# 3d
lmer_fit_Q3 <- lmer(y ~ x +(1|classid), data = dat_copy)</pre>
summary(lmer_fit_Q3)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
##
     Data: dat_copy
##
## REML criterion at convergence: 35607.1
##
## Scaled residuals:
                            ЗQ
##
      Min 1Q Median
                                  Max
## -3.9102 -0.6698 0.0146 0.6663 3.8709
##
## Random effects:
## Groups Name
                      Variance Std.Dev.
## classid (Intercept) 1.880
                            1.371
## Residual
                      2.007
                              1.417
```

```
## Number of obs: 9945, groups: classid, 100
##
## Fixed effects:
##
                Estimate Std. Error
                                           df t value Pr(>|t|)
## (Intercept)
                -0.02359 0.14005 105.47622 -0.168
                                                          0.867
                 1.02485
                            0.04963 9846.41936 20.649
                                                          <2e-16 ***
## x
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
   (Intr)
## x - 0.177
N_Q3 <- nrow(dat)-sum(is.na(dat_copy$y))</pre>
N_Q3
```

[1] 9945

e.

The estimate coefficient is 1.02, which changes a little bit The 95% CI is [1.02-1.96*0.05, 1.02+1.96*0.05], which is [0.92, 1.12] almost converges to the true value

f.

The total sample size used in this Question is 9945

Question 4:

```
# 4a
dat_copy_4 <- dat
z <- rbinom(100*200,1,dat_copy_4$x)</pre>
table(z)
## z
##
       0
## 10002 9998
# 4b
dat_copy_4$y <- ifelse(z==1,NA,dat_copy_4$y)</pre>
lmer_fit_4 <- lmer(y ~ x + (1|classid), data = dat_copy_4)</pre>
summary(lmer_fit_4)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
      Data: dat_copy_4
##
```

```
##
## REML criterion at convergence: 35850.3
##
## Scaled residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
## -3.8356 -0.6795 0.0052 0.6608 3.7058
## Random effects:
## Groups
           Name
                         Variance Std.Dev.
                                  1.369
## classid (Intercept) 1.874
## Residual
                         2.015
                                  1.420
## Number of obs: 10002, groups: classid, 100
## Fixed effects:
##
                Estimate Std. Error
                                           df t value Pr(>|t|)
## (Intercept) 3.442e-03 1.391e-01 1.034e+02 0.025
                                                          0.98
## x
               9.547e-01 6.031e-02 9.903e+03 15.831
                                                         <2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Correlation of Fixed Effects:
   (Intr)
## x - 0.147
d.
  i. The 95% confidence interval is [0.837,1.073], which covers the "truth".
e.
N <- nrow(dat)-sum(is.na(dat_copy_4$y))</pre>
```

We use N = 10002 samples in the model fit.

Question 5:

8522 11478

```
dat_copy_5 <- dat
### a
expit <- function(x){exp(x)/(1+exp(x))}

### b
z <- rbinom(100*200,1, expit(dat_copy_5$y))
table(z)

## z
## 0 1</pre>
```

```
dat_copy_5$y <- ifelse(z==1,NA,dat_copy_5$y)</pre>
### d
lmer_fit_5 <- lmer(y ~ x + (1|classid), data = dat_copy_5)</pre>
summary(lmer_fit_5)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
      Data: dat_copy_5
##
##
## REML criterion at convergence: 28257.5
##
## Scaled residuals:
##
       Min
                1Q Median
                                ЗQ
                                       Max
## -4.0870 -0.6596 0.0090 0.6679 3.1897
##
## Random effects:
## Groups Name
                         Variance Std.Dev.
## classid (Intercept) 1.078
                                1.038
## Residual
                         1.539
                                  1.240
## Number of obs: 8522, groups: classid, 100
##
## Fixed effects:
##
               Estimate Std. Error
                                          df t value Pr(>|t|)
## (Intercept) -0.7488 0.1074 105.0594 -6.972 2.86e-10 ***
                  0.7069
                             0.0475 8423.2269 14.881 < 2e-16 ***
## x
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
## (Intr)
## x -0.208
The new estimate for slope is 0.707.
\mathbf{e}
The 95% confidence interval is [0.614,0.8], which does not cover the "truth".
```

 \mathbf{f}

The total sample size is 8522, based on number of observations.