MLM Nested Project D

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Question 1: data generating process

Question 2: fit the model

```
lmer_fit1 <- lmer(y ~ x + (1 | classid), data = dat)</pre>
summary_lmer_fit1 <- summary(lmer_fit1)</pre>
summary_lmer_fit1
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
      Data: dat
##
## REML criterion at convergence: 71227.3
##
## Scaled residuals:
      Min
            1Q Median
                                3Q
                                       Max
## -4.0143 -0.6761 0.0024 0.6711 3.7584
##
## Random effects:
## Groups Name
                         Variance Std.Dev.
## classid (Intercept) 1.893
                                  1.376
                         2.008
                                  1.417
## Number of obs: 20000, groups: classid, 100
## Fixed effects:
                 Estimate Std. Error
                                             df t value Pr(>|t|)
## (Intercept) -7.493e-03 1.391e-01 1.022e+02 -0.054
                                                           0.957
## x
               9.864e-01 3.496e-02 1.990e+04 28.216
                                                          <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Correlation of Fixed Effects:
## (Intr)
## x -0.126
estimate_x <- summary_lmer_fit1$coefficients[2, 1]
se_x <- summary_lmer_fit1$coefficients[2, 2]</pre>
```

Question 2:

- a. The estimated coefficient of X is 0.986.
- b. The 95% confidence interval for this coefficient estimate is [0.986 1.96 * 0.035, 0.986 + 1.96 * 0.035] = [0.9179, 1.0549]. It covers the true coefficient, which is 1.

Question 3:

```
# 3a
dat_copy <- dat
# 3b
Z_Q3 \leftarrow rbinom(20000, 1, 0.5)
table(Z_Q3)
## Z_Q3
## 9945 10055
# 3c
dat_copy <- dat_copy %>%
   mutate(y = replace(y, 1:n(), ifelse(Z_Q3 == 1, NA, y)))
lmer_fit_Q3 <- lmer(y ~ x + (1 | classid), data = dat_copy)</pre>
summary(lmer_fit_Q3)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
##
      Data: dat_copy
##
## REML criterion at convergence: 35607.1
##
## Scaled residuals:
##
       Min
                1Q Median
                                ЗQ
                                       Max
## -3.9102 -0.6698 0.0146 0.6663 3.8709
##
## Random effects:
## Groups Name
                         Variance Std.Dev.
## classid (Intercept) 1.880
                                  1.371
## Residual
                         2.007
## Number of obs: 9945, groups: classid, 100
##
## Fixed effects:
                 Estimate Std. Error
                                              df t value Pr(>|t|)
## (Intercept)
                 -0.02359
                             0.14005 105.47622
                                                 -0.168
                                                            0.867
                             0.04963 9846.41936 20.649
## x
                  1.02485
                                                           <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
## ## Correlation of Fixed Effects: ## (Intr) ## x -0.177 # 3f N_Q3 <- nrow(dat) - sum(is.na(dat_copy$y)) N_Q3 ## [1] 9945 e. The estimate coefficient is 1.02, which changes a little bit The 95% CI is [1.02 - 1.96 * 0.05, 1.02 + 1.96 * 0.05], which is [0.92, 1.12] almost converges to the true value
```

f.

The total sample size used in this Question is 9945

Question 4:

```
# 4a
dat_copy_4 <- dat</pre>
z <- rbinom(100 * 200, 1, dat_copy_4$x)
table(z)
## z
##
       0
## 10002 9998
dat_copy_4$y <- ifelse(z == 1, NA, dat_copy_4$y)</pre>
# 4c
lmer_fit_4 <- lmer(y ~ x + (1 | classid), data = dat_copy_4)</pre>
summary(lmer_fit_4)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
      Data: dat_copy_4
##
## REML criterion at convergence: 35850.3
## Scaled residuals:
       Min
                1Q Median
                                 3Q
                                        Max
## -3.8356 -0.6795 0.0052 0.6608 3.7058
##
## Random effects:
## Groups Name
                          Variance Std.Dev.
## classid (Intercept) 1.874
                                   1.369
## Residual
                          2.015
                                   1.420
## Number of obs: 10002, groups: classid, 100
##
## Fixed effects:
##
                Estimate Std. Error
                                            df t value Pr(>|t|)
```

```
## (Intercept) 3.442e-03 1.391e-01 1.034e+02 0.025
## x
               9.547e-01 6.031e-02 9.903e+03 15.831
                                                          <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation of Fixed Effects:
     (Intr)
## x -0.147
d.
   i. The 95% confidence interval is [0.837,1.073], which covers the "truth".
e.
N <- nrow(dat) - sum(is.na(dat_copy_4$y))</pre>
We use N = 10002 samples in the model fit.
Question 5:
dat_copy_5 <- dat
### a
expit <- function(x) {</pre>
    \exp(x)/(1 + \exp(x))
z <- rbinom(100 * 200, 1, expit(dat_copy_5$y))</pre>
table(z)
## z
##
       0
## 8522 11478
dat_copy_5$y <- ifelse(z == 1, NA, dat_copy_5$y)</pre>
### d
lmer_fit_5 <- lmer(y ~ x + (1 | classid), data = dat_copy_5)</pre>
summary(lmer_fit_5)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
      Data: dat_copy_5
## REML criterion at convergence: 28257.5
##
## Scaled residuals:
       Min
                1Q Median
                                 3Q
                                         Max
## -4.0870 -0.6596 0.0090 0.6679 3.1897
## Random effects:
```

Variance Std.Dev.

Name

Groups

```
classid (Intercept) 1.078
                               1.038
## Residual
                      1.539
                               1.240
## Number of obs: 8522, groups: classid, 100
##
## Fixed effects:
              Estimate Std. Error
##
                                       df t value Pr(>|t|)
## (Intercept) -0.7488 0.1074 105.0594 -6.972 2.86e-10 ***
                          0.0475 8423.2269 14.881 < 2e-16 ***
## x
                0.7069
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation of Fixed Effects:
##
   (Intr)
## x -0.208
```

The new estimate for slope is 0.707.

 \mathbf{e}

The 95% confidence interval is [0.614,0.8], which does not cover the "truth", besides the intercept also change.

 \mathbf{f}

The total sample size is 8522, based on number of observations.