# MLM Nested Project D

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Compiled on Sat Apr 30 11:26 EDT

### Question 1: data generating process

# Question 2: fit the model

```
lmer_fit1 <- lmer(y ~ x + (1|classid), data = dat)</pre>
summary(lmer_fit1)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
      Data: dat
##
##
## REML criterion at convergence: 71227.3
##
## Scaled residuals:
       Min
           1Q Median
                                3Q
                                       Max
## -4.0143 -0.6761 0.0024 0.6711 3.7584
##
## Random effects:
## Groups
             Name
                         Variance Std.Dev.
## classid (Intercept) 1.893
                                  1.376
## Residual
                         2.008
                                  1.417
## Number of obs: 20000, groups: classid, 100
##
## Fixed effects:
##
                 Estimate Std. Error
                                             df t value Pr(>|t|)
```

```
## (Intercept) -7.493e-03 1.391e-01 1.022e+02 -0.054 0.957
## x 9.864e-01 3.496e-02 1.990e+04 28.216 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
## (Intr)
## x -0.126</pre>
```

#### Question 2:

- a. The estimated coefficient of X is 0.986.
- b. The 95% confidence interval for this coefficient estimate is [0.986 1.96 \* 0.035, 0.986 + 1.96 \* 0.035] = [0.9174, 1.0546]. It covers the true coefficient, which is 1.

## Question 3:

```
# 3a
dat_copy <- dat
# 36
Z_Q3 \leftarrow rbinom(20000, 1, 0.5)
dat_copy <- dat_copy %>% mutate(y = replace(y, 1:n(), ifelse(Z_Q3==1, NA, y)))
# 3d
lmer_fit_Q3 <- lmer(y ~ x +(1|classid), data = dat_copy)</pre>
summary(lmer_fit_Q3)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y \sim x + (1 \mid classid)
##
      Data: dat_copy
##
## REML criterion at convergence: 35607.1
##
## Scaled residuals:
##
       Min
             1Q Median
                                3Q
                                       Max
## -3.9102 -0.6698 0.0146 0.6663 3.8709
##
## Random effects:
## Groups
           Name
                         Variance Std.Dev.
## classid (Intercept) 1.880
                                  1.371
                         2.007
                                  1.417
## Number of obs: 9945, groups: classid, 100
## Fixed effects:
                 Estimate Std. Error
                                             df t value Pr(>|t|)
## (Intercept)
                 -0.02359
                             0.14005 105.47622 -0.168
                                                            0.867
## x
                  1.02485
                             0.04963 9846.41936 20.649
                                                           <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Correlation of Fixed Effects:
## (Intr)
## x -0.177

# 3f
N_Q3 <- nrow(dat)-sum(is.na(dat_copy$y))
N_Q3
## [1] 9945</pre>
```

 $\mathbf{e}.$ 

The estimate coefficient is 0.978, which is a little bit smaller than the previous fit. The 95% CI is [0.9576 - 1.96 \* 0.05, 0.978 + 1.96 \* 0.05], which is [0.86, 1.08] converges to the true value.

f.

The total total sample size used in this Question is 10064

### Question 4:

```
# 4a
z \leftarrow rbinom(100*200,1,dat$x)
# 4b
dat$y_q4 <- ifelse(z==1,NA,dat$y)</pre>
# 4c
lmer_fit_mar \leftarrow lmer(y_q4 \sim x + (1|classid), data = dat)
summary(lmer_fit_mar)
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: y_q4 \sim x + (1 \mid classid)
##
      Data: dat
## REML criterion at convergence: 35850.3
##
## Scaled residuals:
       Min
                1Q Median
                                3Q
                                        Max
## -3.8356 -0.6795 0.0052 0.6608 3.7058
##
## Random effects:
## Groups
                         Variance Std.Dev.
             Name
## classid (Intercept) 1.874
                                   1.369
                         2.015
                                   1.420
## Residual
## Number of obs: 10002, groups: classid, 100
##
## Fixed effects:
                                            df t value Pr(>|t|)
##
                Estimate Std. Error
## (Intercept) 3.442e-03 1.391e-01 1.034e+02 0.025
                                                            0.98
## x
               9.547e-01 6.031e-02 9.903e+03 15.831
                                                         <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation of Fixed Effects:
##
     (Intr)
```

```
## x -0.147
```

 $\mathbf{d}.$ 

i. The 95% confidence interval is [0.837,1.073], which covers the "truth".

e.

```
N \leftarrow sum(z==0)
```

We use N = 10002 samples in the model fit.

# Question 5: