

## TADs for Integrative Task 1

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| <b>TAD Hash Table</b>   |
| Hash Table = $\{e_1, e_2, \dots, e_m\}$ where every element $e_x$ is composed by $(K_x, V_x)$ for a Hash Table with keys Type K, and values type V with a size $m - 1$ .  |
| $\{inv: \text{HashTable size} = m - 1\}$<br>$\{inv: \text{All keys K must be unique.}\}$<br>$\{inv: \text{Every } e_x \text{ must be accessed through hash}(K_x)\}$   |
| Primitive Operations: <ul style="list-style-type: none"><li>• createHashTable: <math>\rightarrow</math> HashTable</li><li>• Hash: <math>K \rightarrow \text{int}</math></li><li>• Add: <math>e \rightarrow \text{HashTable}</math></li><li>• Search: <math>K \rightarrow V</math></li><li>• Delete: <math>K \rightarrow \text{HashTable}</math></li><li>• getValues: <math>\rightarrow e</math></li></ul> |

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| createHashTable() - Constructor   |
| "Creates an empty Hash Table of type (K , V)"                                   |
| {pre: True}   |
| {post: HashTable = $\{(e_1), (e_2), \dots, (e_m)\}$ , Every $e = \text{null}\}$ |

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| Hash(K) - Analyzer   |
| "Enter a key K and return the index in which it will be located in the Hash Table."  |
| {pre: K is an integer $K \geq 0$ }   |
| {post: $\text{hash}(K \text{ key}) = m * (kA \% \text{mod } 1)$ where $\text{hash}(k)$ belongs to $\text{HashTable}[h(k)]$ } |

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| add(e) - Modifier  |
| "Add a new element e (composed of value V and key K) in $\text{HashTable}[h(K)]$ " |
| {pre: K and V must be the same type of object as $\text{HashTable}(K, V)$ }        |

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| {pre: K must be a unique key} |
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| {post: HashTable[hash(K)] = e} |
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| search(K) - Analyzer |
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| "Search for an e using its key K and return the value associated with it." |
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| {pre: K must match the type of K of the HashTable} |
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| {post: V}                       |
| {post: null, K was not found. } |

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| Delete(K) - Modifier |
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| "Delete $e_x$ from the HashTable using its key $K_x$ ." |
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| {pre: $K_x$ must match the type of K of the HashTable} |
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| {post: HashTable[h( $K_x$ )]}                        |
| {post:KeyNotFoundException, $K_x$ couldn't be found} |

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| getValues() - Analyzer |
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| "Returns every value e saved inside the HashTable" |
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| {pre: True} |
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| {post: { $e_1, e_2, \dots, e_m$ }} |
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| <b>TAD Stack</b> |
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| Stack= { $a_1, a_2, \dots, a_m$ } size m - 1 and $a_m$ is the last added node type T. |
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| {inv: The only visible element is $a_m$ }               |
| {inv: $a_x$ can only be added at $a_m$ }                |
| {inv: $a_m$ is the only node that can be removed}       |
| {inv: order $a_1, a_2, \dots, a_m$ must not be changed} |

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| Primitive Operations: <ul style="list-style-type: none"><li>• createStack: -&gt; Stack</li><li>• isEmpty: -&gt; boolean</li></ul> |
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- push:  $a \rightarrow \text{Stack}$
- Top:  $\rightarrow a$
- Pop:  $\rightarrow \text{Stack}$

createStack() - Constructor

“Creates an empty Stack of type T”

{pre: True}

{post: Stack = { $a_1$ }, where  $a_1$  is null}

isEmpty() - Analyzer

“Determines if the stack is empty.”

{pre: True}

{post: true if  $a_m == \text{null}$ }

{post: false if  $a_m \neq \text{null}$ }

push( $a_m$ ) - Modifier

“Add node  $a_m$  to the end of the stack.”

{pre:  $a_m$  must match the type T of the Stack}

{post: Stack = { $a_1, a_2, \dots, a_{m-1}, a_m$ }}

top() - Analyzer

“Returns the value of the last node in the stack ( $a_m$ )”

{pre: True}

{post:  $a_m$ }

{post: StackException, if stack is empty}

pop() - Modifier

“Deletes the last element in the stack ( $a_m$ )”

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| {pre: True}   |
| {post: Stack = {a <sub>1</sub> , a <sub>2</sub> , ..., a <sub>m-1</sub> }, where a <sub>m-1</sub> becomes the new a <sub>m</sub> afterwards}<br>{post: StackException, if stack is empty} |

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| <b>TAD Queue</b>   |
| Queue = {a <sub>1</sub> , a <sub>2</sub> , ..., a <sub>m</sub> } of size m-1 and the last added node type T is a <sub>m</sub> .  |
| {inv: a <sub>m</sub> must be added at the end of the stack}<br>{inv: a <sub>1</sub> must be the first deleted element}<br>{inv: order a <sub>1</sub> , a <sub>2</sub> , ..., a <sub>m</sub> must not be changed}             |
| Primitive Operations: <ul style="list-style-type: none"> <li>• createQueue: -&gt; Queue</li> <li>• isEmpty: -&gt; boolean</li> <li>• enqueue: a -&gt; Queue</li> <li>• dequeue: -&gt; a</li> <li>• front: -&gt; a</li> </ul> |

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| createQueue() - Constructor                                     |
| "Creates an empty Queue of type T"                              |
| {pre: True}   |
| {post: Queue = {a <sub>1</sub> }, where a <sub>1</sub> is null} |

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| isEmpty() - Analyzer  |
| "Determines if the queue is empty."   |
| {pre: True}   |
| {post: true if a <sub>1</sub> == null}<br>{post: false if a <sub>1</sub> != null} |

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| enqueue(a <sub>m</sub> ) - Modifier                            |
| "Add node a <sub>m</sub> to the end of the queue"              |
| {pre: a <sub>m</sub> must be of the same type T as the Queue.} |

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| {post: Queue = {a <sub>1</sub> , a <sub>2</sub> , ..., a <sub>m-1</sub> , a <sub>m</sub> }} |
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| dequeue() - Modifier |
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| "Retrieves and then deletes the first element in the queue(a <sub>1</sub> )" |
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| {pre: True} |
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| {post: returns a <sub>1</sub> and Queue = {a <sub>2</sub> , a <sub>3</sub> , ..., a <sub>m</sub> }, where a <sub>2</sub> becomes the new a <sub>1</sub> afterwards}<br>{post: QueueException, if queue is empty} |
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| front() |
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| "Returns the value of the first node in the queue (a <sub>1</sub> )" |
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| {pre: True} |
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| {post: a}<br>{post: QueueException, if the queue is empty.} |
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| <b>TAD Priority Queue</b> |
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| PriorityQueue = {a <sub>1</sub> , a <sub>2</sub> , ..., a <sub>m</sub> } where each element a <sub>i</sub> and a <sub>j</sub> have an assigned priorities p <sub>i</sub> and p <sub>j</sub> respectively so that if p <sub>i</sub> >= p <sub>j</sub> then i <= j and so { ..., a <sub>i</sub> , a <sub>j</sub> , ...}. |
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| {inv: The element a <sub>m</sub> must be added while maintaining the order of priority.}<br>{inv: a <sub>1</sub> must be the first element removed from the queue, where a <sub>1</sub> has the highest priority and the first added in its priority group.}<br>{inv: The order of elements with the same priority (if any) must be preserved as they were added.} |
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| Primitive Operations: |
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| <ul style="list-style-type: none"><li>• createPriorityQueue: -&gt; PriorityQueue</li><li>• isEmpty: -&gt; boolean</li><li>• enqueue: a -&gt; PriorityQueue</li><li>• dequeue: -&gt; a</li><li>• front: -&gt; a</li></ul> |
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| createPriorityQueue() - Constructor |
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| “Creates an empty Priority Queue of type T.”                          |
| {pre: True}   |
| {post: PriorityQueue = {a <sub>1</sub> } where a <sub>1</sub> = null} |

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| isEmpty() - Analyzer                         |
| “Determines if the priority queue is empty.” |
| {pre: True}                                  |
| {post: true if a <sub>1</sub> == null}       |
| {post: false if a <sub>1</sub> != null}      |

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| enqueue(a <sub>x</sub> ) - Modifier   |
| “Add an item a <sub>x</sub> with a given priority to the queue.”  |
| {pre: item must match the type T}   |
| {post: PriorityQueue = {a <sub>1</sub> , a <sub>2</sub> , ..., a <sub>x</sub> , ... a <sub>m</sub> }, where a <sub>x</sub> is added maintaining the priority order and after any element a <sub>y</sub> with the same priority but added before.} |

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| dequeue() - Modifier  |
| “Retrieves and then deletes the first element in the priority queue (a <sub>1</sub> )”  |
| {pre: True}   |
| {post: returns a <sub>1</sub> (it had the highest priority and was the first of its priority added) and PriorityQueue is updated accordingly to keep the priority order.} |
| {post: PriorityQueueException, if PriorityQueue is empty.}  |

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| front() - Analyzer  |
| “Returns the value of the item with the first added item with the highest priority (a <sub>1</sub> )” |
| {pre: True}   |

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| {post: a}   |
| {post: PriorityQueueException, if PriorityQueue is empty} |