TADs for Integrative Task 2

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TAD Graph

Graph = $\{(V, E) \text{ where } V \text{ represents vertices } \{v_1, v_2, ..., v_n\} \text{ and } E \text{ represents edges } \{e_1, e_2, ..., e_n\} \text{ which connect edges } \{v_x, v_v\}\}.$

 $\{\text{inv: For V}, v_i \neq v_i \text{ if } i \neq j\}$

(inv: If the graph allows loops, e_x can be $\{v_x, v_x\}$)

(inv: If the graph allows parallel edges, the subset of edges in E, $\{e_1, e_2, ..., e_n\}$ can represent the same connection $\{v_x, v_y\}$

{inv: For a directed graph, e_x within E has an order such that $\{v_x, v_y\} \neq \{v_y, v_x\}$ }

{inv: For an undirected graph, e_x within E doesn't have an order meaning that $\{v_x, v_y\} = \{v_y, v_x\}$, and both representations must exist since navegability is not specified.}

{inv: For E, {e₁, e₂, ..., e_n}, each edge has an associated weight w}

Primitive Operations:

- createGraph: Boolean x Boolean x Boolean -> Graph
- addVertex: Value -> Graph
- addEdge: Value x Value -> Graph
- removeVertex: Value -> Graph
- removeEdge: Value x Value -> Graph
- searchVertex: Value -> Vertex
- bFS: Value -> Graph
- dijkstra: Value -> Graph

createGraph(b₁, b₂, b₃)

Creates an empty graph with the 3 specified conditions: b_1 allows parallel edges, b_2 allows loops, b_3 is directed or not.

{pre: b_1 , b_2 , b_3 must be booleans}

{post: Graph = {V, E} where V contains {null} and E contains {null}}

addVertex(v)

Adds a vertex to the graph with value v.

{pre: v must be the same type of value as the Graph.}

{post: Graph = {V, E} where V contains {v} and E contains {null}}

addEdge(v_1, v_2)

Adds the edge e that connects vertices v_1 and v_2 which hold the values of v_1 and v_2 .

{pre: v_1 and v_2 must be of the same type of the value as the Graph.}

{post: Graph = {V, E} where V contains $\{v_1, v_2\}$ and E contains $\{e\}$ which represent $\{v_1, v_2\}$ }

{post: GraphException if either v₁ or v₂ don't exist}

removeVertex(v)

Removes the vertex V from the Graph.

{pre: v must be of the same type of value as the Graph}

{post: Graph = {V, E} where V represents $\{v_1, v_2, ..., v_n\}$ - v and E represents $\{e_1, e_2, ..., e_n\}$ }

{post: GraphException if v doesn't exist}

removeEdge(v₁, v₂)

Removes all edges that connect vertices v_1 and v_2 which hold the value of v_1 and v_2 .

{pre: v_1 and v_2 must be of same type of value as the Graph}

{post: Graph = {V, E} where V represents $\{v_1, v_2, ..., v_n\}$ and E represents $\{e_1, e_2, ..., e_n\}$ - subset $\{e_1, e_2, ..., e_n\}$ that represents $\{v_1, v_2\}$ }

searchVertex(v)

Retrieves the vertex which holds the value of v.

{pre: v must be of the same type of value as the Graph}

{post: Vertex}

{post: null, if the vertex doesn't exist}

bFS(v)

Completes a Breadth-First Search along all connected vertices in the Graph.

{pre: v must be of the same type of value as the Graph}

{post: Graph = {V, E} where V represents $\{v_1, v_2, ..., v_n\}$ which all which are connected have an assigned color, predecessor and distance (number of vertices) relative to the root v and E represents $\{e_1, e_2, ..., e_n\}$

{post: GraphException, if the vertex doesn't exist}

dijkstra(v)

Calculates the shortest path from vertex v to the rest in the graph taking into account the weight of every edge.

{pre: v must be of the type of value as the Graph}

{post: Graph = {V, E} where V represents { v_1 , v_2 , ..., v_n } which are all connected and have an assigned distance which represents the shortest path between v and v_x and a predecessor associated to the vertex by which v_x was found through the minimum relative edge weight and E represents { e_1 , e_2 , ..., e_n } where each e_x has an associated weight w_x } {post: GraphExeception, if the vertex doesn't exist}