

Table 20-IV. Elements of Coordinate Systems (sheet 1 of 2)	
$\mu = 3.986005 \times 10^{14} \text{ meters}^3/\text{sec}^2$	WGS 84 value of the earth's gravitational constant for GPS user
$\dot{\Omega}_e = 7.2921151467 \times 10^{-5} \text{ rad/sec}$	WGS 84 value of the earth's rotation rate
$A = \left( \sqrt{A} \right)^2$	Semi-major axis
$n_0 = \sqrt{\frac{\mu}{A^3}}$	Computed mean motion (rad/sec)
$t_k = t - t_{oe}^*$	Time from ephemeris reference epoch
$n = n_0 + \Delta n$	Corrected mean motion
$M_k = M_0 + nt_k$	Mean anomaly
$M_k = E_k - e \sin E_k$	Kepler's Equation for Eccentric Anomaly (may be solved by iteration) (radians)
$v_k = \tan^{-1} \left\{ \frac{\sin v_k}{\cos v_k} \right\}$ $= \tan^{-1} \left\{ \frac{\sqrt{1-e^2} \sin E_k / (1 - e \cos E_k)}{(\cos E_k - e) / (1 - e \cos E_k)} \right\}$	True Anomaly
<p>* <math>t</math> is GPS system time at time of transmission, i.e., GPS time corrected for transit time (range/speed of light). Furthermore, <math>t_k</math> shall be the actual total time difference between the time <math>t</math> and the epoch time <math>t_{oe}</math>, and must account for beginning or end of week crossovers. That is, if <math>t_k</math> is greater than 302,400 seconds, subtract 604,800 seconds from <math>t_k</math>. If <math>t_k</math> is less than -302,400 seconds, add 604,800 seconds to <math>t_k</math>.</p>	

Table 20-IV. Elements of Coordinate Systems (sheet 2 of 2)

$E_k = \cos^{-1} \left\{ \frac{e + \cos v_k}{1 + e \cos v_k} \right\}$		Eccentric Anomaly
$\Phi_k = v_k + \omega$		Argument of Latitude
$\delta u_k = c_{us} \sin 2\Phi_k + c_{uc} \cos 2\Phi_k$	Argument of Latitude Correction	} Second Harmonic Perturbations
$\delta r_k = c_{rs} \sin 2\Phi_k + c_{rc} \cos 2\Phi_k$	Radius Correction	
$\delta i_k = c_{is} \sin 2\Phi_k + c_{ic} \cos 2\Phi_k$	Inclination Correction	
$u_k = \Phi_k + \delta u_k$		Corrected Argument of Latitude
$r_k = A(1 - e \cos E_k) + \delta r_k$		Corrected Radius
$i_k = i_0 + \delta i_k + (\text{IDOT}) t_k$		Corrected Inclination
$\left. \begin{array}{l} x_k' = r_k \cos u_k \\ y_k' = r_k \sin u_k \end{array} \right\}$		Positions in orbital plane.
$\Omega_k = \Omega_0 + (\dot{\Omega} - \dot{\Omega}_e) t_k - \dot{\Omega}_e t_{oe}$		Corrected longitude of ascending node.
$\left. \begin{array}{l} x_k = x_k' \cos \Omega_k - y_k' \cos i_k \sin \Omega_k \\ y_k = x_k' \sin \Omega_k + y_k' \cos i_k \cos \Omega_k \\ z_k = y_k' \sin i_k \end{array} \right\}$		Earth-fixed coordinates.

#### 20.3.3.4.3.2 Parameter Sensitivity.

The sensitivity of the SV's antenna phase center position to small perturbations in most ephemeris parameters is extreme. The sensitivity of position to the parameters  $\sqrt{A}$ ,  $C_{rc}$  and  $C_{rs}$  is about one meter/meter. The sensitivity of position to the angular parameters is on the order of  $10^8$  meters/semicircle, and to the angular rate parameters is on the order of  $10^{12}$  meters/semicircle/second. Because of this extreme sensitivity to angular perturbations, the value of  $\pi$  used in the curve fit is given here.  $\pi$  is a mathematical constant, the ratio of a circle's circumference to its diameter. Here  $\pi$  is taken as  $\pi = 3.1415926535898$ .

#### 20.3.3.4.3.3 Coordinate Systems.

##### 20.3.3.4.3.3.1 ECEF Coordinate System.

The equations given in Table 20-IV provide the SV's antenna phase center position in the WGS 84 ECEF coordinate system defined as follows: