# Ordinal Variables and Missing Data

# March 22, 2021

## General

- This paper should be an intersection of ordinal variables and missing data. Jeff thinks there is room there for a contribution
- The general idea is that general treatments of missing data (listwise deletion, multiple imputation etc.) lead to different results depending on the type of variable. How you treat Don't Know and Refused and how this treatment affects the results depends greatly on the type of variable that you use to impute the missing data. The idea is that you would need to approach things differently depending on whether you use a nominal, interval, or ordinal variable to fill in values for Don't Know/Refused. So I am developing a method to specifically treat Don't Know/Refused with ordinal variables that improves over current uses that are generic for all types of variables
- This method should be a customized form of multiple imputation that is closer to the data than general multiple imputation. Jeff and Skyler developed affinity scores and hot decking in their BJPS paper. They used the number of exact matches (in the form of other participants) to calculate the affinity score. Instead, I should use a weighted distance solution between ordinal variable categories. I would use the OP model from the blocking paper to weight the distances between the categories in matches (in the form of other participants). In other words, I would use the underlying ordered probit numbers to create the weights. So this would be a specific ordinal variable adjustment of the affinity score building
- Set up chapter structure

## Code

- My code functions for one variable with NAs, for 10,000 iterations
  - I have saved results for inc, age, Dem, Rep for hd.ord and hd.norm
  - For all 4, na.omit performs the best. This isn't surprising, since deleting observations with missing values shouldn't be a problem with MCAR
- My code does not function When run for several variables with NAs
  - It throws up a replacement error somewhere down the line when run for 10,000 iterations. It's never in the same place, so it must be something random
  - Always the same: # of NAs overall. Not always the same between some runs: # of NAs per column, # of rows with NAs
  - Find out why my code doesn't work for NAs in several variables
    - \* The number of NAs inserted wasn't actually the issue. It was in the OPMord code
    - \* I painfully ran 1,000 iterations for two variables, gradually adding one line at a time to the function. I discovered the error was where I assign values to df.cases, specifically where the columns are all combined and the resulting vector added to the data as educ.new

- \* I saved the vector to an empty vector, ran everything for 1,000 iterations, then looked at the vectors and the corresponding versions of df.cases
- \* There were rows with all NAs in df.cases, which makes the vector shorter than the data, which means it can't be assigned to it as a column. I reran the df.cases creation code to find the culprit
- \* I had overlooked that int.df\$Values has one value fewer than there are variable levels, since it lists cutpoints between the levels. For 6 levels, I had assigned int.df\$length(levels(...)), which picks the 6th value of int.df\$Values but it only goes to 5. I had to add -1. Now it's working

#### • Method to insert NAs

- I tried prodNA, which works for MCAR but gives me nothing for MAR. And MCAR works well for na.omit, since by definition it's a random sample of missing data, which doesn't matter
- Use mice ampute()
  - \* It has MCAR and MAR options. MAR is what I need
  - \* It doesn't work on just one variable; it needs at least two
  - \* ampute() works very well
- With the code adjusted (-1), OPMord now works. However, some of the int.dfs don't have all the education levels: int.df with all levels has 6 rows (one fewer than the levels, since each row shows a cutoff), but some have 5. This means OPMcut now doesn't work
  - I could adjust OPMcut to work with fewer levels, but then I would be, in the end, taking means of most data with all levels and some data with fewer levels. That's problematic
  - It's better to discard the iterations where int.df has 5 rows after OPMord has run and then continue with the other functions. I set the code up to do that. However, after about 40 percent of running 12,500 iterations, there was an error: I hadn't factored in that the int.dfs could also have fewer rows than that. A few of them had 4 rows, which caused the error. I adjusted the code to now discard the iterations where int.df has anything other than 6 rows
- The data ran for 12,500 iterations, 80 percent NAs, Rep and inc, hot.deck.ord, hot.deck.norm, na.omit. The results looked promising: hd.ord performed better than hd.norm and na.omit
- More methods
  - Include mice
  - Include Amelia
  - Use the defaults for both since that's what over 90% of people do (even if they shouldn't)
  - Include hot.deck.norm on the original education values (I ran it on the cutpoints)
- hot.deck impContinuous
  - No need to use it, since no variable is continuous (age has more values than sdCutoff but it's nominal, not continuous)
- hot.deck sdCutoff
  - No need to change the default
- Add more variables/NAs

- Add NAs to 6 of the variables
- Demographics I still have: Age(numeric), employment (5 levels), ideology (liberal, conservative, neither), following public affairs (ordinal, 4 levels), media interest (numeric, accumulative count of activities), participation (numeric, accumulative count of activities)
- I can't add them all, since mice and Amelia don't work when there is collinearity
- I used code to find and discard variables with high correlation

## • Percentage of NAs

- I'm currently using 80 percent. Jeff used 20, 50, and 80
- I did one run each for 20, 50, and 80 percent

## • Preliminary results

- Across the board, hd.ord performs better than normal hot.deck, but worse than
   Amelia and mice
- Across the board, Amelia is better than mice for inc and age. It's also better for interest, except for 20 percent NAs, where mice wins
- For Dem, Female, and White, Amelia also edges first, thought mice sometimes is ahead by one unit or so in the fourth decimal
- The difference is less pronounced for the binary variables and most visible in the nominal ones. It is worst for "age", which has the most unique values
- As the percentage of NAs increases, the estimates are further off from the true means. This is to be expected for all methods, but it affects hd.ord and hot.deck much more than Amelia and mice
- Jeff likens this to the search for the pot of gold at the end of the rainbow. There will be something there, somewhere. I just need to find one specific scenario, one specific set of circumstances where I do particularly well or better. He gave me a bunch of pointers/ideas where to go from here. I'm using ampute() to generates NAs MAR. ampute() is part of mice it's not a great surprise that mice then performs really well. amelia() performs even better Jeff thinks amelia() calls mice at some point. ampute() has lots of default settings that are not immediately obvious. Jeff says to mess with those
- Run it with bycases = FALSE (TRUE introduces a very specific pattern of missingness), cont = FALSE, type = "MID"
  - I had to take out White because ampute() complained there were too many variables for bycases = FALSE
  - I ran it for 20 percent NAs and saved framing.nas and ampute() output no significant change in results: hd.ord is better than hot.deck across the board.
     Amelia is better than mice for inc, age, and interest. mice is better for Dem and Female
  - The same for 10 percent
- Running it with ANES data on Code Ocean
  - Previous small tests have shown that the results should not be different when compared to the framing data
  - I have results from running things for 2,363 iterations, but the amelia runtime results were much faster than expected here. I did this run with lapply. I want to rerun this with a loop, as before, before I write anything up here

#### Runtimes

- hd.ord() outperforms hotdeck() (minimally) and massively outperforms mice and Amelia on the framing data
- I have some ANES runtime results for fewer iterations (1,307)
- I also have ANES runtime results for more iterations (2,363) obtained through lapply. Weirdly, amelia is almost as fast as hd.ord here ... I want to rerun this with a loop before I write anything up here
- Own function to create NAs as MAR
  - Jeff: "It's MAR if you 'delete' values in column 1 based on values in column 2", e.g. 'delete' the values for age where income is 1 and where income is 5
  - I wrote a function that samples the ID numbers for a specified percentage of each selected variable's unique values, then replaces the corresponding values of a different variable with NAs, based on the sampled ID numbers
  - I have run this function on the framing data
  - Seems to be more MCAR than MAR, since na.omit performs really well now
- Run ampute with MNAR for framing and ANES data
  - I've written everything up. hd.ord is doing well for binary variables overall, but less so for nominal and ordinal ones
  - MNAR or MAR makes no significant difference
- I've written up the own.NA.rows results
- It is not possible to run the whole ANES data for 10,000 iterations on Jeff's machine or on Code Ocean. It exhausts the memory. After endless trials, I finally managed to do it by sampling 1,000 observations, then running my code on that smaller ANES data set
- I added CCES to my data sets for analysis and set up several coding scripts
- With each data set sampled for 1,000 observations (old framing, CCES, ANES), I got great running times where hd.ord consistently performs far better than amelia
- What doesn't work so far
  - Increasing percentage of NAs == worse hd.ord performance
  - Ordinal and nominal variables == worse hd.ord performance
  - High number of observations == reduced number of iterations (crashes and/or RAM maxing out)
  - High number of observations == makes amelia faster relative to hd.ord
  - 17 ANES education levels == increases needed number of iterations
  - 17 ANES education levels == causes amelia to stop on CO and Jeff
  - ampute() with bycases=FALSE and cont=FALSE == worse hd.ord performance, good na.omit performance
  - own.NA() == na.omit performs best
  - own.NA.rows() == pretty much everything is zero, incl. na.omit (only mice is awful)
  - Running hd.ord with method = p.draw == worse hd.ord performance
  - Running hd.ord with method = p.draw == only works with only binary vars in the data
  - Increasing sdCutoff == only does something with only binary vars in the data
  - Only binary vars in data == no gain in hd.ord performance

- What works so far
  - Results for binary variables == equal performance of hd.ord, mice, amelia
  - Increasing number of variables with NAs (all, not just binary) == better hd.ord performance
  - -1000 observations in data sets == allows 10,000 iterations
  - 1000 observations in data sets == increases amelia running time
  - MNAR == MAR in terms of hd.ord performance
- I ran CCES for 14 NA variables for 10,000 iterations on CO. It took FOREVER because mice took more than 20 hours (!) on its own. I then ran the same code for 100 iterations on my machine. The results are virtually identical, so we really don't need all these thousands of runs. They're good to get good running time numbers, but not for other things. From now on I can test ideas like variables to add etc. on at most 1,000 iterations. No need for any more
- In addition, mice is at best identical to amelia regarding the results. Most of the times, amelia is better. If I do need to run things for 10,000-ish iterations again for some reason, consider leaving mice out of it, if possible. That massively cuts down the runtime of the code
- I selected and included more variables for ANES and framing, then ran those for 1,000
  iterations. The results are getting even closer to zero across the board, including for
  na.omit
- I set up versions of all my functions to work with multiple ordinal variables: OPMordMult, OPMcutMult, hot.deck.ord.mult. I ran this for 1,000 iterations for CCES, ANES, and framing. It produced good results for all binary variables, though not better than before
- So far, I have really good results that are on par with amelia for lots of binary variables. I also have great running times where hd.ord is consistently at least twice as fast as amelia for all data sets with 1,000 observations and 10,000 iterations. That's a good step forward
- I don't think there is a scenario where hd.ord performs better. I'm reaching the stage where I would state that the theory of the latent underlying variable didn't pan out
- Emailed Jeff: I'm at the end of my research. I can't beat amelia, no matter the circumstances. But I get the same results for binary variables, with tons better running time. It looks like the theory of polr to estimate ordinal variables doesn't pay dividends. I want that to be enough for my diss
- Jeff responded: "Go ahead and write it up focusing on the speed and the rigor of your testing of all of these packages. Something like 'Quality Comparison of Major Missing Data Solutions for Discrete Data with a Proposed New Method'. That seems to reflect your extensive testing and understanding of software solutions"

#### Chapter write-up

- Write up the chapter focusing on the performance and speed of the packages under the different circumstances I tested
- Reorganize headings and general outline
- Identify where things are missing with +++
- Gradually keep filling missing sections

- Work in Jeff's feedback
- When I have implemented all of his feedback, Jeff doesn't need to see it again. I can send it out directly to Ryan and Liz
- Perhaps move one or two tables to the appendix