

Large amplitude change in spot-induced rotational modulation of the *Kepler* Ap star KIC 2569073

Jason A. Drury,^{1,2★} Simon J. Murphy,^{1,2} Aliz Derekas,^{3,4} Ádám Sódor,³ Dennis Stello,^{1,2,5} Charles A. Kuehn,^{1,2,6} Timothy R. Bedding,^{1,2} Zsófia Bognár,⁴ László Szigeti,³ Róbert Szakáts,⁴ Krisztián Sárneczky⁴ and László Molnár⁴

¹*School of Physics, Sydney Institute for Astronomy, University of Sydney, Sydney, NSW 2006, Australia*

²*Stellar Astrophysics Center (SAC), Department of Physics and Astronomy, Aarhus University, Aarhus DK-8000, Denmark*

³*ELTE Gothard Astrophysical Observatory, Szent Imre herceg út 112, H-9704 Szombathely, Hungary*

⁴*Konkoly Observatory, Research Centre for Astronomy and Earth Sciences, Hungarian Academy of Sciences, Konkoly Thege Miklós út 15-17, H-1121 Budapest, Hungary*

⁵*School of Physics, University of New South Wales, Sydney, NSW 2052, Australia*

⁶*Department of Physics and Astronomy, University of Northern Colorado, Colorado, 80639 USA*

Accepted 2017 July 7. Received 2017 July 7; in original form 2017 March 15

ABSTRACT

An investigation of the 200×200 pixel ‘superstamp’ images of the centres of the open clusters NGC 6791 and NGC 6819 allows for the identification and study of many variable stars that were not included in the *Kepler* target list. KIC 2569073 ($V = 14.22$), is a particularly interesting variable Ap star that we discovered in the NGC 6791 superstamp. With a rotational period of 14.67 d and 0.034 mag variability, it has one of the largest peak-to-peak variations of any known Ap star. Colour photometry reveals an antiphase correlation between the B band, and the V , R and I bands. This Ap star is a rotational variable, also known as an α^2 CVn star, and is one of only a handful of Ap stars observed by *Kepler*. While no change in spot period or amplitude is observed within the 4 yr *Kepler* time series, the amplitude shows a large increase compared to ground-based photometry obtained two decades ago.

Key words: techniques: photometric – stars: chemically peculiar – stars: individual: KIC 2569073 – stars: rotation – starspots.

1 INTRODUCTION

Chemically peculiar A stars, in short Ap stars, are a spectroscopic subclass of A-type stars. They show markedly enhanced absorption in lines of strontium, chromium, europium, silicon and some rare-earth elements. Strong magnetic fields are also present in Ap stars (Babcock 1947) and often concentrate these overabundances into spots at the magnetic poles. The presence of strong magnetic fields also results in magnetic braking (Stępień 2000), reducing the rotation rate of Ap stars relative to normal A-type stars (Abt & Morrell 1995).

Misaligned magnetic and rotational axes are a common property of Ap stars and are generally described with reference to the oblique rotator model (Babcock 1949; Stibbs 1950). The angle of inclination between these axes combined with the spots at the magnetic poles can result in both spectroscopic and photometric variability (Wolff 1983; Smith 1996). Stars with such spots that show photometric rotational modulation are classified as α^2 CVn variables.

This variability can be used to determine the rotation period of the star.

Stępień (2000) concluded that any angular momentum evolution must occur in Ap stars during the pre-main-sequence phase (see also North 1998; Hubrig, North & Mathys 2000). Furthermore, he showed that magnetic field strength is the critical factor for angular momentum loss in Ap stars, determining the dominant spin-down mechanism. The distribution of rotation periods provides insight into the pre-main-sequence evolution of Ap stars, particularly the initial angular momentum of the protostellar disc and the magnetic field strengths of these stars.

Renson & Manfroid (2009) produced a catalogue containing ~ 2000 confirmed and ~ 1500 probable Ap stars over the entire sky, showing these stars are common. However, few of these stars have long-term continuous photometry that would allow for a detailed analysis of their stellar properties.

At high photometric precision some Ap stars show rapid oscillations (roAp stars) with periods of 5–25 min (Kurtz 1982), but the majority are non-oscillating (noAp) stars. It should be noted that the classification of a noAp star relies only on the non-detection of oscillations. Such oscillations may be present but fall below the

★ E-mail: jason.drury@sydney.edu.au

detection limit. Only 61 roAp stars have been identified to date (Smalley et al. 2015) making these relatively rare. Asteroseismology of roAp stars is important as the driving mechanism is still not fully understood and is an active area of research.

The *Kepler* space telescope has revolutionized the study of variable stars, advancing the detection limit for oscillations down to just a few micromagnitudes. This makes it possible to classify noAp stars more precisely than ever before. *Kepler* observations of seven previously known Ap stars detected pulsations in only one (Balona et al. 2011b). However, four new roAp stars with *Kepler* observations have been identified; three from their pulsation signatures (Balona et al. 2011a; Kurtz et al. 2011; Smalley et al. 2015), and one from a combined analysis of *Kepler* and SuperWASP data (Holdsworth et al. 2014).

With the exception of the roAp star from the SuperWASP project with a pulsational amplitude of 1.4 mmag, all of the roAp stars in the *Kepler* field exhibit pulsation amplitudes below 0.1 mmag that would be undetectable with ground observations. Based on this, Balona et al. (2011a) proposed that noAp stars may exhibit rapid oscillations which are simply below the detection threshold.

In this paper, we present an analysis of the Ap star KIC 2569073 (V694 Lyr, Mochejska, Stanek & Kaluzny 2003). Initially identified as a variable star in *I*- and *B*-band photometry with a period of 15.26 d (V68, Kazarovets et al. 2013), KIC 2569073 was later reported to be constant in *V*-band photometry (de Marchi et al. 2007). Mochejska et al. (2003) conducted a long-term variability survey of NGC 6791 with cluster membership estimates. However, for KIC 2569073 they did not provide a membership estimate; instead they noted its position 4 mag above and 0.3 mag blue of the turn-off for cluster members. This position on the colour-magnitude diagram makes it unlikely to be a cluster member.

We first outline the extraction of the *Kepler* data for KIC 2569073 from the ‘superstamp’ images, the characteristics of these extracted data and the light-curve corrections we have applied. The remainder of Section 2 describes the characteristics and calibration of a spectrum and colour photometry we have obtained. In Section 3, we discuss the classification of this star, detailing the rotation period, variation in light-curve shape and the search for pulsation signatures in the light curve.

2 OBSERVATIONS

2.1 Kepler observations

The *Kepler* space telescope was primarily designed to detect transiting exoplanets and to determine the occurrence rate of small planets in the Milky Way. This required long, well-sampled, high precision time series, which are also critical for studies of intrinsic stellar variability.

Kepler had a fixed observational window covering a 105° field of view within the Cygnus and Lyra constellations, which was observed at a duty cycle >90 per cent between 2009 May and 2013 May. Due to limited onboard storage and connection bandwidth for data download, only specific preselected small ‘postage stamps’ of pixels around each ‘target star’ were selected. As a result, no data were recorded for the majority of stars within the field. In addition, *Kepler* obtained 200×200 pixel ‘superstamp’ images of the centres of the open clusters NGC 6791 and NGC 6819 using its long-cadence (LC) mode of 29.42 min (Koch et al. 2010). We show an image of the NGC 6791 superstamp in Fig. 1(a). These superstamps allow us to identify and study many variables that were not included in the *Kepler* target list. The data are divided

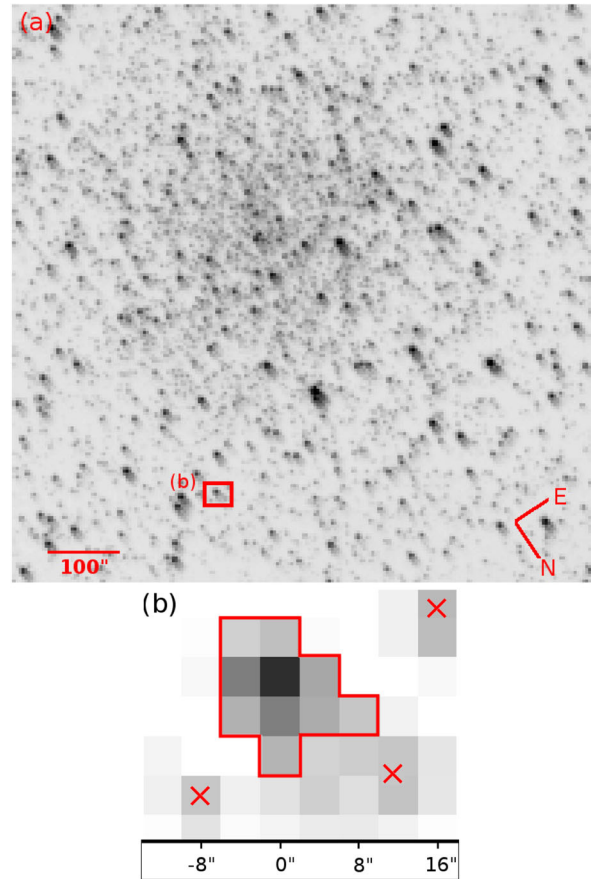


Figure 1. (a) Position of KIC 2569073 on the superstamp of NGC 6791. (b) Subset of pixels around target and example of the custom aperture used to extract the photometric data. Nearby stars are marked with x's.

into quarters: Q1(~ 34 d), Q2–Q16(~ 90 d each) and Q17(~ 33 d), which, with the small interquarter gaps of up to 24 h, total a span of ~ 1426 d of observations, beginning at BJD 2454964.513.

2.1.1 Data extraction and processing

We generated light curves for 25 stars with no nearby contaminants from the superstamp around NGC 6791 using custom defined apertures for each quarter (Kuehn et al. 2015). To generate these custom apertures for each star, we located the brightest pixel of the star in the first image of each quarter and manually inspected all pixels in a square aperture of ± 2 pixels. We included all pixels with a fractional flux of at least 3 per cent of the star's brightest pixel that were not associated with a neighbouring star. To ensure a pixel was not associated with a nearby star, we produced a light curve and Fourier transform for every pixel within a 9×9 pixel² aperture centred on the star's brightest pixel, and manually compared each Fourier transform to the Fourier transform of the brightest pixel. Any pixels with a Fourier transform containing a signal from a contaminant star greater than 3σ above the noise level of the target star were excluded. We summed the flux within the aperture for each image. From the light curves of these 25 stars we found one star with an almost-sinusoidal variability: KIC 2569073. Fig. 1(b) shows its custom aperture for Q1.

KIC 2569073, (J2000.0, 19 20 30.799, +37 50 55.00) (Fig. 1), has a $B - V$ colour of 0.54 mag and an apparent magnitude

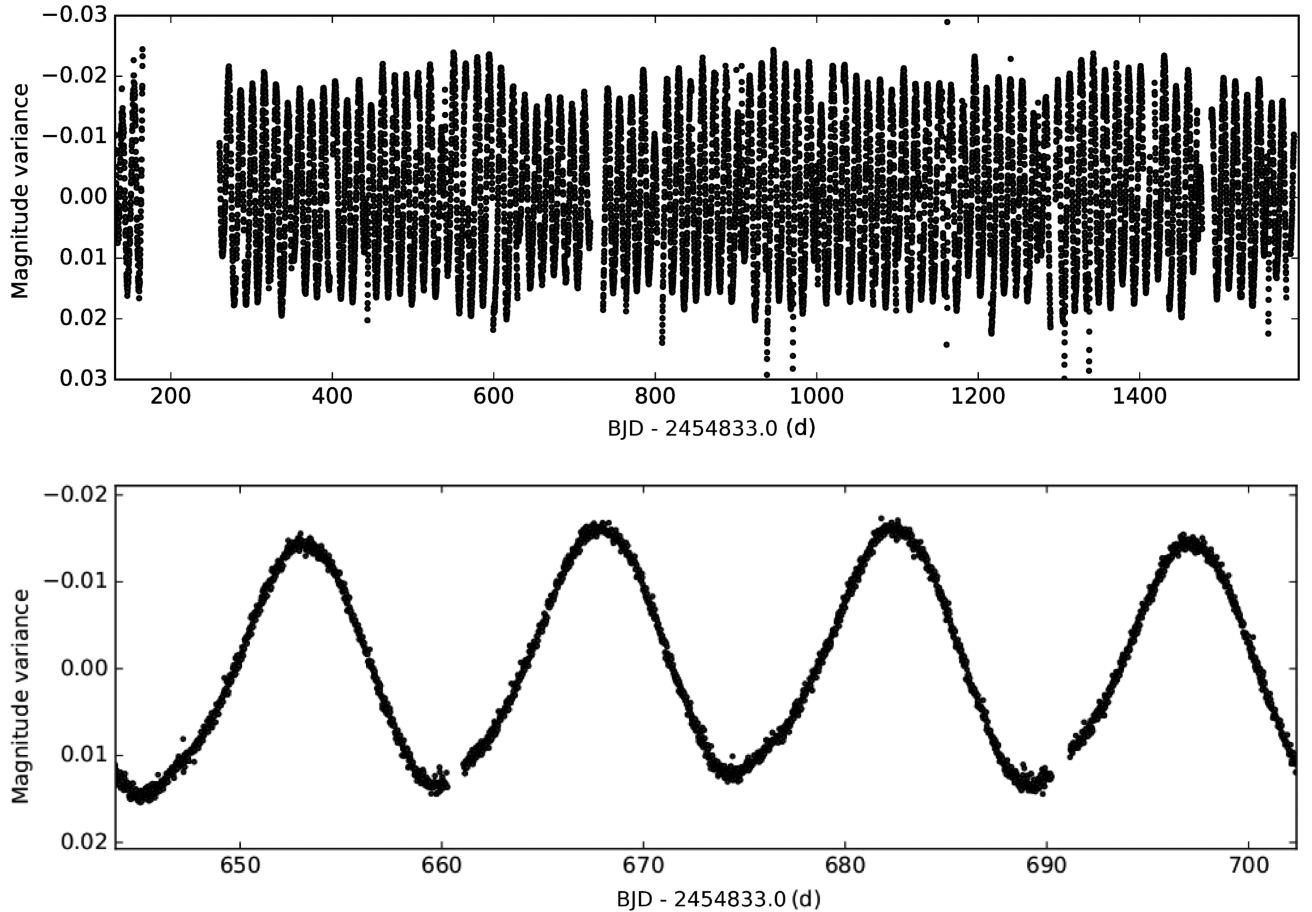


Figure 2. The upper panel shows the full light curve of KIC 2569073 after de-trending. In the lower panel is a zoom of the light curve showing its general shape.

(*V*) of 14.219 mag (Stetson, Bruntt & Grundahl 2003). Both the *Gaia* DR1 and SDSS data bases list three nearby faint stars, 14.47, 16.59 and 16.93 arcsec distant from KIC 2569073, respectively. We have marked their positions in Fig. 1(b) with crosses. The possibility of contamination from these stars was considered and addressed through the pixel mask selection criteria above.

Our raw light curve suffers from a number of systematic flux perturbations due to instrumental effects including the telescope’s 90 d re-orientation period. To correct for these systematics, we fitted and removed fourth-order non-linear trends from each quarter. During quarter 2 (Q2), the spacecraft experienced two operational shutdown periods or safe modes. These safe modes resulted in intraquarter trends in the data that we could not correct for easily, and we decided to discard the Q2 data set from the analysis. The remaining 16 quarters were concatenated to produce the final light curve. In Fig. 2 (upper panel), we show the full corrected light curve of KIC 2569073.

The 1st, 6th and 15th quarters show drifts in the median magnitude of the light curve over the length of the quarters, possibly resulting from incomplete corrections of systematic effects. Furthermore, we note the presence of correlated shifts in the amplitude of the rotational modulation of the star, but are unable to distinguish if this is intrinsic or a result of the drifts in median magnitude.

2.2 NOT observations

We obtained a ground-based, low-resolution ($R \sim 2000$) spectrum of the star using the ALFOSC Échelle spectrograph on the 2.5 m Nordic Optical Telescope (NOT) on La Palma on 2016 May 28. Our 20 min exposure using the #18 grism was centred at 4360 Å, with a spectral range of 3450–5350 Å. The spectrum was reduced using the NOT standard pipeline by the on-site observer. We extracted the final spectrum by summing the flux in the central 3 pixels of the slit. The spectrum was wavelength calibrated using the Balmer series absorption lines.

2.3 Colour photometry

We took multicolour CCD photometry with the 0.6 m Schmidt telescope at Piskéstető Observatory, Hungary. We obtained 120 frames on 25 nights between 2015 April and 2015 July using Johnson/Bessell *B*, *V* and Cousins *R_C*, *I_C* filters. The telescope was equipped with an Apogee ALTA-U 4k × 4k CCD camera. On each night, images were mostly obtained in blocks of 2–3 frames per filter. The images were reduced with IRAF following the standard processing steps of bias subtraction and flat-field correction. Aperture photometry for the target and other field stars were performed on each image using the IRAF qphot task. We used the average magnitude of seven stars as a comparison for the differential magnitude.

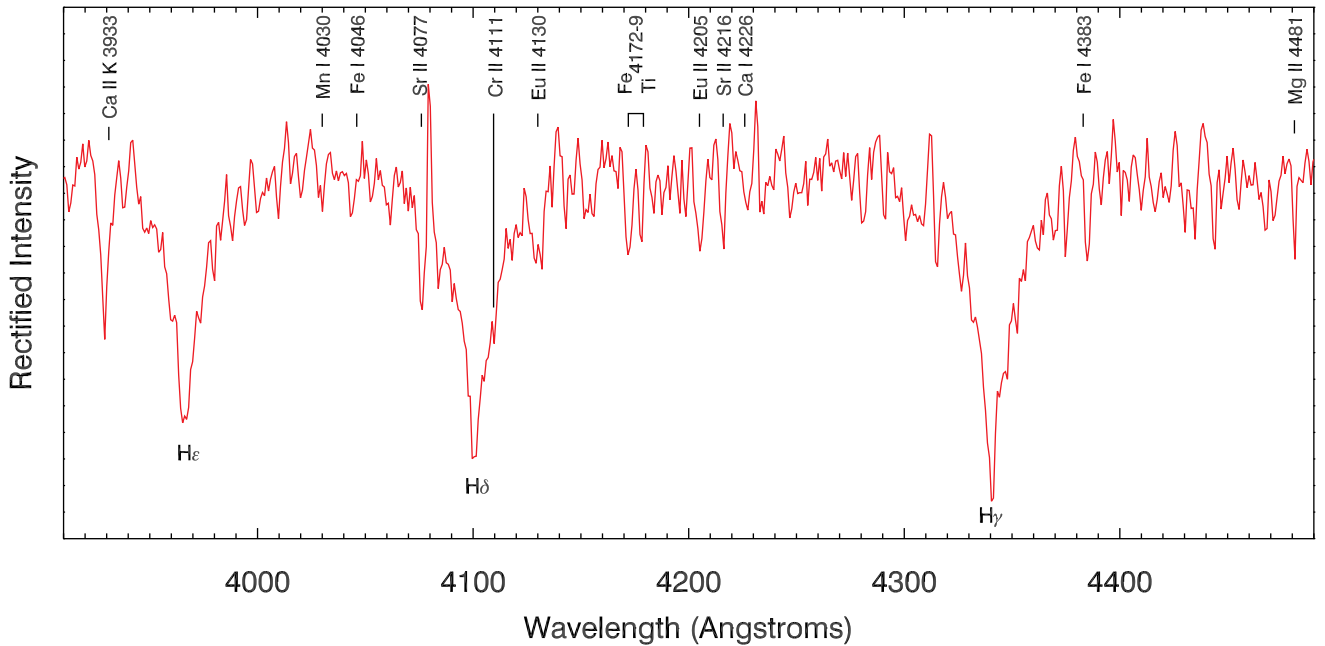


Figure 3. The blue-violet spectrum of KIC 2569073, showing the typical features of an A5 Vp SrCrEu star (see Gray & Corbally 2009), and a broad-but-shallow Ca II K line. Spectral lines relevant to the spectral classification are labelled.

3 RESULTS

3.1 Classification and properties

3.1.1 Spectral classification (A5 Vp SrCrEu)

We compared the spectrum with MK spectral standards, from which we determined a hydrogen line type of A5 V (Fig. 3). We identified all of the typical peculiarities of an Ap SrCrEu star (Gray & Corbally 2009). These are evident in spite of the low signal-to-noise ratio of the spectrum, and a flux spike just redward of the Sr II 4077 line. The Ca lines are notably broad but shallow, which is often seen in magnetic Ap stars with stratified atmospheres. This spectral classification agrees with the *Kepler* Input Catalog’s T_{eff} of ~ 7420 K.

Combined with the historical colour photometry, we are able to confirm this star as a non-member of NGC 6791 as its colour and magnitude suggest it is a foreground object.

3.1.2 Kepler observations

The light curve for KIC 2569073 shows clear variability with a peak-to-peak amplitude of approximately 0.034 mag and a primary period of 14.6679(3) d (Fig. 2). This signature shows at least 10 harmonics in the periodogram and is interpreted as rotational modulation, placing KIC 2569073 as an α^2 CVn variable.

3.1.3 Colour photometry

We folded the colour photometry with the rotation period we determined from the *Kepler* data (Fig. 4). This revealed clear antiphase variations between the *B* light curve and the *V*, *R_C* and *I_C* light curves and shows a peak-to-peak amplitude pattern similar to the one found by Kurtz et al. (1996) for HD 6532, namely that the *B*, *R_C* and *I_C* amplitudes are larger than those of the *V* band. This phenomenon is rare within the visible wavelengths but has been well documented in α^2 CVn stars between visible and UV observations.

Molnar (1973) suggested this phenomenon is caused by the redistribution of flux from rare-earth line-blanketing between the *V* and *B* filter wavelengths. We present these peak-to-peak amplitudes along with the colour photometry obtained by Mochejska et al. (2003) in Table 1. We have converted their values from semi-amplitudes to peak-to-peak amplitudes for ease of comparison.

We note that both values show similar trends with the peak-to-peak amplitude being greater in the *B* and infrared passbands than the *V* band. It should also be noted that the infrared passbands of *I* and *I_C* are not directly comparable. The Mochejska et al. (2003) values, obtained between 1996 and 2002, are significantly smaller than those presented in this work and indicate large, long-term changes in the peak-to-peak rotational modulation amplitude and thus changes in the structure, size or location of the star-spots.

Importantly, the *V* amplitude of KIC 2569073 matches the amplitude observed by *Kepler* as expected due to the similarities in the passbands. Meanwhile, the increase in rotational modulation amplitude from *V* to *R_C* to *I_C* band is now observed for magnetic Ap stars across a range of spectral types from late-B (Gröbel et al. 2017) through early-A (Kurtz et al. 1996) to mid-A stars (this work).

3.2 Pulsation signatures

The spectral class and temperature of KIC 2569073 are similar to those of known roAp stars (Smalley et al. 2015). RoAp stars typically have pulsation periods between 5 and 25 min corresponding to pulsation frequencies above the *Kepler* LC Nyquist frequency. Murphy (2012) noted that the ~ 30 min integration time for the LC *Kepler* data results in amplitude reduction of pulsation frequencies beyond the Nyquist limit, but these pulsations can still be investigated (Murphy, Shibahashi & Kurtz 2013). The amplitude reduction is described by equation (1) where A_0 is the true amplitude, the

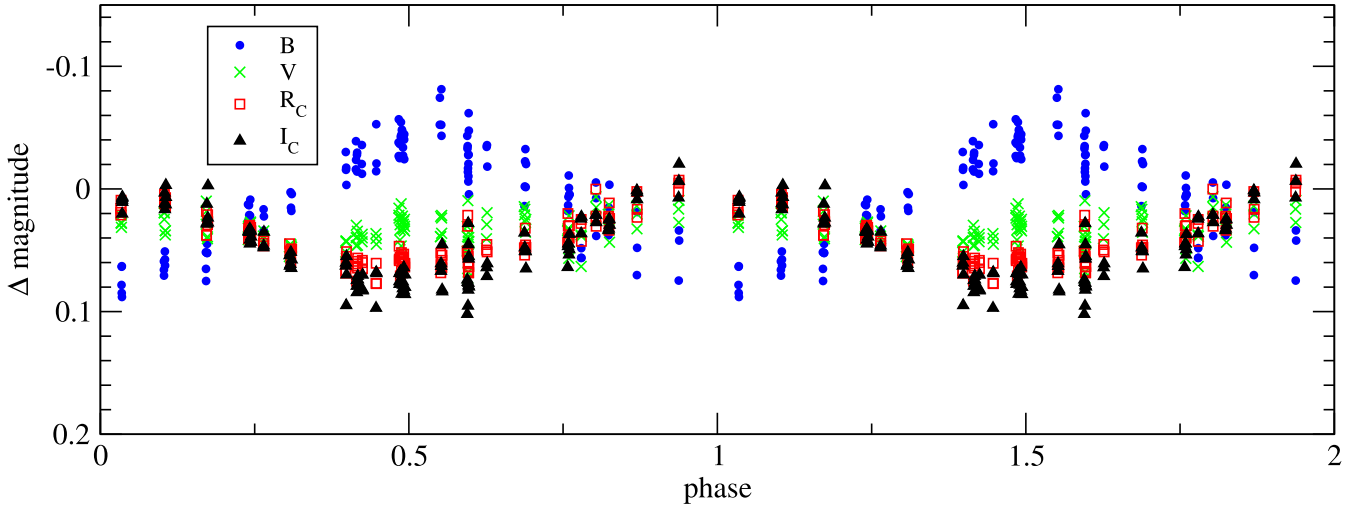


Figure 4. Colour photometry of KIC 2569073 showing antiphase correlation between B and V , R_C and I_C pass bands.

Table 1. Comparison of peak-to-peak amplitudes of the B , V , R_C and I_C photometric observations.

Band	Peak-to-peak amplitude (mag)	Peak-to-peak amplitude (mag) (Mochejska et al. 2003)
B	0.13	0.066
V	0.03	0.006
R_C	0.07	–
I_C	0.28	–
I	–	0.062
K_p	0.34	–

observed amplitude is A and n is the number of observations per oscillation cycle.

$$A = \frac{\sin(\pi/n)}{\pi/n} A_0. \quad (1)$$

To search for pulsation signatures, we identified the rotational frequency as $\nu_{\text{rot}} = 0.78909104 \mu\text{Hz}$ using PERIOD04 (Lenz & Breger 2005) and fitted and subtracted the first 15 harmonics of this frequency (Table 2). The Fourier transform of the residuals is displayed in Fig. 5. We were unable to identify any significant pulsation signatures above the noise level of $15 \mu\text{mag}$ up to a frequency of $3500 \mu\text{Hz}$. It is possible however that there are pulsations in this star below this level. We calculated upper limits for the true amplitudes of any rapid oscillations to be 750 and $90 \mu\text{mag}$ for the 5 and 25 min pulsation periods, respectively. These limits are much higher than the noise level due to amplitude attenuation caused by undersampling (equation 1).

To ensure we are able to detect stellar pulsations in *Kepler* LC data for roAp stars we downloaded the MAST LC data files of the four known roAp stars (KIC 10483436, KIC 10195926, KIC 4768731, KIC 7582608) which have pulsation modes identified in the SC data. We subjected these to the same systematics correction procedure as KIC 2569073. Once again we used PERIOD04 to search for pulsation signatures up to $3500 \mu\text{Hz}$. Only two of these known roAp stars, KIC 10195926 and KIC 7582608, show pulsation signatures above the noise level in the LC data, with the remaining two stars' amplitudes being too heavily attenuated by undersampling in LC for detection. These stars also have the highest oscillation amplitudes in the SC data. This suggests roAp stars may indeed have rapid oscillations which are simply below the limit of detection in LC

Table 2. Frequencies and amplitudes of the identified rotational frequency peaks in the frequency spectrum of KIC 2569073. All amplitudes are determined to $\pm 0.00002 \text{ mag}$.

ID	Frequency (μHz)	Amplitude (σ) (mag)
f_1	0.78909104	0.01718
$2f_1$	1.57818208	0.00149
$3f_1$	2.36727313	0.00039
$4f_1$	3.15636417	0.00017
$5f_1$	3.94545521	0.00011
$6f_1$	4.73454625	0.00002
$7f_1$	5.52363729	0.00004
$8f_1$	6.31272833	0.00004
$9f_1$	7.10181937	0.00005
$10f_1$	7.89091042	0.00004
$11f_1$	8.67995701	0.00006
$12f_1$	9.46904402	0.00002
$13f_1$	10.25813102	0.00004
$14f_1$	11.04721801	0.00003
$15f_1$	11.83630501	0.00002

data. Therefore, we cannot definitively rule out rapid oscillations in KIC 2569073, with amplitudes below our quoted limits. We have included the four roAp stars and their frequencies and amplitudes in Table 3.

3.3 Rotation period variations

The rotation of some Ap stars appears more complicated with evidence of rotational period variations occurring over time-scales of decades (Krtićka et al. 2017). Whilst these variations were of periodic nature and explained by torsional oscillations within the star, no short time-scale studies have been conducted to investigate the stability of these rotation periods. With the unique quality and quantity of data of an α^2 CVn star from *Kepler*, we conducted an observed-minus-calculated (O–C) analysis of the light curve. This constitutes the first in-depth analysis of the stability of the rotation period of an α^2 CVn star and is important in searching for possible spot variation on short time-scales.

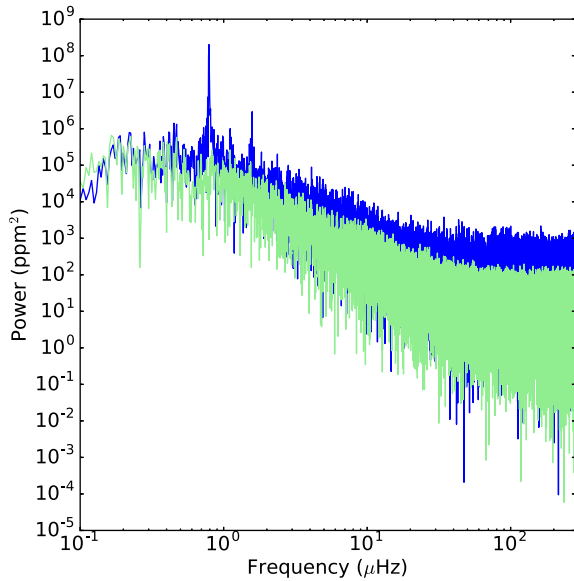


Figure 5. Logarithmic power spectrum of KIC 2569073 (blue), overlaid with the spectrum after removing the main oscillation period and its first 15 harmonics (green).

Table 3. Rapid oscillation frequencies of known *Kepler* roAp stars and their amplitudes from SC data.

KIC ID	Frequency (μHz)	Amplitude (mmag)
10483436	1353	0.068
10195926	972.6	0.176
4768731	711.2	0.062
7582608	2103.4	1.45

We determined the phase variations by a template-fitting O–C method (Sódor et al. 2017) that takes into account the shape of the full rotationally modulated light curve.

To describe the shape of the rotationally modulated light curve unaffected by amplitude, phase and zero-point variations, we fitted 15 harmonics of the rotation frequency (0.0681757 d^{-1}) to a 90 d section of the data starting at 630 d (approximately the section shown in Fig. 2, upper panel), where light-curve-shape variations are negligible. We refer to the result of this Fourier-fit as the template rotation curve (Fig. 6).

For the calculated times of maxima (C), we used the ephemeris

$$T_{\text{max}} = T_0 + 14.6680 \text{ d} \times E,$$

where E is the epoch number, showing the elapsed rotation cycles since the reference epoch, $T_0 = 257.00 \text{ d}$ (BJD 2455090.00). The reference epoch was selected to avoid the presence of large data gaps in the light curve.

The observed times of maxima (O) were determined by fitting the phase shift, along with an amplitude scaling factor and a magnitude zero-point, of the template rotation curve to one rotation-period-long light-curve segments. We omitted segments with poor rotation-phase coverage caused by gaps in the data. The obtained O–C diagram (Fig. 7) contains 65 data points.

Systematic trends in the data typically have similar time-scales to the rotation period. This makes decoupling intrinsic spot (light-curve shape) variations on time-scales of the order of the rotation period difficult. Our O–C analysis shows no coherent variations in the rotation period on time-scales longer than this period.

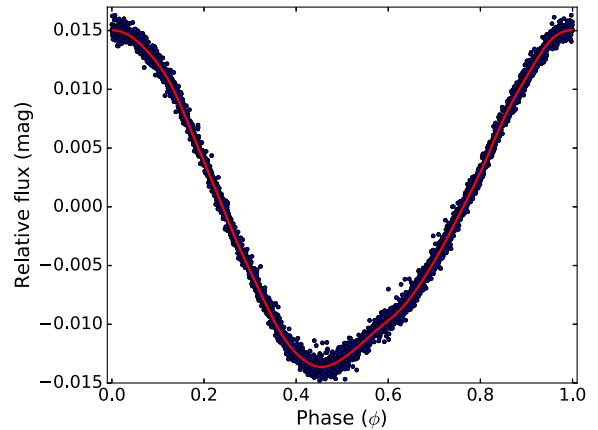


Figure 6. Template rotation curve for KIC 2569073 (red) used to calculate the O–C diagram with 90 d segment of light curve starting at 630 d and phase-folded on the rotation period (blue).

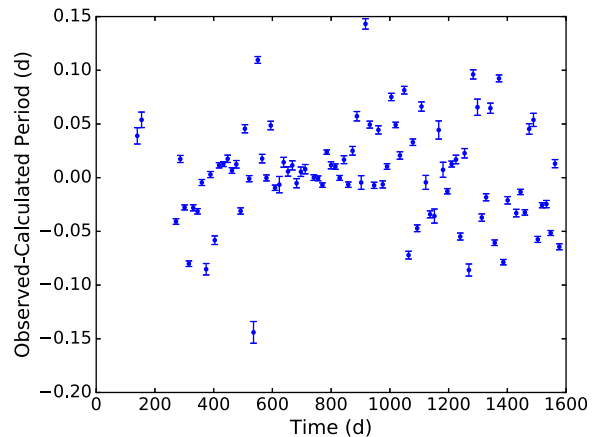


Figure 7. O–C diagram of KIC 2569073 based on the template light curve.

For spot variations on shorter time-scales, the light-curve shape should change visibly from one rotation period to the next. To test this, we plotted the phase-shifted light curve, overlaying the rotational modulation signal upon itself. We detected some minor changes in the light-curve shape in the vicinity of maxima and minima (e.g. at $\sim 373 \text{ d}$), however the strongest period variations in these regions appear to be associated with preceding gaps in the light curve and thus we have concluded these changes originate from instrumental effects. This is supported by the stability in both the light-curve shape and the O–C diagram between 630 and 720 d, where instrumental trends appear to be almost negligible.

We note that the standard errors of the above described fitting process take into account only short time-scale uncorrelated (assumed Gaussian) noise, but do not reflect longer time-scale instrumental variations in the data. To obtain more realistic uncertainty estimations, we repeated the fitting process with light curves de-trended using different order non-linear trends fit to each quarter separately. The median O–C deviation between the different de-trended light curves was calculated to be $\sim 0.11 \text{ d}$. This is twice the standard deviation of the best O–C analysis. As such we conclude that there is no evidence for short-term period variation in the spots of KIC 2569073. They appear to be well anchored to the same position on the star.

4 SUMMARY

We have determined KIC 2569073 to be an α^2 CVn star with a rotational period of 14.668 d. Its peak-to-peak amplitude of 0.034 mag makes it one of the most variable Ap stars in the *Kepler* field. We notice a large change in amplitude of the rotational modulation between the Kepler data set and the one obtained by Mochejska et al. (2003) between 1996 and 2002. Due to the difficulties in obtaining a Kepler light curve free from artefacts of the reduction, we were unable to say whether the pulsational amplitude remains constant over the 4 yr *Kepler* data set. However, it is approximately constant, and changes of the amplitude seen between the Kepler data and the photometry of Mochejska et al. (2003) are not replicated within the *Kepler* data set. Further, we looked for period variations in the 4 yr *Kepler* data set by varying the de-trending parameters in the light-curve reduction and conducting O–C analyses. We determined the period to be constant, within the global uncertainties. These results are important in framing the time-scales of spot evolution for Ap stars.

We have also presented colour photometry, which shows an antiphase relationship between the *B* light curve and the *V*, *R* and *I* light curves. This relationship, along with the long time-scale amplitude modulation in the *Kepler* ($\sim V$) passband, suggests that KIC 2569073 may be particularly useful for studying the formation and evolution of stellar magnetic fields and atmospheres.

ACKNOWLEDGEMENTS

We thank the referee B. Smalley for his comments, which greatly improved this paper.

Funding for the Stellar Astrophysics Centre is provided by The Danish National Research Foundation (Grant agreement no.: DNR106).

IRAF is distributed by the National Optical Astronomy Observatories, which are operated by the Association of Universities for Research in Astronomy, Inc., under cooperative agreement with the National Science Foundation.

This project has been supported by the Hungarian National Research, Development and Innovation Office Grants K-113117, K-115709, K-119517 and PD-116175 of the Hungarian National Research, Development and Innovation Office. AD has been supported by the Postdoctoral Fellowship Programme of the Hungarian Academy of Sciences and by the Tempus Közalapítvány and the MÁEÖ. LM and ÁS have been supported by the János Bolyai Research Scholarship of the Hungarian Academy of Sciences. AD and LSz would like to thank the City of Szombathely for support under Agreement No. 67.177-21/2016.

REFERENCES

- Abt H. A., Morrell N. I., 1995, *ApJS*, 99, 135
 Babcock H. W., 1947, *Phys. Rev.*, 72, 83
 Babcock H. W., 1949, *The Observatory*, 69, 191
 Balona L. A. et al., 2011a, *MNRAS*, 410, 517
 Balona L. A. et al., 2011b, *MNRAS*, 413, 2651
 de Marchi F. et al., 2007, *A&A*, 471, 515
 Gray R. O., Corbally J. C., 2009, *Stellar Spectral Classification*. Princeton University Press, Princeton, NJ
 Gröbel R., Hümmerich S., Paunzen E., Bernhard K., 2017, *New Astron.*, 50, 104
 Holdsworth D. L., Smalley B., Kurtz D. W., Southworth J., Cunha M. S., Clubb K. I., 2014, *MNRAS*, 443, 2049
 Hubrig S., North P., Mathys G., 2000, *ApJ*, 539, 352
 Kazarovets E. V., Samus N. N., Durlevich O. V., Kireeva N. N., Pastukhova E. N., 2013, *Inf. Bull. Var. Stars*, 6052
 Koch D. G. et al., 2010, *ApJ*, 713, L79
 Krtićka J., Mikulášek Z., Henry G. W., Kurfürst P., Karlický M., 2017, *MNRAS*, 464, 933
 Kuehn C. A., Drury J. A., Bellamy B. R., Stello D., Bedding T. R., Reed M., Quick B., 2015, in García R. A., Ballot J., eds, *European Physical Journal Web of Conferences*, Vol. 101. p. 06040
 Kurtz D. W., 1982, *MNRAS*, 200, 807
 Kurtz D. W., Marang F., van Wyk F., Roberts G., 1996, *MNRAS*, 280, 1
 Kurtz D. W. et al., 2011, *MNRAS*, 414, 2550
 Lenz P., Breger M., 2005, *Commun. Asteroseismol.*, 146, 53
 Mochejska B. J., Stanek K. Z., Kaluzny J., 2003, *AJ*, 125, 3175
 Molnar M. R., 1973, *ApJ*, 179, 527
 Murphy S. J., 2012, *MNRAS*, 422, 665
 Murphy S. J., Shibahashi H., Kurtz D. W., 2013, *MNRAS*, 430, 2986
 North P., 1998, *A&A*, 334, 181
 Renson P., Manfroid J., 2009, *A&A*, 498, 961
 Smalley B. et al., 2015, *MNRAS*, 452, 3334
 Smith K. C., 1996, *A&A*, 305, 902
 Sódor Á., Skarka M., Liška J., Bognár Z., 2017, *MNRAS*, 465, L1
 Stępień K., 2000, *A&A*, 353, 227
 Stetson P. B., Bruntt H., Grundahl F., 2003, *PASP*, 115, 413
 Stibbs D. W. N., 1950, *MNRAS*, 110, 395
 Wolff S. C., 1983, *The A-stars: Problems and Perspectives*. Monograph Series on Nonthermal Phenomena in Stellar Atmospheres. NASA Spec. Publ., NASA SP-463

This paper has been typeset from a \LaTeX file prepared by the author.