

```

In[1]:= ClearAll["Global`*"]
coordinateList = {θ, φ}; (* (θ, φ) in terms of (θ, φ) *)

(* Define gμν *)
g =  $\begin{pmatrix} 1 & 0 \\ 0 & \sin[\theta]^2 \end{pmatrix}$ ;

(* Initialize Γμνρ as rank 3 tensor *)
tmp[a_, b_, c_] := 0;
Γ = Array[tmp, {2, 2, 2}];

(* Loop over indices in Γμνρ *)
Do[
  Do[
    Do[
      Do[
        xλ = coordinateList[[λ]];
        xμ = coordinateList[[μ]];
        xv = coordinateList[[ν]];

        Γ[[σ, λ, μ]] +=  $\frac{1}{2}$  (Inverse[g]][[ν, σ]] (∂xλ g[[μ, ν]] + ∂xμ g[[λ, ν]] - ∂xν g[[μ, λ]]);

        (* Γμνρ =  $\frac{1}{2}$  gνσ (  $\frac{\partial g_{\mu\nu}}{\partial x^\lambda} + \frac{\partial g_{\lambda\nu}}{\partial x^\mu} - \frac{\partial g_{\mu\lambda}}{\partial x^\nu}$  ) *)
        {ν, {1, 2}},
        {μ, {1, 2}},
        {λ, {1, 2}},
        {σ, {1, 2}}]

Print["Γθνρ = ", MatrixForm[FullSimplify[Γ[[1]]]]]
Print["Γφνρ = ", MatrixForm[FullSimplify[Γ[[2]]]]]

Γθνρ =  $\begin{pmatrix} 0 & 0 \\ 0 & -\cos[\theta] \sin[\theta] \end{pmatrix}$ 
Γφνρ =  $\begin{pmatrix} 0 & \cot[\theta] \\ \cot[\theta] & 0 \end{pmatrix}$ 

```