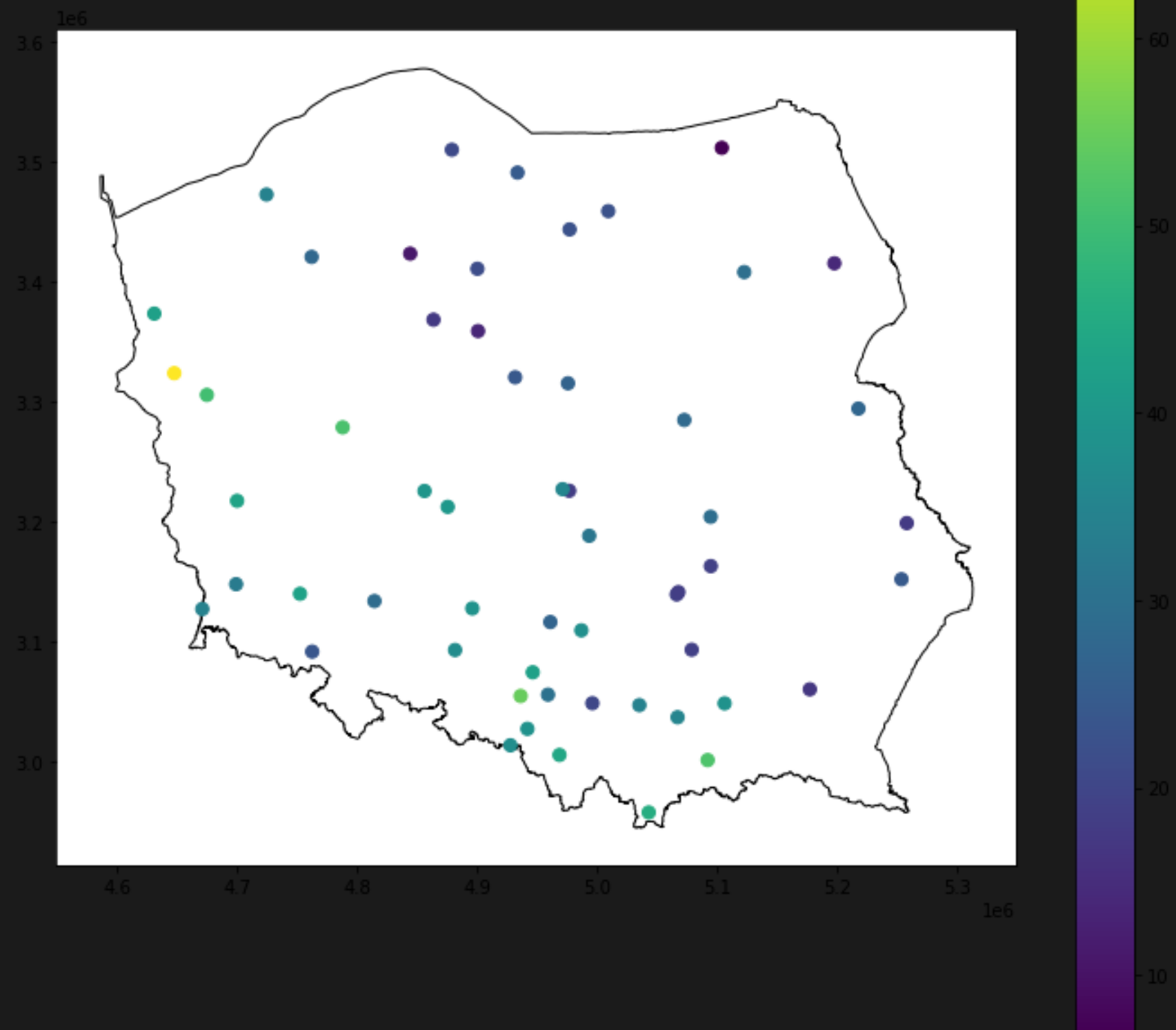


Interpolacja zanieczyszczenia powietrza na podstawie danych z czujników udostępnionych przez Główny Inspektorat Ochrony Środowiska z wykorzystaniem metody Krigingu

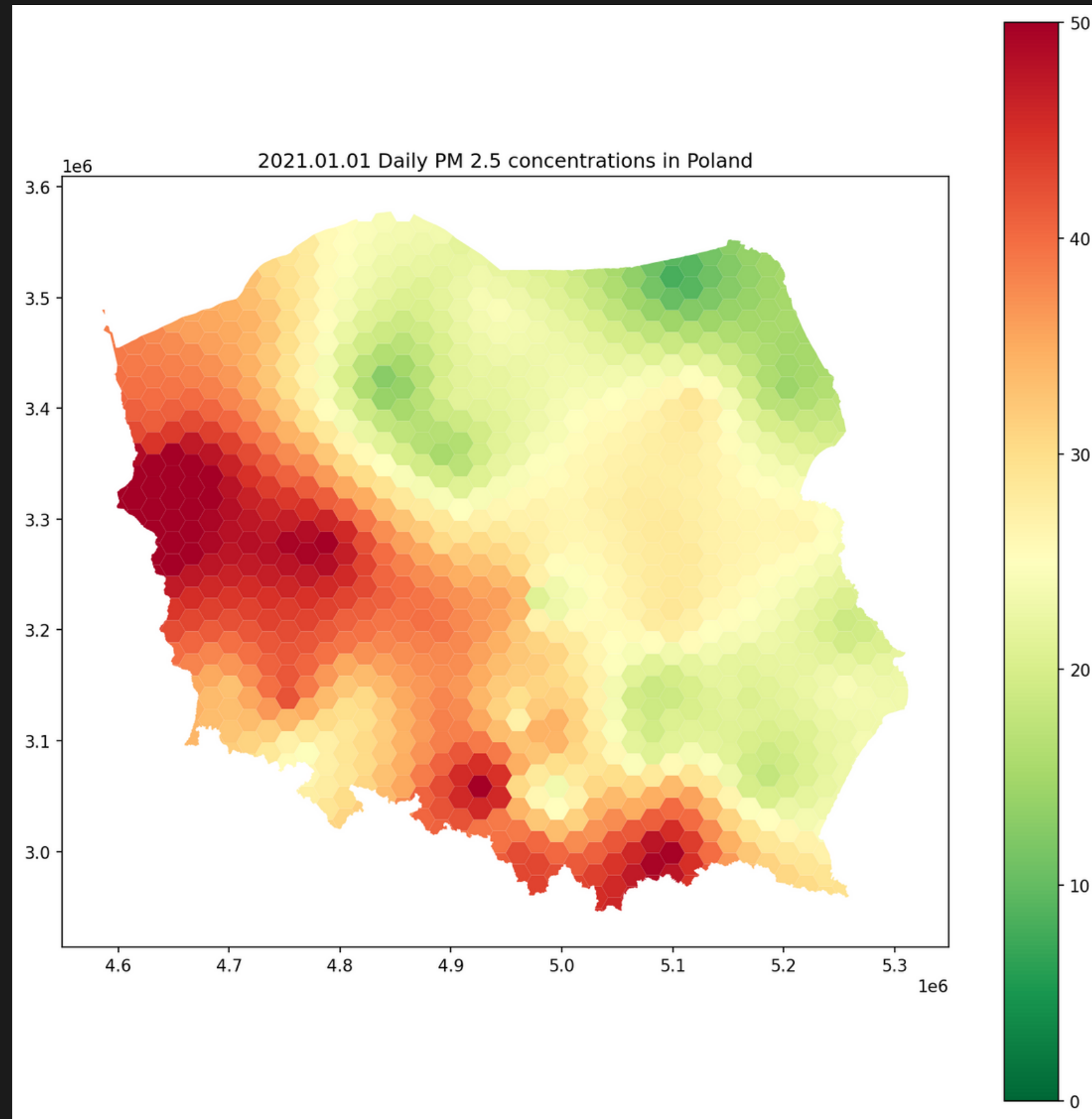
(Mniejszy) Problem

<http://powietrze.gios.gov.pl/pjp/archive>
s



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Cel: "pełne"
pokrycie
powierzchni Polski



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Inverse Distance Weighting



Jak?

$$\hat{y} = \frac{\sum_i \lambda_i y_i}{\sum_i \lambda_i}$$

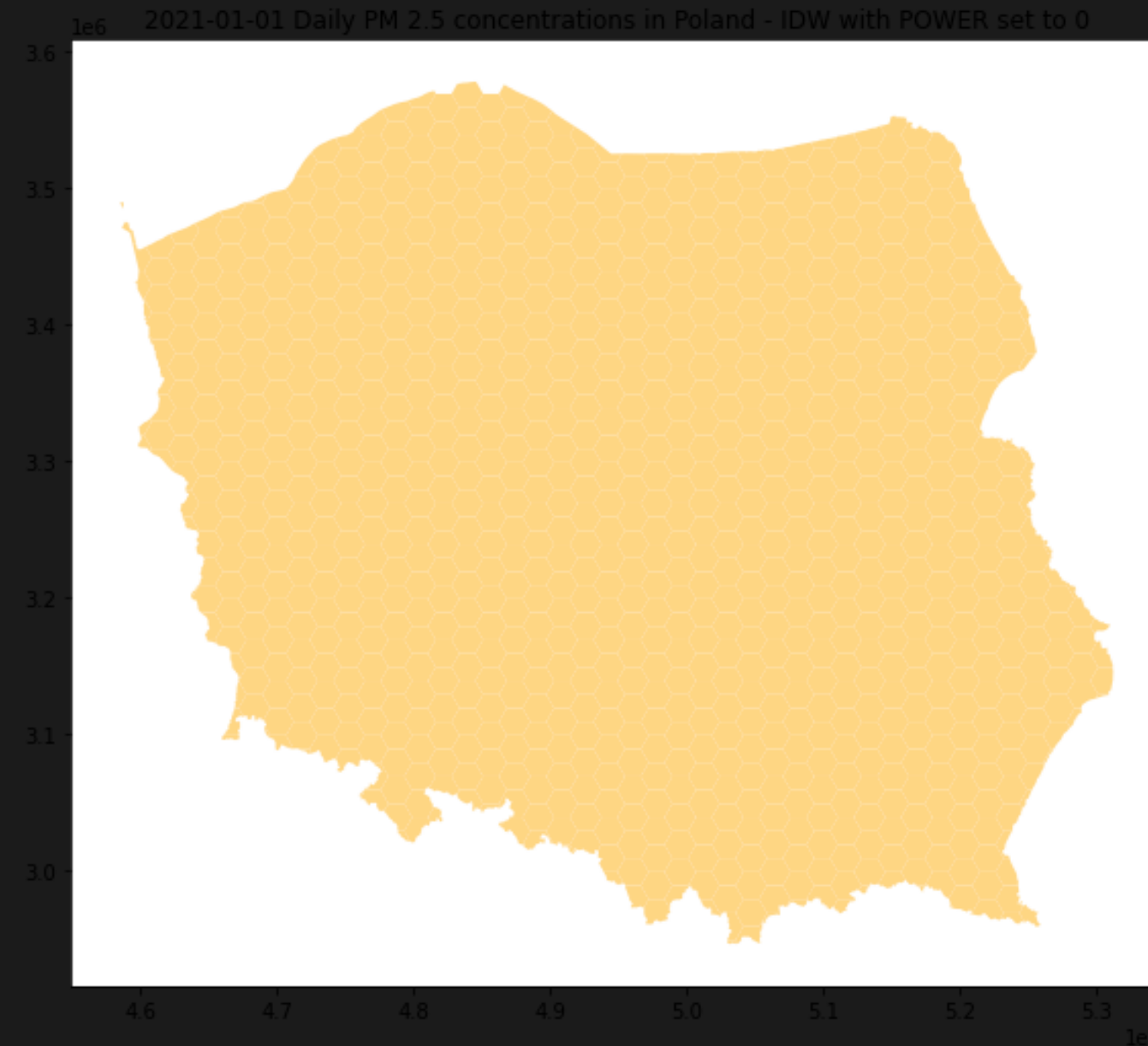
$$\lambda_i = \frac{1}{\left(d_i\right)^p}$$

Inverse Distance Weighting

$$\hat{y} = \frac{\sum_i \lambda_i y_i}{\sum_i \lambda_i}$$

$$\lambda_i = \frac{1}{\left(d_i\right)^p}$$

$$p = 0$$



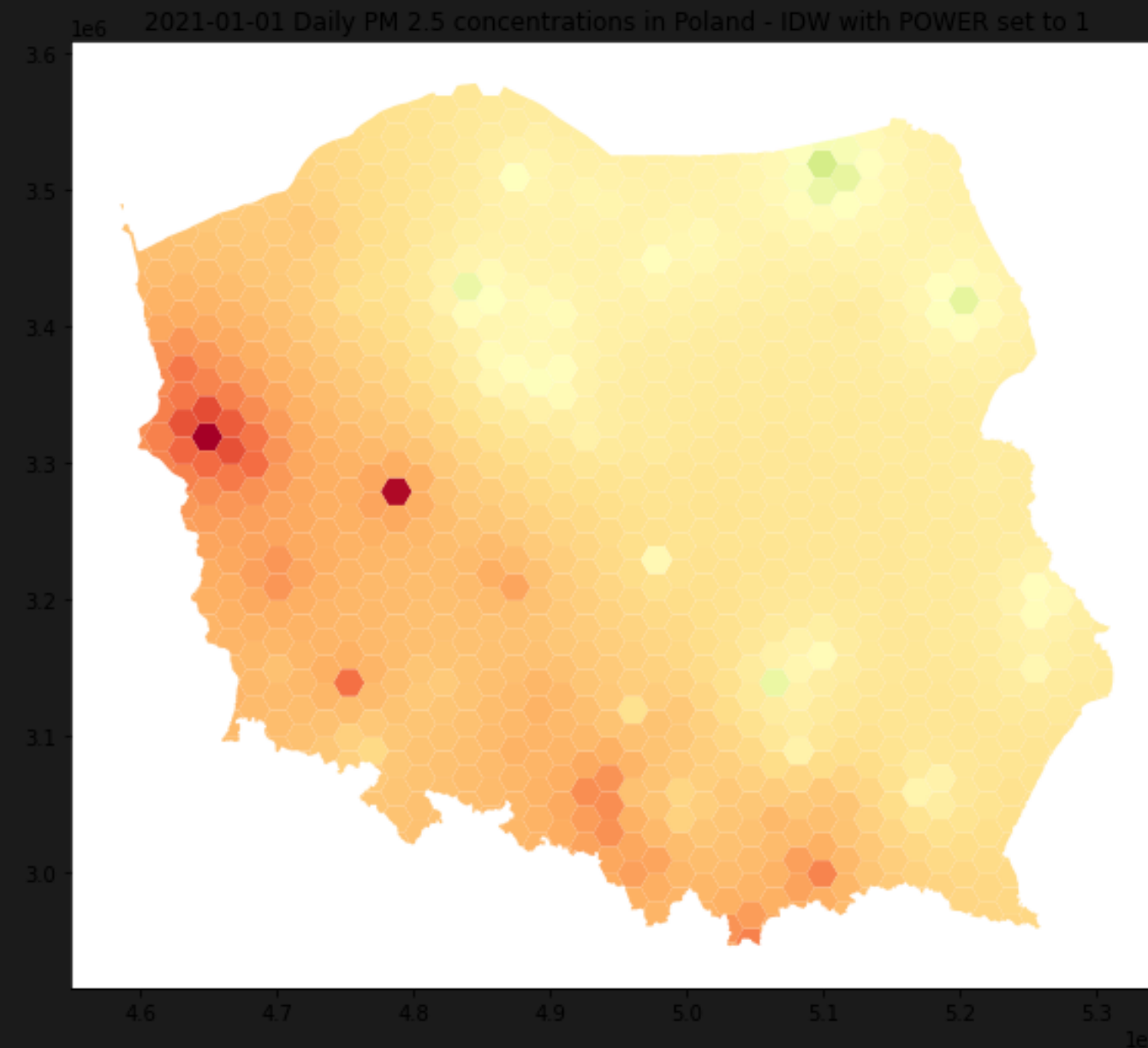
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Inverse Distance Weighting

$$\hat{y} = \frac{\sum_i \lambda_i y_i}{\sum_i \lambda_i}$$

$$\lambda_i = \frac{1}{\left(d_i\right)^p}$$

$p = 1$



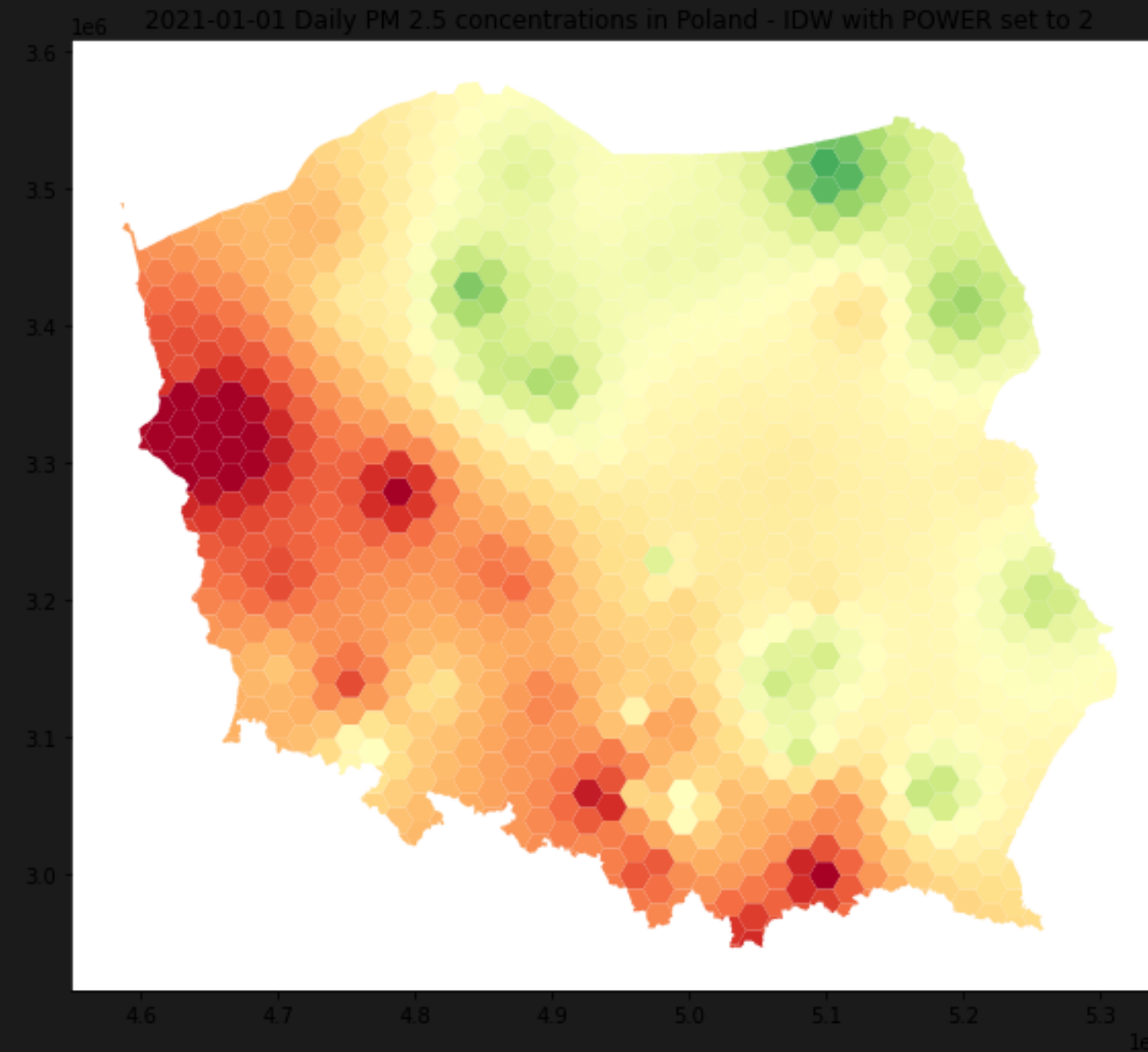
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Inverse Distance Weighting

$$\hat{y} = \frac{\sum_i \lambda_i y_i}{\sum_i \lambda_i}$$

$$\lambda_i = \frac{1}{\left(d_i\right)^p}$$

$$p = 2$$



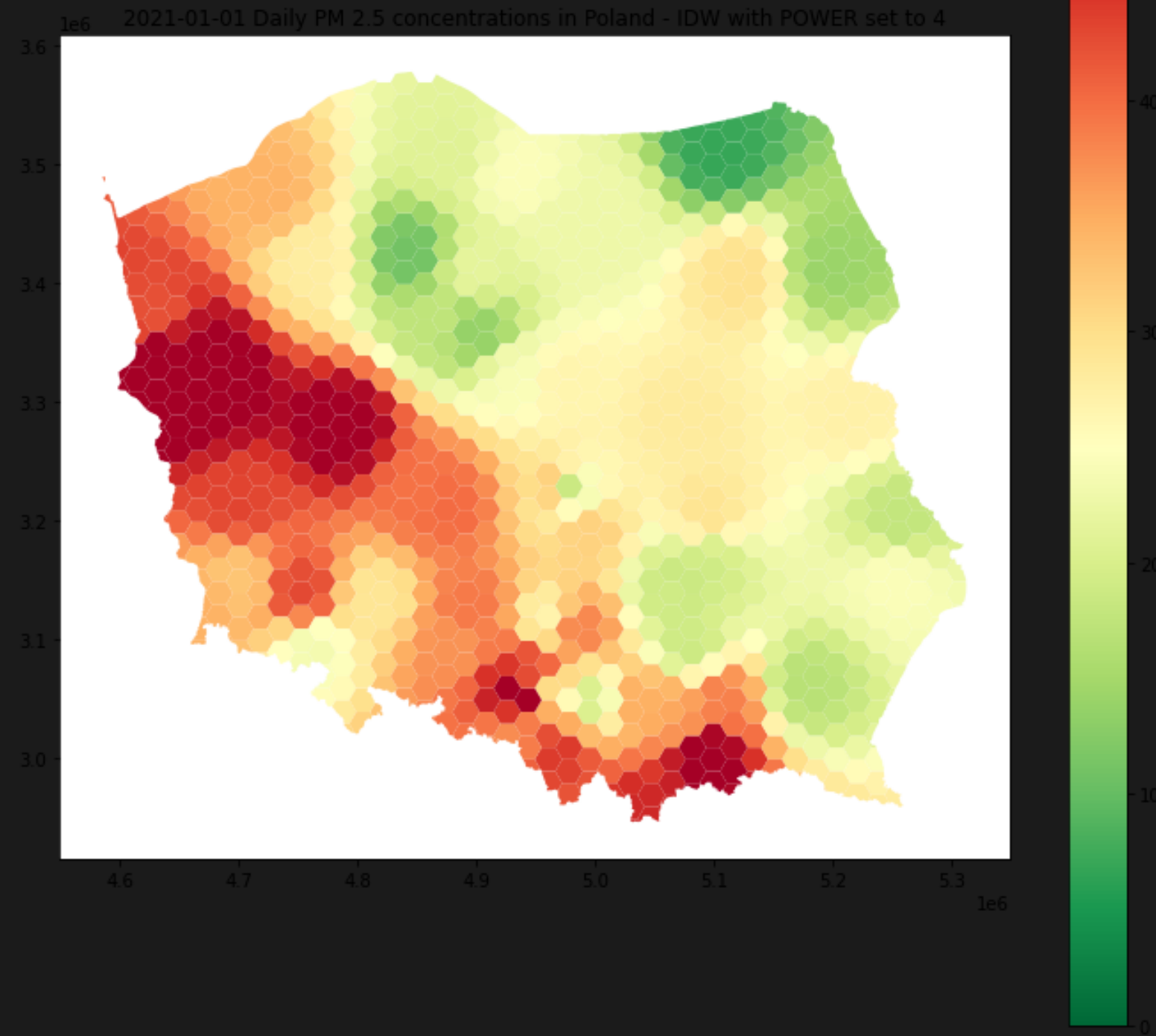
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Inverse Distance Weighting

$$\hat{y} = \frac{\sum_i \lambda_i y_i}{\sum_i \lambda_i}$$

$$\lambda_i = \frac{1}{\left(d_i\right)^p}$$

p == 4



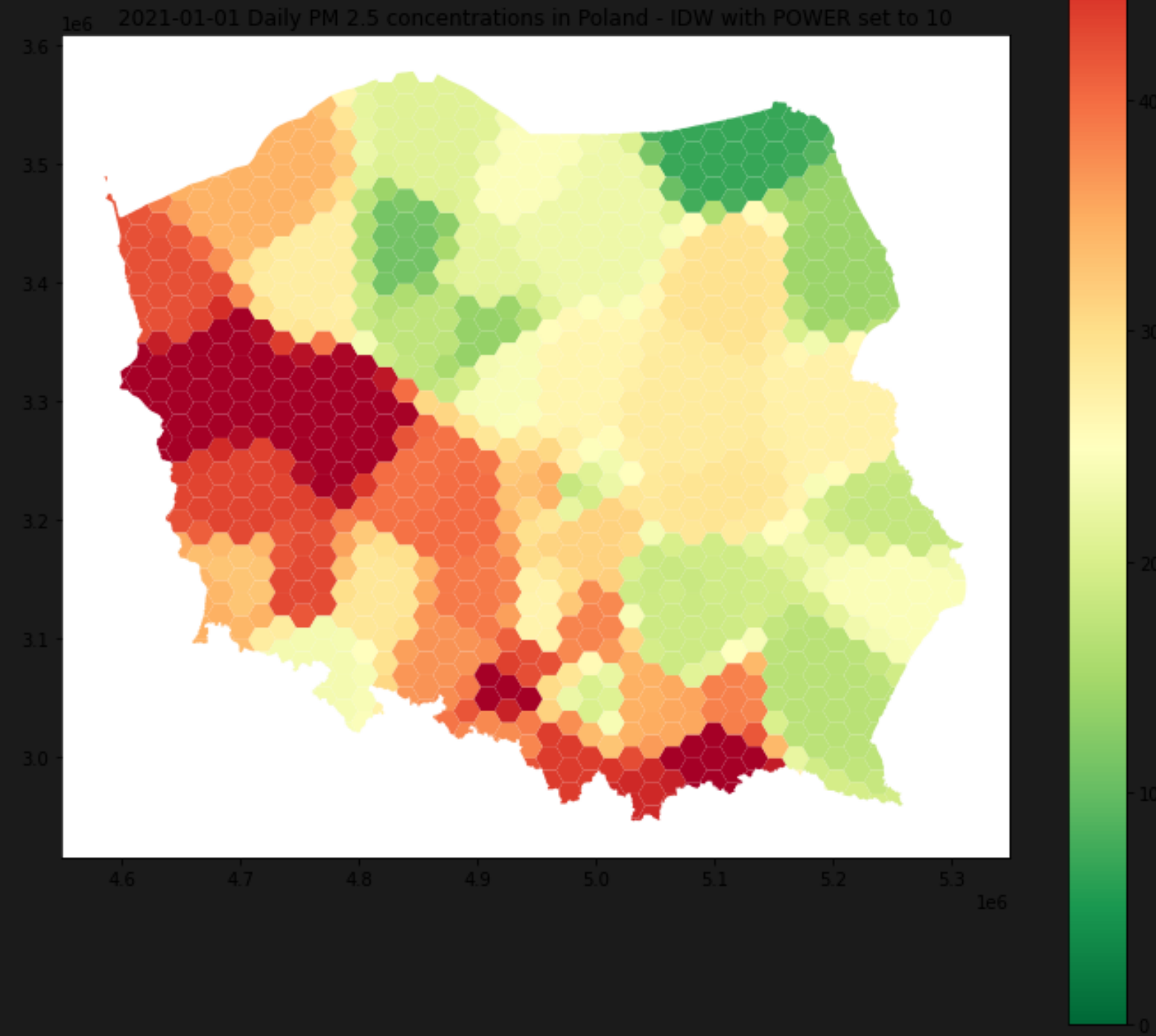
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Inverse Distance Weighting

$$\hat{y} = \frac{\sum_i \lambda_i y_i}{\sum_i \lambda_i}$$

$$\lambda_i = \frac{1}{\left(d_i\right)^p}$$

p == 10



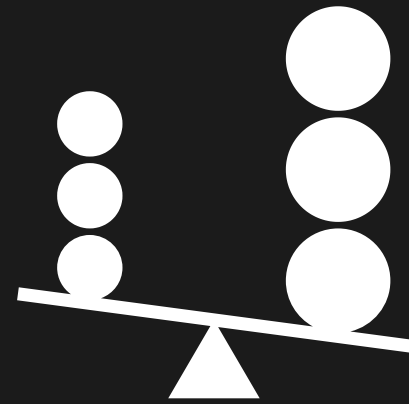
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$$\hat{y} = \frac{\sum_i \lambda_i y_i}{\sum_i \lambda_i}$$

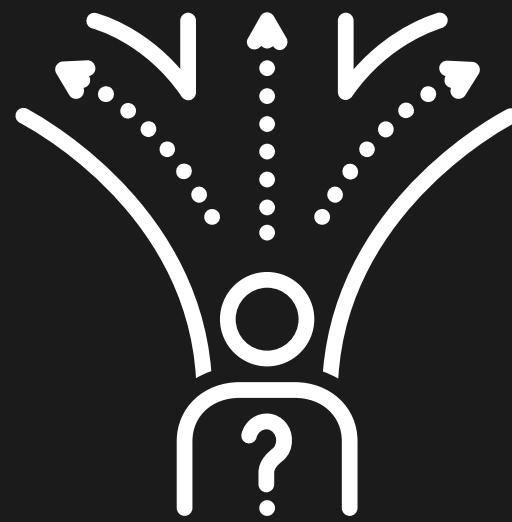
$$\lambda_i = \frac{1}{\left(d_i\right)^p}$$

Problemy

Inverse Distance Weighting



Jaka waga jest właściwa?



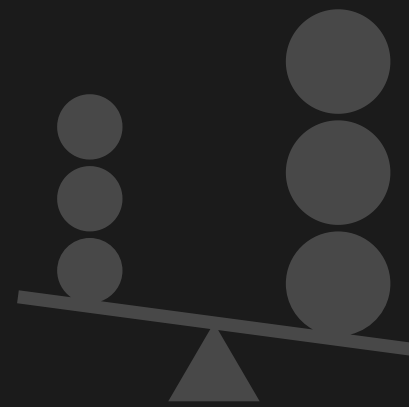
Jak estymować błąd
predykcji?

Inverse Distance Weighting

$$\hat{y} = \frac{\sum_i \lambda_i y_i}{\sum_i \lambda_i}$$

$$\lambda_i = \frac{1}{\left(d_i\right)^p}$$

Problemy



Jaka waga jest właściwa?



Jak estymować błąd
przewidywania?

WALIDACJA
KRZYŻOWA

Inverse Distance Weighting

$$\hat{y} = \frac{\sum_i \lambda_i y_i}{\sum_i \lambda_i}$$

$$\lambda_i = \frac{1}{(d_i)^p}$$

Problemy

**NIEWIELKA LICZBA
PRÓBEK**

Kriging



Czy można to
poprawić?

$$\hat{z} = \sum_{i=1}^K \lambda_i z_i$$

$$\sum_{j=1}^K \lambda_j C(x_i, x_j) - \mu = \overline{C}(x_i, V); i = 1, 2, \dots, K$$

$$\sum_{j=1}^K \lambda_j = 1$$

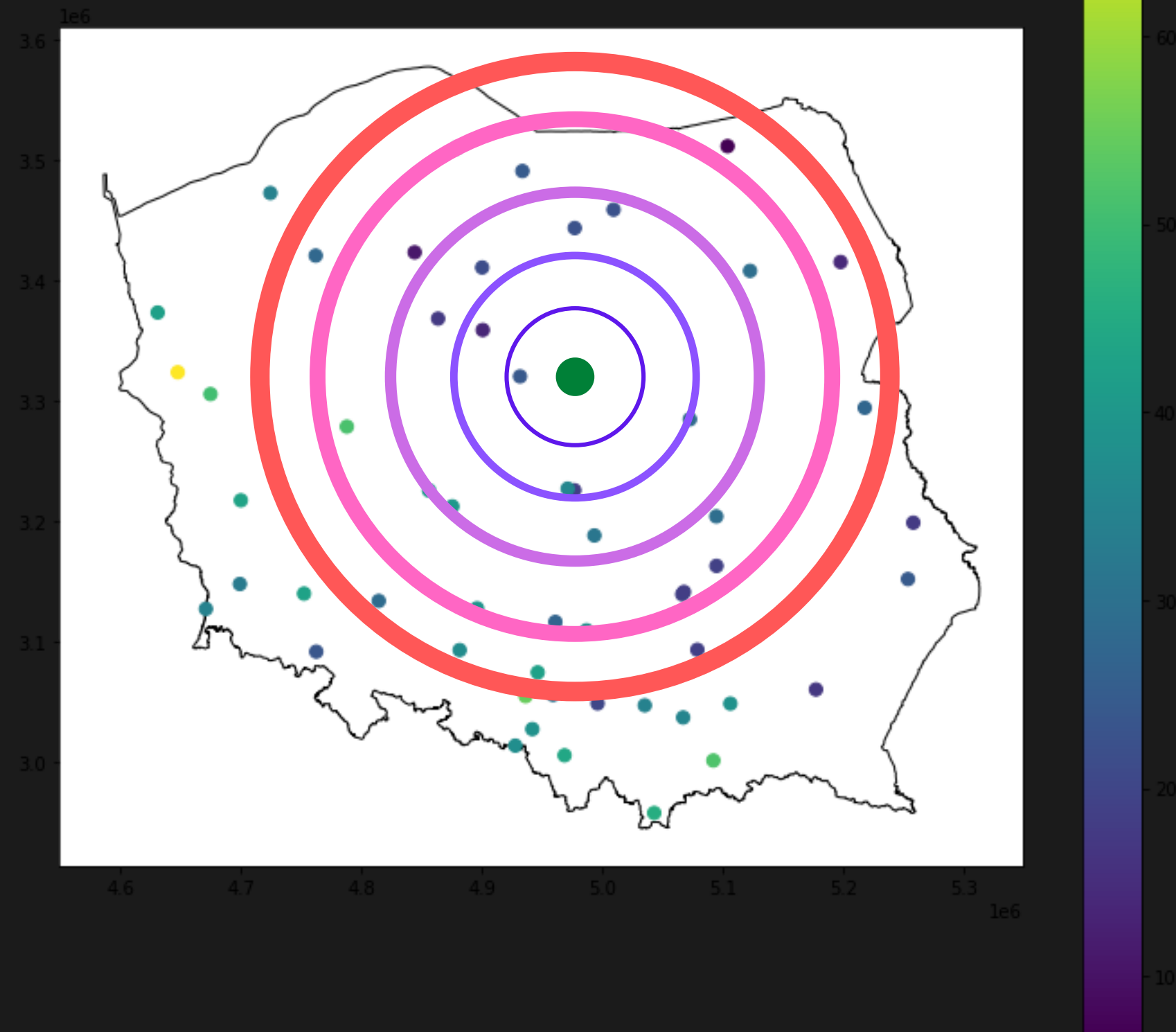
$$\hat{z} = \sum_{i=1}^K \lambda_i z_i$$

$$\sum_{j=1}^K \lambda_j C(x_i, x_j) - \mu = \overline{C}(x_i, V); i = 1, 2, \dots, K$$

$$\sum_{j=1}^K \lambda_j = 1$$

Zmienność w
przestrzeni

Kriging



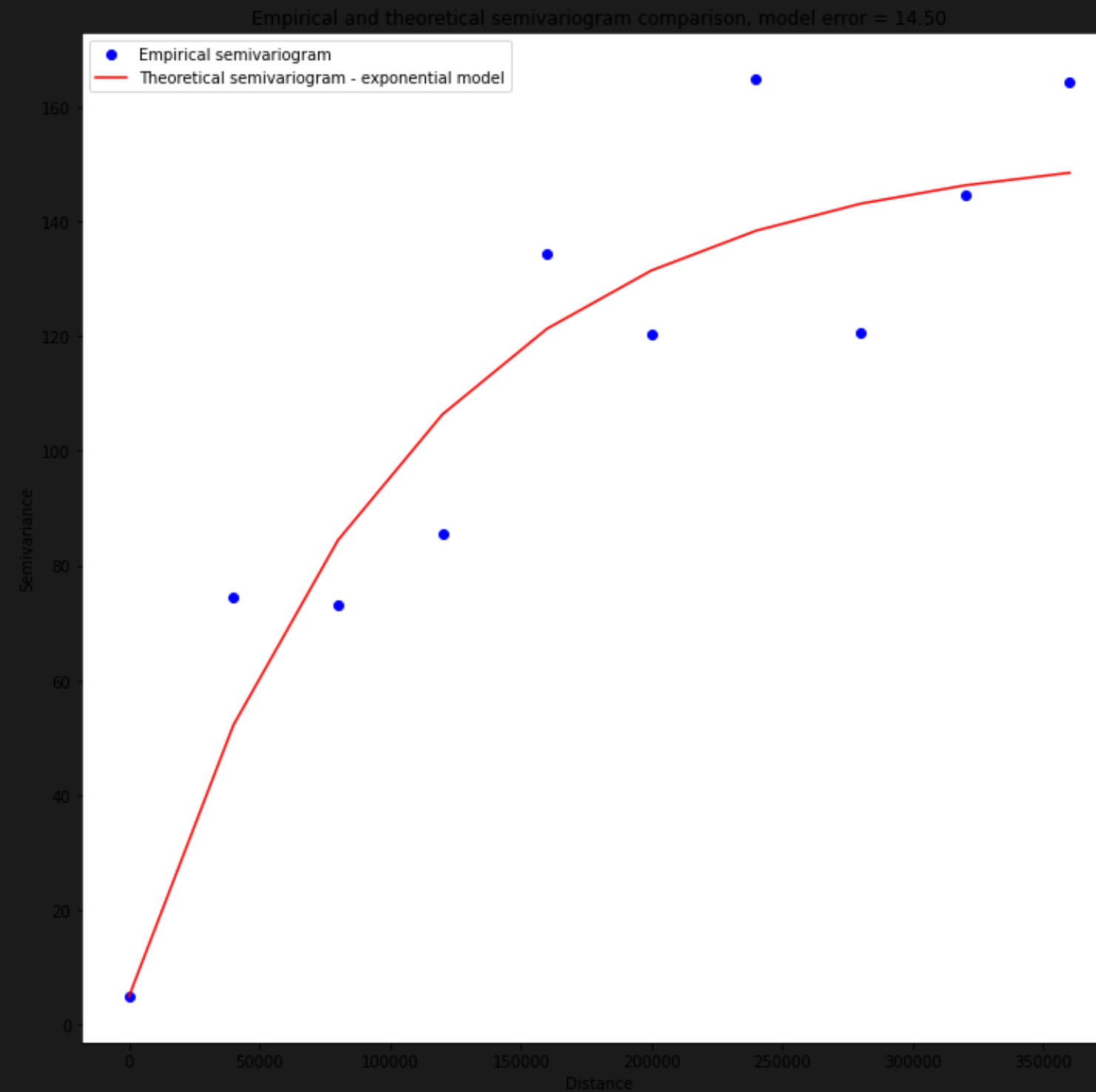
Kriging

$$\widehat{z} = \sum_{i=1}^K \lambda_i z_i$$

$$\sum_{j=1}^K \lambda_j C(x_i, x_j) - \mu = \overline{C}(x_i, V); i = 1, 2, \dots, K$$

$$\sum_{j=1}^K \lambda_j = 1$$

Semiwarijancja



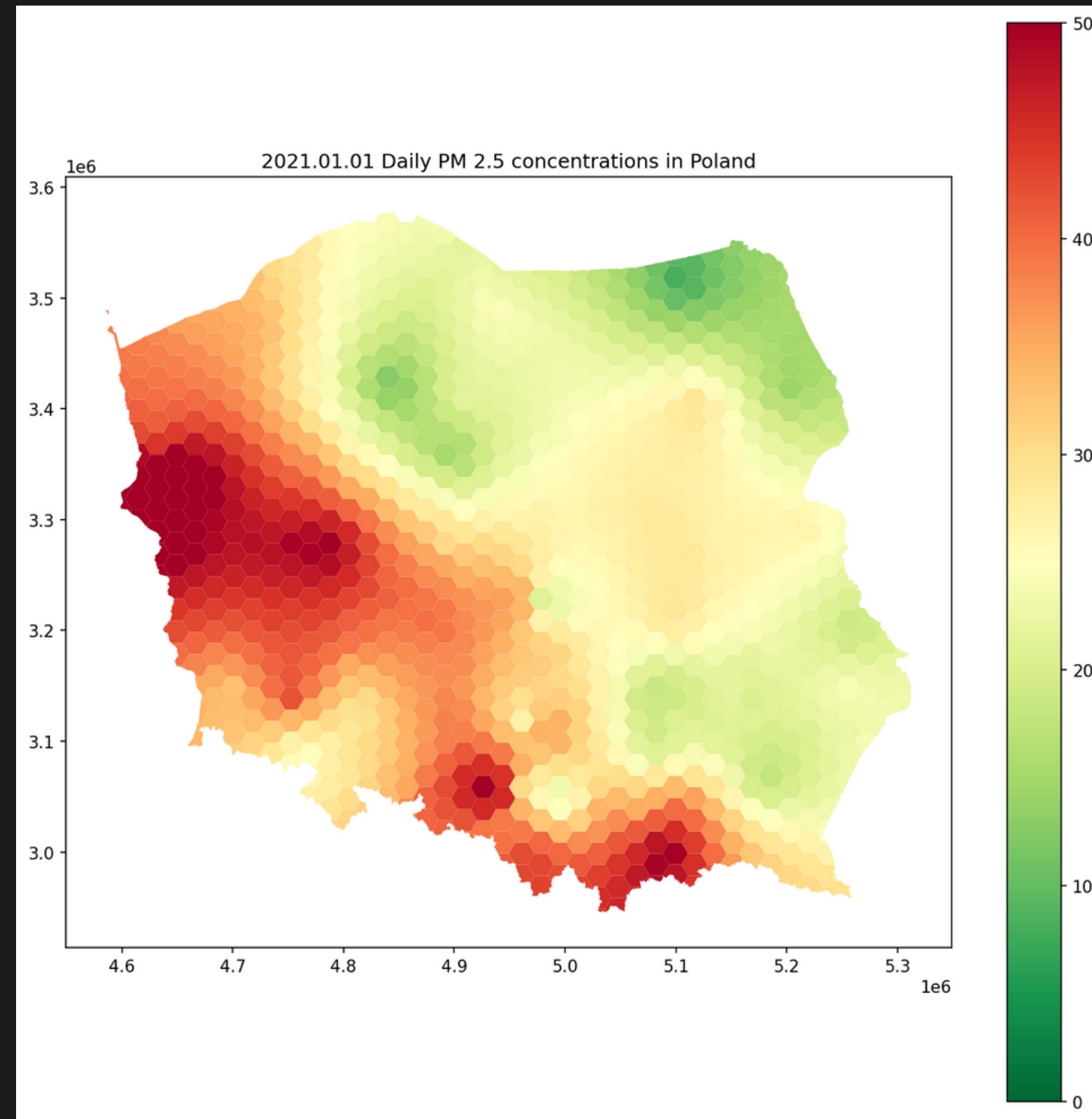
$$\widehat{z} = \sum_{i=1}^K \lambda_i z_i$$

$$\sum_{j=1}^K \lambda_j C(x_i, x_j) - \mu = \overline{C}(x_i, V); i = 1, 2, \dots, K$$

$$\sum_{j=1}^K \lambda_j = 1$$

Kriging

Kriging



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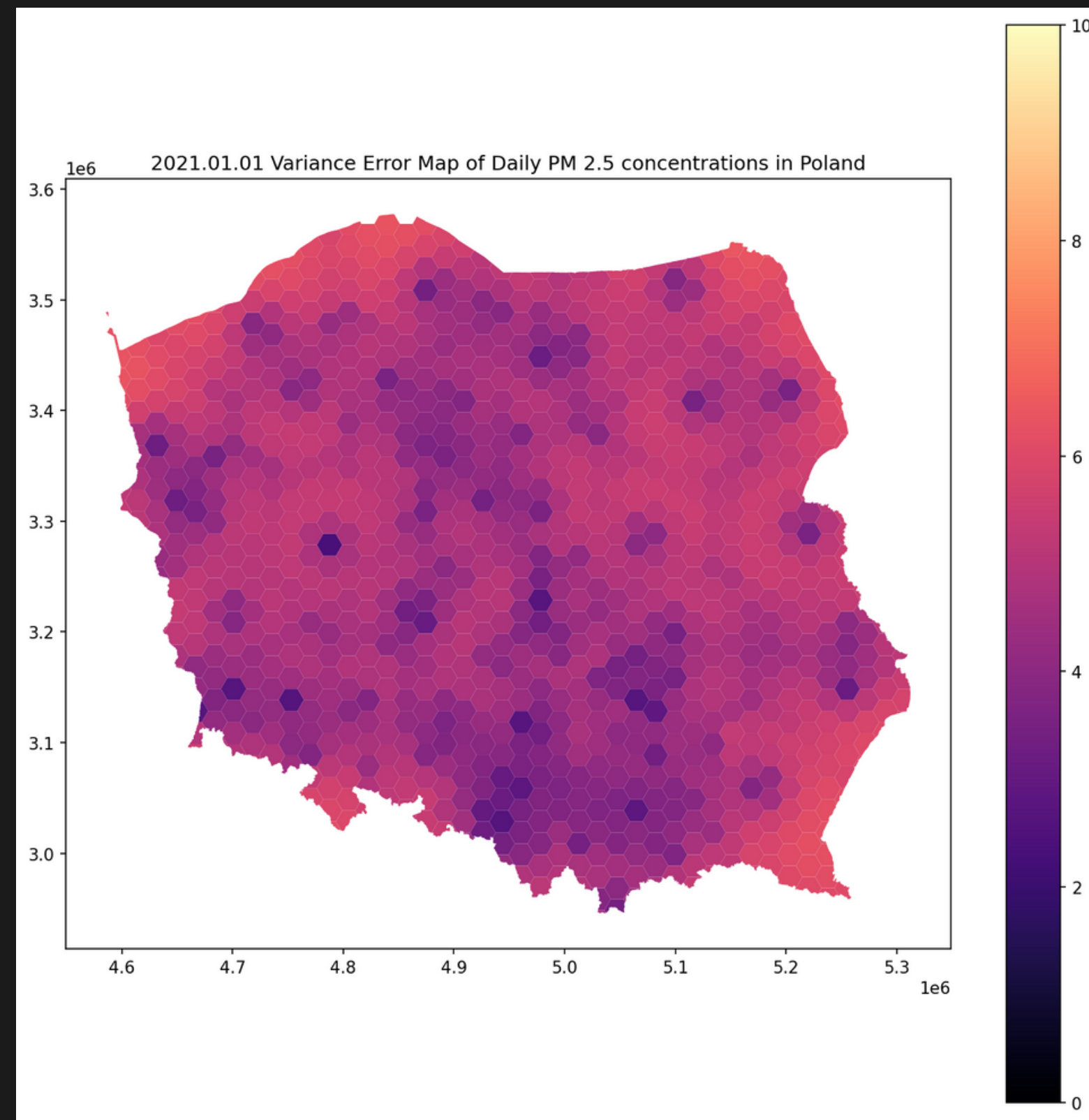
$$\widehat{z} = \sum_{i=1}^K \lambda_i z_i$$

$$\sum_{j=1}^K \lambda_j C(x_i, x_j) - \mu = \overline{C}(x_i, V); i = 1, 2, \dots, K$$

$$\sum_{j=1}^K \lambda_j = 1$$

Przedział błędu

Kriging



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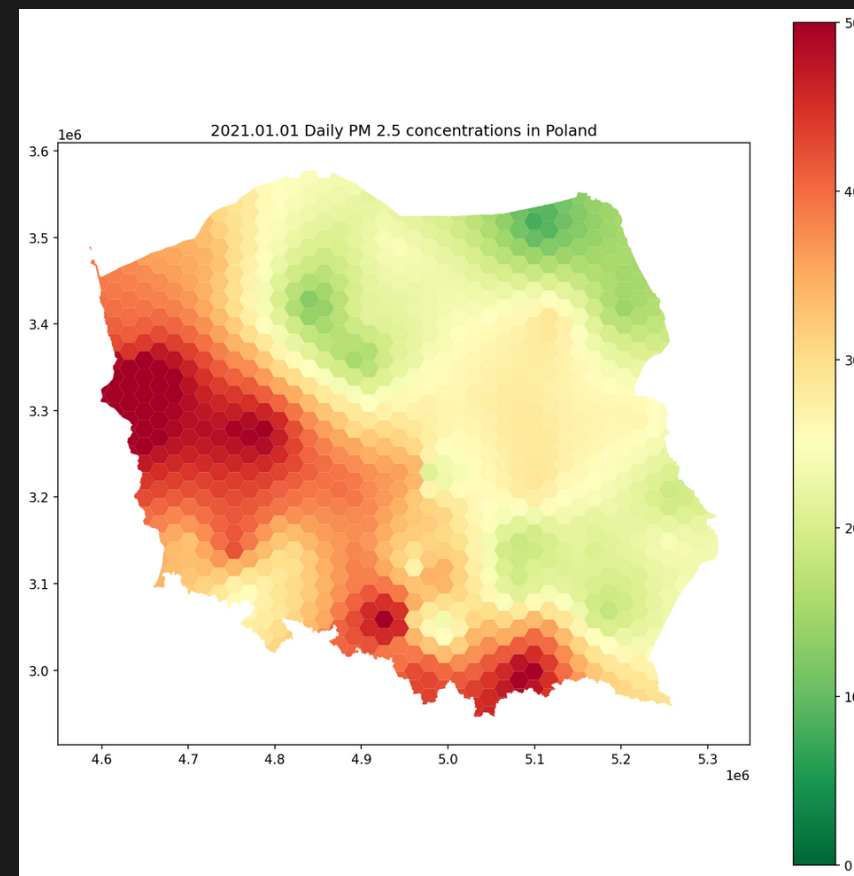
$$\widehat{z} = \sum_{i=1}^K \lambda_i z_i$$

$$\sum_{j=1}^K \lambda_j C(x_i, x_j) - \mu = \overline{C}(x_i, V); i = 1, 2, \dots, K$$

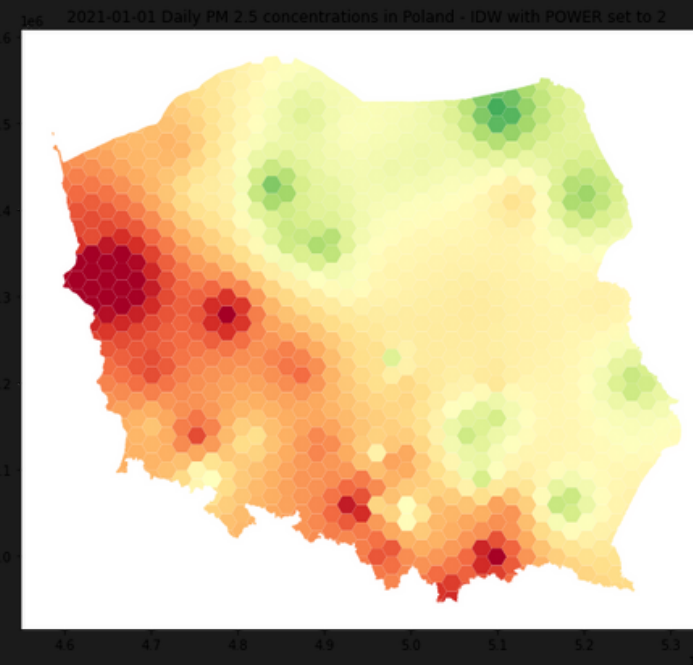
$$\sum_{j=1}^K \lambda_j = 1$$

Zestawienie z IDW

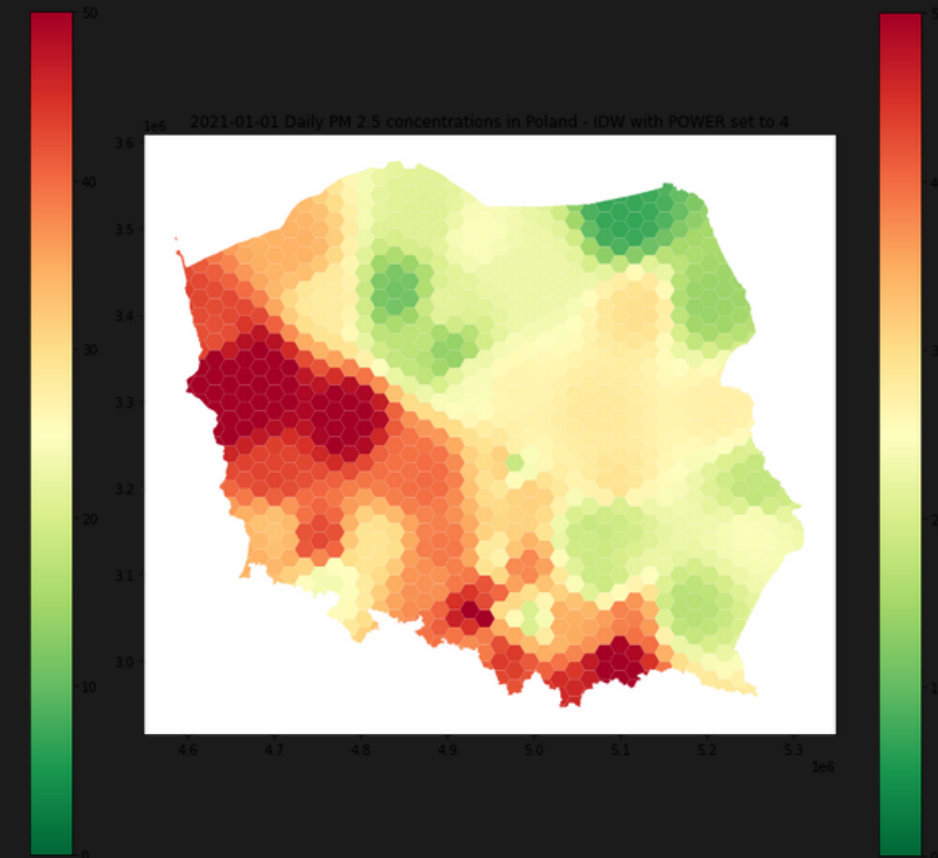
Kriging



IDW p=2



IDW p=4



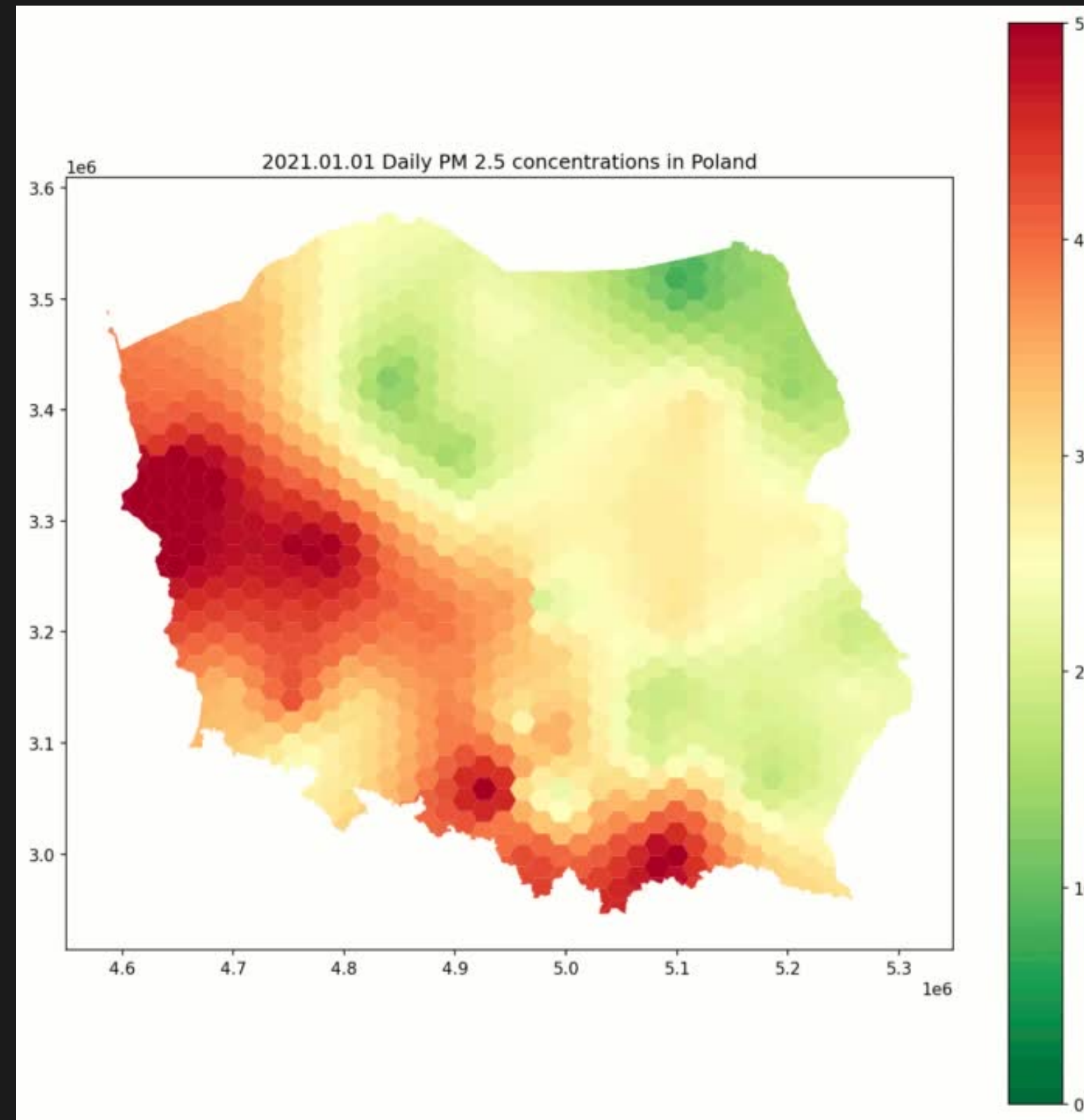
$$\widehat{z} = \sum_{i=1}^K \lambda_i z_i$$

$$\sum_{j=1}^K \lambda_j C(x_i, x_j) - \mu = \overline{C}(x_i, V); i = 1, 2, \dots, K$$

$$\sum_{j=1}^K \lambda_j = 1$$

Kriging -
zestawienie w
czasie

Kriging



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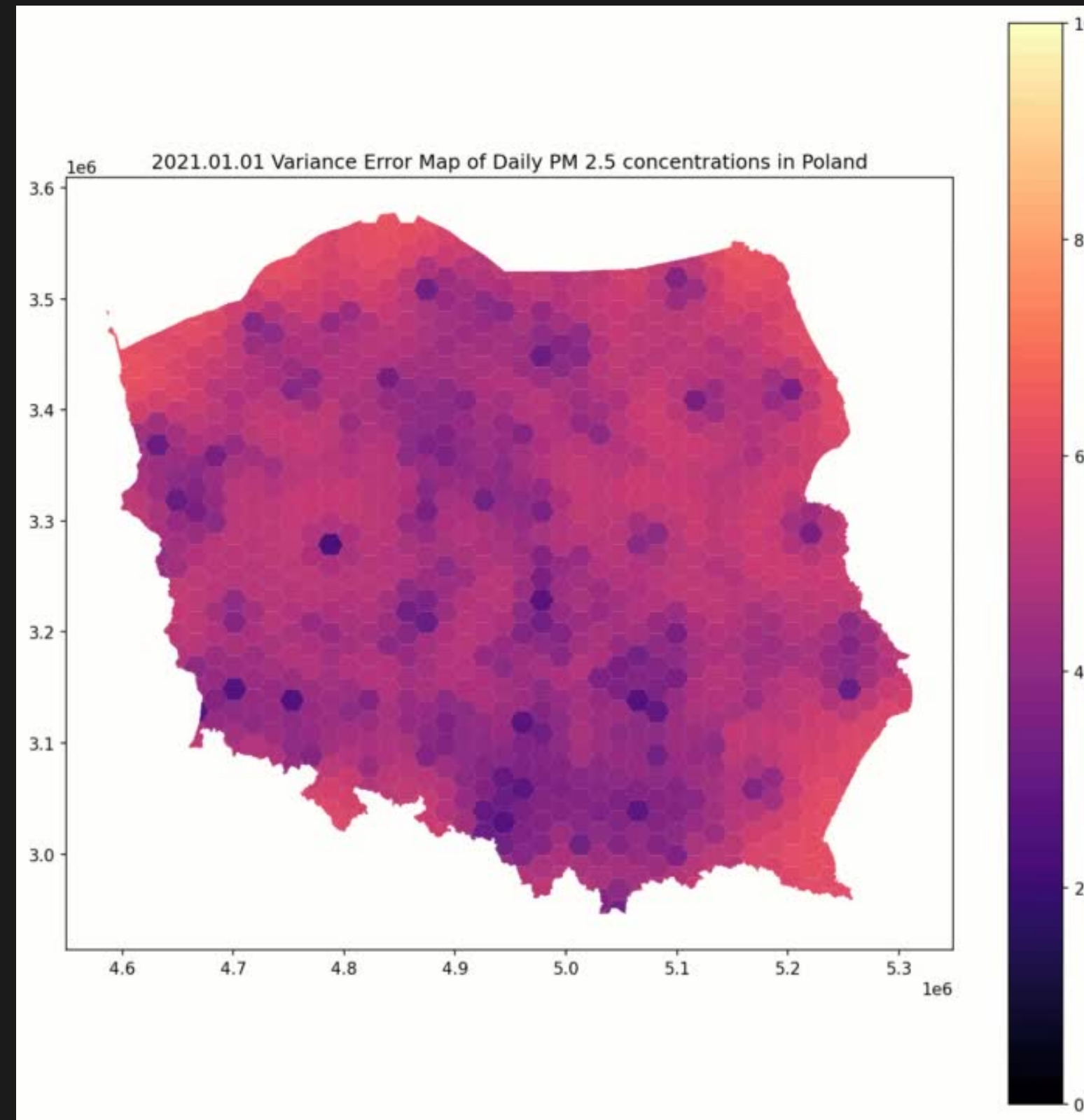
$$\widehat{z} = \sum_{i=1}^K \lambda_i z_i$$

$$\sum_{j=1}^K \lambda_j C(x_i, x_j) - \mu = \overline{C}(x_i, V); i = 1, 2, \dots, K$$

$$\sum_{j=1}^K \lambda_j = 1$$

Kriging –
propagacja błędu
w czasie

Kriging



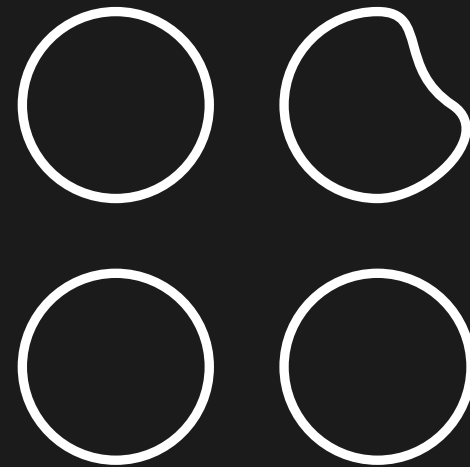
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$$\sum_{j=1}^K \lambda_j C(x_i, x_j) - \mu = \overline{C}(x_i, V); i=1, 2, \dots, K$$

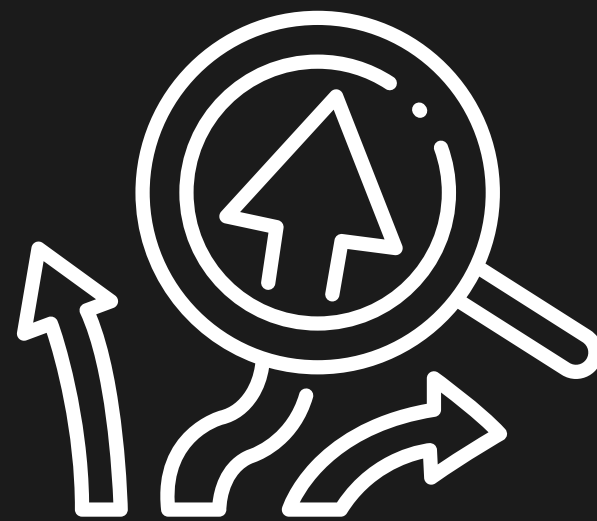
$$\sum_{j=1}^K \lambda_j = 1$$

Problemy i
ograniczenia

Kriging



Czy proces jest
stacjonarny?



Czy proces jest
izotropowy?

Kriging

$$\hat{z} = \sum_{i=1}^K \lambda_i z_i$$

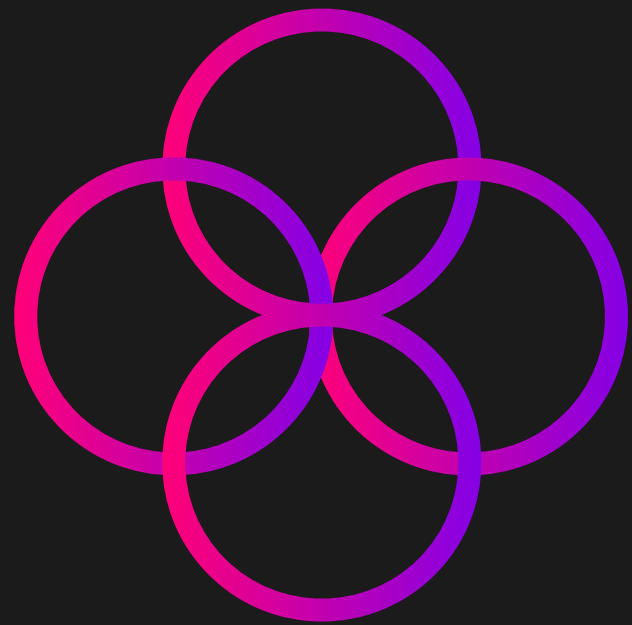
$$\sum_{j=1}^K \lambda_j C(x_i, x_j) - \mu = \overline{C}(x_i, V); i=1, 2, \dots, K$$

$$\sum_{j=1}^K \lambda_j = 1$$

Problemy i
ograniczenia

RELAKSACJA
DZIĘKI RÓŻNYM
RODZAJOM
KRIGINGU

SZYMON MOLINSKI



Linki

MATERIALS

<https://github.com/szymon-datalions/conferences-and-workshops/tree/main/2021/06/SummerDataSocietyConf>

PYTHON - KRIGING

<https://github.com/szymon-datalions/pyinterpolate>

PYPI

<https://pypi.org/project/pyinterpolate/>

AUTOR EMAIL

simon@ml-gis-service.com