

6. Para un sistema de ecuaciones $Ax = b$ siendo A una matriz triangular superior tenemos:

$$\begin{pmatrix} A_{11}x_1 + A_{12}x_2 + A_{13}x_3 + \dots + A_{1n}x_n \\ 0 + A_{22}x_2 + A_{23}x_3 + \dots + A_{2n}x_n \\ \vdots + 0 + A_{33}x_3 + \dots + A_{3n}x_n \\ \vdots \\ 0 + 0 + \dots + A_{n-1,n}x_n \\ 0 + 0 + 0 + \dots + A_{nn}x_n \end{pmatrix} = \begin{pmatrix} b_1 \\ b_2 \\ \vdots \\ b_{n-1} \\ b_n \end{pmatrix}$$

$$x_n = \frac{b_n}{A_{nn}}$$

$$x_{n-1} = \frac{b_{n-1} - A_{n-1,n}x_n}{A_{n-1,n-1}}$$

$$x_{n-2} = \frac{b_{n-2} - A_{n-2,n-1}x_{n-1} - A_{n-2,n}x_n}{A_{n-2,n-2}}$$

$$\Rightarrow x_i = \frac{b_i - \sum_{k=i+1}^n A_{ik}x_k}{A_{ii}}$$