

Computational Linguistics

Parsing

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Introduction

What is parsing?

- Parsing is the process of automatically assigning a structured interpretation to an input string.
- For natural language, this normally means obtaining one – or more likely a few thousands – syntactic or semantic representations ('parses') of a sentence.

Syntactic vs semantic parsing

- **Syntactic parsing** is concerned with the syntactic structure of sentences, i.e. how words combine into acceptable constituents:
 - *[The cat] chases the mouse.*
 - *Sylvester chases the mouse.*
 - **The chases the mouse.*
- **Semantic parsing** is concerned with the meaning of sentences, i.e. 'who did what' in a sentence:
 - *The cat chases the mouse*: the cat is doing the chasing and the mouse is being chased.
 - *It is raining*: nothing is doing the raining.

A syntactic parser: RASP (Briscoe et al, 2006)

```
(|T/txt-sc1/-+|
(|S/np_vp| |We:1_PPIS2|
(|V1/v_np| |describe:2_VV0|
(|NP/det_n1| |a:3_AT1|
(|N1/n1_pp1|
(|N1/ap_n1/-| (|AP/a1| (|A1/a| |robust:4_JJ|)))
(|N1/ap_n1/-| (|AP/a1| (|A1/a| |accurate:5_JJ|)))
(|N1/n_n1| |domain-independent:6_NN1|
(|N1/n| |approach:7_NN1|))))))
(|PP/p1|
(|P1/p_n1| |to:8_II|
(|N1/ap_n1/-| (|AP/a1| (|A1/a| |statistical:9_JJ|)))
(|N1/n_ppart| |parsing:10_NN1|
(|V1/v_ap| |incorporate+ed:11_VVN|
(|AP/a1|
(|A1/adv_a1|
(|AP/a1|
(|A1/a|
(|A/pp_adv-coord/+|
(|PP/p1|
(|P1/p_np| |into:12_II|
(|NP/det_n1| |the:13_AT1|
(|N1/ap_n1/-| (|AP/a1| (|A1/a| |new:14_JJ|)))
(|N1/n_pp-of| |release:15_NN1|
(|PP/p1|
(|P1/p_np| |of:16_IO|
(|NP/det_n1| |the:17_AT1|
(|N1/n-name_n1| |ANLT:18_NP1|
(|N1/n| |toolkit:19_NN1|))))))))))
|.:20_.|
(|A/cj-end_a/-| |and:21_CC| |publicly:22_RR|))))))
(|A1/a_pp-as| |available:23_JJ|
(|PP/p1|
(|P1/p_np| |as:24_CSA|
(|NP/det_n1| |a:25_AT1|
(|N1/n_n1| |research:26_NN1|
(|N1/n| |tool:27_NN1|))))))))))
(|End-punct3/-| |.:28_.|))
```

A semantic parser: Boxer (Bos, 2008)

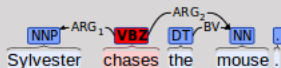
```
% bin/boxer --input working/test.ccg --box
%% This output was generated by the following command:
%% bin/boxer --input working/test.ccg --box

:- multifile      sem/3, id/2.
:- discontinuous sem/3, id/2.
:- dynamic        sem/3, id/2.
%% Every man runs .
id(1,1).
sem(1,[1001:[tok:'Every',pos:'DT',lemma:every,namex:'0'],1002:[tok:m
%%
%%
%% |-----|
%% | .....|
%% |
%% | x1      | x2      |
%% | .....| .....|
%% | man(x1) |> agent(x2,x1) |
%% | _____| run(x2) |
%% |
%%
Attempted: 1. Completed: 1 (100.00%).
```

<http://svn.ask.it.usyd.edu.au/trac/candc/wiki/BoxerSimple>

Analysis as tree

Sylvester chases the mouse.



0

S			
NP		VP	
N	V	NP	
N	V	DET	N
Sylvester	chases	the	N
			N
			mouse.

e3:

_1:proper_q(0:9)[BV x6]

x6:named(0:9)("Sylvester")[]

e3:_chase_v_1(10:16)[ARG1 x6, ARG2 x9]

_2:_the_q(17:20)[BV x9]

x9:_mouse_n_1(21:27)[]

What? 1000s of interpretations?

- Language is highly ambiguous, i.e. a sentence can generally be interpreted in several ways.
- Some examples of ambiguity that humans are aware of:
 - *Kim saw the woman in the park with a telescope.*
 - *Every student read a book.*
 - *Smoke!*
- Some examples of ambiguity that humans (normally) can't detect:
 - *We bake our cakes with love.*
 - *All students have picked a topic for their thesis.*

Lexical/structural ambiguity

- As far as parsing is concerned, we are interested in two types of ambiguity:
 - **Lexical Ambiguity:** a single word can have more than one syntactic category; for example, *smoke* can be a noun or a verb, *her* can be a pronoun or a possessive determiner.
 - **Structural Ambiguity:** there are a few valid tree forms for a single sequence of words:
Kim saw ((the woman in the park) (with a telescope)).
Kim saw ((the woman)(in the park with a telescope)).

Global/local ambiguity

- An important distinction must also be made between:
 - **Global (or total) ambiguity:** in which an entire sentence has several grammatically allowable analyses.
 - **Local (or partial) Ambiguity:** in which portions of a sentence, viewed in isolation, may present several possible options, even though the sentence taken as a whole has only one analysis that fits all its parts.

Global ambiguity

- Global ambiguity can be resolved only by resorting to information outside the sentence (the context, etc.) and so cannot be solved without access to discourse and/or world knowledge.
- A good parser should, however, ensure that all possible readings can be found, so that some further disambiguating process could make use of them.
- For instance:
We bake our cakes with love.

An example from the ERG

```

We bake our cakes with love.
SENT: We bake our cakes with love.
[ LTOP: h0
INDEX: e2 [ e SF: prop TENSE: pres MOOD: indicative PROG: - PERF: - ]
RELS: < [ pron_rel<0:2> LBL: h4 ARG0: x3 [ x PERS: 1 NUM: pl PRONTYPE: std_pron ] ]
[ pronoun_q_rel<0:2> LBL: h5 ARG0: x3 RSTR: h6 BODY: h7 ]
[ "_bake_v_cause_rel"<3:7> LBL: h1 ARG0: e2 ARG1: x3 ARG2: x8 [ x PERS: 3 NUM: pl ] ]
[ def_explicit_q_rel<8:11> LBL: h9 ARG0: x8 RSTR: h10 BODY: h11 ]
[ poss_rel<8:11> LBL: h12 ARG0: e13 [ e SF: prop TENSE: untensed MOOD: indicative PROG: - PERF: - ] ARG1: x8 ARG2: x14 [ x PERS: 1 NUM: pl PRO
NTYPE: std_pron ] ]
[ pronoun_q_rel<8:11> LBL: h15 ARG0: x14 RSTR: h16 BODY: h17 ]
[ pron_rel<8:11> LBL: h18 ARG0: x14 ]
[ "_cake_n_1_rel"<12:17> LBL: h12 ARG0: x8 ]
[ "_with_p_rel<18:22> LBL: h12 ARG0: e19 [ e SF: prop TENSE: untensed MOOD: indicative ] ARG1: x8 ARG2: x20 [ x PERS: 3 NUM: sg ] ]
[ udef_q_rel<23:28> LBL: h21 ARG0: x20 RSTR: h22 BODY: h23 ]
[ "_love_n_of-for_rel"<23:28> LBL: h24 ARG0: x20 ARG1: i25 ] >
HCONS: < h0 qeq h1 h6 qeq h4 h10 qeq h12 h16 qeq h18 h22 qeq h24 > ]
[ LTOP: h0
INDEX: e2 [ e SF: prop TENSE: pres MOOD: indicative PROG: - PERF: - ]
RELS: < [ pron_rel<0:2> LBL: h4 ARG0: x3 [ x PERS: 1 NUM: pl PRONTYPE: std_pron ] ]
[ pronoun_q_rel<0:2> LBL: h5 ARG0: x3 RSTR: h6 BODY: h7 ]
[ "_bake_v_cause_rel"<3:7> LBL: h1 ARG0: e2 ARG1: x3 ARG2: x8 [ x PERS: 3 NUM: pl ] ]
[ def_explicit_q_rel<8:11> LBL: h9 ARG0: x8 RSTR: h10 BODY: h11 ]
[ poss_rel<8:11> LBL: h12 ARG0: e13 [ e SF: prop TENSE: untensed MOOD: indicative PROG: - PERF: - ] ARG1: x8 ARG2: x14 [ x PERS: 1 NUM: pl PRO
NTYPE: std_pron ] ]
[ pronoun_q_rel<8:11> LBL: h15 ARG0: x14 RSTR: h16 BODY: h17 ]
[ pron_rel<8:11> LBL: h18 ARG0: x14 ]
[ "_cake_n_1_rel"<12:17> LBL: h12 ARG0: x8 ]
[ "_with_p_rel<18:22> LBL: h1 ARG0: e19 [ e SF: prop TENSE: untensed MOOD: indicative ] ARG1: e2 ARG2: x20 [ x PERS: 3 NUM: sg ] ]
[ udef_q_rel<23:28> LBL: h21 ARG0: x20 RSTR: h22 BODY: h23 ]
[ "_love_n_of-for_rel"<23:28> LBL: h24 ARG0: x20 ARG1: i25 ] >
HCONS: < h0 qeq h1 h6 qeq h4 h10 qeq h12 h16 qeq h18 h22 qeq h24 > ]
NOTE: 2 readings, added 1587 / 408 edges to chart (141 fully instantiated, 144 actives used, 115 passives used) RAM: 3172k

```

An example from the ERG

```
[ LTOP: h0
INDEX: e2 [ e SF: prop TENSE: pres MOOD: indicativ
RELS: < [ pron_rel<0:2> LBL: h4 ARG0: x3 [ x PERS
[ pronoun_q_rel<0:2> LBL: h5 ARG0: x3 RSTR: h6 B
[ "_bake_v_cause_rel"<3:7> LBL: h1 ARG0: e2 ARG1
[ def_explicit_q_rel<8:11> LBL: h9 ARG0: x8 RSTR
[ poss_rel<8:11> LBL: h12 ARG0: e13 [ e SF: prop
NTYPE: std_pron ] ]
[ pronoun_q_rel<8:11> LBL: h15 ARG0: x14 RSTR: h
[ pron_rel<8:11> LBL: h18 ARG0: x14 ]
[ "_cake_n_1_rel"<12:17> LBL: h12 ARG0: x8 ]
[ _with_p_rel<18:22> LBL: h1 ARG0: e19 [ e SF: p
[ udef_q_rel<23:28> LBL: h21 ARG0: x20 RSTR: h22
[ "_love_n_of-for_rel"<23:28> LBL: h24 ARG0: x20
HCONS: < h0 qeq h1 h6 qeq h4 h10 qeq h12 h16 qeq
NOTE: 2 readings, added 1587 / 408 edges to chart
```

But 1000s?

- Real sentences are often long and complex.

The major difference between a thing that might go wrong and a thing that cannot possibly go wrong is that when a thing that cannot possibly go wrong goes wrong it usually turns out to be impossible to get at and repair.

Douglas Adams

The ERG output

```
NOTE: hit RAM limit while unpacking  
NOTE: 3521 readings, added 88892 / 79464 edges to chart
```


The ideal parser

- The ideal parser is:
 - correct: it only returns valid analyses of a sentence, given the grammar provided;
 - complete: it returns all possible analyses for a sentence;
 - efficient: it is fast.

From rules to sentences

The rules of parsing

- Parsing needs rules (i.e. a grammar):
 - $S \rightarrow NP VP$
 - $NP \rightarrow Det N$
 - ...
- Given a sentence and a grammar, a parser returns all possible analyses of the sentence that use the rules in the grammar.

Context-free grammars (CFG)

- A context-free grammar has the form $G = (N, \Sigma, R, S)$ where:
 - N is a set of non-terminal symbols
 - Σ is a set of terminal symbols
 - R is a set of rules of the form $X \rightarrow Y_1 Y_2 \dots Y_n$ where
 - $n \geq 0$
 - $X \in N$
 - $Y_i \in (N \cup \Sigma)$
 - $S \in N$ is a root symbol.

An example CFG

- $N = \{N, V, Det, NP, VP, S\}$
- $\Sigma = \{the, cow, eats\}$
- $R = \{$
 - Det \rightarrow the
 - N \rightarrow cow
 - V \rightarrow eats
 - NP \rightarrow Det N
 - VP \rightarrow V
 - S \rightarrow NP VP $\}$

Shift-reduce bottom-up parsing

- bottom-up: start with the words in the sentence and build up a tree that terminates with the symbol S .
- shift-reduce: one possible (simple) algorithm for parsing. The algorithm processes the sentence one word at a time, left to right (leftmost derivation) or right to left (rightmost derivation). Two operations are possible:
 - shift: push a word on top of the stack;
 - reduce: replace a set of symbols at the top of the stack with the result of a production rule.

Shift-reduce: an example

- **Queue:** *The cow eats.*
- **Stack:**

Grammar:

Det \rightarrow the

N \rightarrow cow

V \rightarrow eats

NP \rightarrow Det N

VP \rightarrow V

S \rightarrow NP VP

Shift-reduce: an example

- **Queue:** *cow eats.*
- **Stack:** *The*

shift

Grammar:

$\text{Det} \rightarrow \text{the}$

$\text{N} \rightarrow \text{cow}$

$\text{V} \rightarrow \text{eats}$

$\text{NP} \rightarrow \text{Det N}$

$\text{VP} \rightarrow \text{V}$

$\text{S} \rightarrow \text{NP VP}$

Shift-reduce: an example

- **Queue:** *cow eats.*
- **Stack:** *Det*

reduce

Grammar:

$\text{Det} \rightarrow \text{the}$

$\text{N} \rightarrow \text{cow}$

$\text{V} \rightarrow \text{eats}$

$\text{NP} \rightarrow \text{Det N}$

$\text{VP} \rightarrow \text{V}$

$\text{S} \rightarrow \text{NP VP}$

Shift-reduce: an example

- **Queue:** *eats.*
- **Stack:** *Det cow*

shift

Grammar:

Det \rightarrow the

N \rightarrow cow

V \rightarrow eats

NP \rightarrow Det N

VP \rightarrow V

S \rightarrow NP VP

Shift-reduce: an example

- **Queue:** *eats.*
- **Stack:** *Det N*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

V \rightarrow eats

NP \rightarrow Det N

VP \rightarrow V

S \rightarrow NP VP

Shift-reduce: an example

- **Queue:** *eats.*
- **Stack:** *NP*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

V \rightarrow eats

NP \rightarrow Det N

VP \rightarrow V

S \rightarrow NP VP

Shift-reduce: an example

- **Queue:**
- **Stack:** *NP eats*

shift

Grammar:

Det \rightarrow the

N \rightarrow cow

V \rightarrow eats

NP \rightarrow Det N

VP \rightarrow V

S \rightarrow NP VP

Shift-reduce: an example

- Queue:
- Stack: *NP V*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

V \rightarrow eats

NP \rightarrow Det N

VP \rightarrow V

S \rightarrow NP VP

Shift-reduce: an example

- Queue:
- Stack: *NP VP*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

V \rightarrow eats

NP \rightarrow Det N

VP \rightarrow V

S \rightarrow NP VP

Shift-reduce: an example

- Queue:
- Stack: *S*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

V \rightarrow eats

NP \rightarrow Det N

VP \rightarrow V

S \rightarrow NP VP

When to reduce?

- **Queue:** *The cow eats grass on the field.*
- **Stack:**

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *cow eats grass on the field.*
- **Stack:** *The* **shift**

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *cow eats grass on the field.*
- **Stack:** *Det* **reduce**

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *eats grass on the field.*
- **Stack:** *Det cow* **shift**

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *eats grass on the field.*
- **Stack:** *Det N* **reduce**

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *eats grass on the field.*
- **Stack:** *NP* **reduce**

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *grass on the field.*
- **Stack:** *NP eats* **shift**

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *grass on the field.*
- **Stack:** *NP V* **reduce**

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *on the field.*
- **Stack:** *NP V grass*

shift

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *on the field.*
- **Stack:** *NP V N*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *on the field.*
- **Stack:** *NP V NP*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *on the field.*
- **Stack:** *NP VP*

!!reduce!!

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *the field.*
- **Stack:** *NP VP on*

shift

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *the field.*
- **Stack:** *NP VP P*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *field.*
- **Stack:** *NP VP P the*

shift

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *field.*
- **Stack:** *NP VP P Det*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:**
- **Stack:** *NP VP P Det field*

shift

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:**
- **Stack:** *NP VP P Det N*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:**
- **Stack:** *NP VP P NP*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:**
- **Stack:** *NP VP PP*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- Queue:
- Stack: *NP VP*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- Queue:

- Stack: S **reduce**

Resulting parse:

$((the(cow))((eats(grass))((on(the(field))))))$

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *on the field.*
- **Stack:** *NP V NP*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

NP \rightarrow NP PP

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *on the field.*
- **Stack:** *NP V NP on*

shift

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

NP \rightarrow NP PP

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *the field.*
- **Stack:** *NP V NP P*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

NP \rightarrow NP PP

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *field.*
- **Stack:** *NP V NP P the*

shift

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

NP \rightarrow NP PP

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:** *field*.
- **Stack:** *NP V NP P Det*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

NP \rightarrow NP PP

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:**

- **Stack:** *NP V NP P Det field*

shift

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

NP \rightarrow NP PP

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:**
- **Stack:** *NP V NP P Det N*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

NP \rightarrow NP PP

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:**
- **Stack:** *NP V NP P NP*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

NP \rightarrow NP PP

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:**

- **Stack:** *NP V NP PP*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

NP \rightarrow NP PP

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:**
- **Stack:** $NP\ V\ NP$

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

NP \rightarrow NP PP

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- **Queue:**
- **Stack:** *NP VP*

reduce

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

NP \rightarrow NP PP

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

When to reduce?

- Queue:

- Stack: S **reduce**

Resulting parse:

$((the(cow))((eats((grass)(on(the(field)))))))$

Grammar:

Det \rightarrow the

N \rightarrow cow

N \rightarrow grass

N \rightarrow field

n \rightarrow NP

V \rightarrow eats

P \rightarrow on

NP \rightarrow Det N

NP \rightarrow NP PP

PP \rightarrow P NP

N \rightarrow N PP

VP \rightarrow V NP

VP \rightarrow VP PP

S \rightarrow NP VP

Reducing in ambiguous sentences

- When we reduce affects which reading we select in structurally ambiguous sentences:
 - She saw the woman with the telescope.
 - (She (saw (the woman) with (the telescope)))
reduce to *np* after *woman*
 - (She (saw (the (woman with (the telescope)))))
reduce to *np* after *telescope*

Recursive descent top-down parsing

- top-down: start with the symbol S and build up a tree that branches out into the words in the sentence.
- In other words, we first assume that the sentence is well-formed and try to prove it using the rules at our disposal.
- We use the rules left-to-right (as opposed to right-to-left in bottom-up parsing):

$np \rightarrow np\ pp$

top-down: let's expand np into $np\ pp$ and see whether we get to the sentence...

$np \rightarrow np\ pp$

bottom-up: we have an np and a pp , let's reduce them to an np and see whether we get an s ...

Recursive descent: an example

- **Analysis:** s
- **Try:** $s \rightarrow np\ vp$

Grammar:

$Det \rightarrow the$

$N \rightarrow cow$

$V \rightarrow eats$

$NP \rightarrow Det\ N$

$VP \rightarrow V$

$S \rightarrow NP\ VP$

Recursive descent: an example

- **Analysis:** $s(np\ vp)$
- **Try:** $np \rightarrow \text{det } n$

Grammar:

$\text{Det} \rightarrow \text{the}$

$\text{N} \rightarrow \text{cow}$

$\text{V} \rightarrow \text{eats}$

$\text{NP} \rightarrow \text{Det } \text{N}$

$\text{VP} \rightarrow \text{V}$

$\text{S} \rightarrow \text{NP } \text{VP}$

Recursive descent: an example

- **Analysis:** $s(np(det\ n)\ vp)$
- **Try:** $det \rightarrow the$

Grammar:

$Det \rightarrow the$

$N \rightarrow cow$

$V \rightarrow eats$

$NP \rightarrow Det\ N$

$VP \rightarrow V$

$S \rightarrow NP\ VP$

Recursive descent: an example

- **Analysis:** $s(np(det(the) n) vp)$
- **Try:** $n \rightarrow \text{cow}$

Grammar:

$\text{Det} \rightarrow \text{the}$

$\text{N} \rightarrow \text{cow}$

$\text{V} \rightarrow \text{eats}$

$\text{NP} \rightarrow \text{Det N}$

$\text{VP} \rightarrow \text{V}$

$\text{S} \rightarrow \text{NP VP}$

Recursive descent: an example

- **Analysis:** $s(np(det(the) n(cow)) vp)$
- **Try:** $vp \rightarrow eats$

Grammar:

$Det \rightarrow the$

$N \rightarrow cow$

$V \rightarrow eats$

$NP \rightarrow Det N$

$VP \rightarrow V$

$S \rightarrow NP VP$

Recursive descent: an example

- **Analysis:** $s(np(det(the) n(cow)) vp(eats))$
- **STOP**

Grammar:

$Det \rightarrow the$

$N \rightarrow cow$

$V \rightarrow eats$

$NP \rightarrow Det N$

$VP \rightarrow V$

$S \rightarrow NP VP$

Dealing with alternatives

- We can *backtrack*: at each step, the algorithm takes notes of the different alternatives available and tries them in turn. Upon failure, it picks the next alternative. Depth-first algorithm.
- We can try and analyse all alternatives in *parallel*. At each step, all possible alternatives are written. Upon failure, disregard the alternative. Breadth-first algorithm.

Bottom-up vs top-down

- Bottom-up:
 - Always generate trees that are consistent with the words in the sentence.
 - Trees that will never lead to the root symbol are explored.
- Top-down:
 - Wastes time exploring alternatives that are inconsistent with the input.
 - Never wastes time exploring a tree that cannot result in a root symbol.

Better parsing

- A *complete* parse of a sentence will output all possible correct alternatives (those that result in the S symbol and an empty queue).
- But outputting every option can be time-consuming and inefficient...
- Plus, we would like to know which parse is more likely.
- The answer: 1) keep track of all options in one chart; 2) use probabilities.

The CKY algorithm

Why CKY?

- The Cocke-Kasami-Younger (CKY) algorithm: A fast parser designed to overcome the inefficiencies of naive parsing.
- The algorithm relies on:
 - Storing intermediate solutions and only pursuing the ‘promising’ ones (those that will contribute to a full parse).
 - The CKY works with a particular grammar: the Chomsky Normal Form (CNF).

CNF grammars

- A context-free grammar is said to be in Chomsky normal form if all of its production rules are of the following form:
 - $A \rightarrow BC$, or
 - $A \rightarrow a$, or
 - $S \rightarrow \epsilon$
- where A, B and C are non-terminal symbols, a is a terminal symbol (a constant), S is the start symbol, and ϵ is the empty string.
- Note: production rules are restricted to produce 2 non-terminals or 1 terminal. Empty productions are not allowed.

The Well-Formed Substring Table (WFST)

- A well-formed substring table is a data structure that contains partial constituency structures.

	1	2	3
1	DT	JJ	NN
2		NN	
3	NP		
	the	angry	dragon

NP → DT NN

NN → JJ NN

DT → the

JJ → angry

NN → dragon

The CKY algorithm

- 1 Given an input sentence with n tokens, create a matrix M with dimensionality $n * n$. Each cell in the matrix corresponds to a sentence span starting at a particular position. E.g. $M[2][2]$ corresponds to a span of 2 starting at word 2 in the sentence.
- 2 Fill in row 1 of the matrix bottom-up, using rules going to terminals.
- 3 Fill in each subsequent row top-down, using the already filled rows as constraints.

Example

S → *NP VP*
VP → *VP PP*
VP → *V NP*
VP → *eats*
PP → *P NP*
NP → *Det N*
NP → *she*
V → *eats*
P → *with*
NP → *cake*
N → *fork*
Det → *a*

She eats cake with a fork.

Example, step 1

S → *NP VP*
VP → *VP PP*
VP → *V NP*
VP → *eats*
PP → *P NP*
NP → *Det N*
NP → *she*
V → *eats*
P → *with*
NP → *cake*
N → *fork*
Det → *a*

	1	2	3	4	5	6
1						
2						
3						
4						
5						
6						

$_0$ she $_1$ eats $_2$ cake $_3$ with $_4$ a $_5$ fork $_6$

$n=6$. (For clarity, matrix indices start at 1.)

Example, step 2

$S \rightarrow NP VP$
 $VP \rightarrow VP PP$
 $VP \rightarrow V NP$
 $VP \rightarrow eats$
 $PP \rightarrow P NP$
 $NP \rightarrow Det N$
 $NP \rightarrow she$
 $V \rightarrow eats$
 $P \rightarrow with$
 $NP \rightarrow cake$
 $N \rightarrow fork$
 $Det \rightarrow a$

	1	2	3	4	5	6
1	NP	V,VP	NP	P	Det	N
2						
3						
4						
5						
6						
	she	eats	cake	with	a	fork

For i so that $1 \leq i \leq 6$,
 $M[1][i] = \{A | A \rightarrow a_i \text{ in } P\}$.

Example, step 2

S → *NP VP*
VP → *VP PP*
VP → *V NP*
VP → *eats*
PP → *P NP*
NP → *Det N*
NP → *she*
V → *eats*
P → *with*
NP → *cake*
N → *fork*
Det → *a*

	1	2	3	4	5	6
1 ($l = 1$)	NP	V,VP	NP	P	Det	N
2 ($l = 2$)						
3 ($l = 3$)						
4 ($l = 4$)						
5 ($l = 5$)						
6 ($l = 6$)						
	she	eats	cake	with	a	fork

Note: each row corresponds to a particular span length.

Example, step 3

$S \rightarrow NP VP$
 $VP \rightarrow VP PP$
 $VP \rightarrow V NP$
 $VP \rightarrow eats$
 $PP \rightarrow P NP$
 $NP \rightarrow Det N$
 $NP \rightarrow she$
 $V \rightarrow eats$
 $P \rightarrow with$
 $NP \rightarrow cake$
 $N \rightarrow fork$
 $Det \rightarrow a$

	1	2	3	4	5	6
1	NP	V,VP	NP	P	Det	N
2	S	VP			NP	
3						
4						
5						
6						
	she	eats	cake	with	a	fork

Consider spans of length 2:

Each span S can be partitioned into spans S_1 of length 1 and S_2 of length $2 - 1 = 1$

For i so that $1 \leq i \leq 6$,

$M[2][i] \{A | A \rightarrow BC \text{ in } P,$
 with B in $t_{1,i}$ and C in $t_{1,i}\}$

Example, step 3

$S \rightarrow NP VP$
 $VP \rightarrow VP PP$
 $VP \rightarrow V NP$
 $VP \rightarrow eats$
 $PP \rightarrow P NP$
 $NP \rightarrow Det N$
 $NP \rightarrow she$
 $V \rightarrow eats$
 $P \rightarrow with$
 $NP \rightarrow cake$
 $N \rightarrow fork$
 $Det \rightarrow a$

	1	2	3	4	5	6
1	NP	V,VP	NP	P	Det	N
2	S	VP			NP	
3						
4						
5						
6						
	she	eats	cake	with	a	fork

Consider spans of length 2:

Each span S can be partitioned into spans S_1 of length 1 and S_2 of length $2 - 1 = 1$

For i so that $1 \leq i \leq 6$,

$M[2][i] \{A | A \rightarrow BC \text{ in } P,$
 with B in $t_{1,i}$ and C in $t_{1,i}\}$

Example, step 3

$S \rightarrow NP VP$
 $VP \rightarrow VP PP$
 $VP \rightarrow V NP$
 $VP \rightarrow eats$
 $PP \rightarrow P NP$
 $NP \rightarrow Det N$
 $NP \rightarrow she$
 $V \rightarrow eats$
 $P \rightarrow with$
 $NP \rightarrow cake$
 $N \rightarrow fork$
 $Det \rightarrow a$

	1	2	3	4	5	6
1	NP	V,VP	NP	P	Det	N
2	S	VP			NP	
3						
4						
5						
6						
	she	eats	cake	with	a	fork

Consider spans of length 2:

Each span S can be partitioned into spans S_1 of length 1 and S_2 of length $2 - 1 = 1$

For i so that $1 \leq i \leq 6$,

$M[2][i] \{A | A \rightarrow BC \text{ in } P,$
 with B in $t_{1,i}$ and C in $t_{1,i}\}$

Example, step 3

S → *NP VP*
VP → *VP PP*
VP → *V NP*
VP → *eats*
PP → *P NP*
NP → *Det N*
NP → *she*
V → *eats*
P → *with*
NP → *cake*
N → *fork*
Det → *a*

	1	2	3	4	5	6
1	NP	V,VP	NP	P	Det	N
2	S	VP			NP	
3	S			PP		
4						
5						
6						
	she	eats	cake	with	a	fork

Consider spans of length 3:

Possible partitions: 1,2; 2,1.

For i so that $1 \leq i \leq 6$,

$M[3][i] \{ A | A \rightarrow BC \text{ in } P,$
 with B in $t_{k,i}$ and C in $t_{3-k,i+k}$
 for $1 \leq k < 3 \}$

Example, step 3

$S \rightarrow NP VP$
 $VP \rightarrow VP PP$
 $VP \rightarrow V NP$
 $VP \rightarrow eats$
 $PP \rightarrow P NP$
 $NP \rightarrow Det N$
 $NP \rightarrow she$
 $V \rightarrow eats$
 $P \rightarrow with$
 $NP \rightarrow cake$
 $N \rightarrow fork$
 $Det \rightarrow a$

	1	2	3	4	5	6
1	NP	V,VP	NP	P	Det	N
2	S	VP			NP	
3	S			PP		
4						
5						
6						
	she	eats	cake	with	a	fork

Consider spans of length 3:

Possible partitions: 1,2; 2,1.

For i so that $1 \leq i \leq 6$,

$M[3][i] \{ A | A \rightarrow BC \text{ in } P,$
 with B in $t_{k,i}$ and C in $t_{3-k,i+k}$
 for $1 \leq k < 3 \}$

Example, step 3

S → *NP VP*
VP → *VP PP*
VP → *V NP*
VP → *eats*
PP → *P NP*
NP → *Det N*
NP → *she*
V → *eats*
P → *with*
NP → *cake*
N → *fork*
Det → *a*

	1	2	3	4	5	6
1	NP	V,VP	NP	P	Det	N
2	S	VP			NP	
3	S			PP		
4						
5						
6						
	she	eats	cake	with	a	fork

Consider spans of length 4:

Possible partitions: 1,3; 3,1; 2,2.

For i so that $1 \leq i \leq 6$,

$M[4][i] \{ A | A \rightarrow BC \text{ in } P,$
 with B in $t_{k,i}$ and C in $t_{4-k,i+k}$
 for $1 \leq k < 4 \}$

Example, step 3

S → *NP VP*
VP → *VP PP*
VP → *V NP*
VP → *eats*
PP → *P NP*
NP → *Det N*
NP → *she*
V → *eats*
P → *with*
NP → *cake*
N → *fork*
Det → *a*

	1	2	3	4	5	6
1	NP	V,VP	NP	P	Det	N
2	S	VP			NP	
3	S			PP		
4						
5		VP				
6						
	she	eats	cake	with	a	fork

Consider spans of length 5:

Possible partitions: 1,4; 4,1; 3,2; 2,3.

For i so that $1 \leq i \leq 6$,

$M[5][i] \{A | A \rightarrow BC \text{ in } P,$

with B in $t_{k,i}$ and C in $t_{5-k,i+k}$

for $1 \leq k < 5\}$

Example, step 3

S → *NP VP*
VP → *VP PP*
VP → *V NP*
VP → *eats*
PP → *P NP*
NP → *Det N*
NP → *she*
V → *eats*
P → *with*
NP → *cake*
N → *fork*
Det → *a*

	1	2	3	4	5	6
1	NP	V,VP	NP	P	Det	N
2	S	VP			NP	
3	S			PP		
4						
5		VP				
6	S					
	she	eats	cake	with	a	fork

Consider spans of length 6:

Possible partitions: 1,5; 5,1; 2,4; 4,2; 3,3.

For i so that $1 \leq i \leq 6$,

$M[6][i] \{ A | A \rightarrow BC \text{ in } P,$
 with B in $t_{k,i}$ and C in $t_{6-k,i+k}$
 for $1 \leq k < 6 \}$

Example, step 3

S → *NP VP*
VP → *VP PP*
VP → *V NP*
VP → *eats*
PP → *P NP*
NP → *Det N*
NP → *she*
V → *eats*
P → *with*
NP → *cake*
N → *fork*
Det → *a*

	1	2	3	4	5	6
1	NP	V,VP	NP	P	Det	N
2	S	VP			NP	
3	S			PP		
4		VP				
5		VP				
6	S					
	she	eats	cake	with	a	fork

Note: the sentence has a parse if a root symbol (**S**) is found in row *n*.

The algorithm

(20) **Algorithme de Cocke-Younger-Kasami :**

1. Poser $t_{i,1} = \{A \mid A \longrightarrow a_i \text{ est dans } P\}$ pour chaque $i, 1 \leq i \leq n$.
2. Poser $t_{i,j} = \{A \mid \text{pour } k, 1 \leq k < j, A \longrightarrow BC \text{ dans } P, \\ B \text{ est dans } t_{i,k}, \text{ et } C \text{ est dans } t_{i+k,j-k}\}$.
3. Répéter (2) jusqu'à ce que la table soit pleine.

Eric Wehrli. 2005. *L'analyse syntaxique des langues naturelles : problèmes et méthodes*

CKY: a mixed algorithm

- CKY uses a mixture of the bottom-up and top-down algorithms.
- For each row in the matrix, the cells are filled in respecting the constraints of lower-numbered rows (or the terminals, in the case of row 1).
- For each cell, we propose a rule from the grammar (top-down) and validate it against what we know already.
- All alternatives in one chart.

Alternatives in the CKY chart

S → *NP VP*
VP → *VP PP*
VP → *V NP*
VP → *eats*
PP → *P NP*
NP → *Det N*
NP → *she*
V → *eats*
P → *with*
NP → *cake*
N → *fork*
Det → *a*
NP → *NP PP*

	1	2	3	4	5	6
1	NP	,VP	NP	P	Det	N
2	S	VP			NP	
3	S			PP		
4			NP			
5		VP				
6	S					
	she	eats	cake	with	a	fork

(she(eats (cake))(with(a (fork))))

Alternatives in the CKY chart

S → *NP VP*
VP → *VP PP*
VP → *V NP*
VP → *eats*
PP → *P NP*
NP → *Det N*
NP → *she*
V → *eats*
P → *with*
NP → *cake*
N → *fork*
Det → *a*
NP → *NP PP*

	1	2	3	4	5	6
1	NP	V, VP	NP	P	Det	N
2	S	VP			NP	
3	S			PP		
4			NP			
5		VP				
6	S					
	she	eats	cake	with	a	fork

(she (eats)(cake(with(a(fork)))))

Recognition vs parsing

- **Recognition:** is this a sentence or not?
Fill in the chart and check we have an **S** in row n .
- **Parsing:** what is the analysis of the sentence we found?
Keep track of the links used in the algorithm, and return them at the end.

Probabilistic Context-Free Grammars (PCFGs)

Where do grammars come from?

- Manually written: time-consuming, potentially low-coverage, but high precision.
- Learnt from a *treebank*: some text was annotated by humans and the parser is trained on this annotation.
- Automatically induced: unsupervised parsing from raw (or POS-tagged) text. Cheap, and potentially close to what humans do. But so far, precision has remained low.

Treebanking

- The main treebank used by the parsing community is the Penn Treebank (PTB), created in the early 90s.
- Around 1M words of news text, annotated with phrase-structure trees.
- The PTB took 3 years to create, with a few annotators. See Clark (2010) for more historical details.

Problems with the PTB

- Focus on news text. Specific syntax, vocabulary, speakers, etc.
- Relatively small test set (2400 sentences), which has been used over and over again. Possibility of *overfitting* the models.

Putting probabilities on rules

- With the availability of a treebank, we can put probabilities on grammar rules:
 - $s \rightarrow np\ vp\ 0.9$
 - $s \rightarrow vp\ 0.1$
 - ...
- Such probabilities will help us decide which parses are more likely – or in case we want to prioritise efficiency – which alternatives to discard at each decision point.

Probability of a tree

- Given the probabilities assigned to rules $r_1 \dots r_n$, a probability can be assigned to a particular tree:

$$P(T) = \prod_{n \in T} P(r_n) \quad (1)$$

- The best parse is then given by:

$$T(S) = \operatorname{argmax}_{T \in \tau(S)} P(T) \quad (2)$$

Example

<i>S</i>	→	<i>NP VP</i>	1.0
<i>VP</i>	→	<i>VP PP</i>	0.7
<i>VP</i>	→	<i>V NP</i>	0.5
<i>VP</i>	→	<i>eats</i>	0.1
<i>PP</i>	→	<i>P NP</i>	0.8
<i>NP</i>	→	<i>Det N</i>	0.7
<i>NP</i>	→	<i>NP PP</i>	0.2
<i>NP</i>	→	<i>she</i>	0.1
<i>NP</i>	→	<i>cake</i>	0.1
<i>V</i>	→	<i>eats</i>	0.1
<i>P</i>	→	<i>with</i>	0.2
<i>N</i>	→	<i>fork</i>	0.1
<i>Det</i>	→	<i>a</i>	0.2

	1	2	3	4	5	6
1	NP	V,VP	NP	P	Det	N
2	S	VP			NP	
3	S			PP		
4						
5		VP				
6	S					
	she	eats	cake	with	a	fork

(she(eats (cake))(with(a (fork))))

$$P(T) = 0.1 * 0.1 * 0.1 * 0.2 * 0.2 * 0.1 * 0.5 * 0.7 * 0.8 * 0.7 * 1.0 = 7.84 \cdot 10^{-7}$$

Example

<i>S</i>	→	<i>NP VP</i>	1.0
<i>VP</i>	→	<i>VP PP</i>	0.7
<i>VP</i>	→	<i>V NP</i>	0.5
<i>VP</i>	→	<i>eats</i>	0.1
<i>PP</i>	→	<i>P NP</i>	0.8
<i>NP</i>	→	<i>Det N</i>	0.7
<i>NP</i>	→	<i>NP PP</i>	0.2
<i>NP</i>	→	<i>she</i>	0.1
<i>NP</i>	→	<i>cake</i>	0.1
<i>V</i>	→	<i>eats</i>	0.1
<i>P</i>	→	<i>with</i>	0.2
<i>N</i>	→	<i>fork</i>	0.1
<i>Det</i>	→	<i>a</i>	0.2

	1	2	3	4	5	6
1	NP	V,VP	NP	P	Det	N
2	S				NP	
3	S			PP		
4			NP			
5		VP				
6	S					
	she	eats	cake	with	a	fork

(she (eats)(cake(with(a(fork))))))

$$P(T) = 0.1 * 0.1 * 0.1 * 0.2 * 0.2 * 0.1 * 0.7 * 0.8 * 0.2 * 0.5 * 1.0 = 2.24 \cdot 10^{-7}$$

Parser evaluation

Evaluation measures

- The parser is evaluated against a ‘gold standard’, i.e. a manually (or mostly manually) annotated treebank.
- C = number of correct constituents in the system’s parse.
- N = number of constituents in the system’s parse.
- N_G = number of constituents in the correct, gold standard parse.
- Precision: $P = C/N$
- Recall: $P = C/N_G$

Precision and recall

- Precision and recall often work against each other: precise systems don't have large coverage; large-coverage systems let in more errors.
- To calculate a score taking both precision and recall into account, use F-score:

$$(1 + \beta^2) \cdot \frac{\text{precision} \cdot \text{recall}}{(\beta^2 \cdot \text{precision}) + \text{recall}} \quad (3)$$

- For $\beta = 1$, the F-score gives equal weight to precision and recall. For $\beta > 1$, more weight is given to precision. For $\beta < 1$, more weight is given to recall.

How well do they work?

- On the PTB, parsers achieve scores well into the 90% precision.
- But danger that systems have overfitted on the PTB.
- Things are much harder on:
 - spoken language;
 - tweets;
 - generally: other domains, styles.

...

That's it!