A Predictive and Causal Analysis of Fourth Down Attempts in the NFL

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1   Introduction

1.1   Context

The National Football League is a multi-billion dollar industry that has seen rapid growth within the American and International entertainment. This growth has placed more and more importance on the performance of NFL teams as they fight to win games to increase the popularity of their team as Davis and End (2010) argue that successful NFL franchises have measurable economic impacts on their local areas. This revelation has given rise to a age of data analytics in the NFL as teams seek to gain competitive advantages over their rivals. GMs and coaches then explore different avenues of strategies.

In the NFL, a team's offensive possession is structured around a series of four "downs" where they attempt to advance the ball at least 10 yards to earn a new set of downs and maintain possession. When a team reaches fourth down without achieving the needed yardage, they face a pivotal decision. Teams typically choose between three options: punt the ball to establish favorable field position for their defense, attempt a field goal if within reasonable range (worth 3 points), or "go for it" by running an offensive play to try and gain the required yardage. For many years in the NFL there seemed to be a consistent standard that when faced with a fourth down your team will kick a field goal or punt the ball for better field position. The only exception being the dying moments in a game when teams are desperate for a miracle.

In American Football many teams have shifted to being more aggresive on fourth down. Most famously are the Detroit Lions. Since the arrival of their current head coach Dan Campbell, the lions adopted a aggressive strategy to match their aggressive "biting off knee caps" mentality (Birkett, 2023). While the lions have seen success for the first time in years, they have also been criticized for their aggressive play calling. This was highlighted in the 2023-24 playoff divisional round game in which the Lions failed a fourth down attempt that was painted as unnecessary (Sporting News, 2024). After this mid-game failure there seemed to be a shift in momentum and the lions lost the game.

1.2   Research Problem and Key Findings

A result like this causes one ask the question "Did the Lions make the right call?". This question seems to be getting answered as "yes" by the current literature. However, we need to know if different teams should "go-for-it" or not "go-for-it" depending on their situation and team make up. For example, it could be argued that the lions should have attempted the crucial fourth down in the 2023-24 playoff divisional round game. However, if the Panthers (which were a significantly worse team) were is that situation it could be argued that they should not have been as aggressive. This is because the panthers could have had a worse chance of being able to convert on fourth down.

On top of this, we must be weary of any recommendation that is given to a head coach. The truth is that we are not on the field, in the locker rooms, or in team meeting. This means coaches may know more then us in certain game time decision. We must approach this topic with the idea of being more practical and clear to coaches. If we are simply pointing our algorithms and giving black-box predictions we lose all credibility as one would be oblivous to the true depth of decision making in the NFL.

In our analysis we discover via our Generalized Inverse Mills Ratio that coaches are able to factor in variables that are unseen in our data in the decision making process on 4th downs. Coaches also show signs of being able to properly evaluate the performance of players in fourth down situations. However, certain archetypes of quarterback are not being properly evaluated by coaches and factored into decision making by coaches.

1.3   Key Research Questions

This leads us to have a need to answer some key questions about fourth downs in the NFL. First, are coaches in the NFL actually better are making these decision then analysts? Second, is what key variables about players have predictive power in fourth down attempts? In other words, are there players that are more important in fourth down situations when compared to other situations. Finally, do these key variables about players have a causal effect on the outcome of fourth down attempts? Answering these questions will allow coaches to look for key signals in fourth down situations and to know which players to start on that fourth down if it is decided to attempt. This also can be applied in discovering specialty players that are overlooked due to poor performances in situations that are not similar to fourth down.

2   Literature Review

Much discourse revolves around the idea that NFL coaches are acting overly averse to risk, which is lowering their expected wins. Romer (2006) found that teams had begun to move towards a more conservative or safe strategy in the NFL. He argues that teams value successful gambles more then the expected win percentage in a game. He theorizes that the poor decision making is either due to risk aversion or it is due to poor information.

To further this point using matching analysis, Yam and Lopez (2018) quantified this conservative decision-making, finding that teams could gain approximately 0.4 wins per year by being more aggressive on fourth downs.

Goff and Locke (2019) found when revisiting Romer's framework that Romer's core findings are still held to be true. However, they argue that overly conservative calls are not due to poor decision making. Instead they point to risk aversion as they estimate that coaches are willing to give up two-thirds of a expected point to avoid the uncertainty of fourth down attempts.

On top of this, there seems to be evidence that coaches are more cautious when their job is on the line. Owens and Roach (2018) found that in the NCAA coaches are relatively more conservative when they are more likely to be fired. At the same time they found when a coach was likely to be promoted they behave more aggressive then normal.

If a team feels to be "on fire" should they be more aggressive since they feel they have momentum? A important area of literature is the fallacy of the "hot hand". The hot hand is a cognitive bias that leads people to believe that a person who has a successful outcome is more likely to have a successful outcome in future attempts. Gilovich et al. (1985) investigated the "hot hand" and "shooting streaks" in basketball. They found that both players and fans believed in the fallacy despite shots being independent of each other. Losak et al. (2023) similarly discovered that fantasy baseball users gravitated towards "hot" players. At the same time they were unable to identify a viable hot hand strategy in DraftKings DFS baseball.

Despite these common findings in other sports there does seem to be some evidence of momentum existing in the NFL. Roebber et al.(2022, p. 2) defined momentum in the NFL as "the sustained increase in win probability by a single team over the course of at least 2 successive changes in possession". With this definition, they found that streaks of win probability in football are non-random and are in fact predictable with Artificial Neural Network Models.

Lehman & Hahn (2013) looked to identify momentum across and within games in the NFL. Within-period momentum was found to encourage teams to take more risks. Negative within-period momentum was in turn found to encourage teams to take less risks. It was also discovered that across-period momentum has an effect only until a within-period momentum was established in a game

2.1 Research Gaps

A gap in the current research is caused by the lack in quality data. Currently we observe many studies include team-aggregated grades or summary statistics about teams that are playing against each other. While some situations can allow this, our non-parametric models will be able to handle data with thousands of different variables. To take advantage of this, we will have information about every single player that is on the field when the ball is snapped. This will allow us to have better prediction power then previous researchers. These non-parametric models will also allow us to discover key player specific variables that can allow for further causal inference with specific on-field positions.

3 Data

3.1 Sources

Our data was pulled from two main sources.

As a base the nflverse package provided in R gave us play by play data for the years of 2017 to 2023. This includes basic game information and the IDs of players that participated each play. The reason for our cutoff of 2017 is due to the NFL only putting tracking chips in players jerseys as of the 2016 season. The 2016 season however still had many inconsistencies which leads us to drop the year.

The key part then is the merging of Pro Football Focus's aggregated weekly data. The statistics are downloaded as premium player reports on a weekly bases and then aggregated to time lengths of 2 weeks, 12 weeks and 3 years. These time length have been arbitrarly picked which leaves room for future research. It was found that the 12 week time frame better captured the significance and value of players. This is due to the 2 week timeframe struggling with noise while the 3 year timeframe is not sensitive enough to emerging or aging players.

Players from the PFF data set where merged into our base play by play data set based on a 12 step algorithm that matched different player IDs accross the two sources. The steps included pre-match ids, and then was followed by maches based on names, teams and positions etc.

As a final note attendance data was also scrapped from Pro Football Reference. This data was then merged into our base data set to allow for the control of fan attendance in our models.

Variable	Available In	Outcome Data							Select Data						
		Mean	Median	SD	Min	Max	Zero Count	Zero %	Mean	Median	SD	Min	Max	Zero Count	Zero %
Conversion	Outcome Only	0.52	1.00	0.50	0.00	1.00	1923	47.85							
Attempt	Select Only								0.22	0.00	0.41	0.00	1.00	19970	77.98
Yards to Go	Both	4.12	2.00	4.58	1.00	34.00	0	0.00	7.77	7.00	5.73	1.00	46.00	0	0.00
Vegas Win Prob	Both	0.33	0.21	0.34	0.00	1.00	0	0.00	0.47	0.45	0.32	0.00	1.00	0	0.00
Spread Line	Both	1.98	3.00	6.35	-18.00	22.00	0	0.00	1.79	2.50	6.36	-18.00	22.00	44	0.17
Total Line	Both	45.43	45.50	4.55	30.00	63.50	0	0.00	45.01	45.00	4.56	30.00	63.50	0	0.00
Temperature	Both	60.84	70.00	15.35	6.00	93.00	0	0.00	61.73	70.00	15.14	6.00	97.00	0	0.00
Wind	Both	5.34	4.00	5.93	0.00	44.00	1604	39.91	5.42	4.00	5.73	0.00	44.00	9639	37.64
Def Stop Rate (Run)	Both	0.75	0.75	0.04	0.47	1.00	0	0.00	0.75	0.75	0.05	0.47	1.00	0	0.00
Def Stop Rate (Pass)	Both	0.67	0.67	0.04	0.39	0.86	0	0.00	0.67	0.67	0.04	0.37	0.91	0	0.00
QB Short Pass	Outcome Only	62.06	64.84	13.90	0.00	90.20	164	4.08							
QB Medium Pass	Outcome Only	63.36	66.97	17.08	0.00	99.10	209	5.20							
QB Deep Pass	Outcome Only	64.38	68.19	18.05	0.00	96.40	220	5.47							
Starter QB Short	Both	63.95	65.13	9.26	0.00	86.40	58	1.44	63.89	65.12	9.38	0.00	86.40	387	1.51
Starter QB Medium	Both	66.35	67.70	11.16	0.00	94.50	57	1.42	66.36	67.89	11.41	0.00	94.50	395	1.54
Starter QB Deep	Both	67.47	68.76	11.93	0.00	96.00	60	1.49	67.35	68.84	12.14	0.00	99.00	424	1.66

Dataset information: Outcome dataset: 4019 observations, 438 columns | Select dataset: 25608 observations, 123 columns

Figure 1: Key Data Summary

3.2 Variable Selection

Our variables that we work with fall into one of two categories. They are either statistics about players or about the situation of the play. The player variables consist of variables that describe who was on the field. We also have access to player variables of the starting players on each team based on depth chart data provided by nflverse. In both situations the players are sorted into columns based on depth chart position. For example, the starting QB is also in the offense_player_1 slot to allow us to maintain consistancy. Obviously our attempt models are forced to only use the starter player statistics as we cannot use the players on the field to predict the type of player that was called.

4 Methodology

4.1 Tools

The following models include several categories of control variables: *Game Situation Variables* capturing tactical contexts like distance needed, timeouts remaining, and time factors; *Coach Variables* reflecting experience, tenure, background, and historical decision patterns; *Team Stats* measuring performance metrics, efficiency ratings, and formation tendencies; *Season/Team FE* controlling for organizational factors unique to each team-season combination; *Coach FE* isolating individual coaching philosophies and tendencies; *Player Presence* binary indicators tracking which specific players or positions are on the field; *Control Def. Players* accounting for defensive quality, positioning, and scheme; and *Control Off. Players* measuring offensive personnel capabilities and skill ratings.

Tools that have both predictive and causal traits are being employed.

In our data we often had 20,000+ different player variables. This clearly is a situation where predictive tools such as Random Forest and XGBoosting thrive. In the use of XGBoosting we first use boostrapping to tune for optimal hyperparameters. Seccond we will run the tuned model on 1000 train/test bootstrapped splits of data to report the AUC. This process will be done when predicting attempts and conversion.

Similarly we can enact Random Forest to receive a OOB AUC. Random Forest will also let us receive insight into what variables have high importance in predictions based on MDA and MDI. This ranking of variables not only allows us to feature select for XGBoosting but it also assisted in watching what variables could be considered for causal analysis.

For the causal analysis we will be employing the a form of the Heckman correction. This is due to the selection bais in fourth downs. Since not all fourth downs are attempted, we do not have data on the fourth downs that never happened. We look to deal with this bias by using a evolved verison of Heckman's original model. In the original paper it was proposed to use a two step process. In the selection step one would predict the probability of being selected while including a variable that is exogenous to the actual outcome that we are interested in. This estimated probability is then converted into the IMR and used to control for selection bias in the outcome step. This process however assumes linear relationships in the selection stage.

In our case we are in fact not dealing with linear relationships in the selection stage. This is discovered by how we have a increase of almost 20 %pts in AUC when predicting attempts with a XGBoost model instead of a linear model. Therefore our first step in correcting selection bias looks to predict the probability of a attempt of a fourth down. This prediction then is converted into a Generalized IMR that is not bound to the assumptions of a IMR. We then place our GIMR in our outcome equation when estimating the conversion of a fourth down to control for selection bias.

4.2 Framework

4.2.1 Selection Model

Model the binary choice to attempt a play:

$$\text{Attempt}_i = \begin{cases} 1 & \text{if play is attempted} \\ 0 & \text{if play is not attempted} \end{cases} \tag{1}$$

The probability is modeled as:

$$z_i = \text{RF}(\mathbf{X}_i, \mathbf{K}_i, \mathbf{P}_i) \tag{2}$$

The distribution of z is:

Distribution of Offensive Play Probabilities
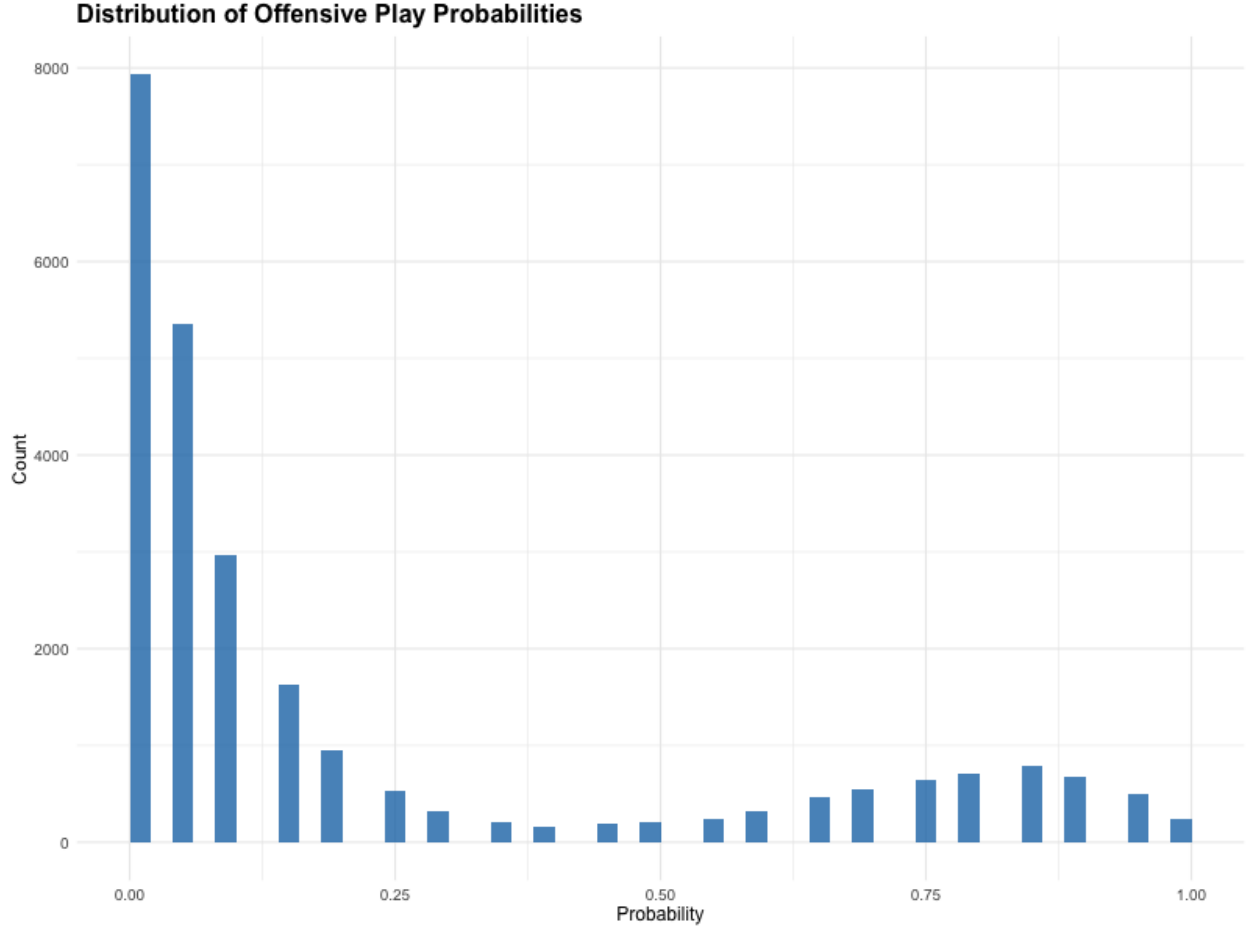
where:

- z_i: predicted probability of attempt
- $\mathbf{X}_i$: covariates excluding kicker and punter grades
- $\mathbf{K}_i$: kicker grades (exogenous)
- $\mathbf{P}_i$: punter grades (exogenous)

The generalized inverse Mills ratio is:

$$\lambda_i = \frac{\phi(z_i)}{1 - z_i} \tag{3}$$

Plot of f(z) = z/(1-z) for z from 0 to 1
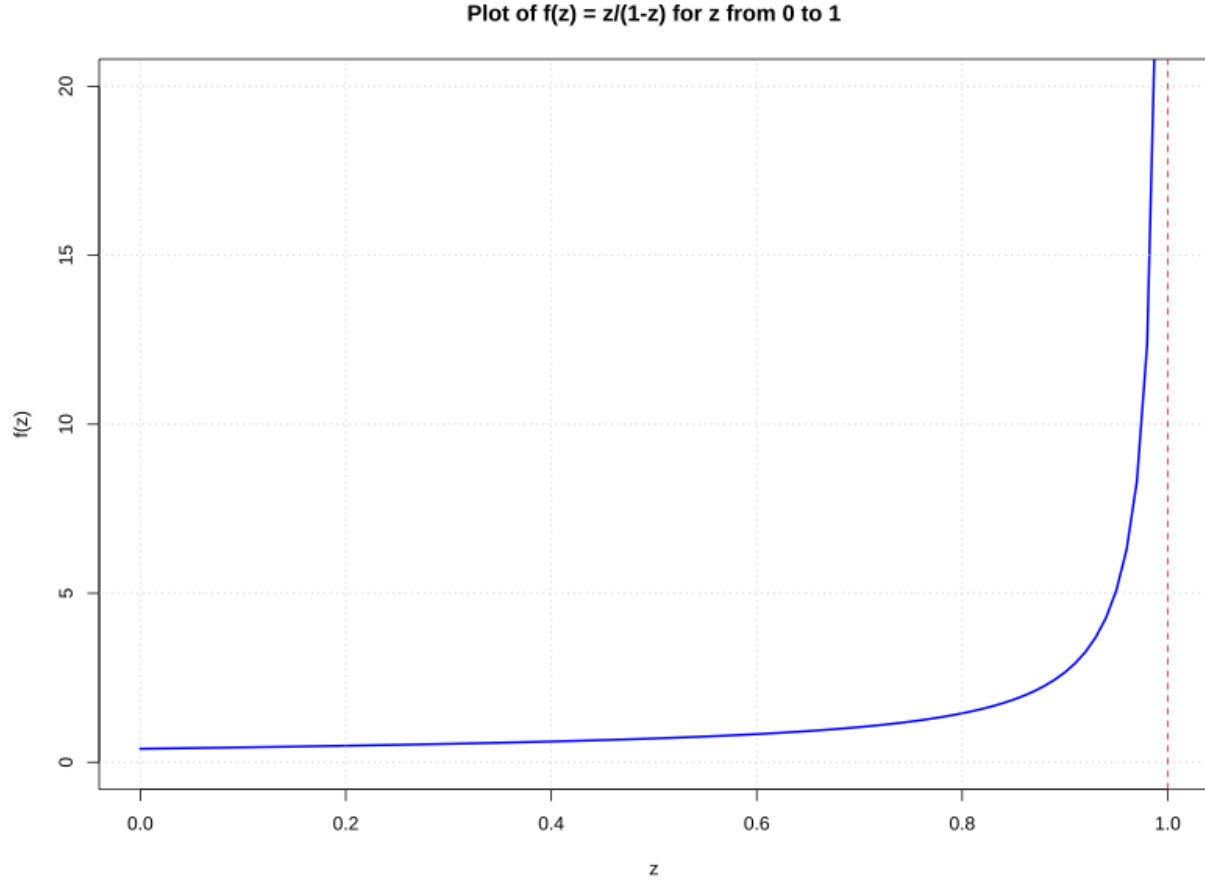
This functional form shifts the weights to emphasis situations where the probability of attempting a play is close to 1.

The first and second order conditions for λ_i are:

$$\frac{d\lambda}{dz} = \frac{\phi(z)(z^2 - z + 1)}{(1-z)^2} > 0$$

$$\frac{d^2\lambda}{dz^2} = \frac{\phi(z)[-z^3 + 2z^2 - 2z + 3]}{(1-z)^3} > 0$$

Thus λ_i is strictly increasing and convex in z_i.

4.2.2 Outcome Model

Model the binary conversion outcome for attempted plays:

$$\text{Convert}_i = \begin{cases} 1 & \text{if attempt is successful} \\ 0 & \text{if attempt fails} \end{cases} \tag{4}$$

The inputed GIMR then has the following distribution:

Distribution of Generalized Inverse Mills Ratio (GIMR)
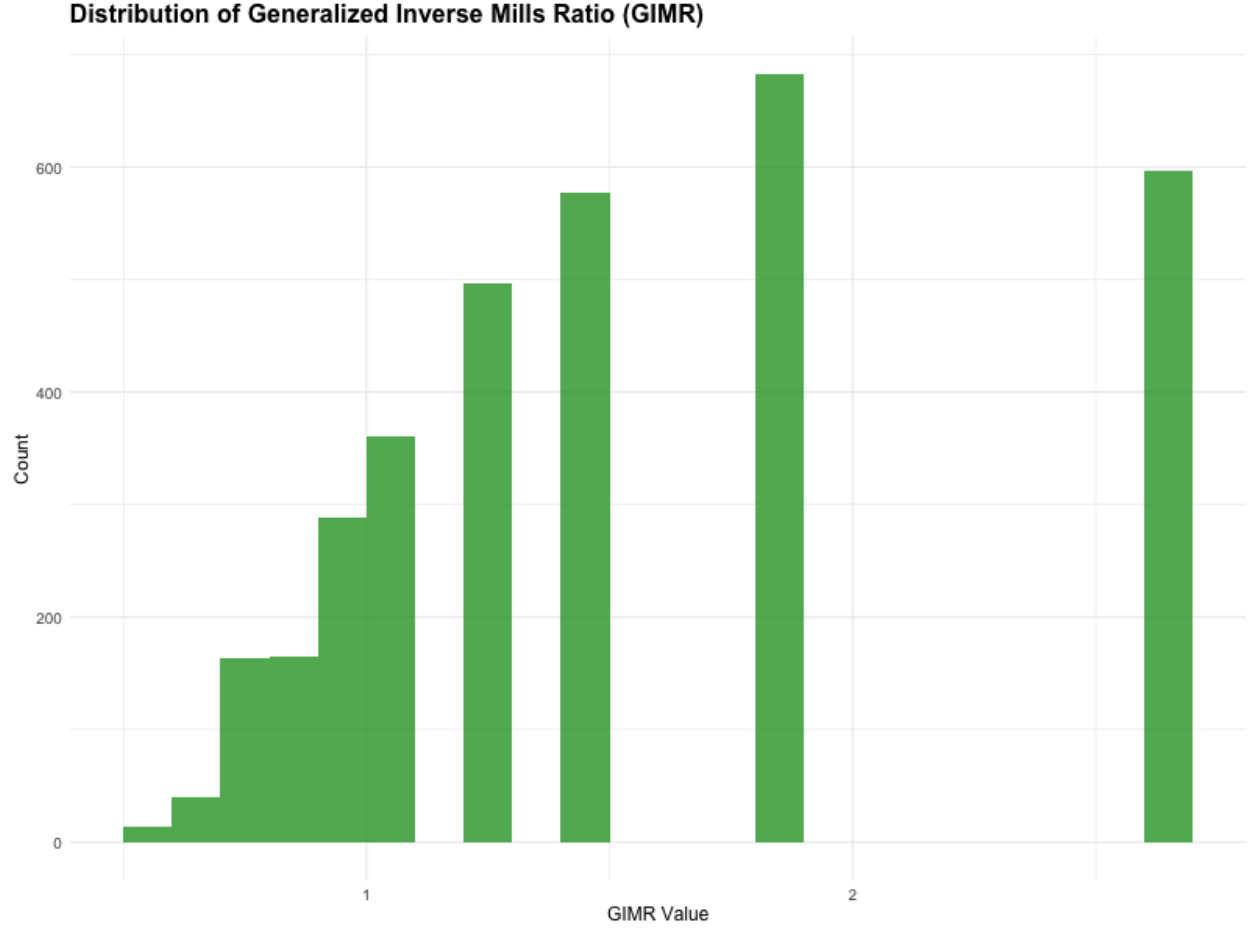
Linear probability model with selection correction:

$$P(\text{Convert}_i = 1|\mathbf{X}_i, \lambda_i) = \mathbf{X}_i\boldsymbol{\beta} + \theta\lambda_i + \varepsilon_i \tag{5}$$

where:

- $\mathbf{X}_i$: covariates excluding kicker and punter grades

- λ_i: generalized inverse Mills ratio

- $\boldsymbol{\beta}$: coefficient vector for main covariates

- θ: selection correction parameter

- ε_i: error term with HC1 robust standard errors

Note: Kicker grades ($\mathbf{K}_i$) and punter grades ($\mathbf{P}_i$) serve as exogenous variables in the selection equation but are excluded from the outcome equation for identification.

Models are estimated separately for offensive outcomes (grades, yards, completions) and defensive outcomes (stops, grades, tackles).

5 Results

5.1 Exogeniety of Kicker and Punter Grades

A key feature in our sample selection correction model, is the exogeniety of a variable that influences the selection equation. In American Football there is the luxery of using third down conversions as a selection bias free area. This is due to how conditions such as desperation or play calling cause a 3rd down to be treated similarly to a fourth down by the coaches. A fourth down is a teams last attempt for that offensive drive. While not in all, there are many cases of third down provide the similar conditions in terms of the coaches decision making. For example if the ball is on a teams own 20 yard line and they are on 3rd and 10, the coach will treat this attempt as a "last chance". This is due to the fact that if the team does not convert on 3rd down they will be forced to punt the ball. There is no situation here where the team can even consider kicking a field goal.

We can first note that the grades of a teams kicker is positively significant in it's effect on the decision to attempt a fourth down. Exogenity of the kicker is now required in the case of the outcome of fourth downs.

When the kicker is not on the field during a fourth down they are unable to effect the decision making of the coaches or plays of the coaches, as there are no further decisions to be made. In a Third down situation we find that kicker grades do have positive significance on the conversion of a third down. This significance, is soley found in the middle of the field, where the kicker is more likely to be used if the third down is not converted. In the situations on third down that would mirror a fourth down, there is no statistical significance. When the kicker is not apart of the decision making process on third down, similarly to fourth down, it does not have a effect on 3rd down conversion.

Variable	Own 1-10	Own 11-20	Own 21-30	Own 31-40	Own 41-50	Opp. 49-40	Opp. 39-30	Opp. 29-20	Opp. 19-10	Opp. 9-1
LPM Model										
Punter Grades (12w)	-3.019***	-0.574	-1.710*	-4.245***	-1.126	-1.913*	-0.091	-0.206	0.101	0.366
Kicker FG Grades (12w)	1.663*	-0.771	0.653	3.210***	1.845*	2.795***	1.638.	0.420	0.647	0.488
Probit Model										
Punter Grades (12w)	-1.576.	-1.056	-1.679*	-4.138***	-1.291	-1.775*	-0.155	-0.110	0.222	0.147
Kicker FG Grades (12w)	1.859*	-0.912	0.705	3.119***	1.858*	2.667***	1.569.	0.280	0.477	0.373
Logit Model										
Punter Grades (12w)	-1.488.	-1.097	-1.763*	-4.087***	-1.142	-1.726*	-0.130	-0.192	0.164	0.136
Kicker FG Grades (12w)	1.781*	-0.821	0.709	3.146***	1.852*	2.629***	1.635.	0.388	0.530	0.417
Controls										
Game Situation	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Environmental	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Coach Variables	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Team Stats	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Player Variables	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Player Presence	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Season/Team FE	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Coach FE	No	No	No	No	No	No	No	No	No	No
Sample Size	988	3,023	6,865	6,924	5,805	4,945	4,271	3,897	3,478	3,080

Note: Values shown are t-statistics from respective model regressions with conversion as the dependent variable   Significance codes: *** p<0.01, ** p<0.05, * p<0.1, . p<0.15

Figure 2: Kicker Offensive Grades

This significance of the kicker and punter grades in key area of the field is due to the coaches being able to properly adjust their decision making for whether or not to attempt a fourth down. This is to say that coaches are properly recognizing how good or bad both their punters and kicker are and making adjustments on their playcalling.

As a note while punters do not show signs of significantly affecting the 4th down attempt probability, they are included. The logic for them remains the same as the kickers and therefore there is no harm in including them in the selection model.
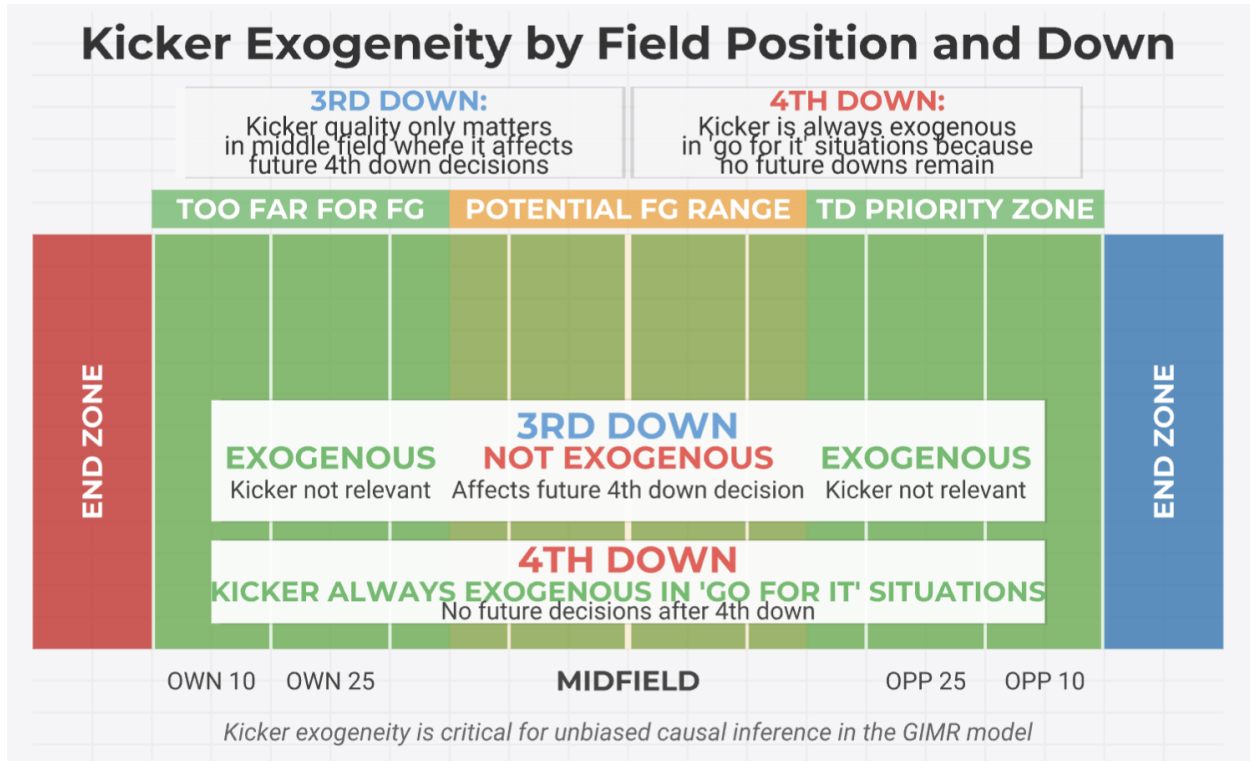
Figure 3: Kicker Plot

5.2 Generalized Inverse Mills Ratio (GIMR)

In examining the following tables the significance of our GIMR is confirmed. This tells us that coaches in the NFL see factors that we cannot and act on them in the proper way. When a coach is more likly to attempt a fourth down conversion attempt that they are then also more likely to convert that fourth down attempt due to unseen variables.

5.3 Player Analysis

5.3.1 Pretense

The exogeniety of kicker grades then allows a bias-free analysis of individual players and coaches. Players are evaluated in terms of their performance in the 12 week timeframe. This time frame is arbitrary and can be a source of future research with how to optimize the measurement of player values.

Players that are used are either "On-Field" or "Starter" players. On-Field players are players that are on the field during the fourth down attempt. Starter players are the players that are listed as the starter on the depth chart. In both situations players are sorted via depth chart postings.

For each of these categories we then create models that focus on either offensive of defensive players. If a offensive model is ran we select multiple features about each player on the offense while keeping one key feature of each defensive player. The opposite is done for the defensive model.

The offensive and defensive models are both measured in three different ways. For offensive models we measure by PFF grades, completions/receptions and yards. For defensive models we measure by PFF grades, stops and tackles. For our current work we will use PFF grades for our main analysis due to it's

ability to capture the overall performance of a player in a specific area. The other measures will be kept as robustness checks.

To evaluate a coaches' decision making, the Attempt Models are able to show if a coach is properly deciding to Attempt a fourth down based on features of players that influence the conversion of a fourth down.

5.3.2 Individual Player Offensive Grades Model Results

	Starter Models			On-Field Models			Attempt Models		
Variable	Starter LPM	Starter Probit	Starter Logit	On-Field LPM	On-Field Probit	On-Field Logit	Attempt LPM	Attempt Probit	Attempt Logit
Quarterbacks									
Short Grades Pass	0.028(0.016)*	0.036(0.019)*	0.036(0.020)*	0.030(0.014)**	0.038(0.017)**	0.040(0.017)**	0.007(0.004)	0.007(0.005)	0.006(0.004)
Medium Grades Pass	-0.014(0.013)	-0.016(0.015)	-0.017(0.016)	-0.002(0.015)	0.001(0.017)	-0.001(0.018)	0.006(0.004)	0.005(0.004)	0.004(0.004)
Deep Grades Pass	-0.013(0.013)	-0.017(0.015)	-0.019(0.016)	-0.021(0.013)	-0.029(0.015)*	-0.029(0.016)*	0.006(0.004)	0.005(0.004)	0.005(0.003)
Running Backs									
Grades Pass Block	-0.021(0.010)**	-0.026(0.012)**	-0.027(0.013)**	0.012(0.010)	0.013(0.011)	0.014(0.012)	-0.004(0.003)	-0.006(0.003)*	-0.005(0.003)*
Grades Run	0.011(0.011)	0.014(0.012)	0.015(0.013)	-0.005(0.011)	-0.006(0.013)	-0.007(0.013)	-0.001(0.003)	-0.001(0.003)	-0.000(0.003)
Short Grades Pass	0.004(0.011)	0.005(0.012)	0.004(0.013)	-0.002(0.010)	-0.002(0.012)	-0.002(0.012)	-0.000(0.003)	0.000(0.003)	0.000(0.003)
Medium Grades Pass	-0.015(0.009)	-0.017(0.011)	-0.017(0.011)	-0.005(0.009)	-0.006(0.010)	-0.006(0.011)	-0.001(0.003)	-0.001(0.003)	-0.001(0.003)
Deep Grades Pass	-0.005(0.010)	-0.006(0.011)	-0.006(0.011)	-0.003(0.009)	-0.003(0.010)	-0.004(0.011)	0.003(0.003)	0.002(0.003)	0.002(0.002)
WR1									
Grades Run Block	0.007(0.015)	0.006(0.018)	0.008(0.018)	-0.011(0.019)	-0.015(0.022)	-0.014(0.023)	-0.006(0.004)	-0.006(0.004)	-0.005(0.004)
Short Grades Pass	0.003(0.013)	0.003(0.015)	0.004(0.016)	0.000(0.016)	-0.002(0.018)	-0.003(0.018)	-0.000(0.004)	-0.000(0.004)	-0.001(0.004)
Medium Grades Pass	0.015(0.013)	0.017(0.015)	0.018(0.016)	0.000(0.014)	0.002(0.016)	0.002(0.017)	0.005(0.004)	0.004(0.004)	0.004(0.004)
Deep Grades Pass	0.001(0.011)	0.001(0.013)	0.001(0.013)	0.002(0.012)	0.005(0.014)	0.005(0.014)	0.003(0.003)	0.004(0.003)	0.003(0.003)
WR2									
Grades Run Block	-0.021(0.016)	-0.025(0.018)	-0.025(0.018)	0.028(0.036)	0.036(0.042)	0.039(0.043)	-0.001(0.004)	-0.001(0.005)	0.001(0.004)
Short Grades Pass	-0.011(0.013)	-0.012(0.015)	-0.014(0.016)	0.013(0.024)	0.016(0.027)	0.016(0.028)	0.008(0.004)**	0.008(0.004)**	0.007(0.003)**
Medium Grades Pass	0.015(0.012)	0.017(0.013)	0.019(0.014)	-0.005(0.020)	-0.009(0.023)	-0.008(0.024)	0.001(0.004)	-0.000(0.004)	-0.000(0.003)
Deep Grades Pass	0.003(0.011)	0.005(0.012)	0.005(0.013)	0.011(0.016)	0.017(0.019)	0.016(0.020)	0.000(0.003)	0.000(0.003)	0.000(0.003)
WR3									
Grades Run Block	-0.007(0.014)	-0.008(0.016)	-0.010(0.016)	0.017(0.027)	0.024(0.031)	0.023(0.033)	-0.001(0.004)	-0.001(0.004)	-0.000(0.004)
Short Grades Pass	-0.014(0.011)	-0.019(0.013)	-0.019(0.013)	-0.002(0.020)	-0.000(0.023)	0.002(0.024)	-0.003(0.003)	-0.003(0.003)	-0.002(0.003)
Medium Grades Pass	0.008(0.010)	0.008(0.012)	0.009(0.012)	0.011(0.019)	0.007(0.022)	0.007(0.023)	0.006(0.003)*	0.005(0.003)	0.005(0.003)
Deep Grades Pass	0.003(0.010)	0.005(0.011)	0.005(0.011)	0.004(0.012)	0.023(0.017)	0.023(0.018)	0.001(0.003)	0.002(0.003)	0.002(0.003)
TE1									
Grades Pass Block	0.025(0.011)**	0.031(0.013)**	0.033(0.014)**	0.024(0.011)**	0.032(0.013)**	0.033(0.014)**	-0.002(0.003)	-0.003(0.003)	-0.002(0.003)
Grades Run Block	-0.015(0.015)	-0.018(0.017)	-0.020(0.018)	-0.013(0.012)	-0.017(0.014)	-0.017(0.015)	-0.000(0.004)	0.002(0.005)	0.001(0.004)
Short Grades Pass	0.004(0.013)	0.004(0.014)	0.003(0.015)	0.000(0.013)	-0.001(0.014)	-0.001(0.015)	0.003(0.004)	0.002(0.004)	0.002(0.003)
Medium Grades Pass	-0.016(0.011)	-0.019(0.012)	-0.020(0.013)	0.017(0.011)	0.020(0.012)*	0.022(0.012)*	0.002(0.003)	0.002(0.003)	0.001(0.003)
Deep Grades Pass	-0.004(0.010)	-0.004(0.011)	-0.004(0.012)	-0.015(0.009)	-0.018(0.011)*	-0.018(0.011)*	0.002(0.003)	0.002(0.003)	0.002(0.003)
OL1									
Grades Pass Block	0.016(0.012)	0.021(0.014)	0.023(0.014)	-0.010(0.009)	-0.013(0.011)	-0.013(0.011)	-0.004(0.003)	-0.004(0.003)	-0.003(0.003)
Grades Run Block	0.004(0.014)	0.006(0.016)	0.005(0.017)	0.006(0.010)	0.007(0.011)	0.009(0.012)	0.001(0.004)	0.000(0.004)	0.000(0.004)
OL2									
Grades Pass Block	-0.008(0.012)	-0.009(0.013)	-0.010(0.014)	-0.005(0.010)	-0.005(0.011)	-0.006(0.011)	-0.000(0.003)	-0.001(0.003)	-0.002(0.003)
Grades Run Block	-0.002(0.014)	-0.003(0.016)	-0.003(0.017)	-0.012(0.010)	-0.015(0.011)	-0.017(0.012)	0.003(0.004)	0.005(0.004)	0.004(0.004)
OL3									
Grades Pass Block	0.010(0.012)	0.010(0.013)	0.012(0.014)	0.007(0.009)	0.009(0.011)	0.010(0.011)	0.001(0.003)	0.001(0.004)	0.001(0.003)
Grades Run Block	-0.015(0.014)	-0.019(0.016)	-0.020(0.017)	0.004(0.009)	0.006(0.011)	0.006(0.011)	-0.004(0.004)	-0.004(0.004)	-0.004(0.004)
OL4									
Grades Pass Block	0.022(0.012)*	0.026(0.014)*	0.028(0.014)*	0.006(0.010)	0.007(0.011)	0.008(0.012)	-0.003(0.003)	-0.004(0.003)	-0.003(0.003)
Grades Run Block	-0.006(0.013)	-0.008(0.015)	-0.009(0.015)	-0.013(0.010)	-0.014(0.011)	-0.016(0.011)	0.000(0.004)	0.001(0.004)	0.001(0.003)
OL5									
Grades Pass Block	0.030(0.012)**	0.034(0.014)**	0.036(0.015)**	-0.011(0.010)	-0.015(0.012)	-0.015(0.012)	0.001(0.003)	0.003(0.004)	0.002(0.003)
Grades Run Block	-0.031(0.013)**	-0.037(0.015)**	-0.037(0.016)**	0.009(0.010)	0.010(0.012)	0.011(0.012)	-0.002(0.004)	-0.002(0.004)	-0.002(0.003)
Perf. Measures									
GIMR	0.040(0.009)***	0.048(0.011)***	0.049(0.012)***	0.040(0.009)***	0.048(0.011)***	0.049(0.012)***			
Control Variables									
Game Situation	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Coach Variables	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Team Stats	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Season/Team FE	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Coach FE	No	No	No	Yes	Yes	Yes	Yes	Yes	Yes
Player Presence	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Control Def. Players	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Control Off. Players	No	No	No	No	No	No	No	No	No

Note:
Marginal effects reported with standard errors in parentheses and significance levels.
* * p < 0.10, ** p < 0.05, *** p < 0.01

Figure 4: Offense Grades Table

5.3.3 Individual Player Defensive Grades Model Results

	Starter Models			On-Field Models			Attempt Models		
Variable	Starter LPM	Starter Probit	Starter Logit	On-Field LPM	On-Field Probit	On-Field Logit	Attempt LPM	Attempt Probit	Attempt Logit
DL1									
Grades Run Defense	0.002(0.015)	0.002(0.018)	0.002(0.018)	-0.005(0.011)	-0.005(0.013)	-0.005(0.013)	-0.006(0.004)	-0.005(0.005)	-0.004(0.004)
Grds Pass Rush Def	0.009(0.015)	0.012(0.017)	0.013(0.018)	-0.015(0.011)	-0.018(0.013)	-0.019(0.013)	0.008(0.004)*	0.009(0.004)*	0.008(0.004)**
DL2									
Grades Run Defense	0.026(0.015)*	0.031(0.017)*	0.031(0.018)*	0.005(0.024)	0.008(0.027)	0.007(0.028)	-0.002(0.004)	-0.002(0.005)	-0.001(0.004)
Grds Pass Rush Def	-0.017(0.014)	-0.020(0.016)	-0.022(0.017)	-0.018(0.023)	-0.023(0.026)	-0.023(0.028)	-0.003(0.004)	-0.003(0.004)	-0.004(0.004)
DL3									
Grades Run Defense	-0.004(0.015)	-0.006(0.017)	-0.006(0.018)	-0.015(0.042)	-0.021(0.047)	-0.019(0.048)	-0.004(0.004)	-0.007(0.005)	-0.006(0.004)
Grds Pass Rush Def	0.002(0.015)	0.006(0.017)	0.004(0.017)	0.002(0.045)	0.007(0.051)	-0.000(0.052)	0.001(0.004)	0.004(0.004)	0.003(0.004)
DL4									
Grades Run Defense	0.012(0.015)	0.012(0.017)	0.014(0.017)	-0.044(0.050)	-0.054(0.058)	-0.056(0.060)	0.000(0.004)	-0.002(0.005)	-0.001(0.004)
Grds Pass Rush Def	-0.004(0.015)	-0.003(0.017)	-0.004(0.017)	-0.017(0.053)	-0.018(0.060)	-0.022(0.062)	-0.002(0.004)	0.000(0.005)	-0.001(0.004)
LB1									
Grades Run Defense	0.027(0.013)**	0.034(0.015)**	0.035(0.016)**	0.006(0.010)	0.006(0.012)	0.006(0.012)	0.001(0.004)	0.000(0.004)	-0.000(0.003)
Man Grades Cov Def	-0.022(0.010)**	-0.027(0.011)**	-0.028(0.012)**	0.005(0.008)	0.007(0.010)	0.007(0.010)	0.002(0.003)	0.003(0.003)	0.003(0.003)
Zone Grades Cov Def	-0.007(0.012)	-0.008(0.014)	-0.008(0.015)	-0.002(0.010)	-0.004(0.011)	-0.003(0.012)	-0.005(0.004)	-0.004(0.004)	-0.004(0.003)
LB2									
Grades Run Defense	0.026(0.013)**	0.033(0.015)**	0.034(0.016)**	-0.014(0.017)	-0.016(0.020)	-0.017(0.020)	0.002(0.004)	0.004(0.004)	0.003(0.004)
Man Grades Cov Def	-0.011(0.010)	-0.013(0.012)	-0.014(0.012)	0.004(0.013)	0.006(0.015)	0.005(0.016)	-0.001(0.003)	-0.002(0.003)	-0.001(0.003)
Zone Grades Cov Def	-0.013(0.012)	-0.017(0.013)	-0.017(0.014)	0.013(0.017)	0.013(0.019)	0.014(0.020)	0.002(0.003)	0.003(0.003)	0.002(0.003)
LB3									
Grades Run Defense	-0.004(0.013)	-0.004(0.015)	-0.005(0.016)	-0.036(0.036)	-0.040(0.041)	-0.044(0.043)	-0.002(0.004)	-0.003(0.004)	-0.003(0.003)
Man Grades Cov Def	0.019(0.011)	0.022(0.013)*	0.023(0.013)*	0.019(0.019)	0.022(0.021)	0.023(0.022)	0.005(0.003)*	0.004(0.003)	0.004(0.003)
Zone Grades Cov Def	-0.001(0.012)	-0.003(0.014)	-0.002(0.015)	-0.041(0.028)	-0.049(0.032)	-0.053(0.034)	0.005(0.004)	0.006(0.004)*	0.005(0.003)*
LB4									
Grades Run Defense	-0.029(0.012)**	-0.034(0.013)**	-0.037(0.014)***	0.031(0.040)	0.033(0.045)	0.035(0.047)	0.002(0.003)	0.002(0.004)	0.002(0.003)
Man Grades Cov Def	0.024(0.012)**	0.029(0.013)**	0.030(0.014)**	-0.003(0.018)	-0.006(0.021)	-0.006(0.022)	-0.000(0.003)	-0.001(0.003)	-0.000(0.003)
Zone Grades Cov Def	0.004(0.013)	0.004(0.015)	0.005(0.016)	-0.004(0.029)	-0.002(0.035)	-0.003(0.036)	-0.001(0.004)	-0.002(0.004)	-0.002(0.003)
CB1									
Grades Run Defense	-0.013(0.015)	-0.015(0.017)	-0.015(0.018)	0.008(0.016)	0.011(0.018)	0.011(0.019)	-0.002(0.004)	-0.002(0.004)	-0.002(0.004)
Man Grades Cov Def	-0.009(0.013)	-0.014(0.015)	-0.013(0.015)	-0.029(0.014)**	-0.033(0.016)**	-0.036(0.016)**	0.000(0.004)	0.001(0.004)	0.001(0.003)
Zone Grades Cov Def	0.007(0.015)	0.010(0.017)	0.009(0.017)	-0.012(0.015)	-0.014(0.017)	-0.014(0.018)	0.000(0.004)	-0.001(0.004)	-0.001(0.004)
CB2									
Grades Run Defense	0.033(0.014)**	0.041(0.016)**	0.043(0.017)**	-0.020(0.020)	-0.022(0.023)	-0.024(0.023)	-0.008(0.004)*	-0.005(0.004)	-0.006(0.004)
Man Grades Cov Def	-0.014(0.012)	-0.018(0.014)	-0.018(0.014)	0.008(0.018)	0.009(0.021)	0.009(0.022)	-0.004(0.004)	-0.004(0.004)	-0.003(0.003)
Zone Grades Cov Def	-0.011(0.014)	-0.015(0.016)	-0.016(0.017)	-0.007(0.021)	-0.008(0.024)	-0.008(0.025)	0.002(0.004)	0.000(0.004)	0.001(0.004)
CB3									
Grades Run Defense	-0.019(0.012)	-0.025(0.014)*	-0.025(0.014)*	0.032(0.033)	0.039(0.037)	0.040(0.039)	-0.005(0.004)	-0.006(0.004)*	-0.006(0.003)*
Man Grades Cov Def	0.019(0.012)	0.026(0.014)*	0.026(0.015)*	-0.000(0.030)	0.005(0.033)	0.006(0.034)	0.011(0.004)***	0.010(0.004)***	0.009(0.003)***
Zone Grades Cov Def	-0.010(0.013)	-0.011(0.016)	-0.012(0.016)	0.029(0.034)	0.033(0.038)	0.035(0.040)	0.002(0.004)	0.004(0.004)	0.004(0.004)
S1									
Grades Run Defense	0.003(0.016)	0.003(0.018)	0.005(0.019)	-0.020(0.013)	-0.023(0.015)	-0.024(0.016)	-0.003(0.005)	-0.004(0.005)	-0.002(0.004)
Man Grades Cov Def	-0.006(0.014)	-0.006(0.016)	-0.007(0.017)	0.000(0.012)	-0.001(0.015)	-0.002(0.016)	-0.003(0.004)	-0.005(0.004)	-0.005(0.004)
Zone Grades Cov Def	-0.005(0.014)	-0.008(0.017)	-0.008(0.017)	0.013(0.012)	0.018(0.014)	0.018(0.015)	0.006(0.004)	0.006(0.004)	0.006(0.004)
S2									
Grades Run Defense	-0.008(0.015)	-0.011(0.018)	-0.011(0.019)	-0.002(0.027)	-0.004(0.030)	-0.006(0.031)	-0.002(0.005)	-0.004(0.005)	-0.003(0.004)
Man Grades Cov Def	-0.009(0.013)	-0.009(0.015)	-0.009(0.016)	-0.008(0.025)	-0.011(0.030)	-0.011(0.031)	0.003(0.004)	0.003(0.004)	0.002(0.004)
Zone Grades Cov Def	-0.004(0.014)	-0.006(0.016)	-0.006(0.016)	0.006(0.026)	0.009(0.030)	0.010(0.032)	0.002(0.005)	0.002(0.005)	0.003(0.004)
S3									
Grades Run Defense	-0.007(0.013)	-0.007(0.015)	-0.007(0.016)	0.010(0.044)	0.011(0.053)	0.009(0.056)	-0.002(0.004)	-0.001(0.004)	-0.000(0.003)
Man Grades Cov Def	-0.003(0.013)	-0.004(0.015)	-0.005(0.016)	-0.016(0.043)	-0.015(0.048)	-0.016(0.051)	0.004(0.004)	0.003(0.004)	0.003(0.003)
Zone Grades Cov Def	0.020(0.015)	0.024(0.017)	0.025(0.018)	0.016(0.047)	0.014(0.055)	0.018(0.059)	-0.005(0.004)	-0.004(0.004)	-0.005(0.004)
Perf. Measures									
GIMR	0.030(0.009)***	0.041(0.012)***	0.043(0.012)***	0.028(0.009)***	0.039(0.012)***	0.040(0.012)***			
Control Variables									
Game Situation	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Coach Variables	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Team Stats	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Season/Team FE	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Coach FE	No	No	No	Yes	Yes	Yes	Yes	Yes	Yes
Player Presence	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Control Off. Players	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Control Def. Players	No	No	No	No	No	No	No	No	No

Note:
Marginal effects reported with standard errors in parentheses and significance levels.
* * p < 0.10, ** p < 0.05, *** p < 0.01

Figure 5: Defense Grades Table

5.3.4 Offensive Player Joint Significance Results

Variable	Starter Models			On-Field Models			Attempt Models		
	Starter LPM	Starter Probit	Starter Logit	On-Field LPM	On-Field Probit	On-Field Logit	Attempt LPM	Attempt Probit	Attempt Logit
Quarterbacks	1.73 [3,4016]	2.00 [3,4016]	2.03 [3,4016]	2.36* [3,4016]	2.95** [3,4016]	2.95** [3,4016]	2.64** [3,25605]	1.75 [3,25605]	1.96 [3,25605]
Running Backs	1.62 [5,4014]	1.80 [5,4014]	1.78 [5,4014]	0.39 [5,4014]	0.39 [5,4014]	0.40 [5,4014]	0.65 [5,25603]	0.77 [5,25603]	0.72 [5,25603]
Wide Receivers	0.70 [12,4007]	0.77 [12,4007]	0.79 [12,4007]	0.31 [12,4007]	0.43 [12,4007]	0.38 [12,4007]	1.11 [12,25596]	1.05 [12,25596]	1.03 [12,25596]
Tight Ends	1.72 [5,4014]	1.87* [5,4014]	1.96* [5,4014]	2.09* [5,4014]	2.58** [5,4014]	2.57** [5,4014]	0.35 [5,25603]	0.39 [5,25603]	0.35 [5,25603]
Offensive Line	1.92** [10,4009]	2.04** [10,4009]	2.09** [10,4009]	0.81 [10,4009]	0.91 [10,4009]	0.97 [10,4009]	0.42 [10,25598]	0.66 [10,25598]	0.63 [10,25598]
Control Variables									
Game Situation	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Coach Variables	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Team Stats	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Season/Team FE	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Coach FE	No	No	No	Yes	Yes	Yes	Yes	Yes	Yes
GIMR	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Player Presence	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Control Def. Players	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Control Off. Players	No	No	No	No	No	No	No	No	No

Note:

F-statistics reported with degrees of freedom [df1,df2] and significance levels. Stars indicate significance of joint test for all variables in position group.

* * p < 0.10, ** p < 0.05, *** p < 0.01

Figure 6: Offense Grades Model Results

5.3.5 Defensive Player Joint Significance Results

Variable	Starter Models			On-Field Models			Attempt Models		
	Starter LPM	Starter Probit	Starter Logit	On-Field LPM	On-Field Probit	On-Field Logit	Attempt LPM	Attempt Probit	Attempt Logit
Defensive Line	0.65 [8,4011]	0.76 [8,4011]	0.71 [8,4011]	1.23 [8,4011]	1.30 [8,4011]	1.29 [8,4011]	1.49 [8,25600]	1.08 [8,25600]	0.97 [8,25600]
Linebackers	2.17** [12,4007]	2.44*** [12,4007]	2.38*** [12,4007]	0.62 [12,4007]	0.64 [12,4007]	0.67 [12,4007]	0.46 [12,25596]	0.52 [12,25596]	0.55 [12,25596]
Cornerbacks	1.55 [9,4010]	1.65* [9,4010]	1.64* [9,4010]	0.84 [9,4010]	0.87 [9,4010]	0.94 [9,4010]	1.82* [9,25599]	1.75* [9,25599]	1.89** [9,25599]
Safeties	0.61 [9,4010]	0.67 [9,4010]	0.70 [9,4010]	0.78 [9,4010]	0.82 [9,4010]	0.86 [9,4010]	1.18 [9,25599]	1.35 [9,25599]	1.14 [9,25599]
Control Variables									
Game Situation	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Coach Variables	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Team Stats	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Season/Team FE	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Coach FE	No	No	No	Yes	Yes	Yes	Yes	Yes	Yes
GIMR	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Player Presence	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Control Off. Players	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Control Def. Players	No	No	No	No	No	No	No	No	No

Note:

F-statistics reported with degrees of freedom [df1,df2] and significance levels. Stars indicate significance of joint test for all variables in position group.

* * p < 0.10, ** p < 0.05, *** p < 0.01

Figure 7: Defense Grades Model Results by Position Groups

5.3.6 Offense Joint Significance Results

Dataset	Starter Models			On-Field Models			Attempt Models		
	Starter LPM	Starter Probit	Starter Logit	On-Field LPM	On-Field Probit	On-Field Logit	Attempt LPM	Attempt Probit	Attempt Logit
Offense Grades	1.41* [35,3984]	1.54** [35,3984]	1.58** [35,3984]	0.89 [35,3984]	1.08 [35,3984]	1.09 [35,3984]	0.87 [35,25573]	0.86 [35,25573]	0.86 [35,25573]
Offense Yards	1.95*** [35,3984]	2.23*** [35,3984]	2.22*** [35,3984]	1.04 [35,3984]	1.16 [35,3984]	1.16 [35,3984]	0.80 [35,25573]	0.97 [35,25573]	0.89 [35,25573]
Offense Completions	1.71*** [35,3984]	1.94*** [35,3984]	1.92*** [35,3984]	1.18 [35,3984]	1.32* [35,3984]	1.30 [35,3984]	0.69 [35,25573]	0.80 [35,25573]	0.71 [35,25573]
Control Variables									
Game Situation	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Coach Variables	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Team Stats	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Season/Team FE	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Coach FE	No	No	No	Yes	Yes	Yes	Yes	Yes	Yes
GIMR	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Player Presence	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Control Def. Players	No	No	No	No	No	No	No	No	No
Control Off. Players	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes

Note:
F-statistics reported with degrees of freedom [df1,df2] and significance levels for ALL position variables combined.
* * p < 0.10, ** p < 0.05, *** p < 0.01

Figure 8: Joint Significance Offense

5.3.7 Defense Joint Significance Results

Dataset	Starter Models			On-Field Models			Attempt Models		
	Starter LPM	Starter Probit	Starter Logit	On-Field LPM	On-Field Probit	On-Field Logit	Attempt LPM	Attempt Probit	Attempt Logit
Defense Grades	1.38* [38,3981]	1.62*** [38,3981]	1.60** [38,3981]	0.59 [38,3981]	0.64 [38,3981]	0.64 [38,3981]	1.05 [38,25570]	1.04 [38,25570]	1.13 [38,25570]
Defense Stops	1.33* [38,3981]	1.48** [38,3981]	1.46** [38,3981]	0.84 [38,3981]	0.88 [38,3981]	0.91 [38,3981]	1.17 [38,25570]	1.13 [38,25570]	1.10 [38,25570]
Defense Tackles	1.12 [38,3981]	1.20 [38,3981]	1.20 [38,3981]	0.78 [38,3981]	0.87 [38,3981]	0.85 [38,3981]	1.12 [38,25570]	1.08 [38,25570]	1.07 [38,25570]
Control Variables									
Game Situation	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Coach Variables	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Team Stats	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Season/Team FE	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Coach FE	No	No	No	Yes	Yes	Yes	Yes	Yes	Yes
GIMR	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Player Presence	Yes	Yes	Yes	Yes	Yes	Yes	No	No	No
Control Off. Players	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Control Def. Players	No	No	No	No	No	No	No	No	No

Note:
F-statistics reported with degrees of freedom [df1,df2] and significance levels for ALL position variables combined.
* * p < 0.10, ** p < 0.05, *** p < 0.01

Figure 9: Joint Significance Defense

5.4 Discusion

The interpretation of Starter and On-Field Models leads us to ask why there is a difference in quality of statistical significance. In our F-Statistic tables Starter Models appear to capture the performance of positions and teams better. Individual player features also seem to measure player performance better as show by a larger amount of significant variables. This leads us to believe that Starter Models have less noise in measurement then On-Field Models due to a higher consistency of players. On-field measurements are subject to players being subbed in and out of the game. While it provides greater detail in measurement it makes player slots have more variance in terms of which players are present where. For example the LB 2 of a team can be slotted into either LB slot 1 or 2 depending on the availability of the LB 1 in a On-Field play. However for a given game that LB 2 player will stay in the second slot for the entire game.

Quarterbacks have been undoubtedly held as the most important player on the field. Signs of joint significance are found across Starter, On-Field and Attempt models. On-Field models show clear significance while the Attempt model also shows signs of statistical significance.

For individual Quarterback Feature importance we find that the Quarterbacks performance on short passes is significant. Since this is held across all models it shows us that coaches are able to properly evaluate the performance of a quarterback in a fourth down situation. However, one difference is found with the On-Field deep passing grades. The negative significance suggests that quarterbacks that are better at deep passing

are less likely to be effective on a fourth down. Coaches are not picking up on this feature as there is no negative significance in the Attempt Models.

One big case of coaches misevaluating a player is found by how a Tight Ends pass blocking grades is consitantly significant across On-Field and Starter Models. However in our Attempts model we find no such significance.

Coaches are including wide receivers in the decision making process as seen by their joint significance in the Attempt Models. However, there is a struggle to find consistant significance in the individual models especially with the On-Field and Starter models.

What is the most interesting is that the Grades of the team's running back are not found to be significant in any model. This is the case even despite how fourth downs often are run plays due to the amount of short yardage situations.

In terms of the defense there is not enough evidence to make statements about individual player features' significance. However, when we test for joint significance of the defensive players there is signs of significance with the Defensive Line and Cornerbacks. Coaches then only produce weakly significant linear results with their attempt model for Cornerbacks. The decision to attempt a fourth down is seen to completely overlook the quality of a teams Starting linebacker core.

6   References

Cook, J. A. (2022). Sample-Selection-Adjusted Random Forests. International Journal of Data Science and Analytics, 14, 375-388. http://dx.doi.org/10.2139/ssrn.4225014

Das, M., Newey, W. K., & Vella, F. (2003). Nonparametric estimation of sample selection models. The Review of Economic Studies, 70(1), 33-58. https://doi.org/10.1111/1467-937X.00236

Gilovich, T., Vallone, R., & Tversky, A. (1985). The hot hand in basketball: On the misperception of random sequences. Cognitive Psychology, 17(3), 295-314. https://doi.org/10.1016/0010-0285(85)90010-6

Goff, B. L., & Locke, C. (2019). Revisiting Romer: Digging Deeper Into Influences on NFL Managerial Decisions. Journal of Sports Economics, 20(5), 673-694. https://doi.org/10.1177/1527002518798686

Heckman, J. J. (1979). Sample Selection Bias as a Specification Error. Econometrica, 47(1), 153-161. https://doi.org/10.2307/1912352

Klein, R. W., & Spady, R. H. (1993). An efficient semiparametric estimator for binary response models. Econometrica, 61(2), 387-421. https://doi.org/10.2307/2951556

Lehman, D. W., & Hahn, J. (2013). Momentum and Organizational Risk Taking: Evidence from the National Football League. Management Science, 59(4), 852-868. https://doi.org/10.1287/mnsc.1120.1574

Losak, J. M., Stenquist, R., & Lovett, M. (2023). Behavioral Biases in Daily Fantasy Baseball: The Case of the Hot Hand. Journal of Sports Economics, 24(3), 352-372. https://doi.org/10.1177/15270025221128955

Owens, M. F., & Roach, M. (2018). Decision-making on the hot seat and the short list: Evidence from college football fourth down decisions. Journal of Economic Behavior & Organization, 148, 226-245. https://doi.org/10.1016/j.jebo.2018.02.023

Roebber, P. J., Schultz, D. M., & Colle, B. A. (2022). On the existence of momentum in professional football. PLOS ONE, 17(6), e0269604. https://doi.org/10.1371/journal.pone.0269604

Romer, D. (2006). Do Firms Maximize? Evidence from Professional Football. Journal of Political Economy, 114(2), 340-365. https://doi.org/10.1086/501171

Yam, D., & Lopez, M. (2018). Quantifying the Causal Effects of Conservative Fourth Down Decision Making in the National Football League. Available at SSRN: https://ssrn.com/abstract=3114242 or http://dx.doi.org/10.2139/ssrn.3114242

Carl, S., Baldwin, B., Sharpe, L., Ho, T., Edwards, J. (2024). nflverse. Play-by-play data for NFL games. Retrieved from https://nflverse.nflverse.com/.

Pro Football Focus (PFF). (2024). NFL Player Performance Data. Accessed via subscription at https://premium.pff.com/nfl/teams/2024/REGPO.

Raymond, S. (2024). *4th Down Analysis App.* Interactive dashboard for analyzing 4th down decisions in the NFL. Available at: https://jzmtko-yigit-aydede.shinyapps.io/NFL_4th_Down_App/.

Sporting News. (2024). Lions' Dan Campbell criticized for fourth-down decisions in playoff loss to 49ers. Retrieved from https://www.sportingnews.com/us/nfl/news/lions-49ers-dan-campbell-fourth-down-decisions/b54ce7cc05c4d55fc7b46285.

Davis, M. C., & End, C. M. (2010). A winning proposition: The economic impact of successful National Football League franchises. *Economic Inquiry*, 48(1), 39–50. https://doi.org/10.1111/j.1465-7295.2008.00124.x

Birkett, D. (2024, January 21). On this date: Memorable kneecap speech. Sports Illustrated. Retrieved from https://www.si.com/nfl/lions/news/on-this-date-memorable-kneecap-speech