# Value Function Iteration Code Comparison

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# **Chapter 1**

# **Class Index**

# 1.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

absDiff < T >  (Functor to compute the absolute difference between elements of two vectors).	5
parameters (Object to store parameter values for VFI problem )	6
vfStep < T > (Functor to update the value function)	8

2 **Class Index** 

# **Chapter 2**

# **File Index**

# 2.1 File List

Here is a list of all documented files with brief descriptions:

ar1.cpp (File containing AR1 function for the VFI problem)	11
auxFuncs.h (Simple auxiliary functions )	13
functors.hpp (File of Thrust functors and functions )	15
global.h (Global header file )	18
kGrid.cpp (File containing function to create capital grid )	21
parameters.cpp (File containing parameters class method for loading VFI parameter values )	22
timer.cpp (File containing basic timer function )	23
vfInit.cpp (File containing function to initialize the value function)	24

4 File Index

# **Chapter 3**

# **Class Documentation**

# 3.1 absDiff< T > Struct Template Reference

Functor to compute the absolute difference between elements of two vectors.

```
#include <functors.hpp>
```

### **Public Member Functions**

• \_\_host\_\_ \_device\_\_ T operator() (const T &x, const T &y) const

template<typename T> struct absDiff< T>

#### 3.1.1 Member Function Documentation

3.1.1.1 template<typename  $T > \_host\_\_ \_device\_\_ T absDiff< T > ::operator() (const T & x, const T & y) const [inline]$ 

Kernel to compute the absolute difference between elements.

#### **Parameters:**

- x value of first vector element.
- y value of second vector element.

#### **Returns:**

absolute difference between elements.

The documentation for this struct was generated from the following file:

• functors.hpp

6 Class Documentation

# 3.2 parameters Class Reference

Object to store parameter values for VFI problem.

```
#include <global.h>
```

#### **Public Member Functions**

• void load (const char \*)

Function to load VFI parameter values to parameters object.

#### **Public Attributes**

• REAL eta

Coefficient of relative risk aversion.

• REAL beta

Time discount factor.

• REAL alpha

Share of capital in the production function.

• REAL delta

Rate of capital depreciation.

• REAL mu

TFP mean.

• REAL rho

TFP persistence.

• REAL sigma

TFP volatility.

• REAL lambda

Number of standard deviations for AR1 approximation.

• int nk

Number of values in capital grid.

• int nz

Number of values in TFP grid.

• REAL tol

Tolerance for convergence.

• char maxtype

Maximization method - choices are 'g' (grid) and 'b' (binary search).

• int howard

Number of howard steps to perform between maximizations - set howard = 1 if max = 'b'.

## 3.2.1 Member Function Documentation

## 3.2.1.1 void parameters::load (const char \* fileName)

This function is a parameters class method which loads parameter values from a text file for storage in the object. The input file must have 13 lines, each line beginning with a parameter value, followed by a comma and a character string describing the parameter. The order of the parameters must correspond to the order in the parameters class description.

#### **Parameters:**

← *fileName* Name of file storing parameter values.

#### **Returns:**

Void.

The documentation for this class was generated from the following files:

- global.h
- parameters.cpp

8 Class Documentation

# 3.3 vfStep< T > Struct Template Reference

Functor to update the value function.

```
#include <functors.hpp>
```

#### **Public Member Functions**

```
• vfStep (parameters _params, bool _howard, T *_K, T *_Z, T *_P, T *_V0, T *_V, T *_G) 
Constructor.
```

• \_\_host\_\_ \_device\_\_ void operator() (const int &hx) const

### **Public Attributes**

• const parameters params

Object containing parameters.

· const bool howard

Boolean for howard step.

• const T \* K

Pointer to capital grid.

• const T \* Z

Pointer to AR1 (TFP) grid.

• const T \* P

Pointer to transition matrix.

• const T \* **V**0

Pointer to current iteration of the value function.

• T \* V

Pointer to the updated value function.

• T \* G

Pointer to current iteration of the capital policy function.

## 3.3.1 Detailed Description

# $template {<} typename \ T{>} \ struct \ vfStep {<} \ T>$

This functor performs one iteration of the value function iteration algorithm, using V0 as the current value function and either maximizing the LHS of the Bellman if howard = false or using the concurrent policy function as the argmax if howard = true. Maximization is performed by either gridMax or binaryMax.

## 3.3.2 Member Function Documentation

Kernel to update the value function.

## **Parameters:**

hx index of V0 (stored as a flat array).

#### **Returns:**

Void.

The documentation for this struct was generated from the following file:

• functors.hpp

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# **Chapter 4**

# **File Documentation**

# 4.1 ar1.cpp File Reference

```
File containing AR1 function for the VFI problem. #include "global.h"
#include <math.h>
#include <thrust/device_vector.h>
```

#### **Functions**

• void ar1 (const parameters &param, thrust::device\_vector< REAL > &Z, thrust::device\_vector< REAL > &P)

Function to compute discrete AR1 approximation values and transition matrix.

## 4.1.1 Detailed Description

#### **Author:**

```
Eric M. Aldrich ealdrich@ucsc.edu
```

#### Version:

1.0

#### Date:

23 Oct 2012

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```
http://www.boost.org/LICENSE_1_0.txt)
```

## **4.1.2** Function Documentation

4.1.2.1 void ar1 (const parameters & param, thrust::device\_vector< REAL > & Z, thrust::device\_vector< REAL > & P)

This function that computes a discrete AR1 approximation and transition matrix using the method of Tauchen (1986).

#### **Parameters:**

- ← param Object of class parameters.
- $\rightarrow$  **Z** Grid of AR1 values.
- $\rightarrow$  **P** AR1 transition matrix values.

#### **Returns:**

## 4.2 auxFuncs.h File Reference

Simple auxiliary functions. #include <iostream>

```
#include <iomanip>
```

#### **Functions**

template < class T > void printMatrix (const bool colMaj, const int M, const int N, const thrust::device\_vector < T > &X, const int printRows, const int printCols, const int digits)

Function to print the elements of a matrix.

template < class T >
 void print Vector (const int N, const thrust::device\_vector < T > &X, const int digits)
 Function to print the elements of a vector.

## 4.2.1 Detailed Description

#### **Author:**

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Eric M. Aldrich ealdrich@ucsc.edu
```

#### Version:

1.0

#### Date:

18 July 2012

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```
http://www.boost.org/LICENSE_1_0.txt)
```

#### **4.2.2** Function Documentation

4.2.2.1 template < class T > void printMatrix (const bool colMaj, const int M, const int N, const thrust::device\_vector < T > & X, const int printRows, const int printCols, const int digits) [inline]

This functions prints a subset of the elements of a matrix to the screen.

#### **Parameters:**

- $\leftarrow$  *colMaj* Boolean indicating if the matrix is stored in column-major format.
- $\leftarrow M$  Number of rows in the data matrix.
- $\leftarrow N$  Number of columns in the data matrix.
- $\leftarrow X$  Array of matrix values.

- ← printRows Number of rows to print.
- $\leftarrow$  *printCols* Number of columns to print.
- ← *precision* Number of significant digits to print.

#### **Returns:**

Void.

# 4.2.2.2 template < class T > void printVector (const int N, const thrust::device\_vector < T > & X, const int digits) [inline]

This functions prints a subset of the elements of a vector to the screen.

#### **Parameters:**

- $\leftarrow N$  Number of elements in the data matrix.
- $\leftarrow X$  Array of vector values.
- ← precision Number of significant digits to print.

#### **Returns:**

# 4.3 functors.hpp File Reference

```
File of Thrust functors and functions. #include <thrust/iterator/zip_iterator.h>
#include <thrust/for_each.h>
#include <thrust/device_vector.h>
#include <cmath>
#include "global.h"
#include <stdio.h>
```

#### Classes

• struct vfStep< T >

Functor to update the value function.

• struct absDiff< T >

Functor to compute the absolute difference between elements of two vectors.

#### **Functions**

```
template < typename T > __host___device__ int binary Val (const T x, const int nx, const T *X)

Device function to find the location of a value in a monotonic grid.
template < typename T > __host___device__ void gridMax (const int klo, const int nksub, const int nk, const int nz, const T ydepK, const T eta, const T beta, const T *K, const T *P, const T *V0, T *V, T *G)

Device function to compute maximum of Bellman objective via grid search.
template < typename T > __host___device__ void binaryMax (const int klo, const int nksub, const int nk, const int nz, const T ydepK, const T eta, const T beta, const T *K, const T *P, const T *V0, T *V, T *G)

Device function to compute maximum of Bellman objective via binary search.
```

# Author:

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Eric M. Aldrich
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Version:
1.0

Date:
```

4.3.1 Detailed Description

12 July 2012

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```
http://www.boost.org/LICENSE_1_0.txt)
```

#### **4.3.2** Function Documentation

4.3.2.1 template < typename  $T > \_host\_\_device\_$  void binaryMax (const int klo, const int nksub, const int nk, const int nz, const T ydepK, const T eta, const T beta, const T \* K, const T \* P, const T \* V0, T \* V, T \* G) [inline]

This function finds the maximum and argmax of the Bellman objective over a specified subgrid of capital by using a binary search algorithm. The algorithm requires concavity and cannot be used with the howard improvement method.

#### **Parameters:**

- $\leftarrow$  *klo* Lower index of the capital grid to begin search.
- ← *nksub* Number of points in the capital grid to include in search.
- $\leftarrow nz$  Length of TFP grid.
- $\leftarrow$  *ydepK* value of output plus depreciated capital.
- ← eta Coefficient of relative risk aversion.
- $\leftarrow$  *beta* Time discount factor.
- $\leftarrow K$  Grid of capital values.
- $\leftarrow P$  TFP transition matrix.
- $\leftarrow$  *V0* Current value function.
- $\rightarrow V$  Updated value function.
- $\rightarrow$  **G** Updated policy function.

#### **Returns:**

Void.

# 4.3.2.2 template < typename T > \_\_host\_\_ \_device\_\_ int binary Val (const T x, const int nx, const T \* X) [inline]

This function finds the first value X[ix] such that  $x \le X[ix]$ , where x is a scalar value, X is a monotonic array, and ix is the index of X.

### **Parameters:**

- $\leftarrow x$  Value to search for in vector X.
- $\leftarrow nx$  Length of array X.
- $\leftarrow X$  Vector of data to search.

#### **Returns:**

imax Integer ix ( $\leq$  nx) such that x  $\leq$  X[ix].

4.3.2.3 template < typename  $T > \underline{\quad \text{host} \quad \quad \text{device} \quad }$  void gridMax (const int klo, const int nk, const int nz, const T ydepK, const T eta, const T beta, const T \* K, const T \* P, const T \* V0, T \* V, T \* G) [inline]

This function finds the maximum and argmax of the Bellman objective function by using a naive grid search: computing the utility at each value of the grid.

#### **Parameters:**

- ← klo Lower index of the capital grid to begin search.
- ← *nksub* Number of points in the capital grid to include in search.
- $\leftarrow$  *nz* Length of TFP grid.
- $\leftarrow$  *ydepK* value of output plus depreciated capital.
- ← eta Coefficient of relative risk aversion.
- $\leftarrow$  *beta* Time discount factor.
- $\leftarrow K$  Grid of capital values.
- $\leftarrow P$  TFP transition matrix.
- $\leftarrow V0$  Current value function.
- $\rightarrow V$  Updated value function.
- $\rightarrow$  **G** Updated policy function.

#### **Returns:**

# 4.4 global.h File Reference

Global header file. #include <thrust/device\_vector.h>

## Classes

class parameters

Object to store parameter values for VFI problem.

## **Typedefs**

• typedef double **REAL** 

## **Functions**

• double curr\_second (void)

\*\*Basic timer function.\*\*

• void ar1 (const parameters &param, thrust::device\_vector< REAL > &Z, thrust::device\_vector< REAL > &P)

Function to compute discrete AR1 approximation values and transition matrix.

void kGrid (const parameters &param, const thrust::device\_vector< REAL > &Z, thrust::device\_vector< REAL > &K)

Function to compute the values of an equally spaced capital grid.

void vfInit (const parameters &param, const thrust::device\_vector< REAL > &Z, thrust::device\_vector< REAL > &V)

Function to initialize value function.

## 4.4.1 Detailed Description

### **Author:**

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Eric M. Aldrich ealdrich@ucsc.edu
```

## Version:

1.0

#### Date:

23 Oct 2012

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```
http://www.boost.org/LICENSE_1_0.txt)
```

#### **4.4.2** Function Documentation

# 4.4.2.1 void ar1 (const parameters & param, thrust::device\_vector< REAL > & Z, thrust::device\_vector< REAL > & P)

This function that computes a discrete AR1 approximation and transition matrix using the method of Tauchen (1986).

#### **Parameters:**

- ← param Object of class parameters.
- $\rightarrow$  **Z** Grid of AR1 values.
- $\rightarrow$  **P** AR1 transition matrix values.

#### **Returns:**

Void.

#### 4.4.2.2 curr\_second (void)

#### **Returns:**

Double precision value representing time.

# 4.4.2.3 void kGrid (const parameters & param, const thrust::device\_vector< REAL > & Z, thrust::device\_vector< REAL > & K)

This function computes an equally spaced capital grid. The upper and lower bounds are the deterministic steady-state values of capital at the highest and lowest values of the TFP process (respectively), scaled by 0.95 and 1.05 (respectively).

#### **Parameters:**

- $\leftarrow$  *param* Object of class parameters.
- $\leftarrow$  **Z** Grid of TFP values.
- $\rightarrow$  **K** Grid of capital values.

### **Returns:**

Void.

# 4.4.2.4 void vfInit (const parameters & param, const thrust::device\_vector < REAL > & Z, thrust::device\_vector < REAL > & V)

This function initializes the value function at the deterministic steady state values for each level of TFP: conditional on a TFP level, the deterministic steady-state value of capital is computed, as well as the associated value function value.

#### **Parameters:**

← param Object of class parameters.

- $\leftarrow Z$  Grid of TFP values.
- $\rightarrow$  V Matrix of value function values.

## **Returns:**

# 4.5 kGrid.cpp File Reference

File containing function to create capital grid. #include "global.h"

```
#include <math.h>
#include <thrust/device_vector.h>
```

#### **Functions**

void kGrid (const parameters &param, const thrust::device\_vector< REAL > &Z, thrust::device\_vector< REAL > &K)

Function to compute the values of an equally spaced capital grid.

## 4.5.1 Detailed Description

#### **Author:**

```
Eric M. Aldrich ealdrich@ucsc.edu
```

#### Version:

1.0

#### Date:

23 Oct 2012

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```
http://www.boost.org/LICENSE_1_0.txt)
```

#### 4.5.2 Function Documentation

4.5.2.1 void kGrid (const parameters & param, const thrust::device\_vector< REAL > & Z, thrust::device\_vector< REAL > & K)

This function computes an equally spaced capital grid. The upper and lower bounds are the deterministic steady-state values of capital at the highest and lowest values of the TFP process (respectively), scaled by 0.95 and 1.05 (respectively).

#### **Parameters:**

- ← param Object of class parameters.
- $\leftarrow$  **Z** Grid of TFP values.
- $\rightarrow$  K Grid of capital values.

#### **Returns:**

# 4.6 parameters.cpp File Reference

File containing parameters class method for loading VFI parameter values. #include "global.h"

```
#include <stdlib.h>
#include <vector>
#include <fstream>
```

## **4.6.1** Detailed Description

#### **Author:**

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Eric M. Aldrich ealdrich@ucsc.edu
```

#### Version:

1.0

#### Date:

23 Oct 2012

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http://www.boost.org/LICENSE\_1\_0.txt)

# 4.7 timer.cpp File Reference

File containing basic timer function. #include <stddef.h>
#include <sys/time.h>

## **Functions**

• double curr\_second (void)

\*\*Basic timer function.

## 4.7.1 Detailed Description

## **Author:**

Kyle Spafford

#### Date:

19 November 2010

Public domain.

## 4.7.2 Function Documentation

## 4.7.2.1 double curr\_second (void)

#### **Returns:**

Double precision value representing time.

# 4.8 vfInit.cpp File Reference

File containing function to initialize the value function. #include "global.h"

```
#include <math.h>
#include <thrust/device_vector.h>
```

#### **Functions**

void vfInit (const parameters &param, const thrust::device\_vector< REAL > &Z, thrust::device\_vector< REAL > &V)

Function to initialize value function.

## 4.8.1 Detailed Description

#### **Author:**

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Eric M. Aldrich ealdrich@ucsc.edu
```

#### Version:

1.0

#### Date:

23 Oct 2012

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```
http://www.boost.org/LICENSE_1_0.txt)
```

## 4.8.2 Function Documentation

# 4.8.2.1 void vfInit (const parameters & param, const thrust::device\_vector< REAL > & Z, thrust::device\_vector< REAL > & V)

This function initializes the value function at the deterministic steady state values for each level of TFP: conditional on a TFP level, the deterministic steady-state value of capital is computed, as well as the associated value function value.

#### **Parameters:**

- ← param Object of class parameters.
- $\leftarrow$  **Z** Grid of TFP values.
- $\rightarrow V$  Matrix of value function values.

#### **Returns:**