# VFI

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# **Chapter 1**

# **Class Index**

# 1.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

| abs_diff< T >  |   |
|--|---|
| Functor to compute the absolute difference between elements of two vectors | Ę |
| ar1Vals< T >   |   |
| Functor to compute discrete AR1 approximation                              | 6 |
| kGrid < T >  |   |
| Functor to compute grid values for capital                                 | 7 |
| transMat< T >  |   |
| Functor to compute transition matrix for discrete AR1 approximation        | 8 |
| vfInit< T >  |   |
| Functor to initialize the value function                                   | ç |
| vfStep< T >  |   |
| Functor to update the value function                                       | ( |

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# **Chapter 2**

# File Index

# 2.1 File List

Here is a list of all documented files with brief descriptions:

| auxFuncs.h  |
|---|
| Simple auxiliary functions                                |
| functors.hpp  |
| File of Thrust functors and functions                     |
| global.cpp  |
| Global variables for the value function iteration problem |
| global.h  |
| Global header file  |
| main.cu   |
| File containing main main function for the VFI problem    |
| timer.cpp   |
| File containing timer function                            |

File Index

# **Chapter 3**

# **Class Documentation**

# 3.1 abs\_diff < T > Struct Template Reference

Functor to compute the absolute difference between elements of two vectors.

```
#include <functors.hpp>
```

### **Public Member Functions**

```
    __host__ _device__ T operator() (const T &x, const T &y) const
```

### 3.1.1 Detailed Description

template<typename T>struct abs\_diff< T>

Functor to compute the absolute difference between elements of two vectors.

### 3.1.2 Member Function Documentation

Kernel to compute the absolute difference between elements.

### **Parameters**

| X | value of first vector element.  |
|---|---------------------------------|
| У | value of second vector element. |

### Returns

absolute difference between elements.

The documentation for this struct was generated from the following file:

6 Class Documentation

# 3.2 ar1Vals < T > Struct Template Reference

Functor to compute discrete AR1 approximation.

```
#include <functors.hpp>
```

### **Public Member Functions**

```
    ar1Vals (int _nz, T _lambda, T _mu, T _sigma, T _rho)
    Constructor.
```

\_\_host\_\_ \_\_device\_\_ T operator() (const int &ix) const

### **Public Attributes**

· const int nz

Number of values in AR1 grid.

const T lambda

Number of standard deviations for AR1 approximation.

· const T mu

AR1 mean.

· const T sigma

AR1 standard deviation.

· const T rho

AR1 persistence.

### 3.2.1 Detailed Description

template<typename T>struct ar1Vals< T>

Functor to compute discrete AR1 approximation.

This functor provides the kernel to compute a discrete AR1 approximation using the method of Tauchen (1986).

### 3.2.2 Member Function Documentation

```
3.2.2.1 template<typename T > _host__ _device__ T ar1Vals< T >::operator() ( const int & ix ) const [inline]
```

Kernel to compute discrete AR1 approximation (using Tauchen's method).

### **Parameters**

```
ix index of the AR1 grid.
```

### **Returns**

Value of the AR1 process at position ix in the grid.

The documentation for this struct was generated from the following file:

# 3.3 kGrid < T > Struct Template Reference

Functor to compute grid values for capital.

```
#include <functors.hpp>
```

### **Public Member Functions**

- kGrid (int \_nk, int \_nz, T \_beta, T \_alpha, T \_delta, T \*\_Z)
   Constructor.
- \_\_host\_\_ \_\_device\_\_ T operator() (const int &ix) const

### **Public Attributes**

· const int nk

Number of values in capital grid.

· const int nz

Number of values in AR1 (TFP) grid.

· const T beta

Time discount factor.

· const T alpha

Capital share in production function.

· const T delta

Depreciation rate.

const T \* Z

Pointer to AR1 (TFP) grid.

## 3.3.1 Detailed Description

template<typename T>struct kGrid<T>

Functor to compute grid values for capital.

This functor provides the kernel to compute an equally spaced grid for capital.

### 3.3.2 Member Function Documentation

3.3.2.1 template<typename T > \_\_host\_\_ \_\_device\_\_ T kGrid < T >::operator() ( const int & ix ) const [inline]

Kernel to compute each K value in grid.

### **Parameters**

| ix index of the A | AR1 grid. |
|-------------------|-----------|
|-------------------|-----------|

### Returns

Value of capital at position ix in the grid.

The documentation for this struct was generated from the following file:

8 Class Documentation

# 3.4 transMat < T > Struct Template Reference

Functor to compute transition matrix for discrete AR1 approximation.

```
#include <functors.hpp>
```

### **Public Member Functions**

```
    transMat (int _nz, T _mu, T _sigma, T _rho, T *_Z, T *_P)
    Constructor.
```

\_\_host\_\_ \_device\_\_ void operator() (const int &ix) const

### **Public Attributes**

· const int nz

Number of values in AR1 grid.

· const T mu

AR1 mean.

· const T sigma

AR1 standard deviation.

const T rho

AR1 persistence.

• T \* Z

Pointer to AR1 grid.

T \* P

Pointer to transition matrix.

## 3.4.1 Detailed Description

template < typename T> struct transMat< T>

Functor to compute transition matrix for discrete AR1 approximation.

This functor provides the kernel to compute the transition matrix for a a discrete AR1 approximation using the method of Tauchen (1986).

### 3.4.2 Member Function Documentation

3.4.2.1 template<typename T > \_\_host\_\_ \_\_device\_\_ void transMat< T >::operator() ( const int & ix ) const [inline]

Kernel to compute transition matrix for discrete AR1 approximation (using Tauchen's method).

### **Parameters**

| ix | index of the AR1 grid. |  |
|----|------------------------|--|

### Returns

Void.

The documentation for this struct was generated from the following file:

## 3.5 vflnit < T > Struct Template Reference

Functor to initialize the value function.

```
#include <functors.hpp>
```

### **Public Member Functions**

```
    vflnit (int _nk, T _eta, T _beta, T _alpha, T _delta, T *_Z, T *_V)

Constructor
```

• \_\_host\_\_ \_device\_\_ void operator() (const int &jx) const

### **Public Attributes**

· const int nk

Number of values in capital grid.

· const T eta

Coefficient of relative risk aversion.

· const T beta

Time discount factor.

· const T alpha

Capital share in production function.

· const T delta

Depreciation rate.

const T \* Z

Pointer to AR1 (TFP) grid.

T \* V

Pointer to current iteration of the value function.

### 3.5.1 Detailed Description

template<typename T>struct vfInit< T>

Functor to initialize the value function.

This functor intializes the value function at the deterministic steady state, for each value of the AR1 (TFP) grid.

### 3.5.2 Member Function Documentation

```
3.5.2.1 template<typename T > __host__ __device__ void vflnit< T >::operator() ( const int & jx ) const [inline]
```

Kernel to initialize value function.

### **Parameters**

| jx | index of the AR1 (TFP) grid. |
|----|------------------------------|

Returns

Void.

The documentation for this struct was generated from the following file:

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## 3.6 vfStep < T > Struct Template Reference

Functor to update the value function.

```
#include <functors.hpp>
```

### **Public Member Functions**

```
    vfStep (int _nk, int _nz, T _eta, T _beta, T _alpha, T _delta, char _maxtype, bool _howard, T *_K, T *_Z, T *_P, T *_V0, T *_V, T *_G)
        Constructor.
    __host__ _device__ void operator() (const int &hx) const
```

### **Public Attributes**

· const int nk

Number of values in capital grid.

· const int nz

Number of values in AR1 (TFP) grid.

· const T eta

Coefficient of relative risk aversion.

· const T beta

Time discount factor.

· const T alpha

Capital share in production function.

const T delta

Depreciation rate.

const char maxtype

Flag to indicate maximization method.

const bool howard

Flag to indicate use of Howard improvement.

• const T \* K

Pointer to capital grid.

const T \* Z

Pointer to AR1 (TFP) grid.

const T \* P

Pointer to transition matrix.

• const T \* V0

Pointer to current iteration of the value function.

• T \* V

Pointer to the updated value function.

T \* G

Pointer to current iteration of the capital policy function.

### 3.6.1 Detailed Description

```
template<typename T>struct vfStep< T>
```

Functor to update the value function.

This functor updates the value function. If howard is FALSE, the value and capital policy functions are updated by maximizing the Belman objective function using the current value function. Maximization is either performed by binary\_max or grid\_max. If howard is TRUE, the value function is updated without maximization, by simply iterating the Belman with the current capital policy function.

## 3.6.2 Member Function Documentation

3.6.2.1 template < typename T > \_\_host\_\_ \_\_device\_\_ void vfStep < T >::operator() ( const int & hx ) const [inline]

Kernel to update the value function.

### **Parameters**

hx index of V0 (stored as a flat array).

### Returns

Void.

The documentation for this struct was generated from the following file:

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# **Chapter 4**

# **File Documentation**

# 4.1 auxFuncs.h File Reference

Simple auxiliary functions.

```
#include <iostream>
#include <iomanip>
```

### **Functions**

template<class T >
 void printMatrix (const bool colMaj, const int M, const int N, T \*X, const int printRows, const int printCols, const int digits)

Function to print the elements of a matrix.

Function to print the elements of a vector.

### 4.1.1 Detailed Description

Simple auxiliary functions.

Author

Eric M. Aldrich

ealdrich@ucsc.edu

Version

1.0

Date

18 July 2012

### Copyright

```
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```

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### 4.1.2 Function Documentation

4.1.2.1 template < class T > void printMatrix ( const bool *colMaj*, const int *M*, const int *N*, T \* X, const int *printRows*, const int *printCols*, const int *digits* )

Function to print the elements of a matrix.

This functions prints a subset of the elements of a matrix to the screen.

### **Parameters**

| colMaj    | boolean indicating if the matrix is stored in column-major format. |
|-----------|--|
| М         | number of rows in the data matrix.                                 |
| N         | number of columns in the data matrix.                              |
| X         | pointer to data matrix.  |
| printRows | number of rows to print.   |
| printCols | number of columns to print.  |
| precision | number of significant digits to print.                             |

### Returns

Void.

4.1.2.2 template < class T > void printVector ( const int N, T \* X, const int digits )

Function to print the elements of a vector.

This functions prints a subset of the elements of a vector to the screen.

### **Parameters**

| N         | number of elements in the data matrix. |
|-----------|--|
| X         | pointer to data matrix.                |
| precision | number of significant digits to print. |

### Returns

Void.

# 4.2 functors.hpp File Reference

File of Thrust functors and functions.

```
#include <thrust/iterator/zip_iterator.h>
#include <thrust/for_each.h>
#include <thrust/device_vector.h>
#include <cmath>
```

### **Classes**

struct ar1Vals

Functor to compute discrete AR1 approximation.

struct transMat< T >

Functor to compute transition matrix for discrete AR1 approximation.

struct kGrid< T >

Functor to compute grid values for capital.

struct vflnit< T >

Functor to initialize the value function.

struct vfStep< T >

Functor to update the value function.

struct abs diff< T >

Functor to compute the absolute difference between elements of two vectors.

### **Functions**

```
    template < typename T >
        __host____device__ int binary_val (const T x, const int n, const T *X)
        Function to find the location of a value in a monotonic grid.
    template < typename T >
        __host____device__ void grid_max (const int klo, const int nksub, const int nk, const int nz, const T ydepK, const T eta, const T beta, const T *K, const T *P, const T *V0, T *V, T *G)
        Function to maximize Belman objective function with naive grid search.
    template < typename T >
        __host____device__ void binary_max (const int klo, const int nksub, const int nk, const int nz, const T ydepK, const T eta, const T beta, const T *K, const T *P, const T *V0, T *V, T *G)
```

Function to maximize Belman objective function with binary search.

### 4.2.1 Detailed Description

File of Thrust functors and functions.

Author

```
Eric M. Aldrich
ealdrich@ucsc.edu
```

Version

1.0

Date

12 July 2012

### Copyright

```
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```

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### 4.2.2 Function Documentation

4.2.2.1 template < typename T > \_\_host\_\_ \_\_device\_\_ void binary\_max ( const int klo, const int nksub, const int nk, const int nk, const T ydepK, const T eta, const T eta,

Function to maximize Belman objective function with binary search.

This function computes the maximum of the Belman objective function for a given pair of state values by using a binary search algorithm, as outlined in Heer and Maussner (2005, p.26).

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### **Parameters**

| klo         | lower index of the capital grid to begin search.           |
|-------------|--|
| nksub       | number of points in the capital grid to include in search. |
| nk          | number of points in the capital grid.                      |
| nz          | number of points in the AR1 (TFP) grid.                    |
| ydepK       | value of output plus depreciated capital.                  |
| eta         | coefficient of relative risk aversion.                     |
| beta        | time discount factor.                                      |
| * <i>K</i>  | pointer to capital grid.                                   |
| * <i>P</i>  | pointer to AR1 (TFP) transition matrix.                    |
| * <i>V0</i> | pointer to current iterate of value function.              |
| * <i>V</i>  | pointer to updated value function.                         |
| *G          | pointer to updated capital policy function.                |

### Returns

Void.

4.2.2.2 template < typename  $T > \_$ host $\_\_$ device $\_$  int binary $\_$ val (const T x, const int n, const T \* X)

Function to find the location of a value in a monotonic grid.

This function finds the first value X[ix] such that X[ix] >= x, where x is a scalar value, X is a monotonic grid, and ix is the index of X.

### **Parameters**

| X  | value to search for in grid X. |
|----|--------------------------------|
| n  | number of values in grid X.    |
| *X | pointer to grid X.             |

### Returns

imax first integer ( $\leq$  n) such that X[ix] >= x.

4.2.2.3 template<typename T > \_host\_ \_device\_ void grid\_max ( const int klo, const int nksub, const int nk, const int nk, const T ydepK, const T eta, const T

Function to maximize Belman objective function with naive grid search.

This function computes the maximum of the Belman objective function for a given pair of state values by searching over each possible value of future capital in the grid for capital.

### **Parameters**

| klo         | lower index of the capital grid to begin search.           |
|-------------|--|
| nksub       | number of points in the capital grid to include in search. |
| nk          | number of points in the capital grid.                      |
| nz          | number of points in the AR1 (TFP) grid.                    |
| ydepK       | value of output plus depreciated capital.                  |
| eta         | coefficient of relative risk aversion.                     |
| beta        | time discount factor.                                      |
| *K          | Fr. 11 11 11 3 1   |
| * <i>P</i>  | pointer to AR1 (TFP) transition matrix.                    |
| * <i>V0</i> | pointer to current iterate of value function.              |
| * <i>V</i>  | pointer to updated value function.                         |
| *G          | pointer to updated capital policy function.                |

Returns

Void.

# 4.3 global.cpp File Reference

Global variables for the value function iteration problem.

```
#include "global.h"
```

### **Variables**

• const REAL eta = 2

Coefficient of relative risk aversion.

• const REAL beta = 0.984

Time discount factor.

• const REAL alpha = 0.35

Share of capital in the production function.

• const REAL delta = 0.01

Rate of capital depreciation.

• const REAL mu = 0.0

TFP mean.

• const REAL rho = 0.95

TFP persistence.

• const REAL sigma = 0.005

TFP volatility.

const int nk = 1024

Number of values in capital grid.

• const int nz = 4

Number of values TFP grid.

• const REAL tol = 1e-8\*(1-beta)

Tolerance for convergence.

• const char maxtype = 'b'

Maximization method - choices are 'g' (grid) and 'b' (binary search).

• const int howard = 1

Number of howard steps to perform between.

### 4.3.1 Detailed Description

Global variables for the value function iteration problem.

Author

```
Eric M. Aldrich
```

```
ealdrich@ucsc.edu
```

Version

1.0

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Date

12 July 2012

### Copyright

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# 4.4 global.h File Reference

Global header file.

## **Typedefs**

• typedef double REAL

### **Functions**

• REAL curr\_second (void)

Basic timer method.

### **Variables**

· const REAL eta

Coefficient of relative risk aversion.

· const REAL beta

Time discount factor.

· const REAL alpha

Share of capital in the production function.

const REAL delta

Rate of capital depreciation.

const REAL mu

TFP mean.

· const REAL rho

TFP persistence.

• const REAL sigma

TFP volatility.

const int nk

Number of values in capital grid.

· const int nz

Number of values TFP grid.

• const REAL tol

Tolerance for convergence.

const char maxtype

Maximization method - choices are 'g' (grid) and 'b' (binary search).

· const int howard

Number of howard steps to perform between.

4.5 main.cu File Reference 19

### 4.4.1 Detailed Description

Global header file.

### 4.4.2 Function Documentation

```
4.4.2.1 REAL curr_second (void)
```

Basic timer method.

Author

Kyle Spafford

Version

1.0

Date

19 November 2010

### Copyright

```
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```

### 4.5 main.cu File Reference

File containing main main function for the VFI problem.

```
#include "global.h"
#include "auxFuncs.h"
#include <iostream>
#include <ctime>
#include "functors.hpp"
#include <thrust/host_vector.h>
#include <thrust/transform.h>
#include <thrust/for_each.h>
#include <thrust/sequence.h>
#include <thrust/sort.h>
```

### **Functions**

• int main ()

Main function for the VFI problem.

## 4.5.1 Detailed Description

File containing main main function for the VFI problem.

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### 4.5.2 Function Documentation

```
4.5.2.1 main ( )
```

Main function for the VFI problem.

This function solves a standard neoclassical growth model with value function iteration, using Thrust. Parallelization occurs at the grid of values for the state space, with each thread finding the maximum of the Bellman objective function for a pair of state values.

```
See Aldrich et al. (2011).
```

## 4.6 timer.cpp File Reference

File containing timer function.

```
#include <stddef.h>
#include <sys/time.h>
#include "global.h"
```

### **Functions**

• REAL curr\_second (void)

Basic timer method.

### 4.6.1 Detailed Description

File containing timer function.

### 4.6.2 Function Documentation

```
4.6.2.1 REAL curr_second ( void )
```

Basic timer method.

Author

Kyle Spafford

Version

1.0

Date

19 November 2010

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# **Bibliography**

Aldrich, E. M., Fernández-Villaverde, J., Gallant, A. R., and Rubio-Ramírez, J. F. (2011), "Tapping the supercomputer under your desk: Solving dynamic equilibrium models with graphics processors," *Journal of Economic Dynamics and Control*, 35, 386–393.