

ValueFunctionIterationCodeComparison

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Chapter 1

Class Index

1.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

[parameters](#) (Object to store parameter values for VFI problem) 5

Chapter 2

File Index

2.1 File List

Here is a list of all documented files with brief descriptions:

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Chapter 3

Class Documentation

3.1 parameters Class Reference

Object to store parameter values for VFI problem.

```
#include <global.h>
```

Public Member Functions

- void [load](#) (const char *)

Function to load VFI parameter values to [parameters](#) object.

Public Attributes

- REAL [eta](#)

Coefficient of relative risk aversion.

- REAL [beta](#)

Time discount factor.

- REAL [alpha](#)

Share of capital in the production function.

- REAL [delta](#)

Rate of capital depreciation.

- REAL [mu](#)

TFP mean.

- REAL [rho](#)

TFP persistence.

- REAL [sigma](#)

TFP volatility.

- REAL [lambda](#)
Number of standard deviations for ARI approximation.
- int [nk](#)
Number of values in capital grid.
- int [nz](#)
Number of values in TFP grid.
- REAL [tol](#)
Tolerance for convergence.
- char [maxtype](#)
Maximization method - choices are 'g' (grid) and 'b' (binary search).
- int [howard](#)
Number of howard steps to perform between maximizations - set howard = 1 if max = 'b'.

3.1.1 Member Function Documentation

3.1.1.1 void [parameters::load](#) (const char **fileName*)

This function is a [parameters](#) class method which loads parameter values from a text file for storage in the object. The input file must have 13 lines, each line beginning with a parameter value, followed by a comma and a character string describing the parameter. The order of the [parameters](#) must correspond to the order in the [parameters](#) class description.

Parameters:

← *fileName* Name of file storing parameter values.

Returns:

Void.

The documentation for this class was generated from the following files:

- [global.h](#)
- [parameters.cpp](#)

Chapter 4

File Documentation

4.1 ar1.cpp File Reference

File containing AR1 function for the VFI problem. `#include "global.h"`

`#include <math.h>`

`#include <Eigen/Dense>`

Functions

- void [ar1](#) (const [parameters](#) ¶m, VectorXR &Z, MatrixXR &P)

Function to compute discrete AR1 approximation values and transition matrix.

4.1.1 Detailed Description

Author:

Eric M. Aldrich
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Version:

1.0

Date:

23 Oct 2012

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http://www.boost.org/LICENSE_1_0.txt)

4.1.2 Function Documentation

4.1.2.1 void ar1 (const parameters & *param*, VectorXR & *Z*, MatrixXR & *P*)

This function that computes a discrete AR1 approximation and transition matrix using the method of Tauchen (1986).

Parameters:

- ← *param* Object of class [parameters](#).
- *Z* Grid of AR1 values.
- *P* AR1 transition matrix values.

Returns:

Void.

4.2 binaryMax.cpp File Reference

File containing binary search maximization function. `#include "global.h"`

`#include <Eigen/Dense>`

`#include <math.h>`

Functions

- void `binaryMax` (const int &klo, const int &nksub, const REAL &ydepK, const REAL eta, const REAL beta, const VectorXR &K, const VectorXR &Exp, REAL &V, int &G)

Function to compute maximum of Bellman objective via binary search.

4.2.1 Detailed Description

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23 Oct 2012

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http://www.boost.org/LICENSE_1_0.txt)

4.2.2 Function Documentation

4.2.2.1 void `binaryMax` (const int &klo, const int &nksub, const REAL &ydepK, const REAL eta, const REAL beta, const VectorXR &K, const VectorXR &Exp, REAL &V, int &G)

This function finds the maximum and argmax of the Bellman objective over a specified subgrid of capital by using a binary search algorithm. The algorithm requires concavity and cannot be used with the howard improvement method.

Parameters:

- ← *klo* Lower index of the capital grid to begin search.
- ← *nksub* Number of points in the capital grid to include in search.
- ← *ydepK* value of output plus depreciated capital.
- ← *eta* Coefficient of relative risk aversion.
- ← *beta* Time discount factor.
- ← *K* Grid of capital values.

- ← *Exp* Expected value function continuation values.
- *V* Updated value function.
- *G* Updated policy function.

Returns:

Void.

4.3 binaryVal.cpp File Reference

File containing a function which finds the approximate location of a value in a vector with monotonically increasing values. `#include "global.h"`

Functions

- `int binaryVal (const REAL &x, const VectorXR &X)`
Function to find the location of a value in a monotonic grid.

4.3.1 Detailed Description

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Version:

1.0

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23 Oct 2012

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http://www.boost.org/LICENSE_1_0.txt)

4.3.2 Function Documentation

4.3.2.1 `int binaryVal (const REAL &x, const VectorXR &X)`

This function finds the first value $X[ix]$ such that $x \leq X[ix]$, where x is a scalar value, X is a monotonic array, and ix is the index of X .

Parameters:

- ← x Value to search for in vector X .
- ← nx Length of array X .
- ← X Vector of data to search.

Returns:

$imax$ Integer ix ($\leq nx$) such that $x \leq X[ix]$.

4.4 global.h File Reference

Global header file. `#include <Eigen/Dense>`

Classes

- class [parameters](#)
Object to store parameter values for VFI problem.

Typedefs

- typedef double **REAL**
- typedef Eigen::Matrix< REAL, Eigen::Dynamic, 1 > **VectorXR**
- typedef Eigen::Matrix< REAL, 1, Eigen::Dynamic > **RowVectorXR**
- typedef Eigen::Matrix< REAL, Eigen::Dynamic, Eigen::Dynamic > **MatrixXR**
- typedef Eigen::Array< REAL, Eigen::Dynamic, 1 > **ArrayXR**
- typedef Eigen::Array< REAL, Eigen::Dynamic, Eigen::Dynamic > **ArrayXXR**

Functions

- double [curr_second](#) (void)
Basic timer function.
- void [ar1](#) (const [parameters](#) ¶m, VectorXR &Z, MatrixXR &P)
Function to compute discrete AR1 approximation values and transition matrix.
- void [kGrid](#) (const [parameters](#) ¶m, const VectorXR &Z, VectorXR &K)
Function to compute the values of an equally spaced capital grid.
- void [vfInit](#) (const [parameters](#) ¶m, const VectorXR &Z, MatrixXR &V)
Function to initialize value function.
- void [vfStep](#) (const [parameters](#) ¶m, const bool &howard, const VectorXR &K, const VectorXR &Z, const MatrixXR &P, const MatrixXR &V0, MatrixXR &V, MatrixXi &G)
Function to update value function.
- int [binaryVal](#) (const REAL &x, const VectorXR &X)
Function to find the location of a value in a monotonic grid.
- void [gridMax](#) (const int &klo, const int &nksub, const REAL &ydepK, const REAL eta, const REAL beta, const VectorXR &K, const VectorXR &Exp, REAL &V, int &G)
Function to compute maximum of Bellman objective via grid search.
- void [binaryMax](#) (const int &klo, const int &nksub, const REAL &ydepK, const REAL eta, const REAL beta, const VectorXR &K, const VectorXR &Exp, REAL &V, int &G)
Function to compute maximum of Bellman objective via binary search.

4.4.1 Detailed Description

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http://www.boost.org/LICENSE_1_0.txt)

4.4.2 Function Documentation

4.4.2.1 void ar1 (const parameters & *param*, VectorXR & *Z*, MatrixXR & *P*)

This function that computes a discrete AR1 approximation and transition matrix using the method of Tauchen (1986).

Parameters:

- ← *param* Object of class [parameters](#).
- *Z* Grid of AR1 values.
- *P* AR1 transition matrix values.

Returns:

Void.

4.4.2.2 void binaryMax (const int & *klo*, const int & *nksub*, const REAL & *ydepK*, const REAL *eta*, const REAL *beta*, const VectorXR & *K*, const VectorXR & *Exp*, REAL & *V*, int & *G*)

This function finds the maximum and argmax of the Bellman objective over a specified subgrid of capital by using a binary search algorithm. The algorithm requires concavity and cannot be used with the howard improvement method.

Parameters:

- ← *klo* Lower index of the capital grid to begin search.
- ← *nksub* Number of points in the capital grid to include in search.
- ← *ydepK* value of output plus depreciated capital.
- ← *eta* Coefficient of relative risk aversion.
- ← *beta* Time discount factor.

- ← ***K*** Grid of capital values.
- ← ***Exp*** Expected value function continuation values.
- ***V*** Updated value function.
- ***G*** Updated policy function.

Returns:

Void.

4.4.2.3 int binaryVal (const REAL & x, const VectorXR & X)

This function finds the first value $X[ix]$ such that $x \leq X[ix]$, where x is a scalar value, X is a monotonic array, and ix is the index of X .

Parameters:

- ← ***x*** Value to search for in vector X .
- ← ***nx*** Length of array X .
- ← ***X*** Vector of data to search.

Returns:

imax Integer ix ($\leq nx$) such that $x \leq X[ix]$.

4.4.2.4 curr_second (void)**Returns:**

Double precision value representing time.

4.4.2.5 void gridMax (const int & klo, const int & nksub, const REAL & ydepK, const REAL eta, const REAL beta, const VectorXR & K, const VectorXR & Exp, REAL & V, int & G)

This function finds the maximum and argmax of the Bellman objective function by using a naive grid search: computing the utility at each value of the grid.

Parameters:

- ← ***klo*** Lower index of the capital grid to begin search.
- ← ***nksub*** Number of points in the capital grid to include in search.
- ← ***ydepK*** value of output plus depreciated capital.
- ← ***eta*** Coefficient of relative risk aversion.
- ← ***beta*** Time discount factor.
- ← ***K*** Grid of capital values.
- ← ***Exp*** Expected value function continuation values.
- ***V*** Updated value function.
- ***G*** Updated policy function.

Returns:

Void.

4.4.2.6 void kGrid (const parameters & *param*, const VectorXR & *Z*, VectorXR & *K*)

This function computes an equally spaced capital grid. The upper and lower bounds are the deterministic steady-state values of capital at the highest and lowest values of the TFP process (respectively), scaled by 0.95 and 1.05 (respectively).

Parameters:

- ← *param* Object of class [parameters](#).
- ← *Z* Grid of TFP values.
- *K* Grid of capital values.

Returns:

Void.

4.4.2.7 void vfInit (const parameters & *param*, const VectorXR & *Z*, MatrixXR & *V*)

This function initializes the value function at the deterministic steady state values for each level of TFP: conditional on a TFP level, the deterministic steady-state value of capital is computed, as well as the associated value function value.

Parameters:

- ← *param* Object of class [parameters](#).
- ← *Z* Grid of TFP values.
- *V* Matrix of value function values.

Returns:

Void.

4.4.2.8 void vfStep (const parameters & *param*, const bool & *howard*, const VectorXR & *K*, const VectorXR & *Z*, const MatrixXR & *P*, const MatrixXR & *V0*, MatrixXR & *V*, MatrixXi & *G*)

This function performs one iteration of the value function iteration algorithm, using *V0* as the current value function and either maximizing the LHS of the Bellman if *howard* = false or using the concurrent policy function as the argmax if *howard* = true. Maximization is performed by either [gridMax](#) or [binaryMax](#).

Parameters:

- ← *param* Object of class [parameters](#).
- ← *howard* Indicates if the current iteration of the value function will perform a maximization (false) or if it will simply compute the new value function using the concurrent policy function (true).
- ← *K* Grid of capital values.
- ← *Z* Grid of TFP values.
- ← *P* TFP transition matrix.
- ← *V0* Matrix storing current value function.
- *V* Matrix storing updated value function.

↔ **G** Matrix storing policy function (updated if howard = false).

Returns:

Void.

4.5 gridMax.cpp File Reference

File containing grid search maximization function. `#include "global.h"`

```
#include <Eigen/Dense>
```

```
#include <math.h>
```

```
#include <iostream>
```

Functions

- void `gridMax` (const int &klo, const int &nksub, const REAL &ydepK, const REAL eta, const REAL beta, const VectorXR &K, const VectorXR &Exp, REAL &V, int &G)

Function to compute maximum of Bellman objective via grid search.

4.5.1 Detailed Description

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1.0

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23 Oct 2012

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http://www.boost.org/LICENSE_1_0.txt)

4.5.2 Function Documentation

4.5.2.1 void `gridMax` (const int &klo, const int &nksub, const REAL &ydepK, const REAL eta, const REAL beta, const VectorXR &K, const VectorXR &Exp, REAL &V, int &G)

This function finds the maximum and argmax of the Bellman objective function by using a naive grid search: computing the utility at each value of the grid.

Parameters:

- ← **klo** Lower index of the capital grid to begin search.
- ← **nksub** Number of points in the capital grid to include in search.
- ← **ydepK** value of output plus depreciated capital.
- ← **eta** Coefficient of relative risk aversion.
- ← **beta** Time discount factor.

- ← ***K*** Grid of capital values.
- ← ***Exp*** Expected value function continuation values.
- ***V*** Updated value function.
- ***G*** Updated policy function.

Returns:

Void.

4.6 kGrid.cpp File Reference

File containing function to create capital grid. `#include "global.h"`

`#include <math.h>`

`#include <Eigen/Dense>`

Functions

- void `kGrid` (const `parameters` ¶m, const VectorXR &Z, VectorXR &K)

Function to compute the values of an equally spaced capital grid.

4.6.1 Detailed Description

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Eric M. Aldrich
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Version:

1.0

Date:

23 Oct 2012

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http://www.boost.org/LICENSE_1_0.txt)

4.6.2 Function Documentation

4.6.2.1 void kGrid (const parameters ¶m, const VectorXR & Z, VectorXR & K)

This function computes an equally spaced capital grid. The upper and lower bounds are the deterministic steady-state values of capital at the highest and lowest values of the TFP process (respectively), scaled by 0.95 and 1.05 (respectively).

Parameters:

← *param* Object of class `parameters`.

← *Z* Grid of TFP values.

→ *K* Grid of capital values.

Returns:

Void.

4.7 main.cpp File Reference

File containing main function for the VFI problem. `#include "global.h"`

```
#include <math.h>
#include <ctime>
#include <typeinfo>
#include <Eigen/Dense>
#include <iostream>
#include <fstream>
```

Functions

- `int main()`
Main function for the VFI problem.

4.7.1 Detailed Description

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Version:

1.0

Date:

23 Oct 2012

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http://www.boost.org/LICENSE_1_0.txt)

4.7.2 Function Documentation

4.7.2.1 `main()`

This function solves a standard neoclassical growth model with value function iteration on a CPU.

See Aldrich, Eric M., Jesus Fernandez-Villaverde, A. Ronald Gallant and Juan F. Rubio-Ramirez (2011), Tapping the supercomputer under your desk: Solving dynamic equilibrium models with graphics processors, *Journal of Economic Dynamics & Control*, 35, 386-393.

Returns:

0 upon successful completion, 1 otherwise.

4.8 parameters.cpp File Reference

File containing [parameters](#) class method for loading VFI parameter values. `#include "global.h"`

```
#include <stdlib.h>
```

```
#include <vector>
```

```
#include <fstream>
```

4.8.1 Detailed Description

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Version:

1.0

Date:

23 Oct 2012

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http://www.boost.org/LICENSE_1_0.txt)

4.9 timer.cpp File Reference

File containing basic timer function. `#include <stddef.h>`
`#include <sys/time.h>`

Functions

- double `curr_second` (void)
Basic timer function.

4.9.1 Detailed Description

Author:

Kyle Spafford

Date:

19 November 2010

Public domain.

4.9.2 Function Documentation

4.9.2.1 double curr_second (void)

Returns:

Double precision value representing time.

4.10 vfInit.cpp File Reference

File containing function to initialize the value function. `#include "global.h"`

```
#include <math.h>
#include <Eigen/Dense>
#include <iostream>
```

Functions

- void `vfInit` (const `parameters` ¶m, const VectorXR &Z, MatrixXR &V)
Function to initialize value function.

4.10.1 Detailed Description

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Version:

1.0

Date:

23 Oct 2012

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http://www.boost.org/LICENSE_1_0.txt)

4.10.2 Function Documentation

4.10.2.1 void vfInit (const parameters & param, const VectorXR & Z, MatrixXR & V)

This function initializes the value function at the deterministic steady state values for each level of TFP: conditional on a TFP level, the deterministic steady-state value of capital is computed, as well as the associated value function value.

Parameters:

- ← *param* Object of class `parameters`.
- ← *Z* Grid of TFP values.
- *V* Matrix of value function values.

Returns:

Void.

4.11 vfStep.cpp File Reference

File containing main iterative step of the VFI problem. `#include "global.h"`

```
#include <math.h>
#include <iostream>
#include <typeinfo>
#include <Eigen/Dense>
#include <stdlib.h>
```

Functions

- `void vfStep (const parameters ¶m, const bool &howard, const VectorXR &K, const VectorXR &Z, const MatrixXR &P, const MatrixXR &V0, MatrixXR &V, MatrixXi &G)`

Function to update value function.

4.11.1 Detailed Description

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Version:

1.0

Date:

23 Oct 2012

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http://www.boost.org/LICENSE_1_0.txt)

4.11.2 Function Documentation

4.11.2.1 `void vfStep (const parameters ¶m, const bool &howard, const VectorXR &K, const VectorXR &Z, const MatrixXR &P, const MatrixXR &V0, MatrixXR &V, MatrixXi &G)`

This function performs one iteration of the value function iteration algorithm, using V0 as the current value function and either maximizing the LHS of the Bellman if `howard` = false or using the concurrent policy function as the argmax if `howard` = true. Maximization is performed by either `gridMax` or `binaryMax`.

Parameters:

← *param* Object of class `parameters`.

- ← *howard* Indicates if the current iteration of the value function will perform a maximization (false) or if it will simply compute the new value function using the concurrent policy function (true).
- ← *K* Grid of capital values.
- ← *Z* Grid of TFP values.
- ← *P* TFP transition matrix.
- ← *V0* Matrix storing current value function.
- *V* Matrix storing updated value function.
- ↔ *G* Matrix storing policy function (updated if howard = false).

Returns:

Void.