

# Transformations

# 3D scene lives in a coordinate system

- When it comes to defining shape, location, orientation and other properties of 3D scene elements we rely on using **points and vectors**.
- Points and vectors are represented with **three coordinates: (x,y,z)**
- These values are meaningless without a **coordinate system** that defines origin of the space and gives three linearly independent vectors that define x,y and z axis of a space.
- Origin and three vectors define a **frame** which defines coordinate systems.
- <IMAGE: 3D COORDINATE SYSTEM, POINTS, VECTORS, OBJECTS>
  - Point or vector in 3D space depend on its relationship to the frame – point can have same absolute position in space but its coordinates depend on frame.

# 3D scene requires a standard frame

- Note that coordinate system is defined with origin and three vectors.
- But point and vectors depend on coordinate system!
- Therefore, we define **world space** – a standard frame – with origin  $(0,0,0)$  and vectors  $(1,0,0)$ ,  $(0,1,0)$  and  $(0,0,1)$ .
- All other frames will be defined with respect to this world coordinate system.

# Note: coordinate system handedness

- Axis of  $x, z$  and  $z$  vectors defining coordinate system can face in one of two directions.
- Left coordinate system
- Right coordinate system
- <IMAGES>

# Elements of 3D scene are described with vectors

- Points
- Vectors
- Normals
- Rays



Elements of 3D scene are moved using  
matrix operations

- TODO

# Important matrices are transformation matrices

- Modeling elements, 3D scene and animations relies on transformations
  - Translation
  - Rotation
  - Scale
  - Look-at notation



# Translation

# Scaling

# Rotation

# Moving directed objects

- Camera movement using look-at notation

# Matrix and coordinate system

- Relationship between matrix and coordinate system

Special care: transformations on normals

# Other coordinate systems

# Literature

- <https://github.com/lorentzo/IntroductionToComputerGraphics/wiki/Foundations-of-3D-scene-modeling>