3D model shapes

Implicit surfaces

Implicit surface: basics

- In foundations of 3D scene modeling we have discussed parametric curves and surfaces.

- Implicit surfaces form another useful class for modeling and **shape representation**.
  - Often used in **intersection testing with rays** since they are simpler to intersect than parametric surface

- **Implicit function**: $f(x,y,z) = 0$
  - Point (x,y,z) is on implicit surface if the result is zero when point (x,y,z) is inserted into function
  - Signed distance: negative if (x,y,z) inside or positive if (x,y,z) outside will be returned – therefore name **signed distance functions** is used.
  - Normal (essential shading information) can be computed using partial derivatives – the gradient of f. <FORMULA>
    - In Practice, central difference can be used for approximating gradient <FORMULA>

- <EXAMPLES of SDFs: https://iquilezles.org/articles/distfunctions/>

Implicit surface: modeling

- **Constructive solid geometry** algorithms (subtraction, addition - union) can be easily done with them
- SDFs can be easily deformed or blended
  - This is called blobby modelling → **metaballs**
- <examples>:
  - https://www.playstation.com/de-de/games/dreams/
  - Blender metaballs
- Transformations are done using the inverse transform applied to p, e.g., f(p-t)
- Repeating object can be done using r=mod(p,c).

Implicit surface: rendering

- https://www.scratchapixel.com/lessons/3d-basic-rendering/minimal-ray-tracer-rendering-simple-shapes

- For visualization, ray-marching is often used.
  - This method also enables calculating shadows, reflections, AO and other effects.

  - <example: raymarching>

Implicit surface: rendering

- Another approach is to turn the SDF into surface consisting of triangles.

- Famous algorithm for this is **marching cubes algorithm***

* Different polygonizational algorithms and GPU methods are presented for real-time rendering.

Isosurface: examples

- https://dl.acm.org/doi/10.1145/3023368.3023377

- **https://store.steampowered.com/app/661920/Claybook/**

Constructive solid geometry

- Two main methods for visualization:
  - Stencil buffer
  - Analytical storage

Subdivision curves and surfaces

Subdivision curves and surfaces

- Used to make **smooth** curves and surfaces

- Gap between discrete surface (triangle meshes) and continuous surfaces (e.g., Bezier patches)
  - Useful for dynamic level of detail

<example: mesh surface, parametric surface, subdivision surface>

<example:level of detail>

Subdivision curves: intuition

- Corner cutting algorithm explains subdivision curves well.
  - Initial polygon P_0 is given which specifies control polygon: vertices are control points
  - Corners of given polygon are cut and this is repeated until **sharp corners are removed** $P_0 \rightarrow P_1 \rightarrow \ldots \rightarrow P_n$
  - Result is called **limit curve** $\rightarrow$ smooth curve since all corners are cut off
  - Analogy: low-pass filtering – all sharp corners (high frequency) are removed.
  - \<image\>

Subdivision curves

- Subdivision process can be done in many possible ways

- Subdivision surface is characterized by subdivision scheme

- <example: meshlab subdivision>
  https://pymeshlab.readthedocs.io/en/0.1.8/filter_list.html#subdivision_surfaces_butterfly_subdivision

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Subdivision curves: Chaikin scheme

- Given initial polygon P0 with n vertices this is simple method to raptly generate smooth curve

- Chaikin scheme creates two new vertices between each subsequent pairs of vertices

- After each step, original vertices are discarded and new points are reconnected – new points are created ¼ away from original vertices
  - <image>
  - <formula>

- Properties:
  - This scheme generates quadratic B-spline
  - Works only for closed polygons

Subdivision curves: schemes

- Two main subdivision schemes exists:
  - Approximating
  - Interpolating
- Approximating
  - Chaikin scheme
  - Since (original) vertices are discarded or modified, limit curve does not lie on vertices of original polygon
- Interpolating
  - Contains all vertices from previous step: limit curve goes through all points - interpolating

Subdivision curves: interpolating scheme

- An example: 4 point interpolatory subdivision scheme*
  - 4 nearest points are took for creating a new point
  - All points from previous step are kept
  - Tensions parameter: 0 → linear interpolation, > 0 → curves with different continuity parameters
  - Does not work directly for open polygons.
  - \<formula\>
  - \<image\>

* https://cgvr.cs.uni-bremen.de/papers/c2scheme/c2scheme.pdf

Subdivision curves: in practice

- Examples in animation and modeling:
  http://multires.caltech.edu/pubs/sig00notes.pdf

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Subdivision surfaces

- Introduced concepts on subdivision curves apply to subdivision surfaces

- Paradigm for defining smooth, continuous surfaces from meshes with arbitrary topology
  - Infinite level of detail is provided: arbitrary number of triangles/polygons can be generated
  - <example>

- Inspection of continuity is mathematically involved process and thus not straightforward.

- Simple and easily implemented rules needed for subdivision. Two phases, that characterize subdivision scheme:
  - In first, **refinement phase**, new vertices are created and reconnected for some or all vertices of **control mesh** (initial mesh). Different refinement methods exist (e.g., how the polygon can be split)
  - Second, **smoothing phase**, computes new positions for some or all vertices in the mesh. Different schemes dictates the continuity of surface and whenever the surface is approximating or interpolating.
  - <phases example>

Subdivision surfaces: types

- Subdivision schemes can be:
  - Stationary or non-stationary
    - Stationary – same rules are used in each step
    - Non-stationary – changes steps based on current step
  - Uniform or non-uniform
    - Uniform – same rules for every vertex or edge
    - Non-uniform – different rules for vertices or edges, e.g., edges that are on boundary of a surface.
  - Triangle or polygon based

Subdivision surfaces: Loop subdivision

- TODO RTR BOOK

- Meshlab example

Subdivision surfaces: Catmull-Clark

- TODO RTR BOOK

- Meshlab example

Displacement and subdivision

- TODO RTR BOOK

- Blender example

Subdivision surfaces: production

- Pixar OpenSubdiv

- RTR BOOK

Subdivision surfaces

- Catmull-Clark subdivision surfaces

Voxels

Voxels

- TODO

Operations on meshes

Operations on meshes

- Tessellation and triangulation – RTR 16

- Consolidation – RTR 16

- Simplification – RTR 16

- Compression – RTR 16

Digitalization

Digitalization

- Scanning, photogrammertry, measuring

- https://alicevision.org/#photogrammetry

Procedural modeling

Procedural modeling

- Shape
  - Procedural geometry
- Material
- Noise
- Shaders
- Noding system