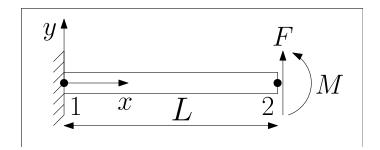
Stiffness matrix for a cantilever bending beam

Compute the stiffness matrix of the bending beam model in the figure above using two approaches:

- 1. by writing the strain complementary energy,
- 2. from the compliance matrix

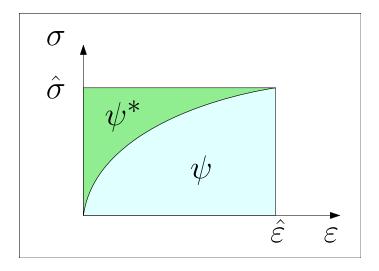
when the shear strain related to the shear load:

- 1. is neglected (Euler-Bernoulli's thin beam case);
- 2. is not neglected (Timoshenko's relatively thick beam case). The beam in the -plane is clamped at the node 1 and is submitted to both a shear force and a torque at the node 2.



Refresher: complementary strain energy

Consider the following uniaxial stress-strain curve:



The strain energy	density is the are	ea underneath	the stress-strain	curve

The complementary strain energy density is the complementaty area to obtain a rectangular area

In the linear case the two areas are equal, i.e.

The complementary energy expresses the energy in terms of stress rather than in terms of strains and it is suitable when one wants to apply e.g. Castigliano theorem.